

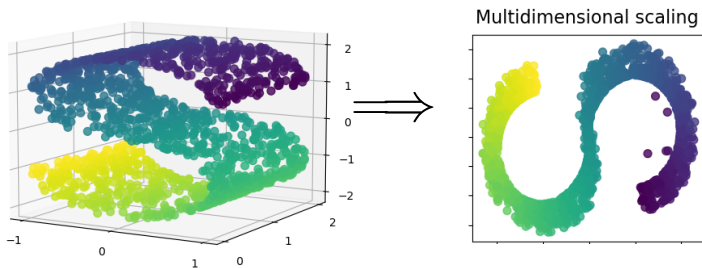
Projecting to low dimensions while preserving distances

Let D be the matrix of measured pairwise distances.

Multidimensional scaling (MDS) finds $x_i \in \mathbb{R}^k$ to minimize

$$\text{STRESS}(x) = \sum_{i>j} (D_{ij} - \|x_i - x_j\|)^2$$

where k is small.



[Pedregosa et al., 2011]

Bayesian MDS

- First published by Oh and Raftery [Oh and Raftery, 2001]
- Let D be the matrix of measured distances between points
- Assumes

$$D_{ij} \sim N(\|x_i - x_j\|, \sigma^2) I(D_{ij} > 0)$$

- where $x_i \in \mathbb{R}^k$
- Need to specify priors for x_i and σ^2

MassiveMDS: an OpenCL implementation of likelihood and gradient functions for MDS

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Massive Parallelization Boosts Big Bayesian Multidimensional Scaling

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ABSTRACT

Big Bayes is the computationally intensive co-application of big data and large, expressive Bayesian models for the analysis of complex phenomena in scientific inference and statistical learning. Standing as an example, Bayesian multidimensional scaling (MDS) can help scientists learn viral trajectories through space-time, but its computational burden prevents its wider use. Crucial MDS model calculations scale quadratically in the number of observations. We partially mitigate this limitation through massive parallelization using multi-core central processing units, instruction-level vectorization and graphics processing units (GPUs). Fitting the MDS model using Hamiltonian Monte Carlo, GPUs can deliver more than 100-fold speedups over serial calculations and thus extend Bayesian MDS to a big data setting. To illustrate, we employ Bayesian MDS to infer the rate at which different seasonal influenza virus subtypes use worldwide air traffic to spread around the globe. We examine 5392 viral sequences and their associated 14 million pairwise distances arising from the number of commercial airline seats per year between viral sampling locations. To adjust for shared evolutionary history of the viruses, we implement a phylogenetic extension to the MDS model and learn that subtype H3N2 spreads most effectively, consistent with its epidemic success relative to other seasonal influenza subtypes. Finally, we provide MassiveMDS, an open-source, stand-alone C++ library and rudimentary R package, and discuss program design and high-level implementation with an emphasis on important aspects of computing architecture that become relevant at scale.

ARTICLE HISTORY

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KEYWORDS

Bayesian phylogeography;
Graphics processing unit;
Hamiltonian Monte Carlo;
Massive parallelization;
Single-instruction,
multiple-data

Some questions I still have

- The code contains a lot of fitting "precision" of the MDS likelihood, but nothing in the paper about this. Is this referring to the float precision used to compute the likelihood?
- There are also mentions of learning traits, which I think has to do with the integration of this package to BEAST



Oh, M.-S. and Raftery, A. E. (2001).

Bayesian multidimensional scaling and choice of dimension.
Journal of the American Statistical Association,
96(455):1031–1044.



Pedregosa, F., Varoquaux, G., Gramfort, A., Michel, V.,
Thirion, B., Grisel, O., Blondel, M., Prettenhofer, P., Weiss,
R., Dubourg, V., Vanderplas, J., Passos, A., Cournapeau,
D., Brucher, M., Perrot, M., and Duchesnay, E. (2011).

Scikit-learn: Machine learning in Python.

Journal of Machine Learning Research, 12:2825–2830.