Strain-space model for Sars-CoV-2

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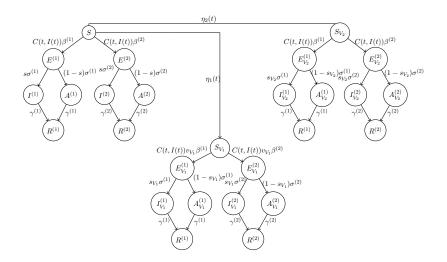
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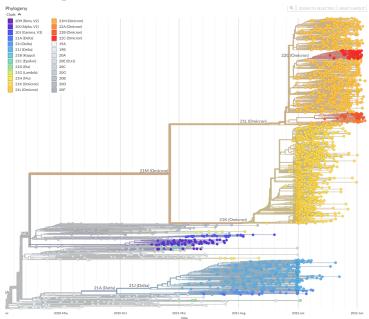
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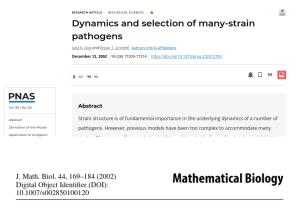
Modeling multiple infections is challenging



How to incorporate more data?



A useful approximation

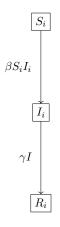


J.R. Gog · J. Swinton

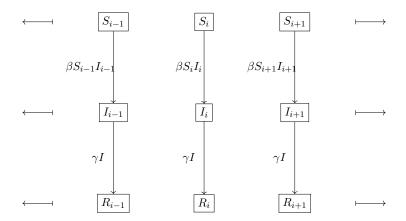
A status-based approach to multiple strain dynamics

Received: 5 April 2000 / Revised version: 24 July 2001 / Published online: 8 February 2002 – © Springer-Verlag 2002

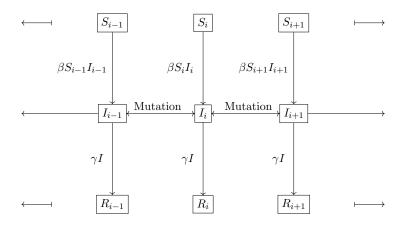
Begin with simple SIR model



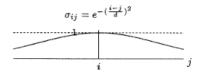
Organize strains on a lattice



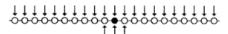
Strains mutate into adjacent strains



Infections provide cross-immunity to nearby strains



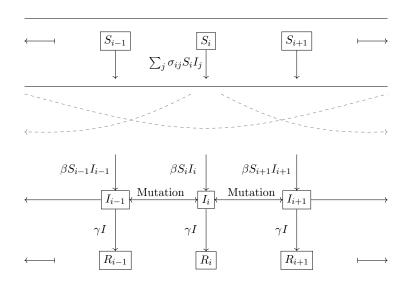
Cross-immunity to nearby strains



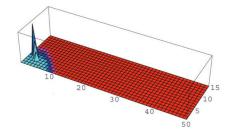
Mutation to adjacent strains

[Gog and Grenfell, 2002]

Full strain lattice model in 1 dimension

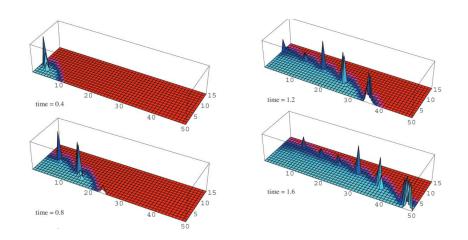


Extending the strain lattice to 2 dimensions



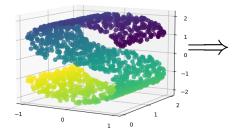
[Gog and Grenfell, 2002]

Extending the strain lattice to 2 dimensions



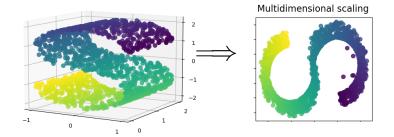
[Gog and Grenfell, 2002]

Projecting to low dimensions while preserving distances



[Pedregosa et al., 2011]

Projecting to low dimensions while preserving distances

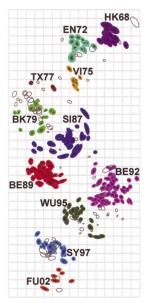


[Pedregosa et al., 2011]

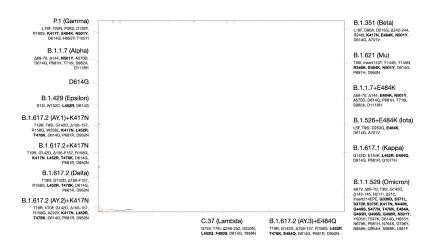
Approximating genomic data in 2 dimesions



Approximating genomic data in 2 dimesions

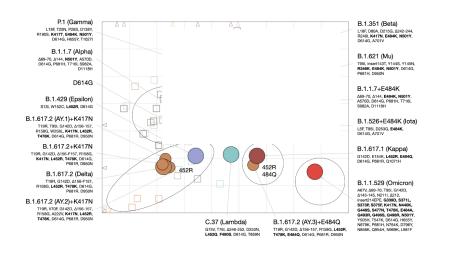


Mapping SARS-CoV-2 in 2D



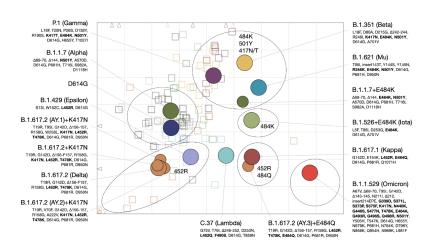
[Wilks et al., 2022]

Mapping SARS-CoV-2 in 2D



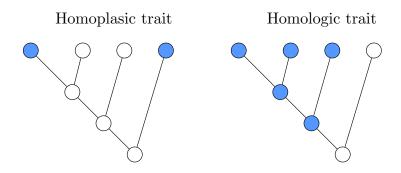
[Wilks et al., 2022]

Mapping SARS-CoV-2 in 2D



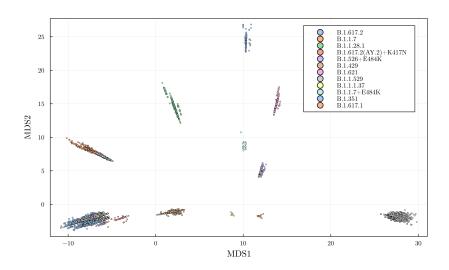
[Wilks et al., 2022]

Methods of adding more genomes: homoplasic sites

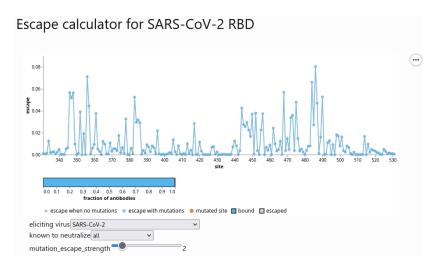


[Page and Holmes, 2009]

Homoplasic mutations map

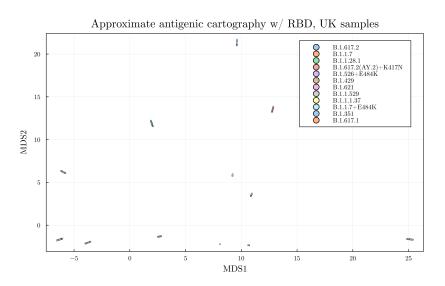


Methods of adding more genomes: polyclonal antibody binding studies

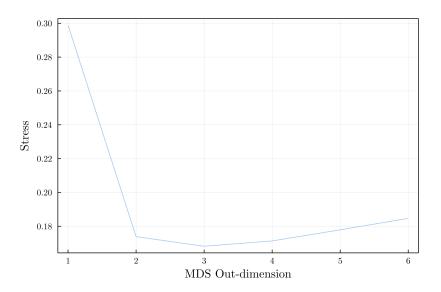


[Greaney et al., 2022]

Antibody Binding map



Evaluating the MDS approximation



Model parameters/variables

_	Symbol	Description
	N	Size of variant grid
	S_{ij}	Population susceptible to variant $(i, j) \in [0, N]^2$
	I_{ij}	Population infected by variant $(i, j) \in [0, N]^2$
	R_{ij}	Recovered/Immune to variant $(i, j) \in [0, N]^2$
	σ_{ijkl}	Probability that exposure to variant (i, j) causes
		immunity
		to variant (k, l)
	eta_{ij}	Transmission rate of variant (i, j)
	v(t)	vaccination rate at time t
	s(t)	stringency at t
	ξ	Recovery rate of all strains
	γ	Rate of immunity loss of all strains

Table of symbols for Model 2

Model Equations

$$\frac{S_{ij}}{dt} = -\sum_{kl} s(t)\beta_{kl}\sigma_{ijkl}S_{ij}I_{kl} + \gamma R_{ij} - V(t)S \tag{1}$$

$$\frac{I_{ij}(t)}{dt} = s(t)\beta_{ij}S_{ij}I_{ij} - \xi I_{ij} + M\left(-4I_{ij} + I_{i-1,j} + I_{i+1,j} + I_{i,j-1} + I_{i,j+1}\right) \tag{2}$$

$$\frac{R_{ij}(t)}{dt} = \xi I_{ij} - \gamma R_{ij} + V(t)S \tag{3}$$

Boundary conditions: $I_{0,j} = 0, I_{j,0} = 0, I_{N,j} = 0, I_{j,N} = 0$ Initial conditions computed from genomic data in GISAID (gifs of model dynamics) $\,$

Further work

- Estimating a nonlocal diffusion kernel
- Better model fitting
- Predicting vaccine targets

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Mutation homoplasy

