

sixth EDITION

SIMULATION with Arena

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What is Simulation?

Chapter 1

Last revision December 21, 2013

Simulation Is ...

- ***Simulation*** – very broad term – methods and applications to imitate or mimic real systems, usually via computer
- Applies in many fields, industries
- Very popular, powerful
- Book covers simulation in general, *Arena* simulation software in particular
- This chapter – general ideas, terminology, examples of applications, good/bad things, kinds of simulation, software options, how/when simulation is used

Systems

- **System** – facility or process, actual or planned
 - Examples abound ...
 - Manufacturing facility
 - Bank operation
 - Airport operations (passengers, security, planes, crews, baggage)
 - Transportation/logistics/distribution operation
 - Hospital facilities (emergency room, operating room, admissions)
 - Computer network
 - Freeway system
 - Business process (insurance office)
 - Criminal justice system
 - Chemical plant
 - Fast-food restaurant
 - Supermarket
 - Theme park
 - Emergency-response system
 - Shipping ports, berths
 - Military combat, logistics

Work With the System?

- **Study system – measure, improve, design, control**
 - Maybe just play with actual system
 - Advantage — unquestionably looking at the right thing
 - But often impossible in reality with actual system
 - System doesn't exist
 - Would be disruptive, expensive, dangerous

Models

- **Model** – set of assumptions/approximations about how system works
 - Study model instead of real system ... usually much easier, faster, cheaper, safer
 - Can try wide-ranging ideas with model
 - Make your mistakes on the computer where they *don't* count, rather than for real where they *do* count
 - Often, just *building* model is instructive – regardless of results
 - Model *validity* (any kind of model ... not just simulation)
 - Care in building to mimic reality faithfully
 - Level of detail
 - Get same conclusions from model as you would from system
 - More in Chapter 13

Types of Models

- **Physical (*iconic*) models**
 - Tabletop material-handling models
 - Mock-ups of fast-food restaurants
 - Flight simulators
- **Logical (*mathematical*) models**
 - Approximations, assumptions about system's operation
 - Often represented via computer program in appropriate software
 - Exercise program to try things, get results, learn about model behavior

Studying Logical Models

- If model is simple enough, use traditional mathematical analysis ... get exact results, lots of insight into model
 - Queueing theory
 - Differential equations
 - Linear programming
- But complex systems can seldom be *validly* represented by simple analytic model
 - Danger of over-simplifying assumptions ... model validity?
 - Type III error – working on the wrong problem
- Often, complex system requires complex model, analytical methods don't apply ... what to do?

Computer Simulation

- **Methods for studying wide variety of models of systems**
 - Numerically evaluate on computer
 - Use software to imitate system's operations, characteristics, often over time
- **Can use to study simple models, but should not use if an analytical solution is available**
- **Real power of simulation – studying complex models**
- **Simulation can tolerate complex models since we don't even aspire to an analytical solution**

Popularity of Simulation

- **Has been consistently ranked as the most useful, popular tool in broader area of operations research / management science**
 - 1978: M.S. graduates of CWRU O.R. Department ... after graduation
 1. Statistical analysis
 2. Forecasting
 3. Systems Analysis
 4. Information systems
 5. Simulation
 - 1979: Survey 137 large firms, which methods used?
 1. Statistical analysis (93% used it)
 2. Simulation (84%)
 3. Followed by LP, PERT/CPM, inventory theory, NLP, ...

Popularity of Simulation (cont'd.)

- 1980: (A)IIE O.R. division members
 - First in utility and interest — simulation
 - First in familiarity — LP (simulation was second)
- 1983, 1989, 1993: Longitudinal study of corporate practice
 1. Statistical analysis
 2. Simulation
- 1989: Survey of surveys
 - Heavy use of simulation consistently reported
- 2012 (Powers thesis): Literally exponential growth in number of simulation papers
- **Since most of these surveys, hardware/software have improved, making simulation even more attractive**
 - Historical impediment to simulation – computer speed

Advantages of Simulation

- **Flexibility to model things as they are (even if messy and complicated)**
 - Avoid *looking where the light is* (a morality play):
You're walking along in the dark and see someone on hands and knees searching the ground under a street light.
You: "What's wrong? Can I help you?"
Other person: "I dropped my car keys and can't find them."
You: "Oh, so you dropped them around here, huh?"
Other person: "No, I dropped them over there." (Points into the darkness.)
You: "Then why are you looking here?"
Other person: "Because this is where the light is."
- **Allows uncertainty, nonstationarity in modeling**
 - The only thing that's for sure: nothing is for sure
 - Danger of ignoring system variability
 - Model validity

Advantages of Simulation (cont'd.)

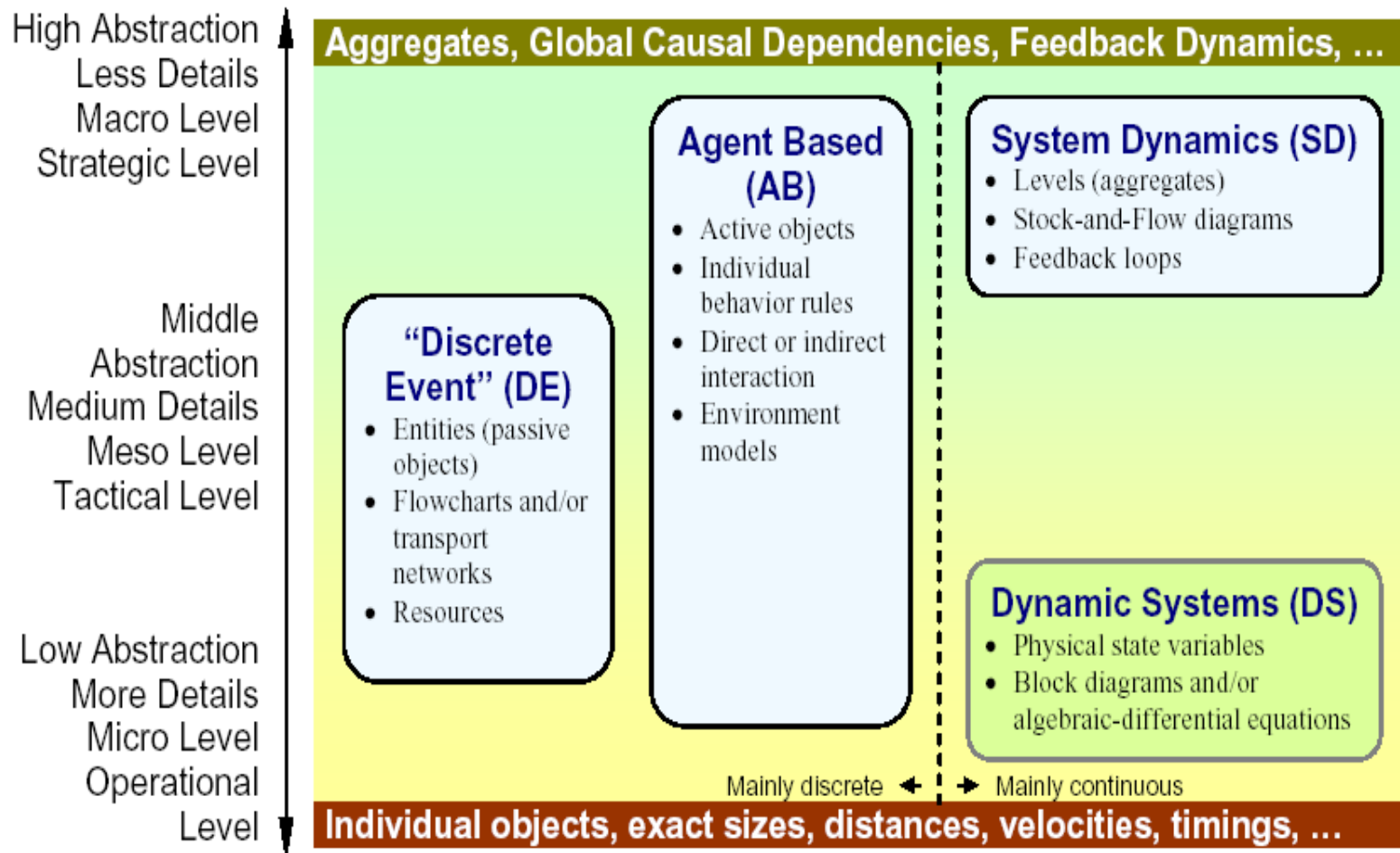
- **Advances in computing/cost ratios**
 - Estimated that 75% of computing power is used for various kinds of simulations
 - Dedicated machines (e.g., real-time shop-floor control)
- **Advances in simulation software**
 - Far easier to use (GUIs)
 - No longer as restrictive in modeling constructs (hierarchical, down to C)
 - Statistical design & analysis capabilities

The Bad News

- **Don't get exact answers, only approximations, estimates**
 - Also true of many other modern methods
 - Can bound errors by machine roundoff
- **Get random output (*RIRO*) from stochastic simulations**
 - Statistical design, analysis of simulation experiments
 - Exploit: noise control, replicability, sequential sampling, variance-reduction techniques
 - Catch: “standard” statistical methods seldom work

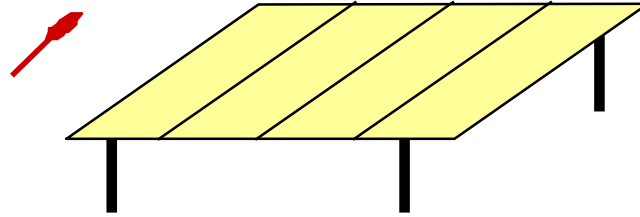
Different Kinds of Simulation

- **Static vs. *Dynamic***
 - Does time have a role in model?
- **Continuous-change vs. *Discrete-change***
 - Can “state” change continuously, or only at discrete points in time?
- **Deterministic vs. *Stochastic***
 - Is everything for sure or is there uncertainty?
- **Most operational models:**
 - *Dynamic, Discrete-change, Stochastic*
 - But Chapter 2 discusses one static model
 - And Chapter 11 discusses continuous and combined discrete-continuous models



approaches (paradigms) in simulation modeling on abstraction level scale (source: Borshev and Filippov (2004))

Simulation by Hand: The Buffon Needle Problem



- Estimate π (George Louis Leclerc, c. 1733)
- Toss needle of length l onto table with stripes d ($>l$) apart
- $P(\text{needle crosses a line}) = \frac{2l}{\pi d}$
- Repeat; tally \hat{p} = proportion of times a line is crossed
- Estimate π by $\frac{2l}{\hat{p}d}$

Just for fun:

<http://www.mste.uiuc.edu/reese/buffon/bufjava.html>

<http://www.angelfire.com/wa/hurben/buff.html>

Why Toss Needles?

- **Buffon needle problem seems silly now, but has important simulation features:**
 - Experiment to *estimate* something hard to compute exactly (in 1733)
 - *Randomness*, so estimate will not be exact; estimate the error in the estimate
 - *Replication* (the more the better) to reduce error
 - *Sequential sampling* to control error — keep tossing until probable error in estimate is “small enough”
 - *Variance reduction* (*Buffon Cross*)

Using Computers to Simulate

- **General-purpose languages (C, C++, C#, Java, Matlab, FORTRAN, others)**
 - Tedious, low-level, error-prone
 - But, almost complete flexibility
- **Support packages for general-purpose languages**
 - Subroutines for list processing, bookkeeping, time advance
 - Widely distributed, widely modified
- **Spreadsheets**
 - Usually static models (only *very* simple dynamic models)
 - Financial scenarios, distribution sampling, SQC
 - Examples in Chapter 2 (one static, one dynamic)
 - Add-ins are available (@RISK, Crystal Ball)

Using Computers to Simulate (cont'd.)

- **Simulation languages**

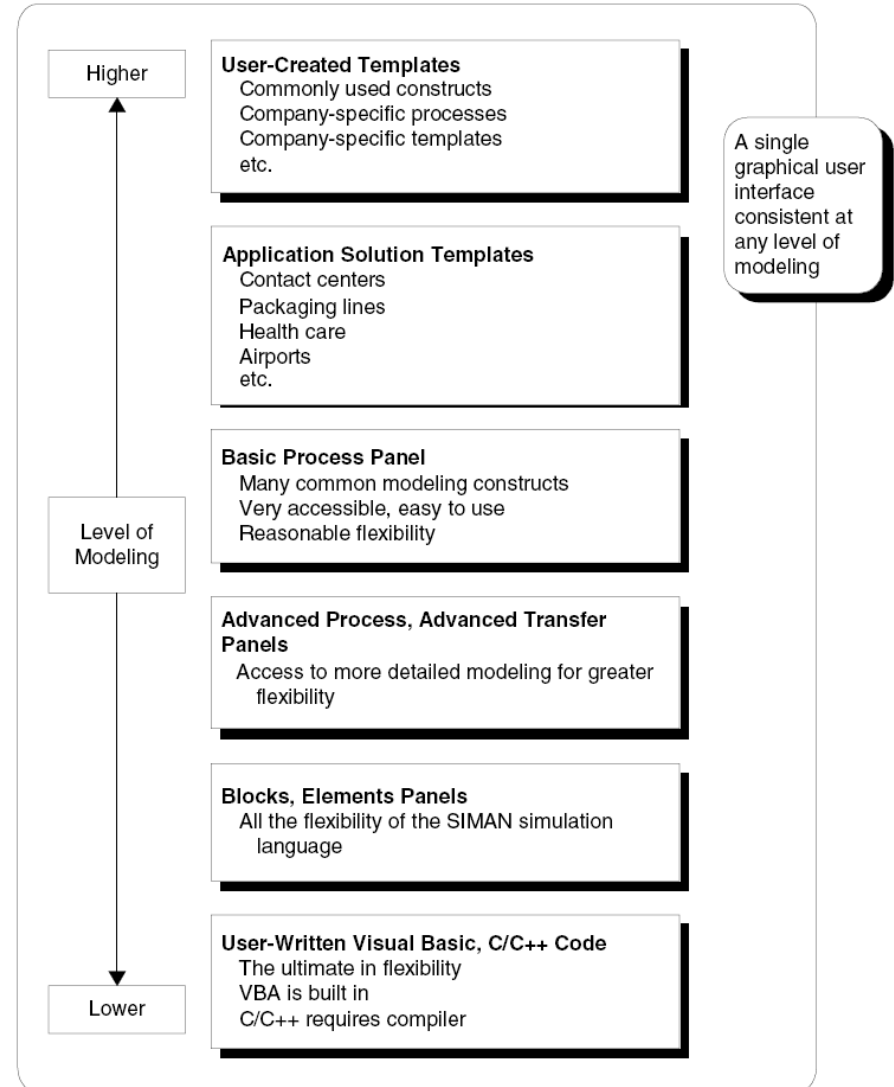
- GPSS, SLX, SIMAN (on which Arena is based, included in Arena)
- Popular, some still in use
- Learning curve for features, effective use, syntax

- **High-level simulators**

- Very easy, graphical interface
- Domain-restricted (manufacturing, communications)
- Limited flexibility — model validity?

Where Arena Fits In

- **Hierarchical structure**
 - Multiple levels of modeling
 - Mix different modeling levels together in same model
 - Often, start high then go lower as needed
- **Get ease-of-use advantage of simulators without sacrificing modeling flexibility**



When Simulations are Used

- **Use of simulation has evolved with hardware, software**
- **Early years (1950s – 1960s)**
 - Very expensive, specialized tool
 - Required big computers, special training
 - Mostly in FORTRAN (or even Assembler)
 - Processing cost as high as \$1000/hour for a sub-PC level machine

When Simulations are Used (cont'd.)

- **Formative years (1970s – early 1980s)**
 - Computers got faster, cheaper
 - Value of simulation more widely recognized
 - Simulation software improved, but still languages to be learned, typed, batch processed
 - Often used to clean up “disasters” in auto, aerospace industries
 - Car plant; heavy demand for certain model
 - Line underperforming
 - Simulated, problem identified
 - But demand had dried up — simulation was too late

When Simulations are Used (cont'd.)

- **Recent past (late 1980s – mid 2000s)**
 - Microcomputer power
 - Software expanded into GUIs, animation
 - Wider acceptance across more areas
 - Traditional manufacturing applications
 - Services
 - Health care
 - “Business processes”
 - Still mostly in large firms
 - Simulation is often part of “specs”

When Simulations are Used (cont'd.)

- **Present**

- Proliferating into smaller firms
- Becoming a standard tool
- Being used earlier in design phase
- Real-time control
- 3D graphics, business dashboards

- **Future**

- Integration with other applications for visualization, analysis
- Networked sharing of data in real time
- Internet-enabled distributed model building, execution
- Specialized vertical “templates” for specific industries, firms
- Better model re-usability, operational decision making
- Automated statistical design, analysis