Automatic Verification of Avionic Synchronous Safety Critical Embedded Software

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Motivation



All Computer Scientists Have Experienced Bugs



It is preferable to verify that safety-critical programs do not go wrong before running them.

Static Analysis by Abstract Interpretation

Static analysis: analyse the program at compile-time to verify a program runtime property (e.g. the absence of some categories of bugs)

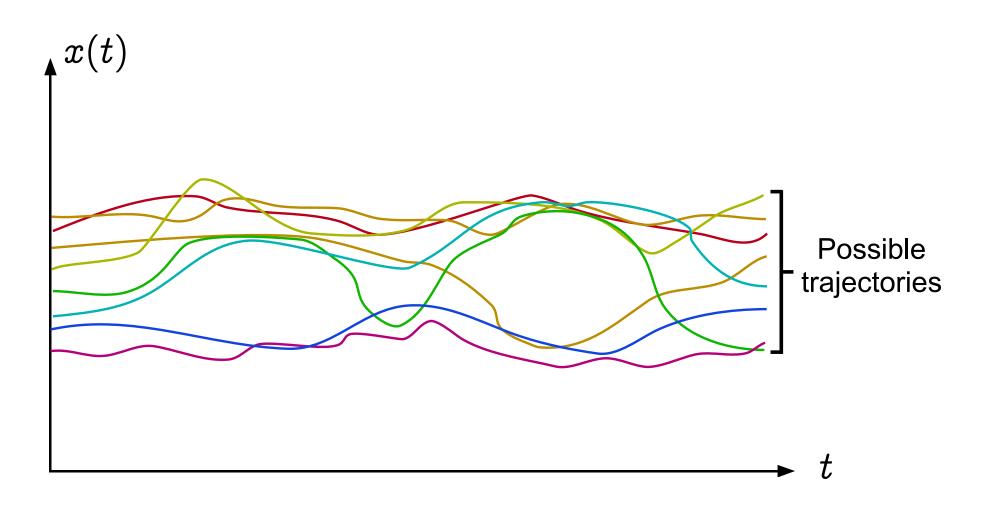
Undecidability \longrightarrow

Abstract interpretation: effectively compute an abstraction/sound approximation of the program semantics,

- which is precise enough to imply the desired property, and
- coarse enough to be efficiently computable.

Abstract Interpretation, Informally

Operational Semantics



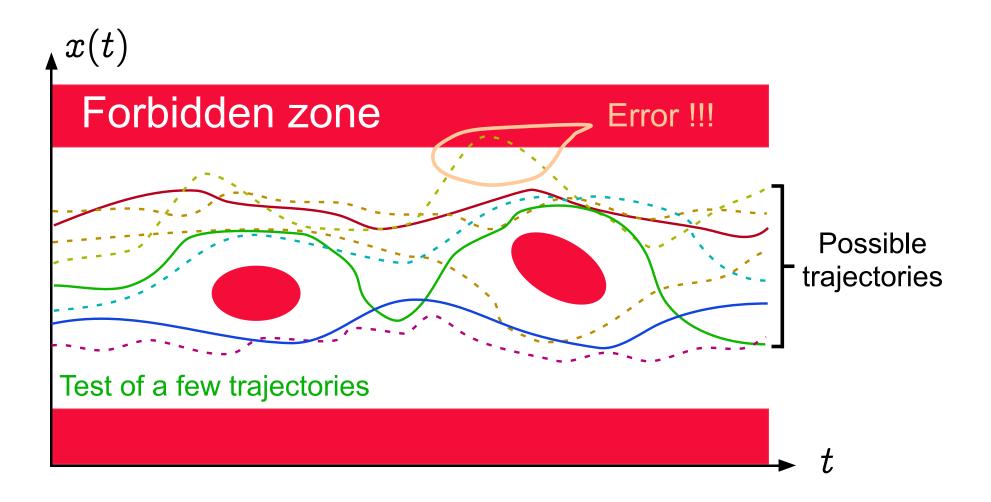


Safety property



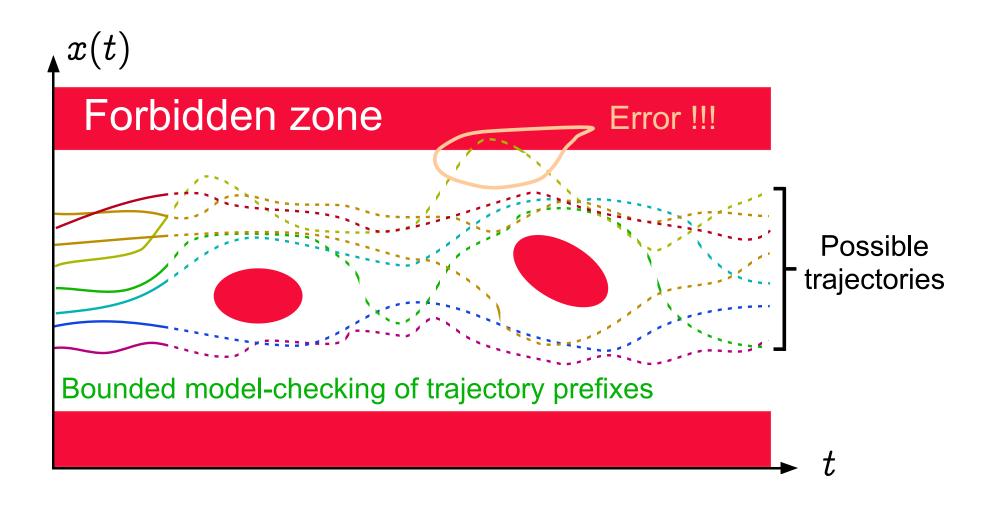


Test/Debugging is Unsafe



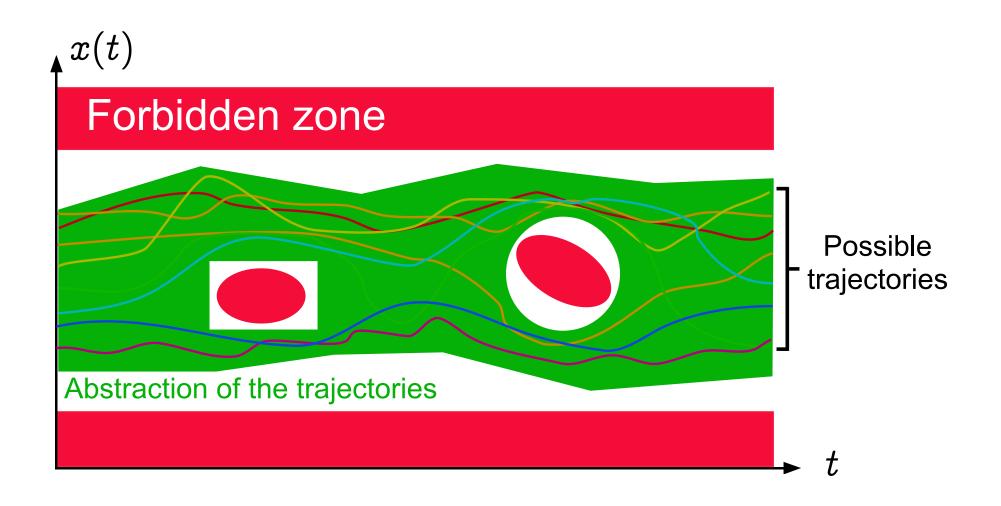


Bounded Model Checking is Unsafe



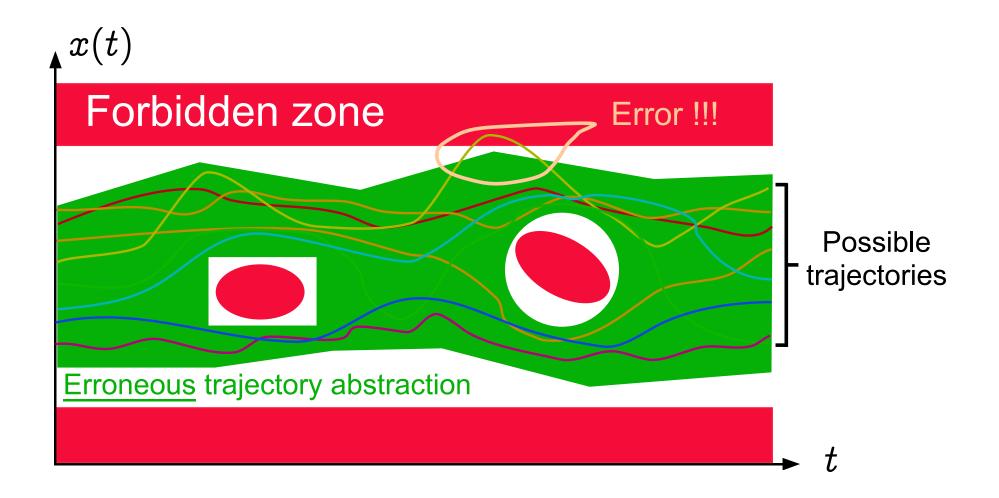


Abstract Interpretation



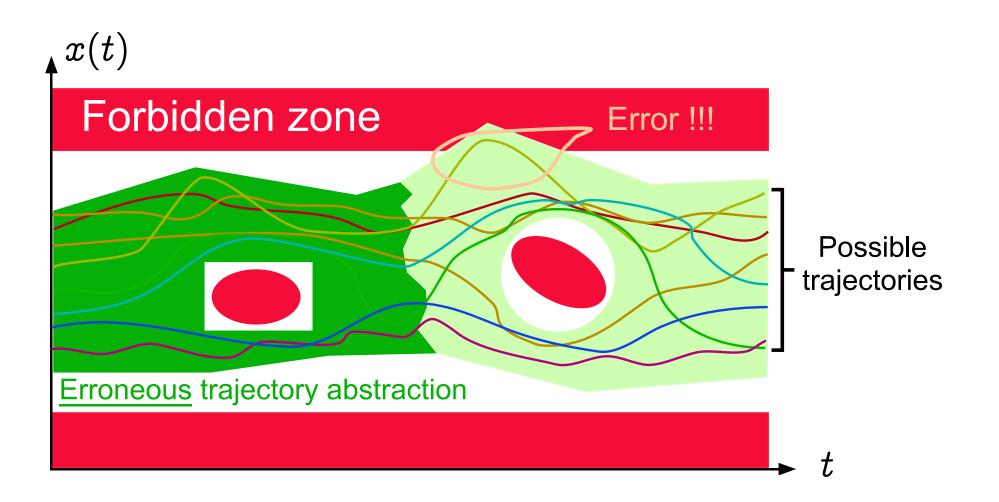


Soundness: Erroneous Abstraction — I



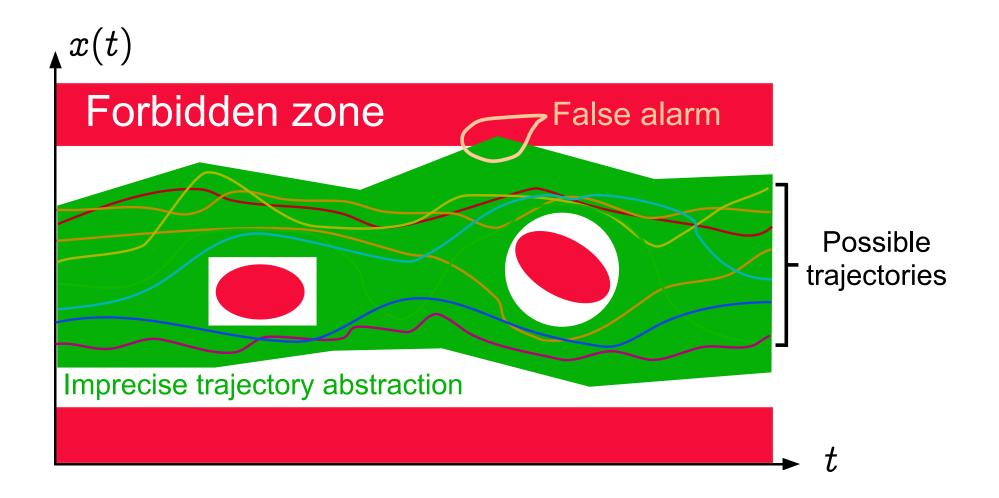


Soundness: Erroneous Abstraction — II





Imprecision \Rightarrow False Alarms



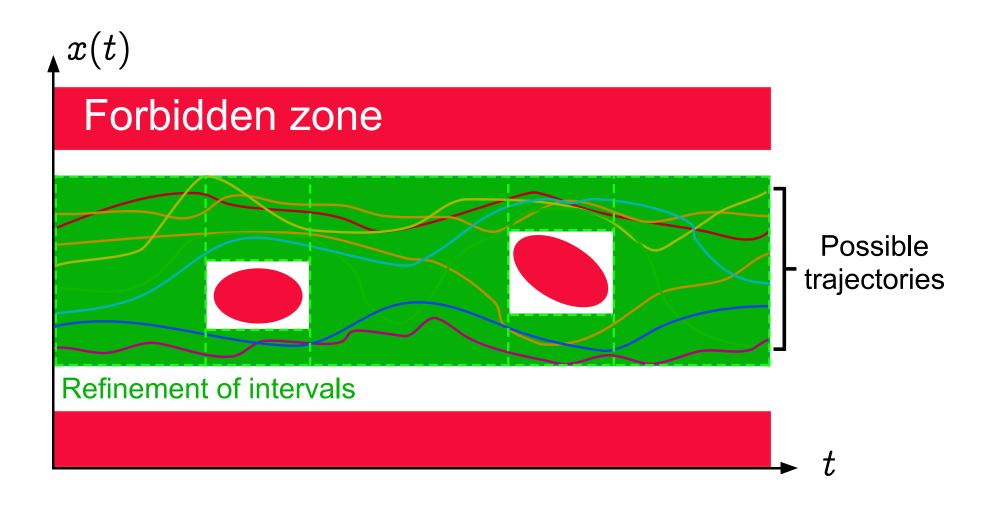


Interval Abstraction \Rightarrow False Alarms

x(t)Forbidden zone False alarms Possible trajectories Imprecise trajectory abstraction by intervals



Refinement by Partitionning





Abstract Interpretation, formal sketch

Reference

- [POPL'77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In 4^{th} ACM POPL.
- [Thesis '78] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse ès sci. math. Grenoble, march 1978.
- [POPL '79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In 6^{th} ACM POPL.



Syntax of Programs

```
variables X \in \mathbb{X}
                                                  types T\in\mathbb{T}
E
                                                  arithmetic expressions E \in \mathbb{E}
                                                  boolean expressions B \in \mathbb{B}
D ::= T X;
                                                  \text{declarations } D \in \mathbb{D}, \quad \text{vars}(D) = \{X\}
     \mid TX;D'
                                                  X \not\in \mathrm{vars}(D'), \, \mathrm{vars}(D) = \{X\} \cup \mathrm{vars}(D')
C ::= X = E;
                                                  commands C \in \mathbb{C} \quad (E \prec C)
          while B C'
                                                    (B \prec C, C' \prec C)
          if B C'
                                                     (B \prec C, C' \prec C)
          if B C' else C'' (B \prec C, C' \prec C, C'' \prec C)
      \{ \mathbf{C}_1 \ldots \mathbf{C}_n \}, (n \geq 0) \qquad (C_1 \prec C, \ldots, C_n \prec C)
P ::= D C
                                                  \operatorname{program}\ P\in\mathbb{P}\quad (C\prec P)
```



Concrete Semantic Domain of Programs

Reachability properties:

program properties where \subseteq is implication, \emptyset is false, \cup is disjunction.

Concrete Reachability Semantics of Programs

$$\mathcal{S}[\![X=E;]\!]R \stackrel{\mathrm{def}}{=} \{
ho[X\leftarrow\mathcal{E}[\![E]\!]
ho] \mid
ho\in R\cap\mathrm{dom}(E)\}$$
 $ho[X\leftarrow v](X) \stackrel{\mathrm{def}}{=} v, \qquad
ho[X\leftarrow v](Y) \stackrel{\mathrm{def}}{=}
ho(Y)$
 $\mathcal{S}[\![if\ B\ C']\!]R \stackrel{\mathrm{def}}{=} \mathcal{S}[\![C']\!](\mathcal{B}[\![B]\!]R) \cup \mathcal{B}[\![\neg B]\!]R$
 $\mathcal{B}[\![B]\!]R \stackrel{\mathrm{def}}{=} \{
ho\in R\cap\mathrm{dom}(B)\mid B\ \mathrm{holds\ in\ }
ho\}$
 $\mathcal{S}[\![if\ B\ C'\ \mathrm{else}\ C'']\!]R \stackrel{\mathrm{def}}{=} \mathcal{S}[\![C']\!](\mathcal{B}[\![B]\!]R) \cup \mathcal{S}[\![C'']\!](\mathcal{B}[\![\neg B]\!]R)$
 $\mathcal{S}[\![\mathrm{while}\ B\ C']\!]R \stackrel{\mathrm{def}}{=} \mathrm{let}\ \mathcal{W} = \mathrm{lfp}_0^{\subseteq}\ \lambda\mathcal{X}\cdot R \cup \mathcal{S}[\![C']\!](\mathcal{B}[\![B]\!]\mathcal{X})$
 $\mathrm{in\ }(\mathcal{B}[\![\neg B]\!]\mathcal{W})$
 $\mathcal{S}[\![\{\}\}]\!]R \stackrel{\mathrm{def}}{=} R$
 $\mathcal{S}[\![\{C_1\dots C_n\}]\!]R \stackrel{\mathrm{def}}{=} \mathcal{S}[\![C_n]\!] \circ \dots \circ \mathcal{S}[\![C_1]\!] \quad n>0$
 $\mathcal{S}[\![D\ C]\!]R \stackrel{\mathrm{def}}{=} \mathcal{S}[\![C]\!](\mathcal{S}[\![D]\!]) \quad (\mathrm{uninitialized\ variables})$

Example: Abstract Semantic Domain of Programs

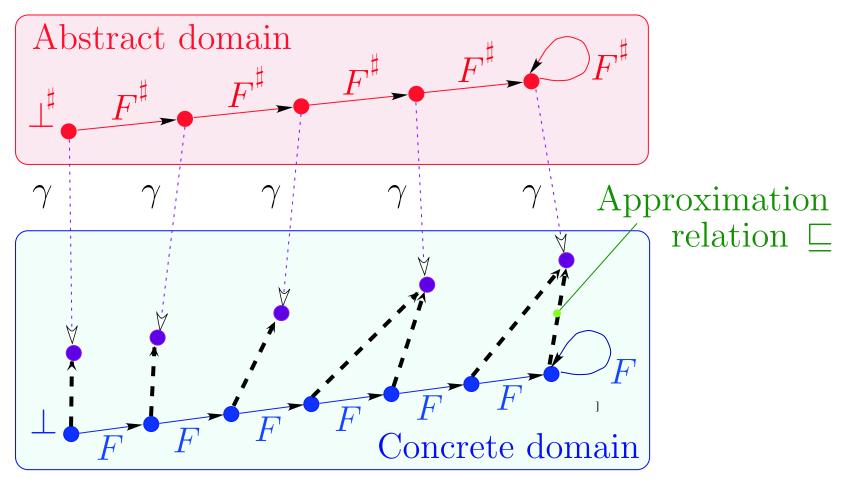
$$\langle \mathcal{D}^{\sharp} \llbracket P
rbracket, \perp, \perp \rangle$$

such that:

$$\langle \mathcal{D}, \subseteq \rangle \xrightarrow{\gamma} \langle \mathcal{D}^{\sharp} \llbracket P \rrbracket, \sqsubseteq \rangle$$

hence $\langle \mathcal{D}^{\sharp} \llbracket P \rrbracket$, \sqsubseteq , \bot , $\sqcup \rangle$ is a complete lattice such that $\bot = \alpha(\emptyset)$ and $\sqcup X = \alpha(\cup \gamma(X))$

Approximate Fixpoint Abstraction



$$F\circ\gamma\sqsubseteq\;\gamma\circ F^\sharp\;\Rightarrow\;\mathsf{lfp}\,F\sqsubseteq\gamma(\mathsf{lfp}\,F^\sharp)$$



Abstract Reachability Semantics of Programs

$$\mathcal{S}^{\sharp} \llbracket X = E; \rrbracket R \stackrel{\text{def}}{=} \alpha(\{\rho[X \leftarrow \mathcal{E}\llbracket E \rrbracket \rho] \mid \rho \in \gamma(R) \cap \text{dom}(E)\})$$

$$\mathcal{S}^{\sharp} \llbracket \text{if } B \ C' \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket R) \sqcup \mathcal{B}^{\sharp} \llbracket \neg B \rrbracket R$$

$$\mathcal{B}^{\sharp} \llbracket B \rrbracket R \stackrel{\text{def}}{=} \alpha(\{\rho \in \gamma(R) \cap \text{dom}(B) \mid B \text{ holds in } \rho\})$$

$$\mathcal{S}^{\sharp} \llbracket \text{if } B \ C' \text{ else } C'' \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket R) \sqcup \mathcal{S}^{\sharp} \llbracket C'' \rrbracket (\mathcal{B}^{\sharp} \llbracket \neg B \rrbracket R)$$

$$\mathcal{S}^{\sharp} \llbracket \text{while } B \ C' \rrbracket R \stackrel{\text{def}}{=} \text{let } \mathcal{W} = \text{Ifp}_{\bot}^{\sqsubseteq} \lambda \mathcal{X} \cdot R \sqcup \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket \mathcal{X})$$

$$\text{in } (\mathcal{B}^{\sharp} \llbracket \neg B \rrbracket \mathcal{W})$$

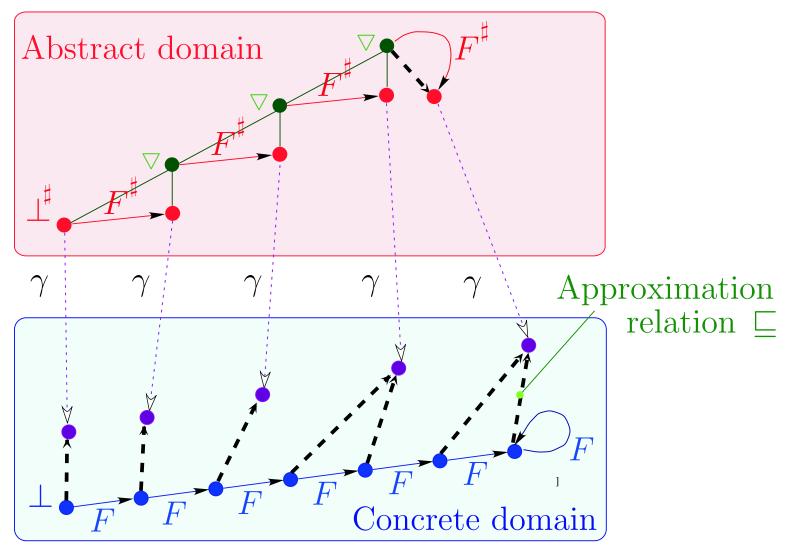
$$\mathcal{S}^{\sharp} \llbracket \{\} \rrbracket R \stackrel{\text{def}}{=} R$$

$$\mathcal{S}^{\sharp} \llbracket \{C_{1} \dots C_{n}\} \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C_{n} \rrbracket \circ \dots \circ \mathcal{S}^{\sharp} \llbracket C_{1} \rrbracket \quad n > 0$$

$$\mathcal{S}^{\sharp} \llbracket D \ C \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C \rrbracket (\top) \quad \text{(uninitialized variables)}$$



Convergence Acceleration with Widening





Example: Abstract Semantics with Convergence Acceleration ¹

$$\mathcal{S}^{\sharp} \llbracket X = E; \rrbracket R \stackrel{\text{def}}{=} \alpha(\{\rho[X \leftarrow \mathcal{E}\llbracket E \rrbracket \rho] \mid \rho \in \gamma(R) \cap \text{dom}(E)\})$$

$$\mathcal{S}^{\sharp} \llbracket \text{if } B C' \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket R) \sqcup \mathcal{B}^{\sharp} \llbracket \neg B \rrbracket R$$

$$\mathcal{B}^{\sharp} \llbracket B \rrbracket R \stackrel{\text{def}}{=} \alpha(\{\rho \in \gamma(R) \cap \text{dom}(B) \mid B \text{ holds in } \rho\})$$

$$\mathcal{S}^{\sharp} \llbracket \text{if } B C' \text{ else } C'' \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket R) \sqcup \mathcal{S}^{\sharp} \llbracket C'' \rrbracket (\mathcal{B}^{\sharp} \llbracket \neg B \rrbracket R)$$

$$\mathcal{S}^{\sharp} \llbracket \text{while } B C' \rrbracket R \stackrel{\text{def}}{=} \text{let } \mathcal{F}^{\sharp} = \lambda \mathcal{X} \cdot \text{let } \mathcal{Y} = R \sqcup \mathcal{S}^{\sharp} \llbracket C' \rrbracket (\mathcal{B}^{\sharp} \llbracket B \rrbracket \mathcal{X})$$

$$\text{in if } \mathcal{Y} \sqsubseteq \mathcal{X} \text{ then } \mathcal{X} \text{ else } \mathcal{X} \bigvee \mathcal{Y}$$

$$\text{and } \mathcal{W} = \text{Ifp}_{\bot}^{\sqsubseteq} \mathcal{F}^{\sharp} \text{ in } (\mathcal{B}^{\sharp} \llbracket \neg B \rrbracket \mathcal{W})$$

$$\mathcal{S}^{\sharp} \llbracket \{\} \rrbracket R \stackrel{\text{def}}{=} R$$

$$\mathcal{S}^{\sharp} \llbracket \{C_{1} \ldots C_{n}\} \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C_{n} \rrbracket \circ \ldots \circ \mathcal{S}^{\sharp} \llbracket C_{1} \rrbracket \quad n > 0$$

$$\mathcal{S}^{\sharp} \llbracket D C \rrbracket R \stackrel{\text{def}}{=} \mathcal{S}^{\sharp} \llbracket C \rrbracket (\top) \quad \text{(uninitialized variables)}$$

¹ Note: \mathcal{F}^{\sharp} not monotonic!





Applications of Abstract Interpretation

Applications of Abstract Interpretation

- Static Program Analysis [POPL '77], [POPL '78], [POPL '79] including Dataflow Analysis [POPL '79], [POPL '00], Setbased Analysis [FPCA '95], Predicate Abstraction [Manna's festschrift '03], ...
- Syntax Analysis [TCS 290(1) 2002]
- Hierarchies of Semantics (including Proofs) [POPL '92], [TCS 277(1–2) 2002]
- Typing & Type Inference [POPL '97]

Applications of Abstract Interpretation (Cont'd)

- (Abstract) Model Checking [POPL '00]
- Program Transformation [POPL '02]
- Software Watermarking [POPL '04]
- Bisimulations [RT-ESOP '04]

All these techniques involve sound approximations that can be formalized by abstract interpretation

A Practical Application of Abstract Interpretation to the Verification of Safety Critical Embedded Control-Command Software

Reference

- [1] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. Design and implementation of a special-purpose static program analyzer for safety-critical real-time embedded software. The Essence of Computation: Complexity, Analysis, Transformation. Essays Dedicated to Neil D. Jones, LNCS 2566, pages 85–108. Springer, 2002.
- [2] B. Blanchet, P. Cousot, R. Cousot, J. Feret, L. Mauborgne, A. Miné, D. Monniaux, and X. Rival. A static analyzer for large safety-critical software. PLDI'03, San Diego, June 7–14, ACM Press, 2003.



ASTRÉE: A Sound, Automatic, Specializable, Domain-Aware, Parametric, Modular, Efficient and Precise Static Program Analyzer

www.astree.ens.fr

- C programs:
 - with
 - * pointers (including on functions), structures and arrays
 - * floating point computations
 - * tests, loops and function calls
 - * limited branching (forward goto, break, continue)



• without

- union
- dynamic memory allocation
- recursive function calls
- backward branching
- conflict side effects
- C libraries
- Application Domain: safety critical embedded real-time synchronous software for non-linear control of very complex control/command systems.

Concrete Operational Semantics

- International norm of C (ISO/IEC 9899:1999)
- restricted by implementation-specific behaviors depending upon the machine and compiler (e.g. representation and size of integers, IEEE 754-1985 norm for floats and doubles)
- restricted by user-defined programming guidelines (such as no modular arithmetic for signed integers, even though this might be the hardware choice)
- restricted by program specific user requirements (e.g. assert)

Abstract Semantics

- Reachable states for the concrete operational semantics
- Volatile environment is specified by a *trusted* configuration file.

Implicit Specification: Absence of Runtime Errors

- No violation of the norm of C (e.g. array index out of bounds)
- No implementation-specific undefined behaviors (e.g. maximum short integer is 32767)
- No violation of the programming guidelines (e.g. static variables cannot be assumed to be initialized to 0)
- No violation of the programmer assertions (must all be statically verified).

Example application

 Primary flight control software of the Airbus A340/A380 fly-by-wire system





- C program, automatically generated from a proprietary high-level specification (à la Simulink/SCADE)
- A340 family: 132,000 lines, 75,000 LOCs after preprocessing, 10,000 global variables, over 21,000 after expansion of small arrays
- A380: × 3

The Class of Considered Periodic Synchronous Programs

declare volatile input, state and output variables; initialize state and output variables;

loop forever

- read volatile input variables,
- compute output and state variables,
- write to volatile output variables;
 wait for clock ();

end loop

- Requirements: the only interrupts are clock ticks;
- Execution time of loop body less than a clock tick [3].

Reference

[3] C. Ferdinand, R. Heckmann, M. Langenbach, F. Martin, M. Schmidt, H. Theiling, S. Thesing, and R. Wilhelm. Reliable and precise WCET determination for a real-life processor. *ESOP* (2001), LNCS 2211, 469–485.



Characteristics of the ASTRÉE Analyzer

- Static: compile time analysis (\neq run time analysis Rational Purify, Parasoft Insure++)
- Program Analyzer: analyzes programs not micromodels of programs (\neq PROMELA in SPIN or Alloy in the Alloy Analyzer)
- Automatic: no end-user intervention needed (\neq ESC Java, ESC Java 2)
- **Sound:** covers the whole state space (\neq MAGIC, CBMC) so never omit potential errors (\neq UNO, CMC from coverity.com) or sort most probable ones (\neq Splint)

Characteristics of the ASTRÉE Analyzer (Cont'd)

Multiabstraction: uses many numerical/symbolic abstract domains (\neq symbolic constraints in Bane or the canonical abstraction of TVLA)

Infinitary: all abstractions use infinite abstract domains with widening/narrowing (\neq model checking based analyzers such as VeriSoft, Bandera, Java PathFinder)

Efficient: always terminate (\neq counterexample-driven automatic abstraction refinement BLAST, SLAM)

Characteristics of the ASTRÉE Analyzer (Cont'd)

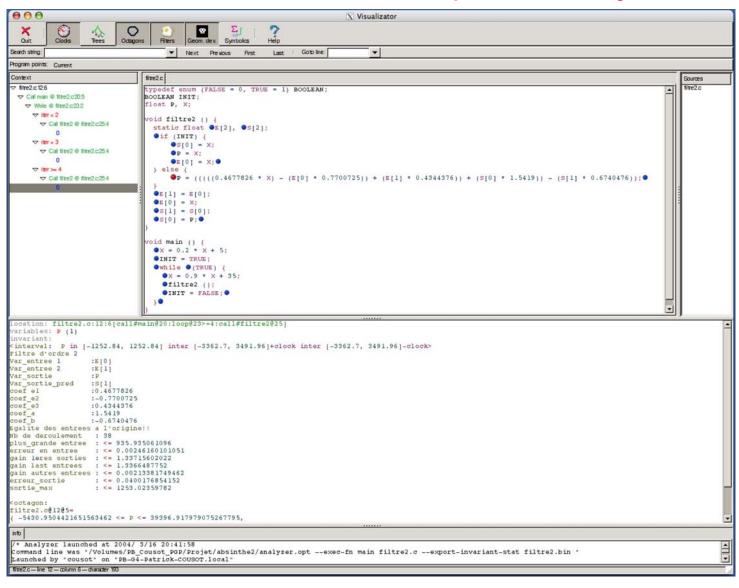
- Specializable: can easily incorporate new abstractions (and reduction with already existing abstract domains) (\neq general-purpose analyzers PolySpace Verifier)
- Domain-Aware: knows about control/command (e.g. digital filters) (as opposed to specialization to a mere programming style in C Global Surveyor)
- Parametric: the precision/cost can be tailored to user needs by options and directives in the code

Characteristics of the ASTRÉE Analyzer (Cont'd)

Automatic Parametrization: the generation of parametric directives in the code can be programmed (to be specialized for a specific application domain)

Modular: an analyzer instance is built by selection of O-CAML modules from a collection each implementing an abstract domain

Example of Analysis Session





Benchmarks (Airbus A340 Primary Flight Control Software)

- 132,000 lines, 75,000 LOCs after preprocessing
- Comparative results (commercial software):

```
4,200 (false?) alarms,
```

3.5 days;

• Our results:

```
alarms,40mn on 2.8 GHz PC,300 Megabytes
```

→ A world première!

(Airbus <u>A380</u> Primary Flight Control Software)

- 350,000 lines
- $\underline{\underline{0}}$ alarms (last week!),

7h² on 2.8 GHz PC,

1 Gigabyte

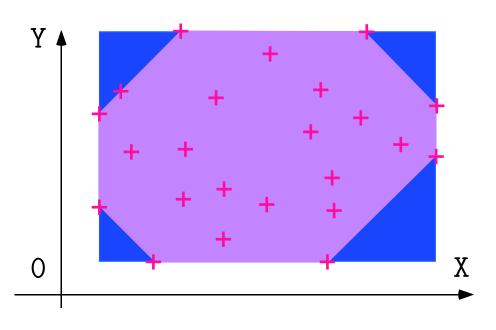
→ A world grand première!

² We are still in a phase where we favour precision rather than computation costs, and this should go down. For example, the A340 analysis went up to 5 h, before being reduced by requiring less precision while still getting no false alarm.



Examples of Abstractions

General-Purpose Abstract Domains: Intervals and Octagons



$$\left\{egin{array}{l} 1 \leq x \leq 9 \ 1 \leq y \leq 20 \end{array}
ight.$$

Octagons [4]:

$$\left\{egin{array}{l} 1 \leq x \leq 9 \ x+y \leq 77 \ 1 \leq y \leq 20 \ x-y \leq 04 \end{array}
ight.$$

Difficulties: many global variables, arrays (smashed or not), IEEE 754 floating-point arithmetic (in program <u>and</u> analyzer) [5]

Reference _

- [4] A. Miné. A New Numerical Abstract Domain Based on Difference-Bound Matrices. In *PADO'2001*, LNCS 2053, Springer, 2001, pp. 155–172.
- [5] A. Miné. Relational abstract domains for the detection of floating-point run-time errors. In ESOP'04, Barcelona, LNCS 2986, pp. 1—17, Springer, 2004.



Floating-Point Computations

• Code Sample:

```
/* float-error.c */
int main () {
  float x, y, z, r;
  x = 1.00000019e+38;
  y = x + 1.0e21;
  z = x - 1.0e21;
  r = y - z;
  printf("%f\n", r);
} % gcc float-error.c
% ./a.out
0.00000
```

$$(x+a)-(x-a)\neq 2a$$

```
/* double-error.c */
int main () {
double x; float y, z, r;
/* x = ldexp(1.,50) + ldexp(1.,26); */
x = 1125899973951488.0;
y = x + 1;
z = x - 1;
r = y - z;
printf("%f\n", r);
% gcc double-error.c
% ./a.out
134217728.000000
```

Symbolic abstract domain

- Interval analysis: if $x \in [a, b]$ and $y \in [c, d]$ then $x y \in [a c, b d]$ so if $x \in [0, 100]$ then $x x \in [-100, 100]!!!$
- The symbolic abstract domain propagates the symbolic values of variables and performs simplifications;
- Must maintain the maximal possible rounding error for float computations (overestimated with intervals);



Clock Abstract Domain for Counters

• Code Sample:

```
R = 0;
while (1) {
  if (I)
    { R = R+1; }
  else
    { R = 0; }
  T = (R>=n);
  wait_for_clock ();
}
```

- Output T is true iff the volatile input I has been true for the last n clock ticks.
- The clock ticks every s seconds for at most h hours, thus R is bounded.
- To prove that R cannot overflow, we must prove that R cannot exceed the elapsed clock ticks (impossible using only intervals).

• Solution:

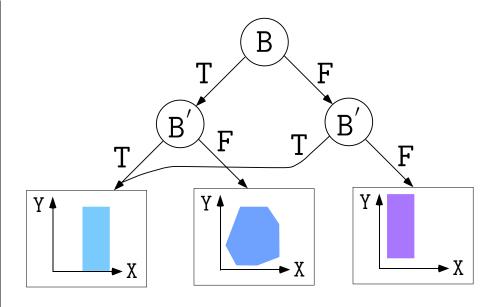
- We add a phantom variable clock in the concrete user semantics to track elapsed clock ticks.
- For each variable X, we abstract three intervals: X, X+clock, and X-clock.
- If X+clock or X-clock is bounded, so is X.



Boolean Relations for Boolean Control

• Code Sample:

```
/* boolean.c */
typedef enum {F=0,T=1} BOOL;
BOOL B;
void main () {
  unsigned int X, Y;
  while (1) {
    B = (X == 0);
    if (!B) {
      Y = 1 / X;
```



The boolean relation abstract domain is parameterized by the height of the decision tree (an analyzer option) and the abstract domain at the leafs



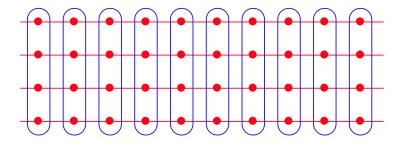
Control Partitionning for Case Analysis

• Code Sample:

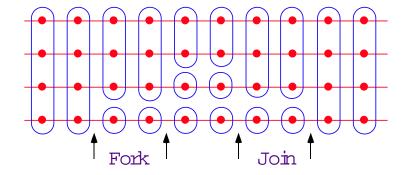
```
/* trace_partitionning.c */
void main() {
  float t[5] = {-10.0, -10.0, 0.0, 10.0, 10.0};
  float c[4] = {0.0, 2.0, 2.0, 0.0};
  float d[4] = {-20.0, -20.0, 0.0, 20.0};
  float x, r;
  int i = 0;
  ... found invariant -100 \le x \le 100 ...

while ((i < 3) && (x >= t[i+1])) {
    i = i + 1;
  }
  r = (x - t[i]) * c[i] + d[i];
}
```

Control point partitionning:

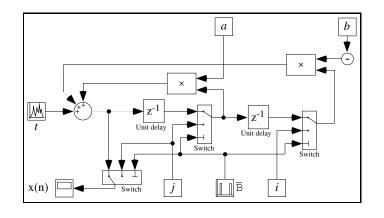


Trace partitionning:



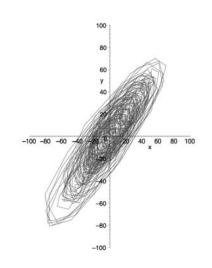
Delaying abstract unions in tests and loops is more precise for non-distributive abstract domains (and much less expensive than disjunctive completion).

2^d Order Digital Filter:

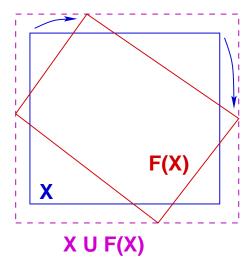


Ellipsoid Abstract Domain for Filters

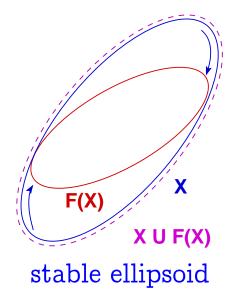
- ullet Computes $X_n = \left\{egin{array}{l} lpha X_{n-1} + eta X_{n-2} + Y_n \ I_n \end{array}
 ight.$
- The concrete computation is bounded, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an ellipsoid.



execution trace



unstable interval





```
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
                                                 Filter Example [6]
BOOLEAN INIT; float P, X;
void filter () {
  static float E[2], S[2];
  if (INIT) { S[O] = X; P = X; E[O] = X; }
  else { P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4))
             + (S[0] * 1.5)) - (S[1] * 0.7)); }
 E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;
 /* S[0], S[1] in [-1327.02698354, 1327.02698354] */
void main () { X = 0.2 * X + 5; INIT = TRUE;
  while (1) {
    X = 0.9 * X + 35; /* simulated filter input */
    filter (): INIT = FALSE: }
```

Reference

[6] J. Feret. Static analysis of digital filters. In ESOP'04, Barcelona, LNCS 2986, pp. 33—-48, Springer, 2004.



(Automatic) Parameterization

- All abstract domains of ASTRÉE are parameterized, e.g.
 - variable packing for octagones and decision trees,
 - partition/merge program points,
 - loop unrollings,
 - thresholds in widenings, ...;
- End-users can either parameterize by hand (analyzer options, directives in the code), or
- choose the automatic parameterization (default options, directives for pattern-matched predefined program schemata).

The main loop invariant for the A340

A textual file over 4.5 Mb with

- 6,900 boolean interval assertions ($x \in [0; 1]$)
- 9,600 interval assertions $(x \in [a; b])$
- 25,400 clock assertions $(x+\text{clk} \in [a;b] \land x-\text{clk} \in [a;b])$
- 19,100 additive octagonal assertions $(a \le x + y \le b)$
- 19,200 subtractive octagonal assertions ($a \le x y \le b$)
- 100 decision trees
- 60 ellipse invariants, etc ...

involving over 16,000 floating point constants (only 550 appearing in the program text) \times 75,000 LOCs.

Possible origins of imprecision and how to fix it

In case of false alarm, the imprecision can come from:

- Abstract transformers (not best possible) improve algorithm;
- Automatized parametrization (e.g. variable packing)
 improve pattern-matched program schemata;
- Iteration strategy for fixpoints —— fix widening ³;
- Inexpressivity i.e. indispensable local inductive invariant are inexpressible in the abstract → add a new abstract domain to the reduced product (e.g. filters).

³ This can be very hard since at the limit only a precise infinite iteration might be able to compute the proper abstract invariant. In that case, it might be better to design a more refined abstract domain.





Conclusion

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- Most applications of abstract interpretation tolerate a small rate (typically 5 to 15%) of false alarms:
 - Program transformation \rightarrow do not optimize,
 - Typing → reject some correct programs, etc,
 - WCET analysis → overestimate;
- Some applications require no false alarm at all:
 - Program verification.
- Theoretically possible [SARA '00], practically feasible [PLDI '03]

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The Future & Grand Challenges

Future (5 years):

- Asynchronous concurrency (for less critical software)
- Functional properties (reactivity)
- Industrialization

Grand challenge:

- Verification from specifications to machine code (verifying compiler)
- Verification of systems (quasi-synchrony, distribution)

THE END, THANK YOU

More references at URL www.di.ens.fr/~cousot www.astree.ens.fr.





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