

Coupled models of structured contagion processes in human-environment systems

Peter C. Jentsch

Department of Applied Mathematics, University Of Waterloo

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Supervised by Chris T. Bauch and Madhur Anand

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Introduction

Contagious processes

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- A contagious process is one that is able to propagate itself through a set of hosts
- Contagious processes shape our lives in many important ways
- Current situation has thrust the importance of modeling infections into popular consciousness

Coupled systems

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- Coupling can often dramatically affect stability, e.g. coupled oscillators
- Human-environment systems focus on dynamics of humanity and the environment viewed as a whole
- My thesis attempts to show that this perspective provides useful answers to important problems

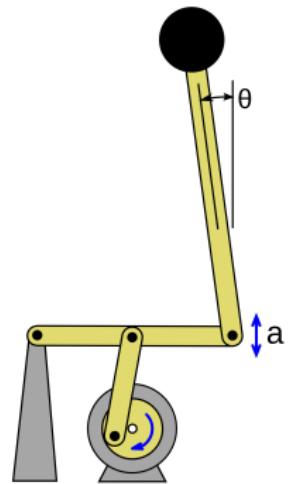


Figure: Kapitza's pendulum

Source: Chris Burks

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- Population beliefs about the usage of non-pharmaceutical interventions (NPIs) can have a major effect on the epidemic landscape
- Population age distribution is a key factor in both NPI usage and COVID-19 mortality
- Vaccine rollout important to reducing mortality in the long term (Bubar et al., 2020; Buckner, Chowell, and Springborn, 2020)

Outline of project

- ① Describe age-structured compartmental model of COVID-19 infection in a population, coupled to model of social distancing dynamics.
- ② Fit model to data from Ontario, Canada
- ③ Evaluate outcomes from different vaccination strategies, comparing vaccination of vulnerable populations vs vaccination of susceptible populations

Compartmental model overview

Disease Compartments

$S_i(t)$: Susceptible

$S_{2,i}(t)$: Vaccinated but still
susceptible

$V_i(t)$: Vaccinated and
immune

$E_i(t)$: Exposed

$P_i(t)$: Pre-symptomatic

$I_{a,i}(T)$: Infectious and
asymptomatic

$I_{s,i}(t)$: Infectious and
symptomatic

$R_i(t)$: Recovered

where $i = 1 \dots 16$ comprises age
structure

Social compartments

$x(t)$: Uses NPIs

$1 - x(t)$: Does not use NPIs

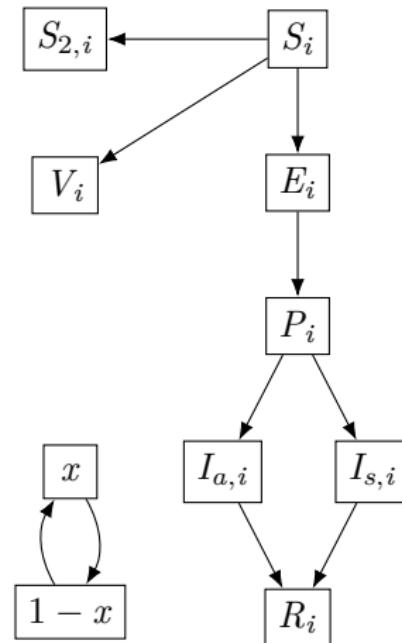


Figure: Compartments

Game theory as a model of NPI adoption

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P1 \ P2	use NPI	don't use NPI
use NPI	low risk, NPIs unpleasant	med risk
don't use NPI	med risk, NPIs unpleasant	high risk

Table: NPI adoption as a two-player game (between P1 and P2)

Vaccination strategies

We compare four vaccination strategies

- > 60 first
- < 20 first
- Uniform
- Contact-based

with respect to reduction in cumulative mortality after 5 years.

Contact-based vaccination strategy

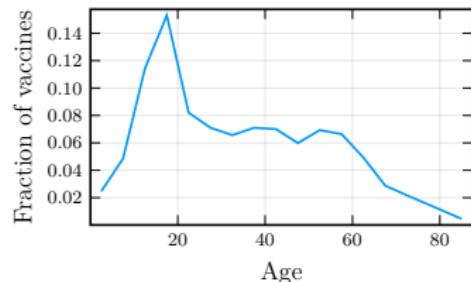


Figure: Vaccine allocation by age in the contact-based vaccination strategy.

Computed as the normalized leading eigenvector of the sum of the contact matrices.

Parameterization

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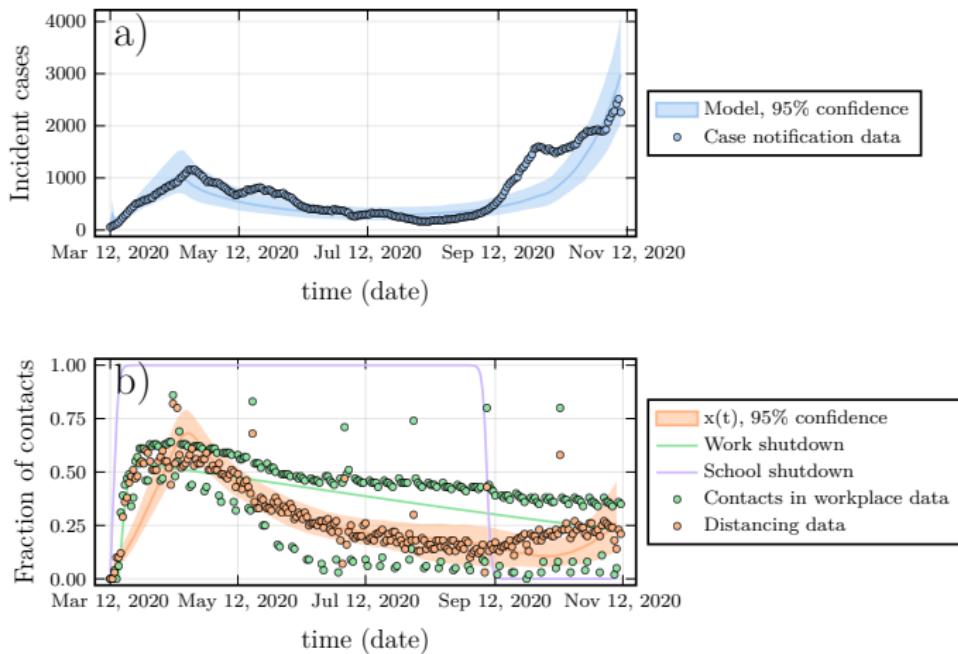


Figure: Model parameterization used, physical distancing matches reported cases.

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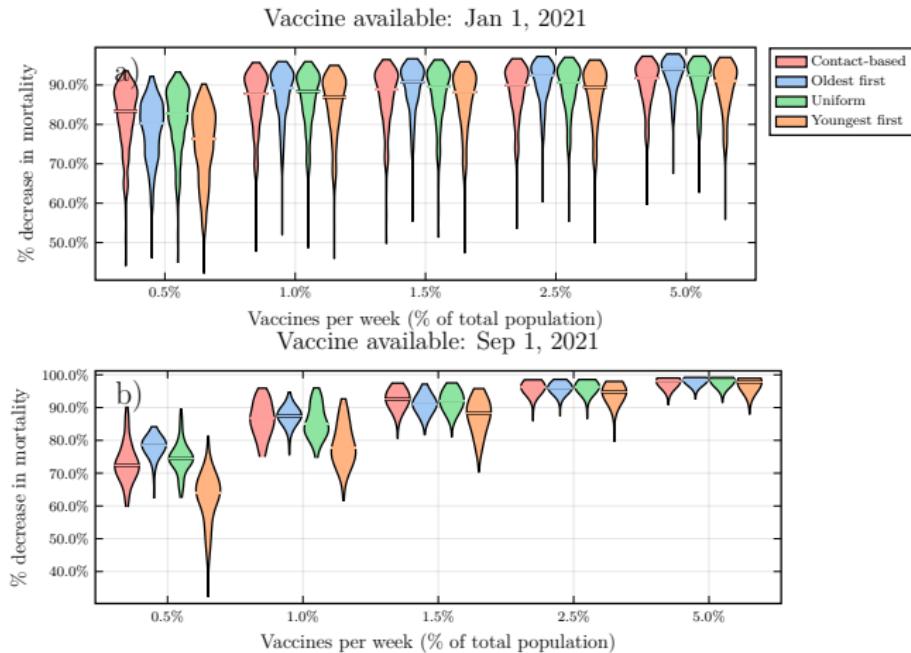
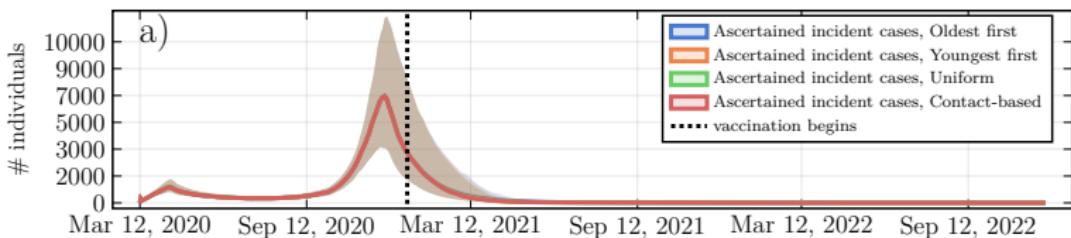


Figure: Percentage reduction in mortality for four strategies depends on vaccination start date and the vaccination rate.

Vaccination begins on Jan 1, 21, 1.5% of pop. vaccinated per week



Vaccination begins on Jan 1, 21, 0.5% of pop. vaccinated per week

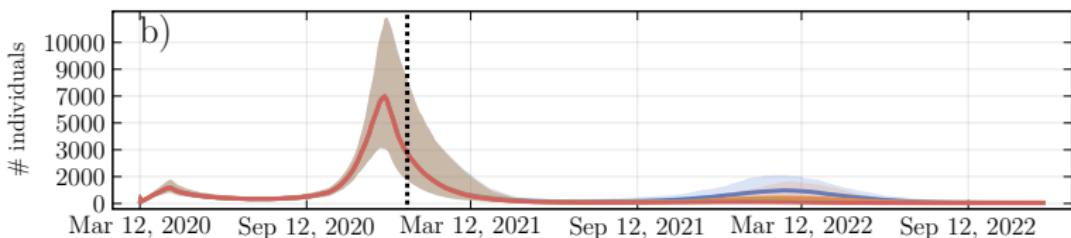
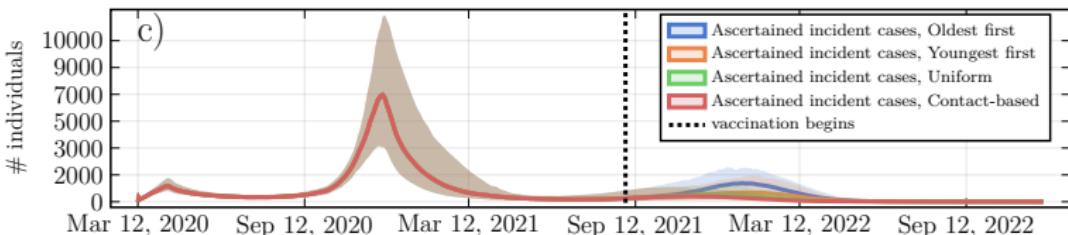


Figure: (a) timely vaccination prevents third wave, (b) partial vaccination and indirect protection help during the third wave

Vaccination begins on Sep 1, 21, 1.5% of pop. vaccinated per week



Vaccination begins on Sep 1, 21, 0.5% of pop. vaccinated per week

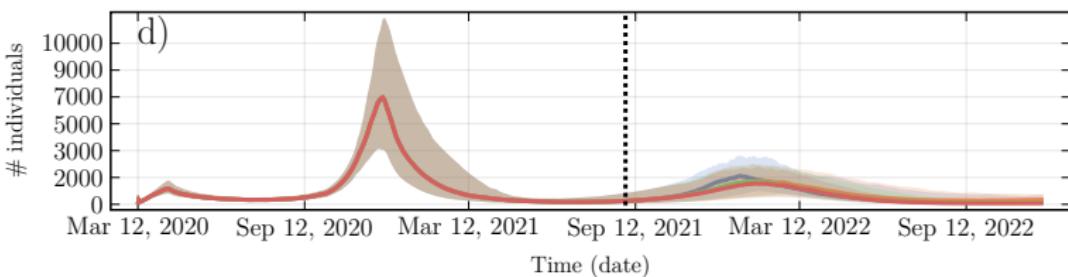


Figure: c) with a later start date but higher vaccination rate, partial vaccination and indirect protection help during the third wave as in b), (d) slow and late vaccination fails to prevent third wave.

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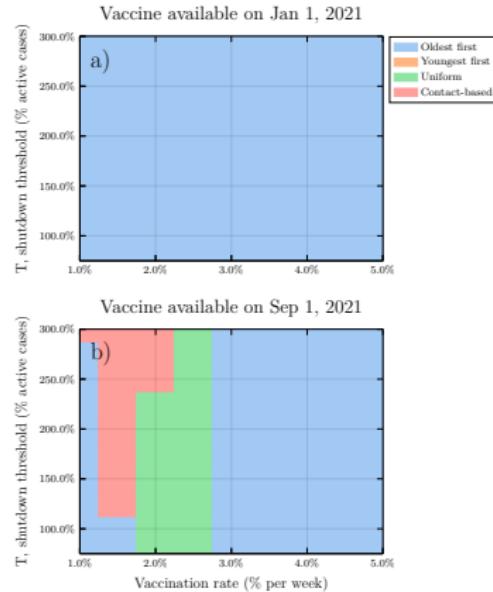


Figure: Later start to vaccination favours transmission-interrupting strategies for moderate vaccination rates. Each parameter pair is colored according to the strategy that prevents most deaths on average, over all realizations of the model.

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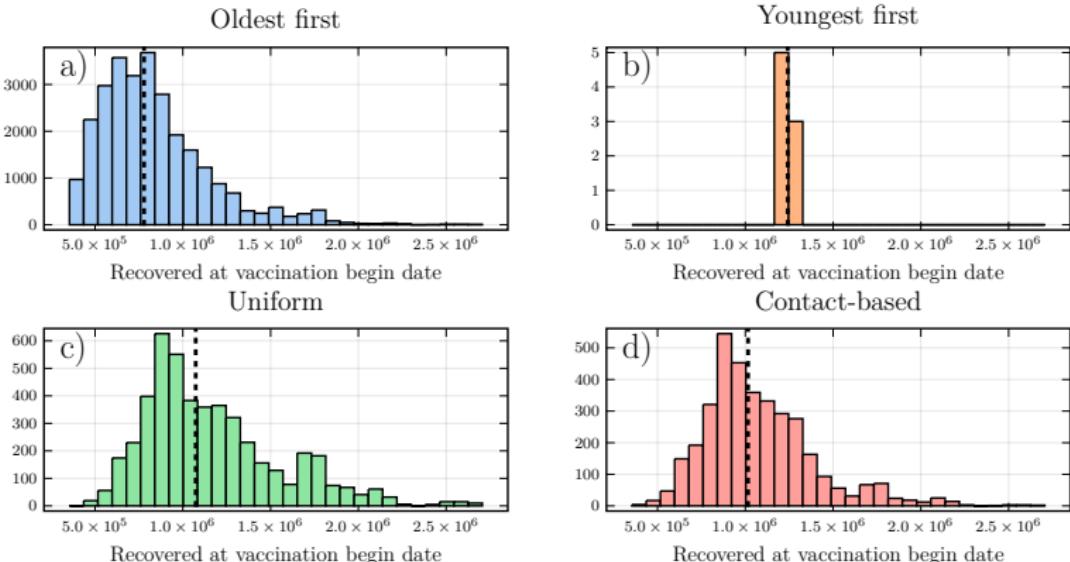


Figure: More pre-existing natural immunity makes transmission-interrupting strategies more effective. Histogram of no. recovered at vaccination begin date, according to best strategy for that realization, over all parameter values in sensitivity analysis. Vertical lines are the median.

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- We described an age structured compartmental model of Sars-CoV-2 infection and vaccination coupled to a social model
- Showed that sometimes transmission interrupting strategies can be more effective
- Depends on the pre-existing immunity in the population

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Project 2

- Invasive forest pests cause incredible damage to ecosystems and lumber resources
- Evidence shows that movement of firewood is a major long distance vector (Koch et al. (2014))
- Education and awareness is a major way we try to reduce this vector



Figure: an Emerald Ash Borer, which devastated Ash populations in North America

Outline of project

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- ① Adapt a model such as Barlow et al. (2014) to a larger, more realistic network
- ② Use model to compare three possible prevention measures
 - Education/awareness
 - Inspection of moved firewood
 - Quarantine of highly susceptible forest patches
- ③ Assess measures across a range of parameter values and time horizons

Model

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$$\frac{dS_i}{dt} = \underbrace{rS_i \left(1 - \frac{(S_i + I_i)}{K}\right)}_{\text{Logistic Growth Of Forest}} - \underbrace{AS_i(I_i + B_i)\theta_k(I_i - I_a)}_{\text{Infestation term}} \quad (1)$$

$$\frac{dI_i}{dt} = \underbrace{-\gamma I_i}_{\text{Death of infested trees}} + \underbrace{AS_i(I_i + B_i)\theta_k(I_i - I_a)}_{\text{Susceptibles become infested}} - \underbrace{d \sum_{j=1, j \neq i}^N P_{j,i}(1 - C_e)(1 - L_j)I_j}_{\text{Total infested wood leaving due to transport}} \quad (2)$$

$$\frac{dB_i}{dt} = \underbrace{-\gamma B_i}_{\text{Decay of firewood}} + d \underbrace{\sum_{j=1, j \neq i}^N P_{i,j}(1 - C_e)(1 - L_j)I_j}_{\text{Import of fallen wood}} \quad (3)$$

$$\frac{dL_i}{dt} = \sigma L_i(1 - L_i) \left(\underbrace{U}_{\text{Net cost to transport firewood}} + \underbrace{s(2L_i - 1)}_{\text{Social influence term}} + \underbrace{fI_i}_{\text{Impact of infestation}} \right) \quad (4)$$

We use $T_i(t)$, computed from equation 5 to be the total number of infested trees in patch i up to time t .

$$\frac{dT_i}{dt} = AS_i(I_i + B_i)\theta_k(I_i - I_a) \quad (5)$$

Define $T(t) = \frac{1}{N} \sum_{i=1}^N T_i(t)$ to be the average total number of infested trees up to t .

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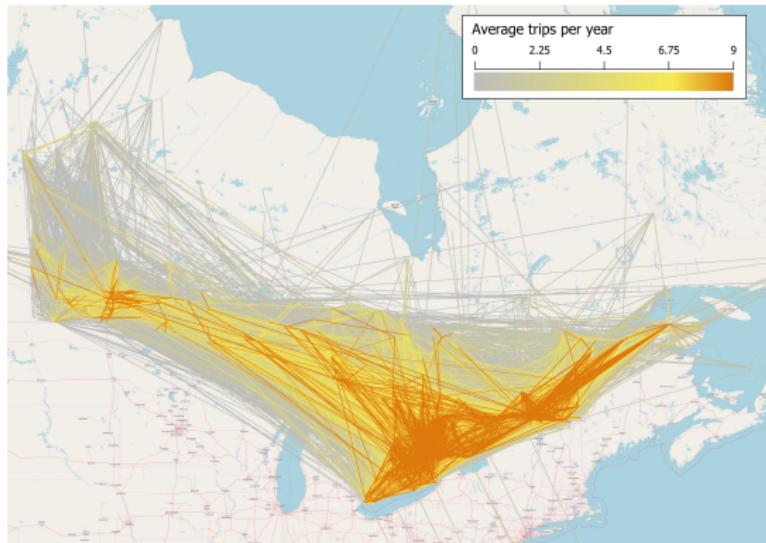


Figure: Travel network used to weight edges in firewood transport network

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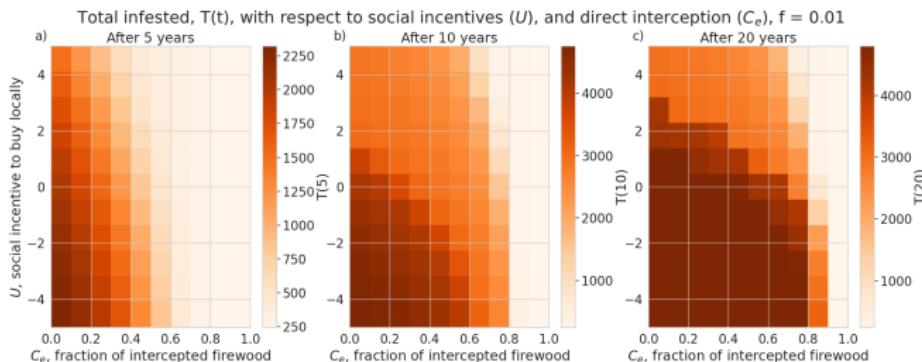


Figure: Neither increasing U nor C_e are effective at long time scales. Total number of infested trees per node over 5 (a), 10 (b), and 20 (c) years

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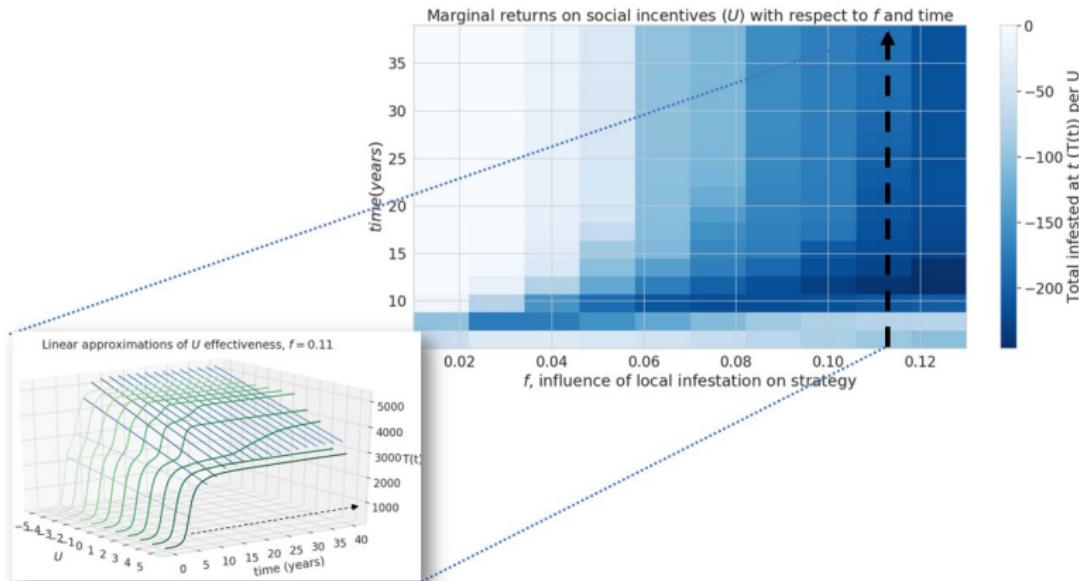


Figure: The influence of infestation on transport strategy, f , can hinder the intervention by public outreach, in the long-term (after approximately 20 years). Efficacy of social incentives on infestation after time T . Inset graph shows an example of cross-section along the line $f = 0.11$

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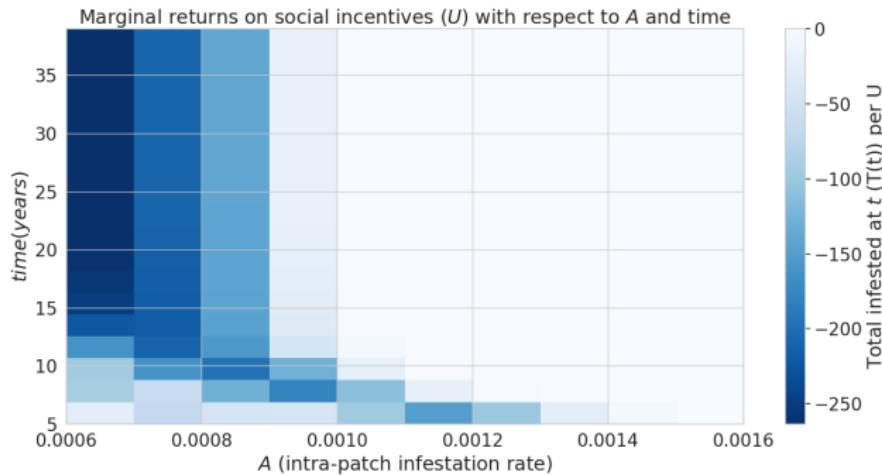


Figure: Increasing U becomes ineffective over time if A is sufficiently large. Efficacy of social incentives on infestation after time period T with respect to A , the intra-patch infestation parameter.

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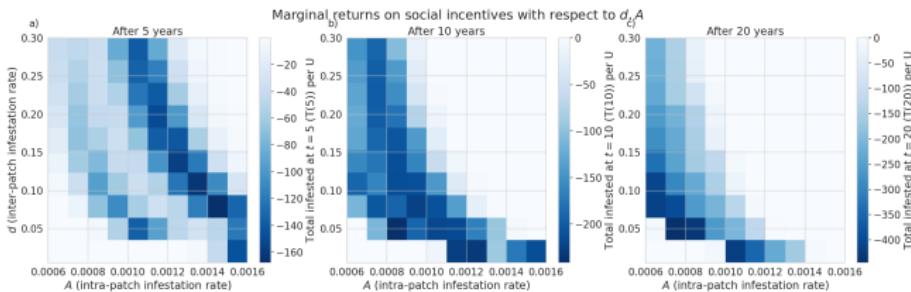


Figure: The social incentive to not transport firewood, U , is more effective with lower pest spread rates. Efficacy of social incentives on infestation after time T intra-patch spreading rate A , affects infestation outcomes.

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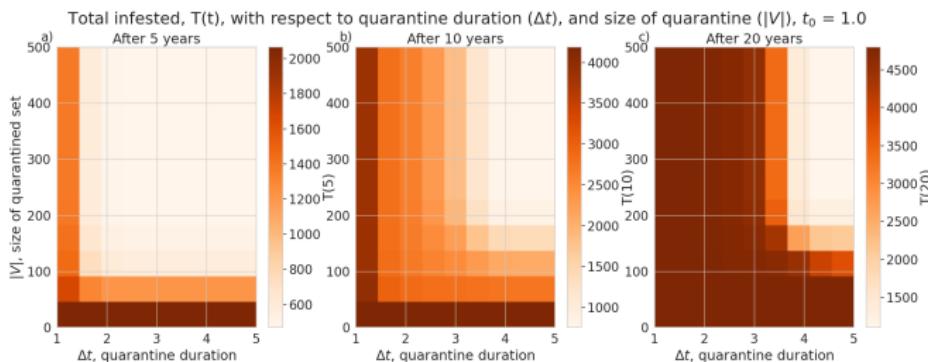


Figure: Quarantine needs to include many patches for long term effects. Average total infested trees ($T(t)$) after 5, 10 and 15 years (panels a), b), and c) respectively), assuming the quarantine begins one year after the pest is introduced.

Discussion

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- Firewood inspection not likely to be effective in implementation
- Education, represented as social incentives, are able to decrease infection in the short term, but dependent on pest-specific parameters
- Patch quarantine can be effective if sufficiently many patches are isolated, and the pest is detected early

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- Wildfire and bark beetles are disturbances integral to coniferous forest ecosystems in the western cordillera of North America (Kaufmann et al., 2008)
- Bark beetle outbreaks have always been destructive, but seem to be worse in recent decades
- Literature on causal relationship between bark beetle outbreaks and wildfire is extensive but inconclusive (Axelson, Alfaro, and Hawkes (2009))
- Existing modelling of these two coupled disturbances is sparse

Project Outline

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- Extend existing model of Duncan et al. (2015) to include wildfires
- Explore parameter regime of extended model
- Introduce forest stand thinning procedures to reduce MPB outbreaks
- Show that these stand thinning procedures are able to work due to increased stand heterogeneity

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$$j_{n+1,1} = dJ_n + I_{n-2} + F_n \quad (6a)$$

$$j_{n+1,k} = (1-d)j_{n,k-1} - \frac{\alpha_1}{T} P_n j_{n,k-1}, \quad k = 2 \dots K-1, K \quad (6b)$$

$$S_{n+1} = S_n + (1-d)j_{n,K} - \left(I_n + \frac{\alpha_2}{T} P_n I_n \right) - \frac{\alpha_2}{T} P_n (S_n + (1-d)j_{n,K}) - \sigma_F \xi_n \quad (6c)$$

$$I_{n+1} = r_1 I_n e^{-\beta_1(T-S_{n+1})} - \frac{\alpha_2}{T} P_n I_n + \sigma_I \xi_n \quad (6d)$$

$$F_{n+1} = P_n \left[\frac{\alpha_1}{T} \sum_{k=1}^{K-1} j_{n,k} + \frac{\alpha_2}{T} (S_n + (1-d)j_{n,K}) + \frac{\alpha_2}{T} I_n \right] + \sigma_F \gamma_n \quad (6e)$$

$$P_n = T - \sum_{i=1}^n F_i e^{-\kappa(n-i)} \quad (6f)$$

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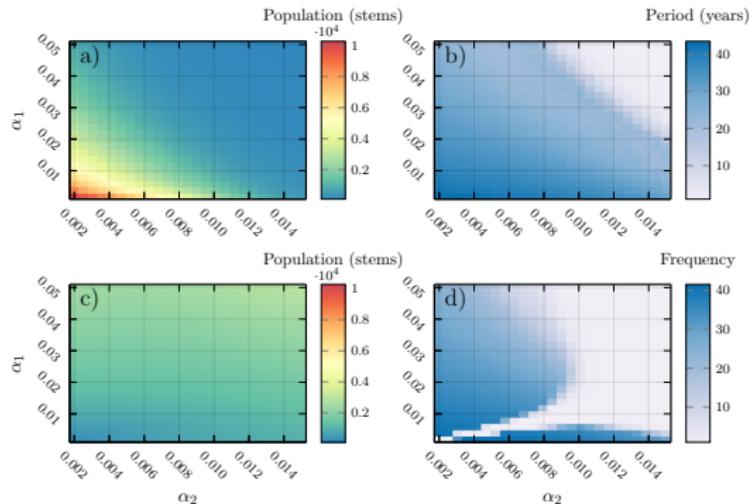


Figure: Increasing burning rates α_1, α_2 reduce MPB outbreak size, cause stability in fire regimes. Panels: a) Average size of largest MPB population, b) Average frequency of MPB outbreaks, c) Average size of largest fire season, d) Average frequency of severe fire seasons. All measured at equilibrium.

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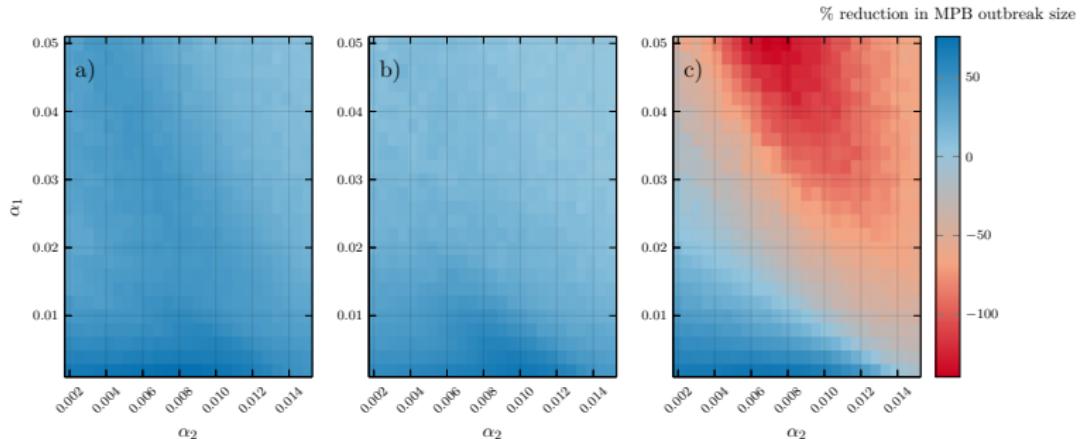


Figure: FTP most effective with small a) $\tau = 0.15, m = 8$, b) with $\tau = 0.15, m = 8$ applied every 5 years, c) controlled burning with $\tau = 0.15, m = 8$, with respect to burning rates α_1, α_2 .

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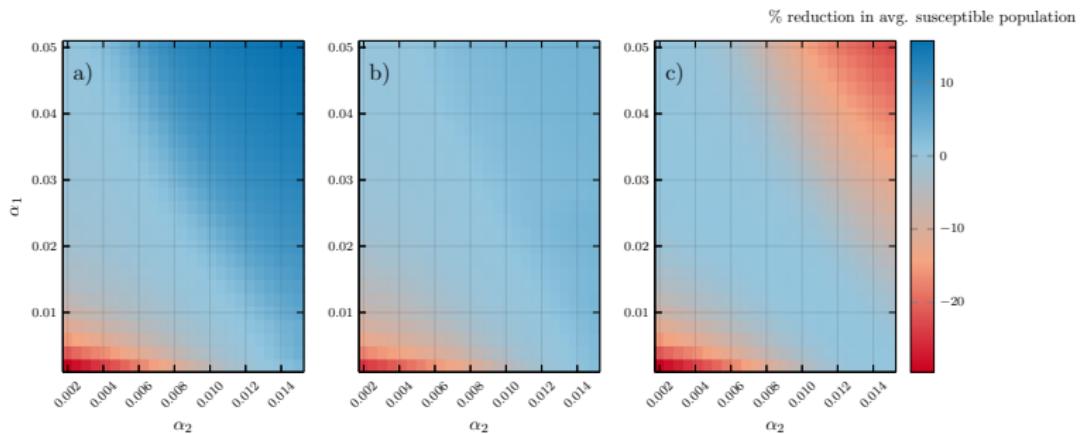


Figure: Percentage change in average susceptible (mature) forest population compared to no FTP with a) $\tau = 0.15, m = 8$, b) with $\tau = 0.15, m = 8$ applied every 5 years, c) controlled burning with $\tau = 0.15, m = 8$, with respect to burning rates α_1, α_2 .

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- We show that increasing fire prevalence is able to dampen MPB outbreaks by increasing stand heterogeneity
- Stand heterogeneity can also be increased through forest thinning or prescribed burning, which also dampens MPB outbreaks.
- These results are consistent with ecological evidence (Seidl et al. (2016) and Kaufmann et al. (2008))

Overall conclusion

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- Chapter 1: developed a disease-behaviour model of COVID-19 to address questions about vaccine prioritization
- Chapter 2: we used a socio-ecological model of forest pest spread to compare the efficacy of measures to prevent invasive pest spread
- Chapter 3: we created a model of coupled MPB and wildfire dynamics to shed light on the stand dynamics of this ecosystem

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References

Thank you!

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