

« Software Verification by Abstract Interpretation and the ASTRÉE Static Analyzer »

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Abstract

Abstract interpretation is a theory of sound approximation of the behavior of dynamic systems, in particular the semantics of programming languages. This is the formal basis for automatic correctness proofs by static analysers considering an over-approximation of the set of all possible executions of the program. Contrary to bug-finding methods (e.g. by test, bounded model-checking or error pattern search), no potential error is ever omitted. Hence the proof of satisfaction of a specification is always mathematically valid. Contrary to refinement-based methods, termination is always guaranteed. However, by undecidability of such proofs, the abstraction may yield false alarms whenever a synthesized inductive argument (e.g. a loop invariant) is too weak to make the proof. In this case, some executions considered in the abstract, that is in the over-approximation, might lead to an error while not corresponding to a concrete, that is actual, execution. All the difficulty of the undecidable verification problem is therefore to design safe/sound over-approximations that are coarse enough to be effectively computable by the static analyzer and precise enough to avoid false alarms (the errors leading to true alarms can only be eliminated by correcting the program that does not satisfy the specification).

After a brief introduction to abstract interpretation, we will present the ASTRÉE static analyser (www.astree.ens.fr) for proving the absence of runtime errors (such as buffer overrun, dangling pointer, division by zero, float overflow, modular integer arithmetic overflow, ...) in real-time synchronous control/command C applications. The ASTRÉE static analyser uses generalist abstractions (like intervals, octagons, decision trees, symbolic execution, etc) and abstractions for the specific application domain (to cope with filters, integrators, slow divergences due to rounding errors, etc). Since 2003, these domain-specific abstractions allowed for the verification of the absence of runtime errors in several large avionic software, a world première.

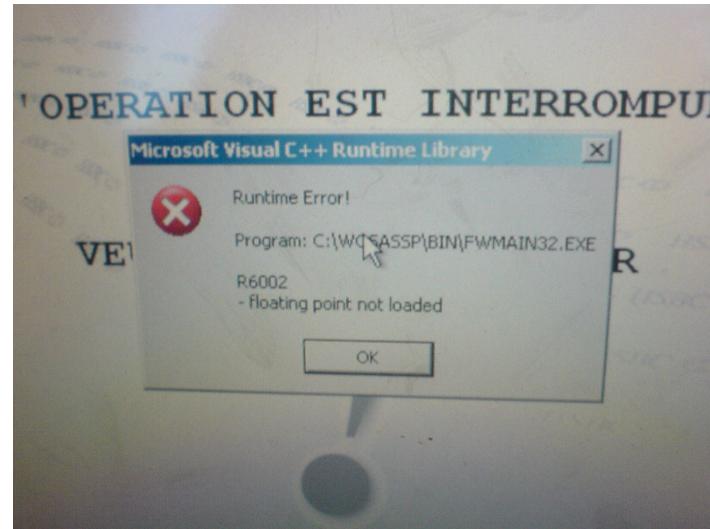
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1. Motivation

Bugs Now Show-Up in Everyday Life

- Bugs now appear frequently in everyday life (banks, cars, telephones, . . .)
- Example (HSBC bank ATM¹ at 19 Boulevard Sébastopol in Paris, failure on Nov. 21st 2006 at 8:30 am):



¹ cash machine, cash dispenser, automatic teller machine.

A Strong Need for Software Better Quality

- Poor software quality is not acceptable in **safety** and **mission critical software** applications.



- The present state of the art in software engineering does not offer sufficient quality guarantees

The Complexity of Software Design

- The design of complex software is difficult and economically critical
- Example (www.designnews.com/article/CA6475332.html):
“Boeing Confirms 787 Delay, Fasteners, Flight Control Software Code Blamed
John Dodge, Editor-in-Chief – Design News, September 5, 2007

Boeing officials confirmed today that a fastener shortage and problems with flight control software have pushed “first flight” of the Boeing 787 Dreamliner to sometime between mid-November and mid-December (see News Releases).

...

The software delays involve Honeywell Aerospace, which is responsible for flight control software. The work on this part of the 787 was simply underestimated, said Bair.”

The Security of Complex Software

- Complex software is subject to security vulnerabilities
- Example (www.wired.com/politics/security/news/2008/01/dreamliner_security)

“FAA: Boeing’s New 787 May Be Vulnerable to Hacker Attack

Kim Zetter, freelance journalist in Oakland, CA, Jan. 4, 2008

Boeing’s new 787 Dreamliner passenger jet may have a serious security vulnerability in its onboard computer networks ...

According to the FAA document published in the Federal Register (mirrored at Cryptome.org), the vulnerability exists because the plane’s computer systems connect the passenger network with the flight-safety, control and navigation network. It also connects to the airline’s business and administrative-support network, which communicates maintenance issues to ground crews.

Tool-Based Software Design Methods

- New tool-based software design methods will have to emerge to face the unprecedented growth and complexification of critical software
- E.g. FCPC (Flight Control Primary Computer)
 - A220: 20 000 LOCs,
 - A340 (V1): 130 000 LOCS
 - A340 (V2): 250 000 LOCS
 - A380: 1.000.000 LOCS
 - A350: static analysis to be integrated in the software production



Static Analysis

A *static analyzer* is a program that

- takes as **input**:
 - a **program** P (written in some given programming language \mathbb{P} with a given semantics $\mathfrak{S}_{\mathbb{P}}$)
 - a **specification** S (implicit $S[P]$ or written in some specification language \mathbb{S} with a given semantics $\mathfrak{S}_{\mathbb{S}}$)
- always *terminates* and delivers *automatically* as **output**:
 - a **diagnosis** on the validity of the program semantics with respect the specification semantics

Difficulties of Static Analysis

- automatic + infinite state + termination \implies undecidable!
- for a programming (and a specification) language, not for a given model of a given program:

$$\forall P \in \mathbb{P} : \forall S \in \mathbb{S} : \mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathcal{S}_{\mathbb{S}}[P, S]?$$

or, more simply for an *implicit specification* $\mathfrak{S}[P]$:

$$\forall P \in \mathbb{P} : \mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathfrak{S}[P]?$$

Soundness and Completeness

- Soundness: for all $P \in \mathbb{P}$, if the answer is yes (no) then $\mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathfrak{S}[P]$ (resp. $\mathfrak{S}_{\mathbb{P}}[P] \not\subseteq \mathfrak{S}[P]$)
- Completeness: for all $P \in \mathbb{P}$, if $\mathfrak{S}_{\mathbb{P}}[P] \subseteq \mathfrak{S}[P]$ ($\mathfrak{S}_{\mathbb{P}}[P] \not\subseteq \mathfrak{S}[P]$) then the answer is yes (resp. no)

We always require SOUNDNESS!

Undecidability \implies no completeness

Problems with Formal Methods

- **Formal specifications** (abstract machines, temporal logic, ...) are costly, complex, error-prone, difficult to maintain, not mastered by casual programmers
- **Formal semantics** of the specification and programming language are inexistant, informal, unrealistic or complex
- **Formal proofs** are partial (static analysis), do not scale up (model checking) or need human assistance (theorem proving & proof assistants)
⇒ **High costs** (for specification, proof assistance, etc).

Avantages of Static Analysis

- Formal specifications are implicit (no need for explicit, user-provided specifications)
- Formal semantics are approximated by the static analyzer (no user-provided models of the program)
- Formal proofs are automatic (no required user-interaction)
- Costs are low (no modification of the software production methodology)
- Scales up to 100.000 to 1.000.000 LOCS
- Rapid and large diffusion in embedded software production industries

Disadvantages of Static Analysis

- **Imprecision** (acceptable in some applications like WCET or program optimization)
- **Incomplete** for program verification
- **False alarms** are due to **unsuccessful automatic proofs** in 5 to 15% of the cases

For example, 1% of 500.000 potential (true or false) alarms is 5.000, too much to be handled by hand!

Remedies to False Alarms in ASTRÉE

- ASTRÉE is specialized to specific program properties²
- ASTRÉE is specialized to real-time synchronous control/command programs written in C
- ASTRÉE offers possibilities of refinement³

The cost of adapting ASTRÉE to a specific program, should be a small fraction of the cost to test the specific program properties verified by ASTRÉE.

² proof of absence of runtime errors

³ parametrizations and analysis directives

2. Informal Introduction to Abstract Interpretation

Abstract Interpretation

There are two **fundamental concepts** in computer science (and in sciences in general) :

- **Abstraction** : to reason on complex systems
- **Approximation** : to make effective undecidable computations

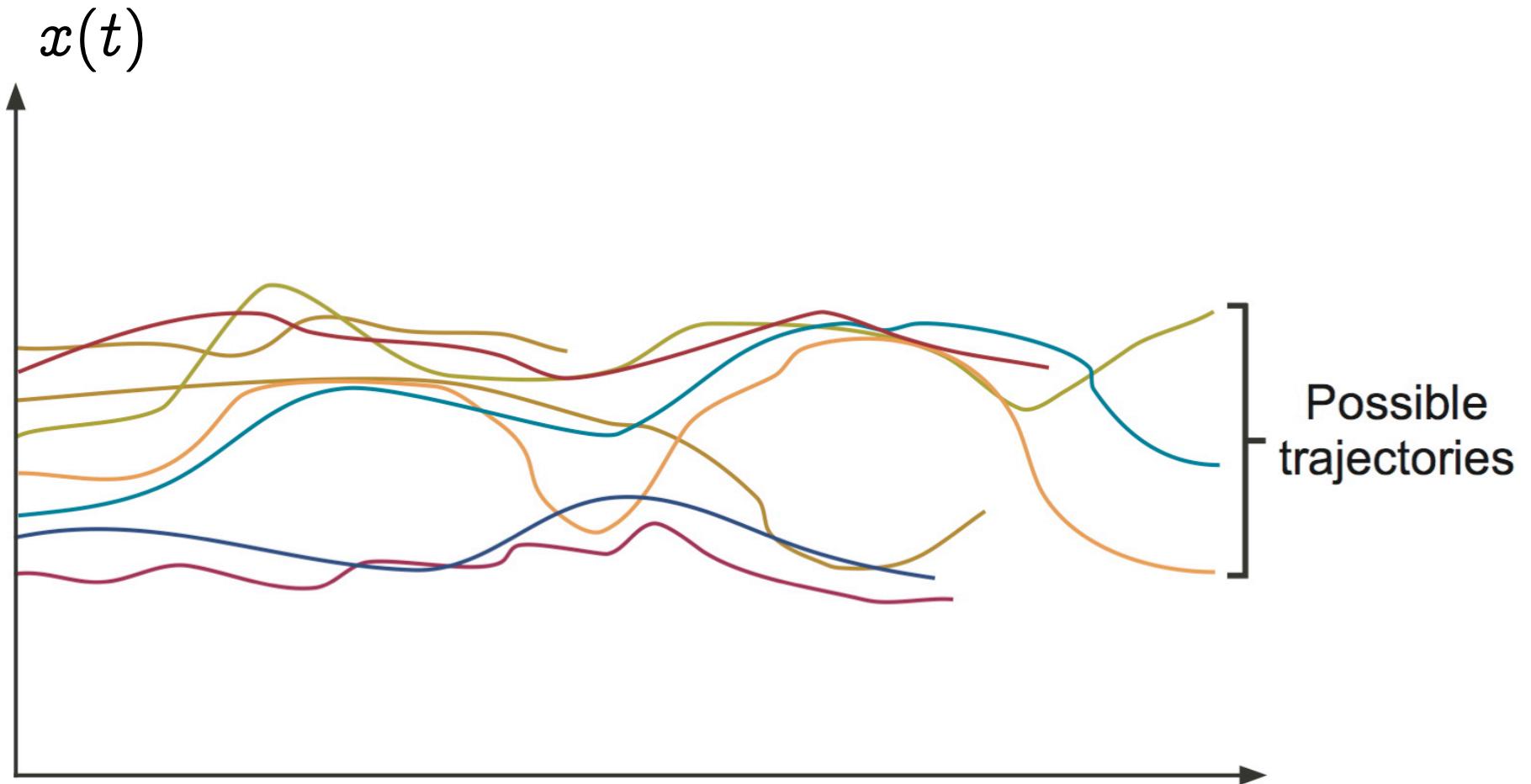
These concepts are formalized by **abstract interpretation** [CC77, Cou78, CC79, Cou81, CC92]

References

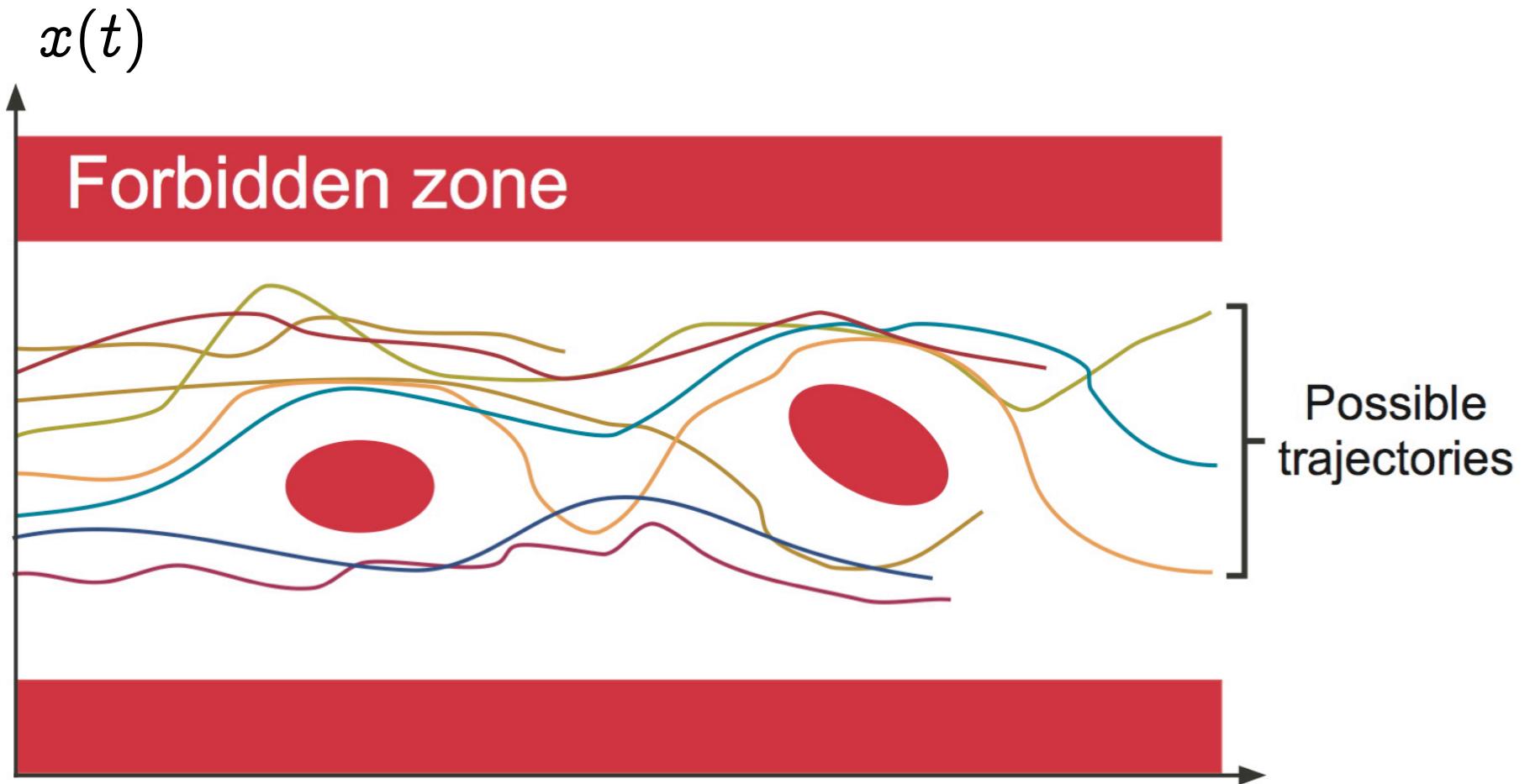
- [POPL '77] P. Cousot and R. Cousot. Abstract interpretation: a unified lattice model for static analysis of programs by construction or approximation of fixpoints. In *4th ACM POPL*.
- [Thesis '78] P. Cousot. Méthodes itératives de construction et d'approximation de points fixes d'opérateurs monotones sur un treillis, analyse sémantique de programmes. Thèse ès sci. math. Grenoble, march 1978.
- [POPL '79] P. Cousot & R. Cousot. Systematic design of program analysis frameworks. In *6th ACM POPL*.

Principle of Abstraction

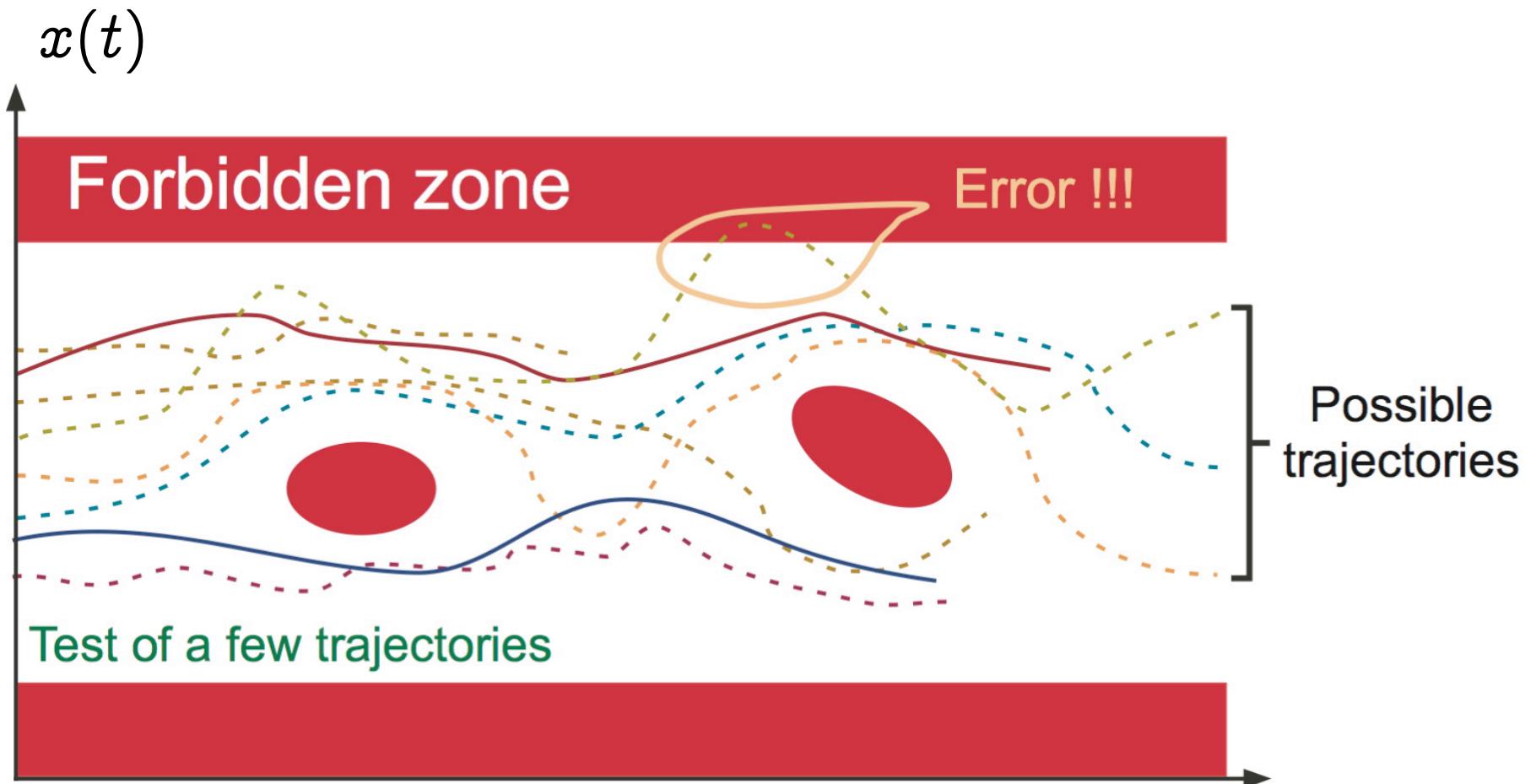
Operational semantics



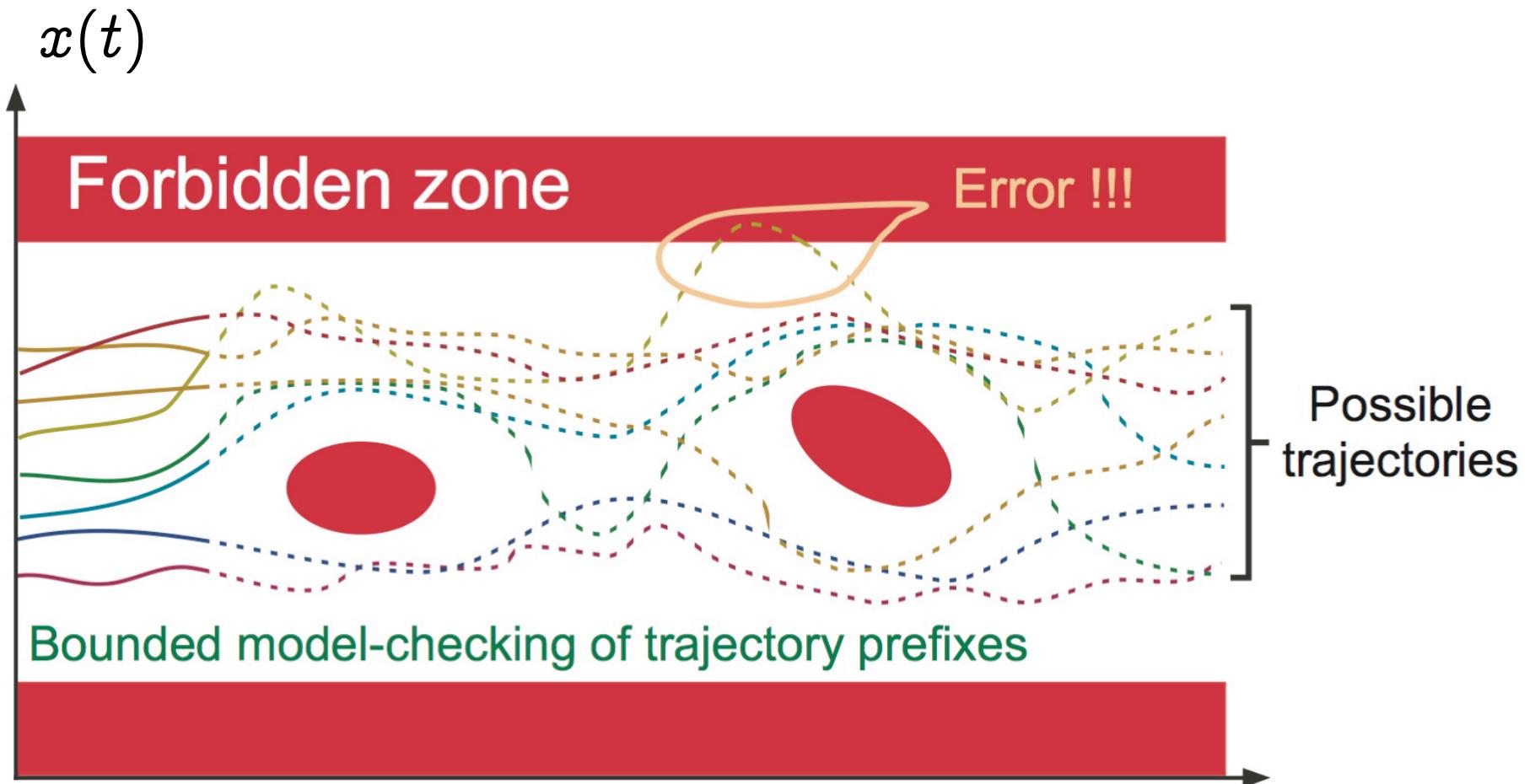
Safety property



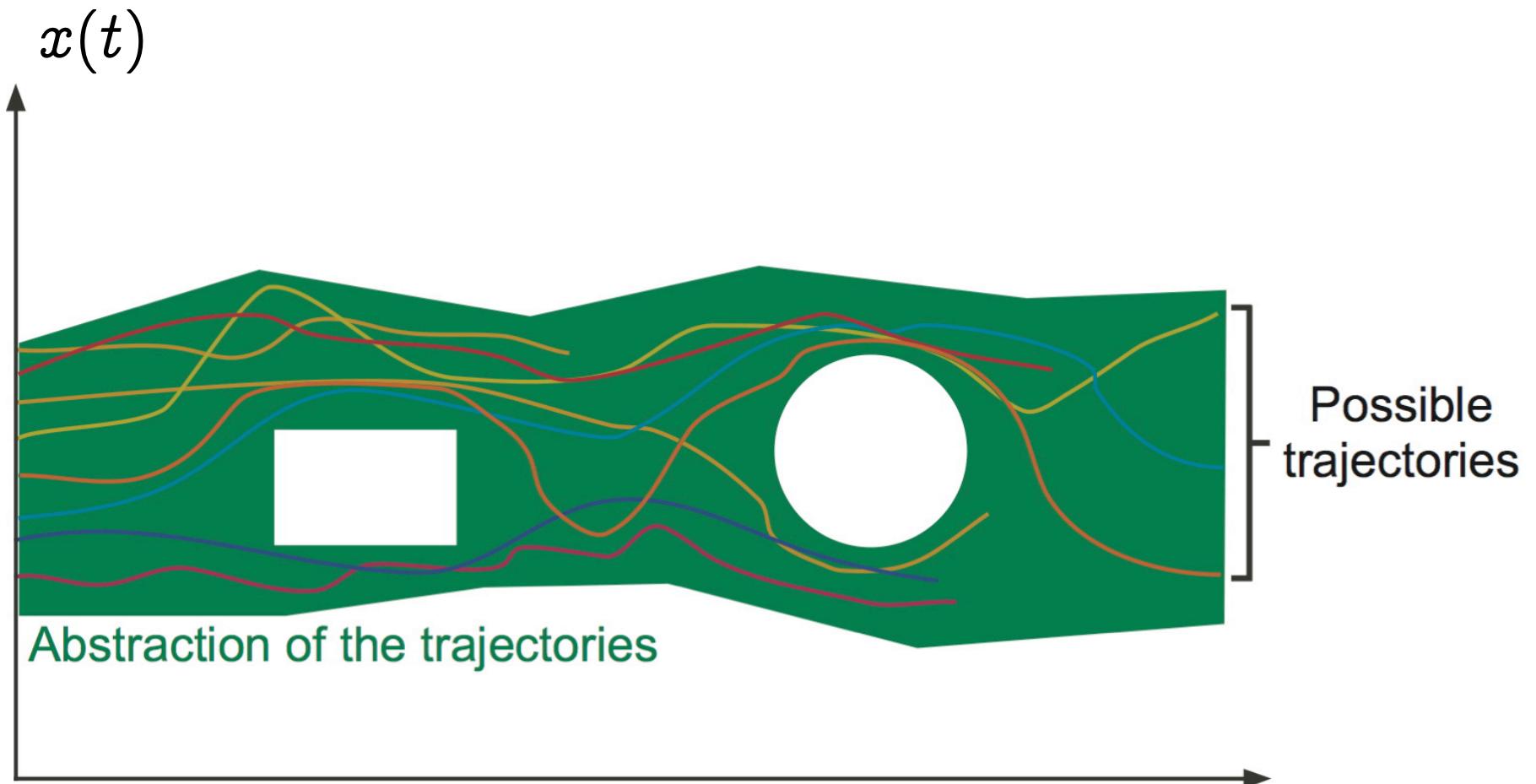
Test/Debugging is Unsafe



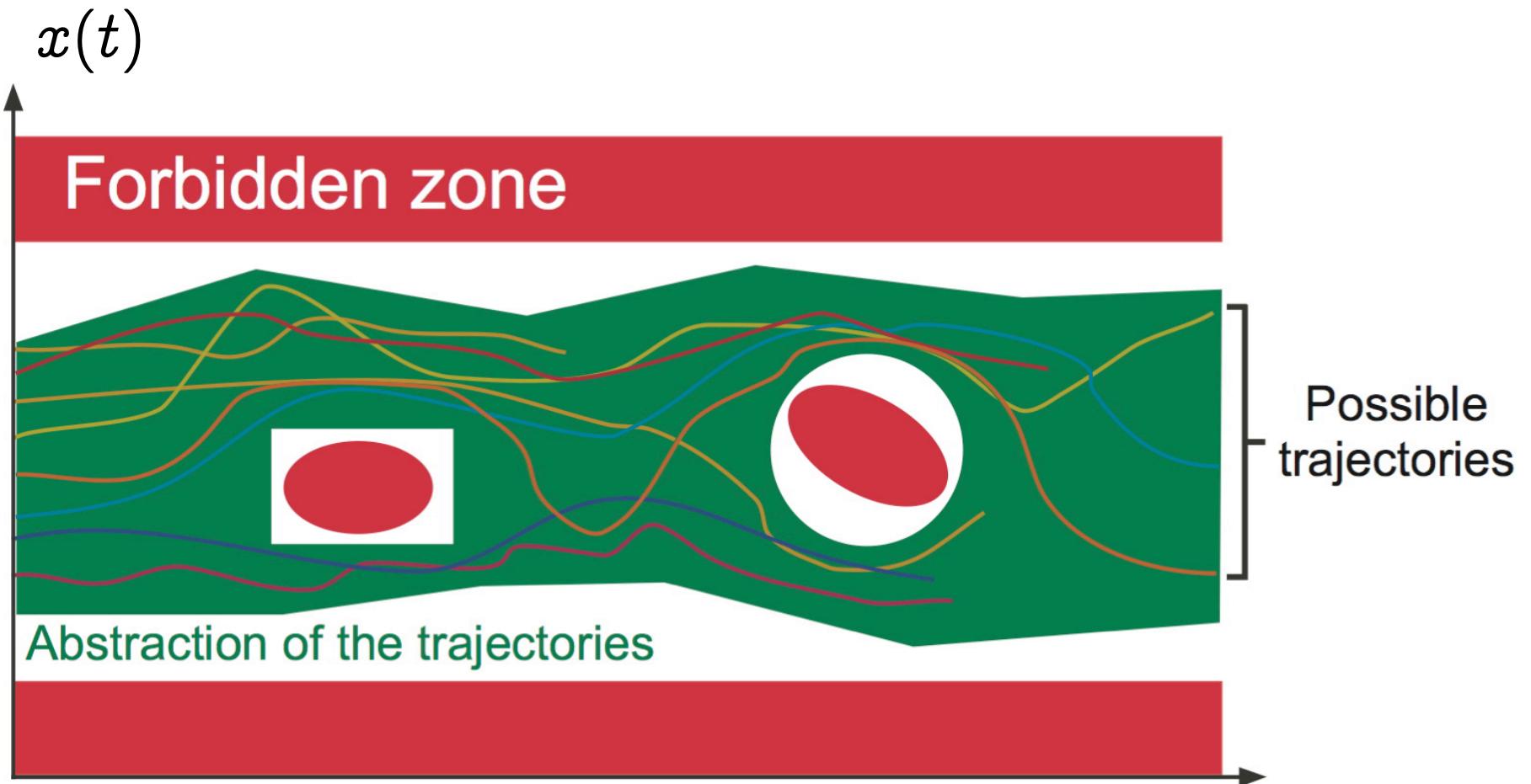
Bounded Model Checking is Unsafe



Over-Approximation

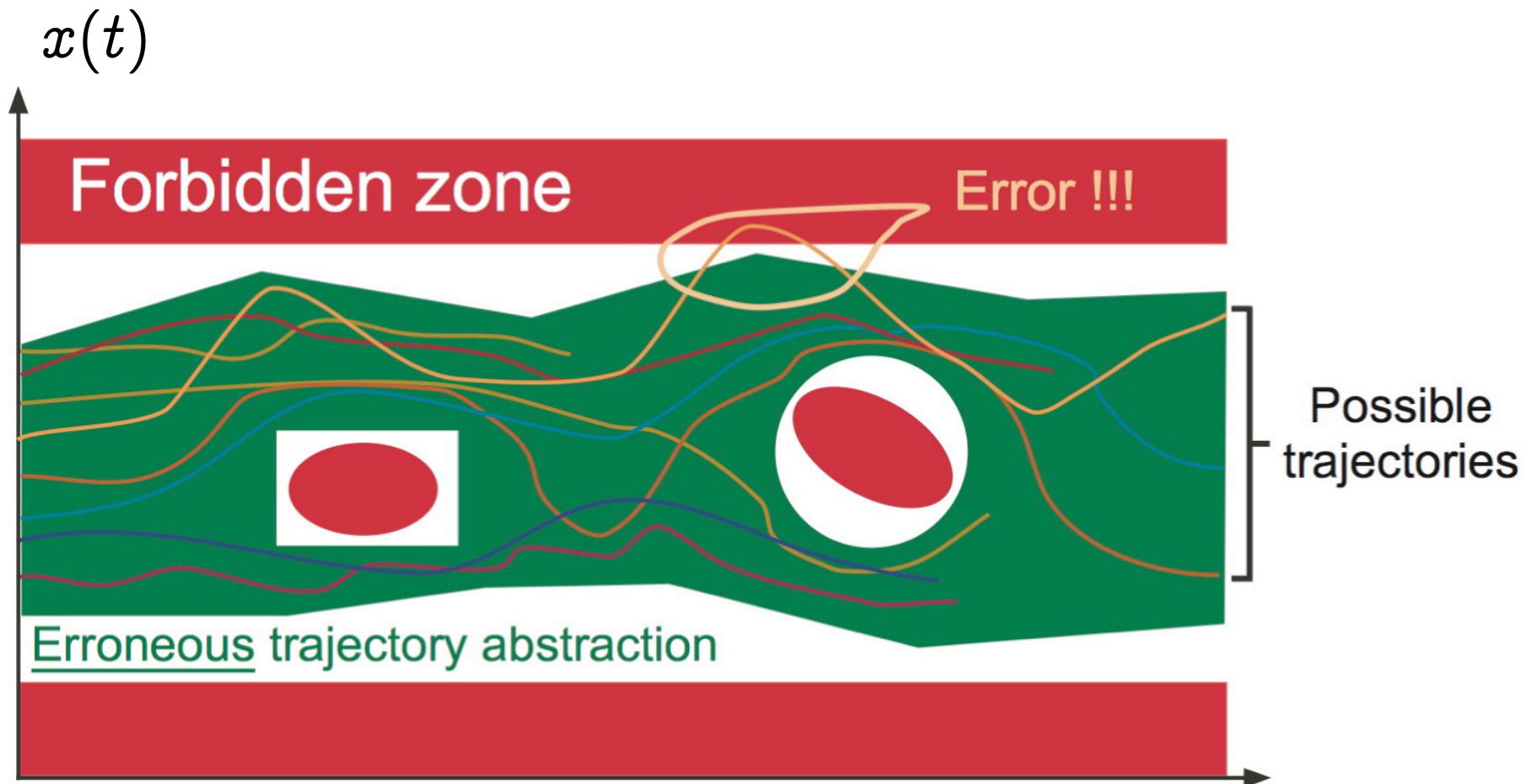


Abstract Interpretation is Sound



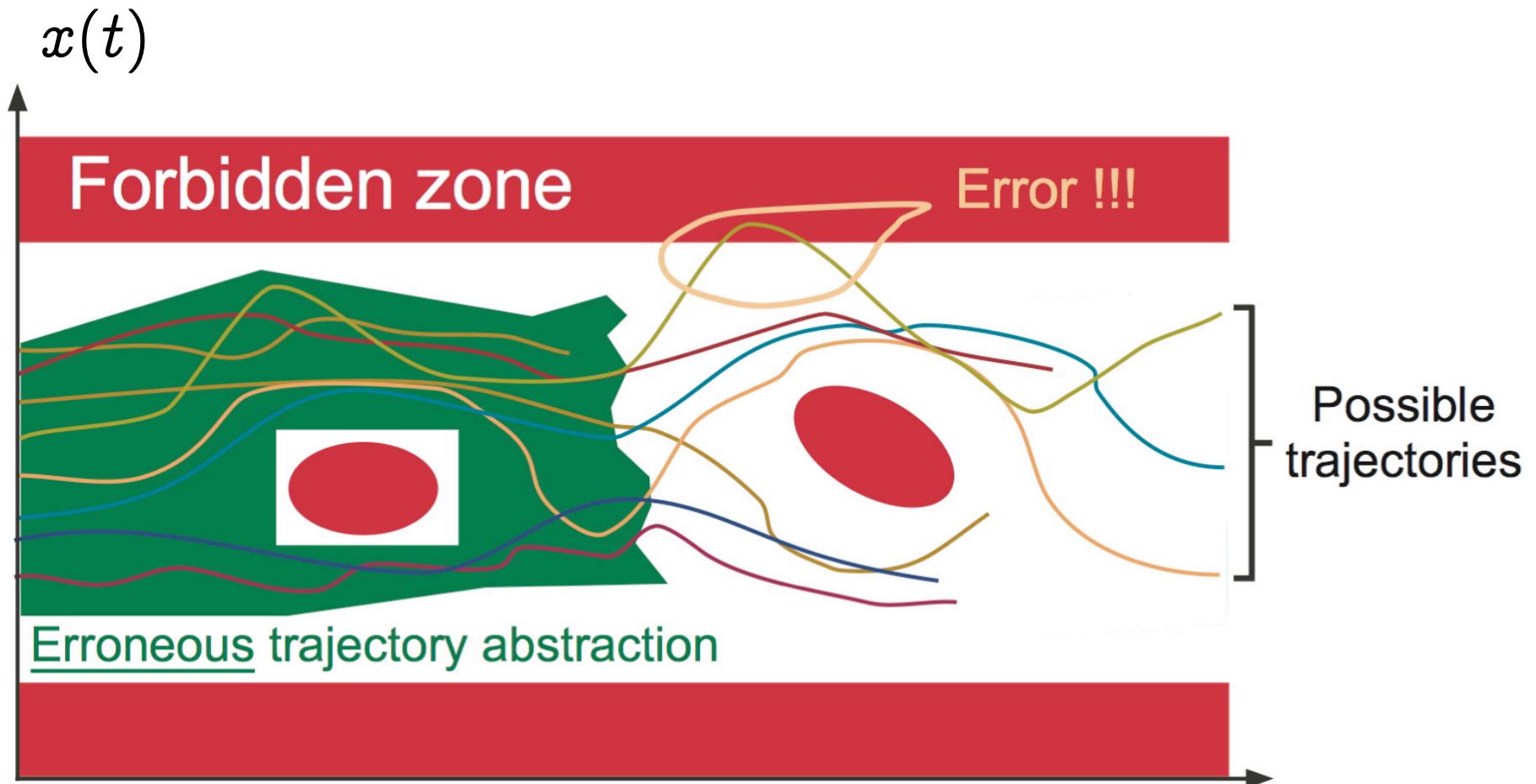
Soundness and Incompleteness

Soundness Requirement: Erroneous Abstraction⁴



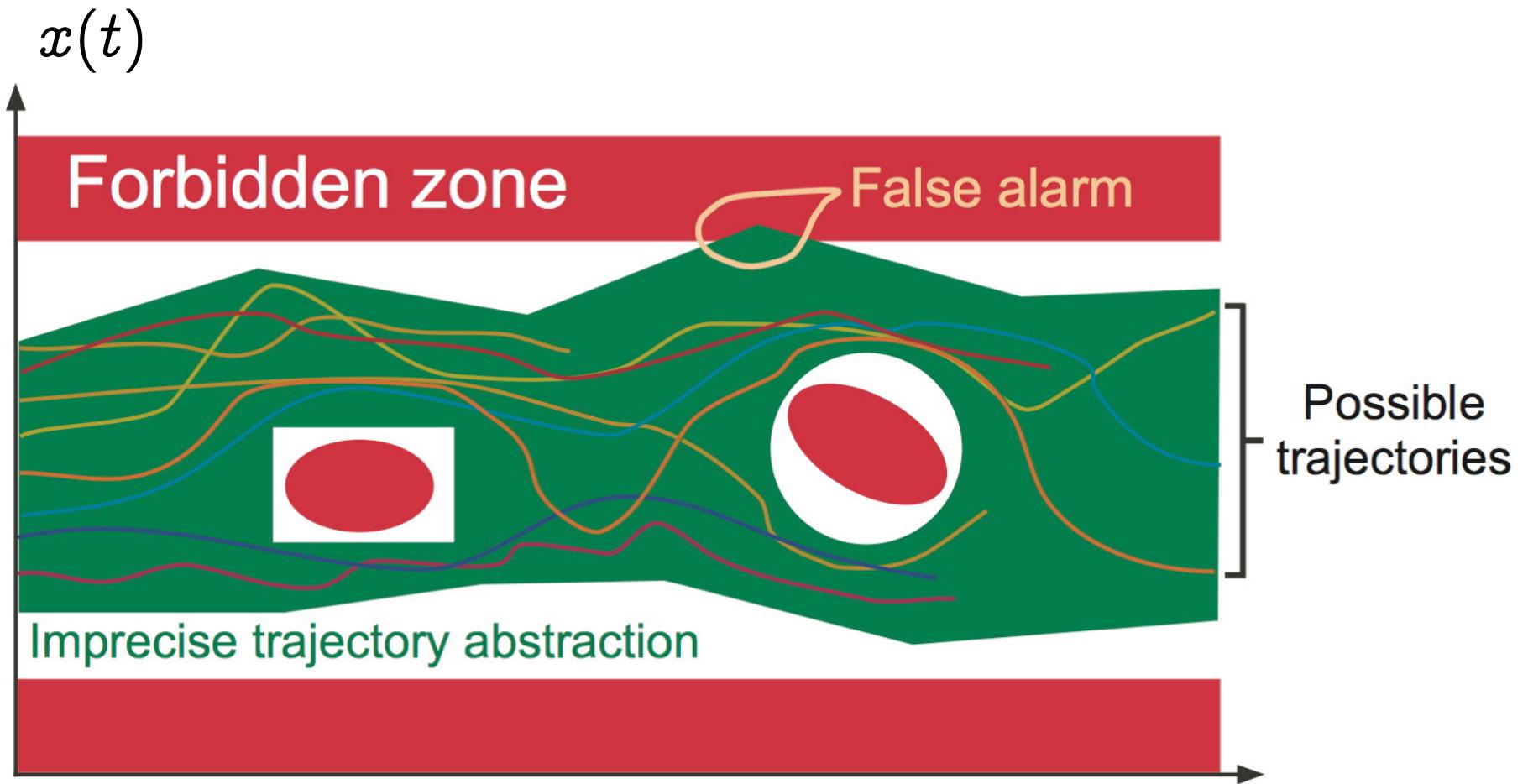
⁴ This situation is always excluded in static analysis by abstract interpretation.

Soundness Requirement: Erroneous Abstraction⁵



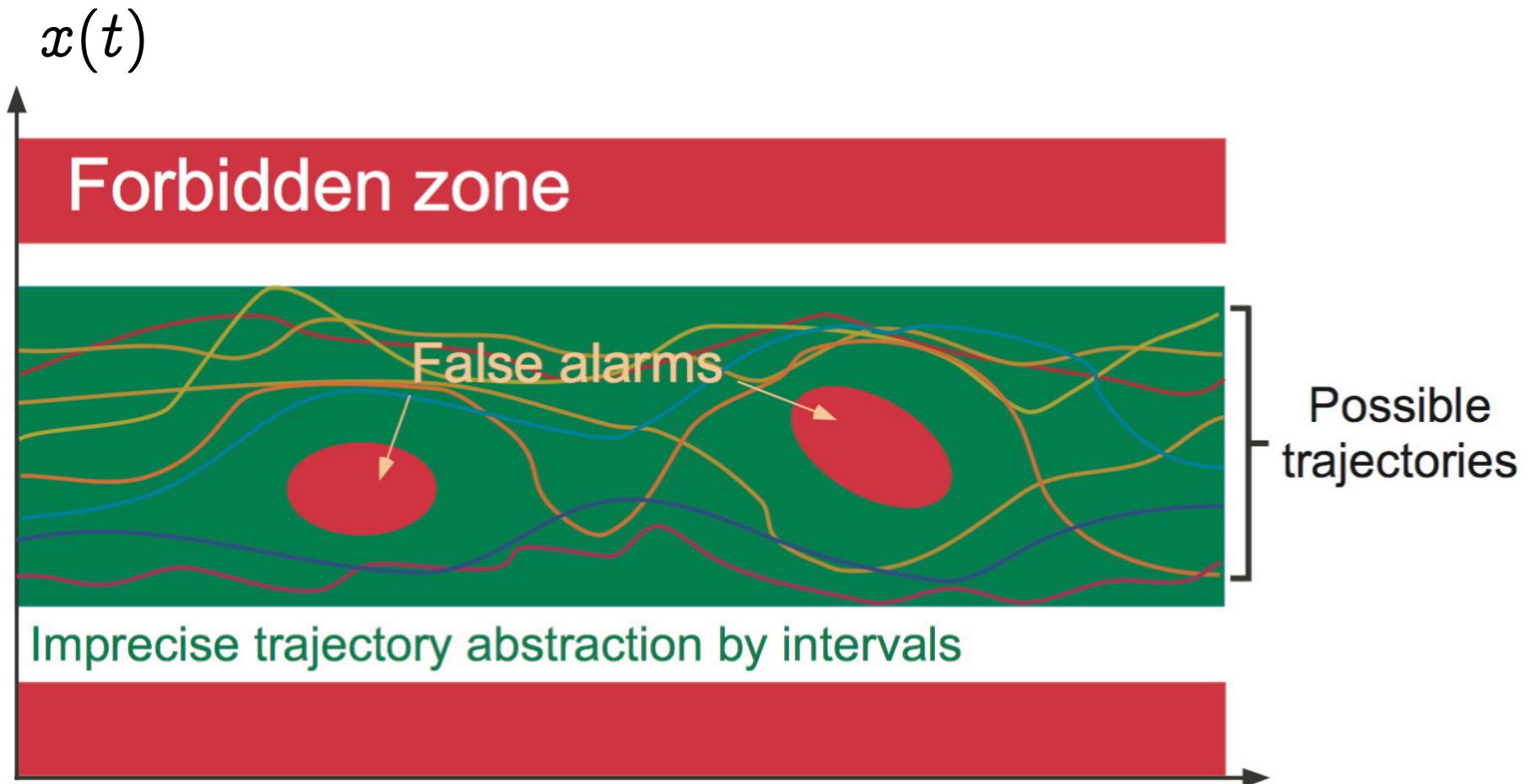
⁵ This situation is always excluded in static analysis by abstract interpretation.

Imprecision \Rightarrow False Alarms

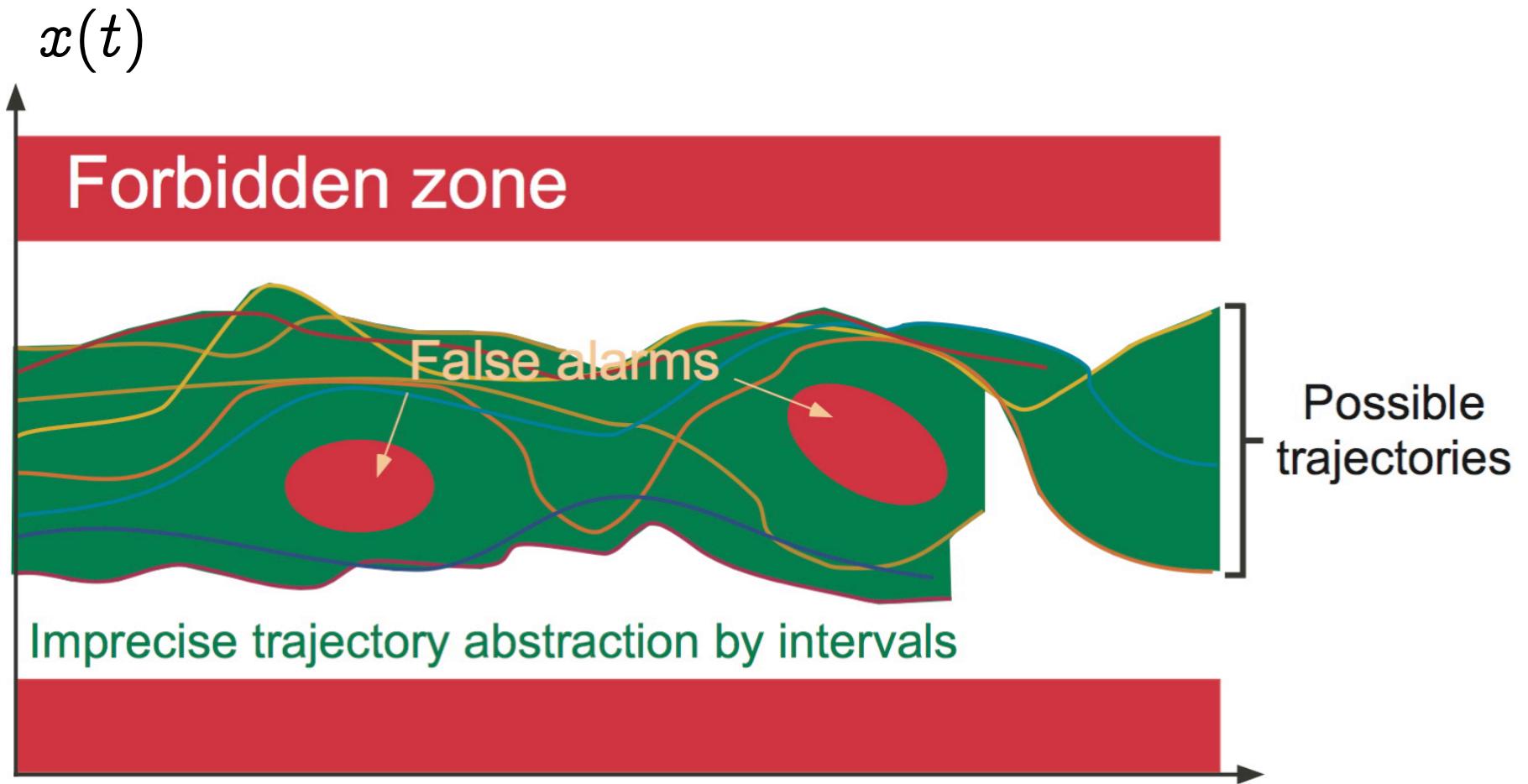


Design by Refinement

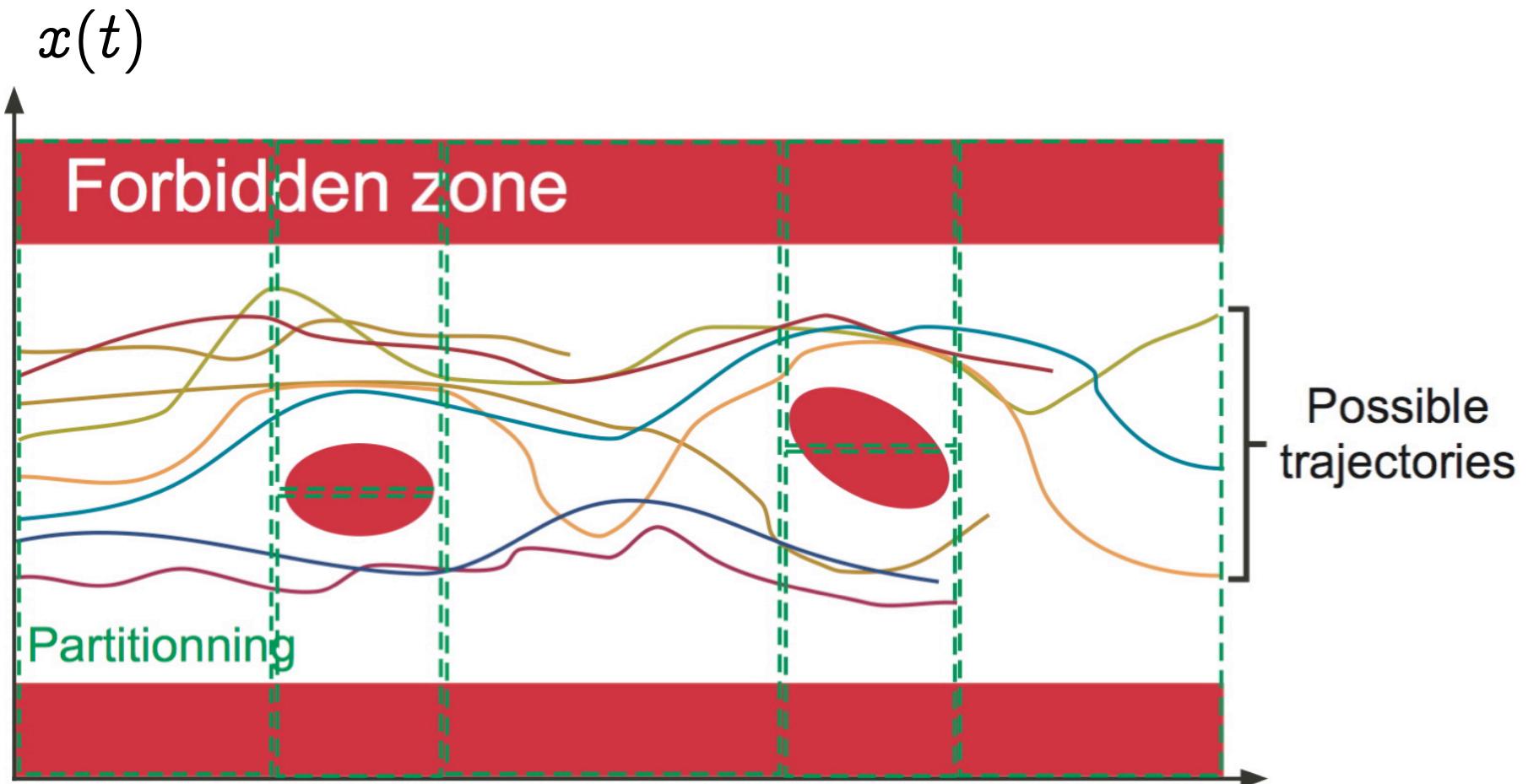
Global Interval Abstraction → False Alarms



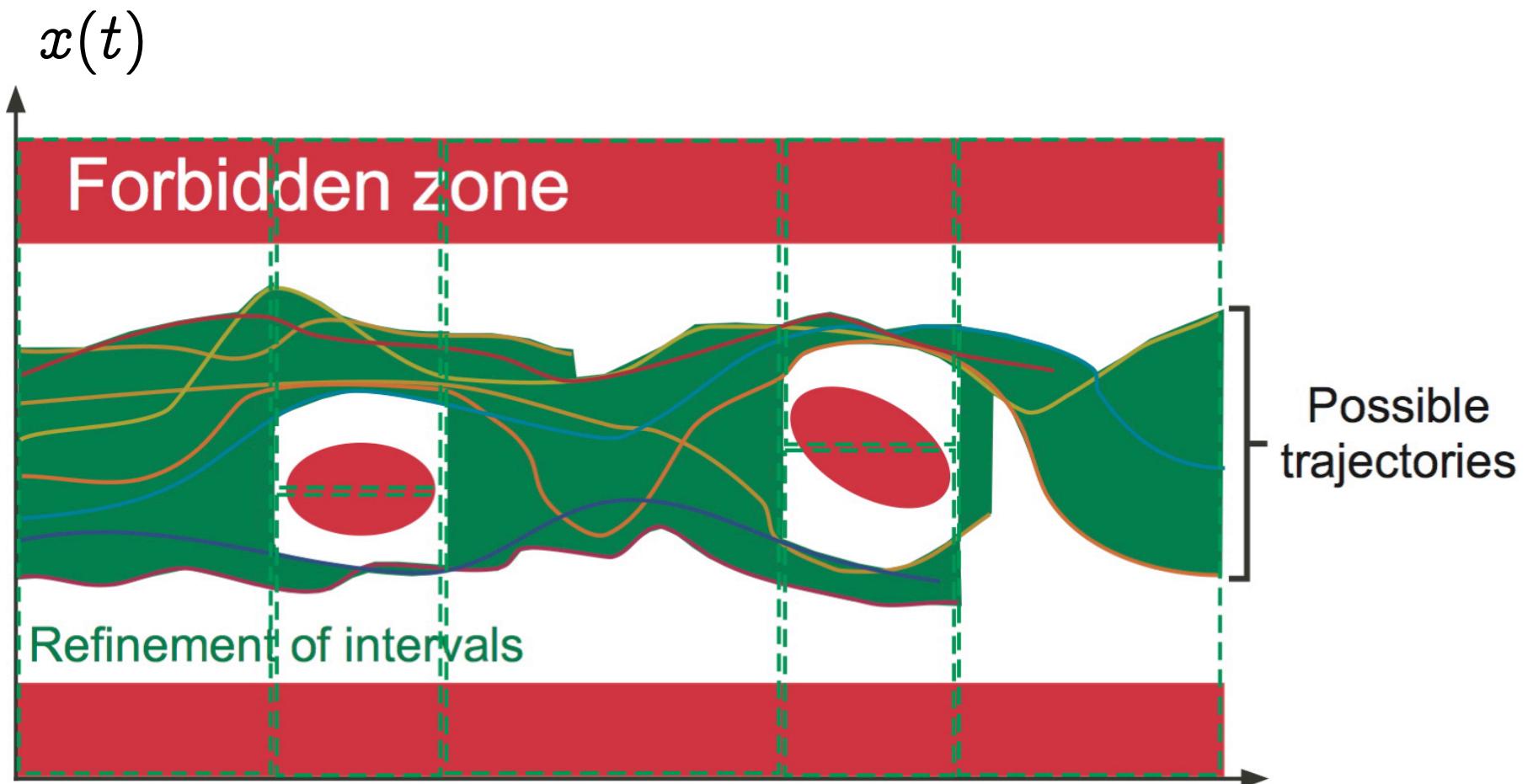
Local Interval Abstraction → False Alarms



Refinement by Partitionning

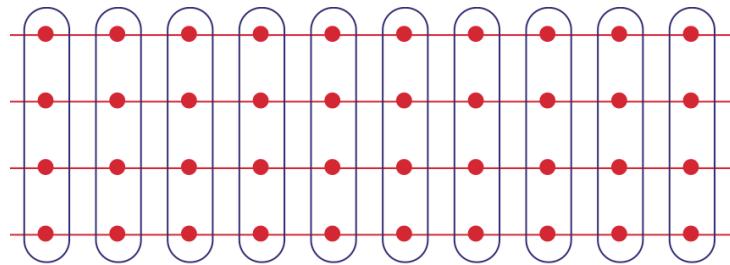


Intervals with Partitionning

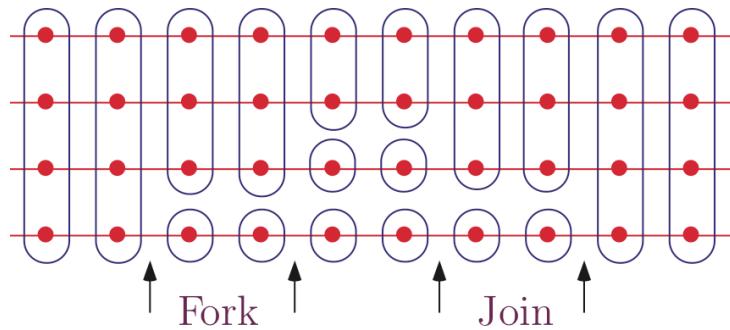


State-based versus Trace-based Partitioning

State-based partitionning at control points:



Trace-based partitionning at control points:



Delaying abstract unions in tests and loops is more precise for non-distributive abstract domains (and much less expensive than disjunctive completion).

Trace Partitioning

Principle:

- Semantic equivalence:

$$\begin{array}{l} \text{if (B) \{} \text{C1} \text{\}} \text{ else \{} \text{C2} \text{\}; C3} \\ \quad \downarrow \\ \text{if (B) \{} \text{C1; C3} \text{\}} \text{ else \{} \text{C2; C3} \text{\};} \end{array}$$

- More precise in the abstract: concrete execution paths are merged later.

Application:

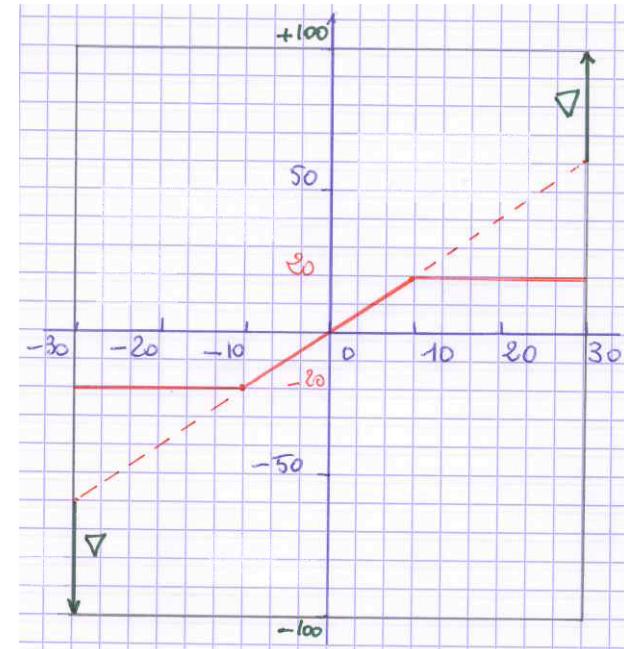
```
if (B)
  { X=0; Y=1; }
else
  { X=1; Y=0; }
R = 1 / (X-Y);
```

cannot result in a
division by zero

Case analysis with loop unrolling

- Code Sample:

```
/* trace_partitionning.c */
void main() {
    float t[5] = {-10.0, -10.0, 0.0, 10.0, 10.0};
    float c[4] = {0.0, 2.0, 2.0, 0.0};
    float d[4] = {-20.0, -20.0, 0.0, 20.0};
    float x, r;
    int i = 0;
    __ASTREE_known_fact((-30.0 <= x) && (x <= 30.0));
    while ((i < 3) && (x >= t[i+1])) {
        i = i + 1;
    }
    r = (x - t[i]) * c[i] + d[i];
    __ASTREE_log_vars((r));
}
```



```
% astree -exec-fn main -no-trace -no-relational trace-partitionning.c |& egrep "(WARN)|(r in)"
direct = <float-interval: r in [-20, 20] >
%
% astree -exec-fn main -no-partition -no-trace -no-relational trace-partitionning.c \
|& egrep "(WARN)|(r in)"
direct = <float-interval: r in [-100, 100] >
%
```

3. The ASTRÉE static analyzer

<http://www.astree.ens.fr/>

Project Members



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⁶ Nov. 2001 — Nov. 2003.

⁷ Nov. 2001 — Aug. 2007.

Programs Analyzed by ASTRÉE and their Semantics

Programs analysed by ASTRÉE

- Application Domain: large safety critical embedded real-time synchronous software for non-linear control of very complex control/command systems.
- C programs:
 - with
 - basic numeric datatypes, structures and arrays
 - pointers (including on functions),
 - floating point computations
 - tests, loops and function calls
 - limited branching (forward goto, break, continue)

- with (cont'd) **NEW**
 - union [Min06a]
 - pointer arithmetics & casts [Min06a]
- without
 - dynamic memory allocation
 - recursive function calls
 - unstructured/backward branching
 - conflicting side effects
 - C libraries, system calls (parallelism)

Such limitations are quite common for embedded safety-critical software.

The Class of Considered Periodic Synchronous Programs

```
declare volatile input, state and output variables;  
initialize state and output variables;  
loop forever  
  - read volatile input variables,  
  - compute output and state variables,  
  - write to output variables;  
  -- ASTREE_wait_for_clock ();  
end loop
```

Task scheduling is static:

- Requirements: the only interrupts are clock ticks;
- Execution time of loop body less than a clock tick,
as verified by the aiT WCET Analyzers [FHL⁺01].

Concrete Operational Semantics

- International norm of C (ISO/IEC 9899:1999)
- *restricted by implementation-specific behaviors* depending upon the machine and compiler (e.g. representation and size of integers, IEEE 754-1985 norm for floats and doubles)
- *restricted by user-defined programming guidelines* (such as no modular arithmetic for signed integers, even though this might be the hardware choice)
- *restricted by program specific user requirements* (e.g. assert, execution stops on first runtime error⁸)

⁸ semantics of C unclear after an error, equivalent if no alarm

Different Classes of Run-time Errors

1. Errors terminating the execution ⁹. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.
2. Errors not terminating the execution with predictable outcome ¹⁰. ASTRÉE warns and continues with worst-case assumptions.
3. Errors not terminating the execution with unpredictable outcome¹¹. ASTRÉE warns and continues by taking into account only the executions that did not trigger the error.

⇒ ASTRÉE is sound with respect to **C standard**, unsound with respect to **C implementation**, unless **no false alarm**.

⁹ floating-point exceptions e.g. (invalid operations, overflows, etc.) when traps are activated

¹⁰ e.g. overflows over signed integers resulting in some signed integer.

¹¹ e.g. memory corruptionss.

Specification Proved by ASTRÉE

Implicit Specification: Absence of Runtime Errors

- No violation of the norm of C (e.g. array index out of bounds, division by zero)
- No implementation-specific undefined behaviors (e.g. maximum short integer is 32767, NaN)
- No violation of the programming guidelines (e.g. static variables cannot be assumed to be initialized to 0)
- No violation of the programmer assertions (must all be statically verified).

Modular Arithmetic

Modular arithmetics is not very intuitive

In C:

```
% cat -n modulo-c.c
```

```
1 #include <stdio.h>
2 int main () {
3     int x,y;
4     x = -2147483647 / -1;
5     y = ((-x) -1) / -1;
6     printf("x = %i, y = %i\n",x,y);
7 }
8
```

```
% gcc modulo-c.c
```

```
% ./a.out
```

```
x = 2147483647, y = -2147483648
```

Static Analysis with ASTRÉE

```
% cat -n modulo.c
 1 int main () {
 2 int x,y;
 3 x = -2147483647 / -1;
 4 y = ((-x) -1) / -1;
 5 __ASTREE_log_vars((x,y));
 6 }
 7

% astree -exec-fn main -unroll 0 modulo.c \
|& egrep -A 1 "<integers>|(WARN)"
modulo.c:4.4-18::[call#main@1]: WARN: signed int arithmetic range
{2147483648} not included in [-2147483648, 2147483647]
<integers (intv+cong+bitfield+set): y in [-2147483648, 2147483647] /\ Top
x in {2147483647} /\ {2147483647} >
```

ASTRÉE signals the overflow and goes on with an unkown value.

Float Overflow

Float Arithmetics does Overflow

In C:

```
% cat -n overflow.c
 1 void main () {
 2     double x,y;
 3     x = 1.0e+256 * 1.0e+256;
 4     y = 1.0e+256 * -1.0e+256;
 5     __ASTREE_log_vars((x,y));
 6 }
% gcc overflow.c
% ./a.out
x = inf, y = -inf
```

```
% astree -exec-fn main
overflow.c |& grep "WARN"
overflow.c:3.4-23:: [call#main1]:
WARN: double arithmetic range
[1.79769e+308, inf] not
included in [-1.79769e+308,
1.79769e+308]
overflow.c:4.4-24:: [call#main1]:
WARN: double arithmetic range
[-inf, -1.79769e+308] not
included in [-1.79769e+308,
1.79769e+308]
```

The Ariane 5.01 maiden flight

- June 4th, 1996 was the maiden flight of Ariane 5



The Ariane 5.01 maiden flight failure

- June 4th, 1996 was the maiden flight of Ariane 5
- The launcher was destroyed after 40 seconds of flight because of a software overflow¹²



¹² A 16 bit piece of code of Ariane 4 had been reused within the new 32 bit code for Ariane 5. This caused an uncaught overflow, making the launcher uncontrollable.

Rounding

Example of rounding error

```
/* float-error.c */
int main () {
    float x, y, z, r;
    x = 1.000000019e+38;
    y = x + 1.0e21;
    z = x - 1.0e21;
    r = y - z;
    printf("%f\n", r);
}
% gcc float-error.c
% ./a.out
0.000000
```

```
/* double-error.c */
int main () {
    double x; float y, z, r;
    /* x = ldexp(1.,50)+ldexp(1.,26); */
    x = 1125899973951488.0;
    y = x + 1;
    z = x - 1;
    r = y - z;
    printf("%f\n", r);
}
% gcc double-error.c
% ./a.out
134217728.000000
```

$$(x + a) - (x - a) \neq 2a$$

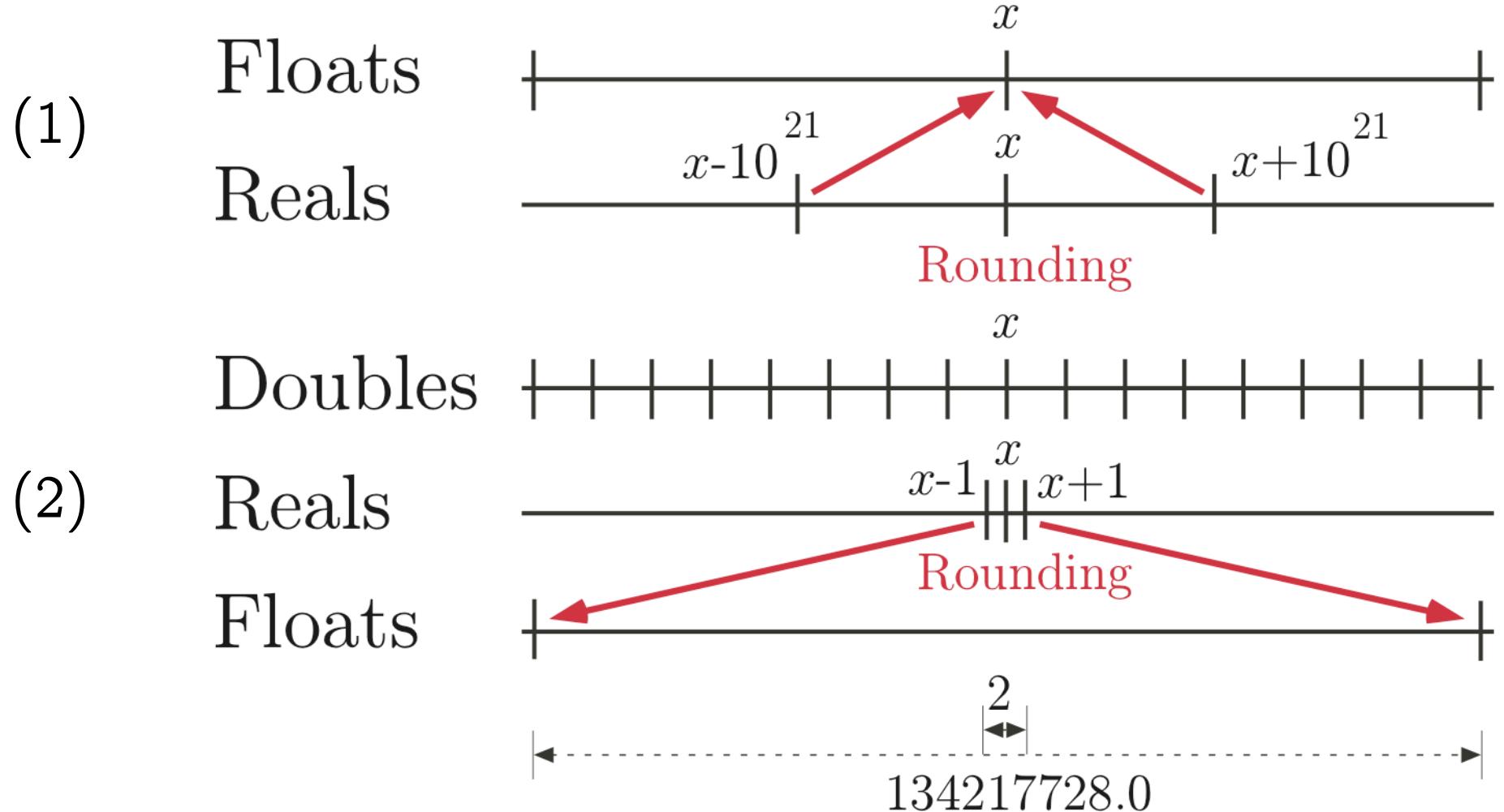
Example of rounding error

```
/* float-error.c */
int main () {
    float x, y, z, r;
    x = 1.000000019e+38;
    y = x + 1.0e21;
    z = x - 1.0e21;
    r = y - z;
    printf("%f\n", r);
}
% gcc float-error.c
% ./a.out
0.000000
```

```
/* double-error.c */
int main () {
    double x; float y, z, r;
    /* x = ldexp(1.,50)+ldexp(1.,26); */
    x = 1125899973951487.0;
    y = x + 1;
    z = x - 1;
    r = y - z;
    printf("%f\n", r);
}
% gcc double-error.c
% ./a.out
0.000000
```

$$(x + a) - (x - a) \neq 2a$$

Explanation of the huge rounding error



Static analysis with ASTRÉE¹³

```
% cat -n double-error.c
 2 int main () {
 3 double x; float y, z, r;;
 4 /* x = ldexp(1.,50)+ldexp(1.,26); */
 5 x = 1125899973951488.0;
 6 y = x + 1;
 7 z = x - 1;
 8 r = y - z;
 9 __ASTREE_log_vars((r));
10 }

% gcc double-error.c
% ./a.out
134217728.000000
% astree -exec-fn main -print-float-digits 10 double-error.c |& grep "r in
direct = <float-interval: r in [-134217728, 134217728] >
```

¹³ ASTRÉE makes a worst-case assumption on the rounding ($+\infty$, $-\infty$, 0, nearest) hence the possibility to get -134217728.

Example of accumulation of small rounding errors

```
% cat -n rounding-c.c
 1 #include <stdio.h>
 2 int main () {
 3     int i; double x; x = 0.0;
 4     for (i=1; i<=1000000000; i++) {
 5         x = x + 1.0/10.0;
 6     }
 7     printf("x = %f\n", x);
 8 }
```

```
% gcc rounding-c.c
% ./a.out
x = 99999998.745418
%
```

since $(0.1)_{10} = (0.0001100110011001100\dots)_2$

Static analysis with ASTRÉE

```
% cat -n rounding.c
 1 int main () {
 2     double x; x = 0.0;
 3     while (1) {
 4         x = x + 1.0/10.0;
 5         __ASTREE_log_vars((x));
 6         __ASTREE_wait_for_clock();
 7     }
 8 }

% cat rounding.config
__ASTREE_max_clock((1000000000));

% astree -exec-fn main -config-sem rounding.config -unroll 0 rounding.c \
|& egrep "(x in)|(\\|x\\|)|(WARN)" | tail -2
direct = <float-interval: x in [0.1, 200000040.938] >
|x| <= 1.*((0. + 0.1/(1.-1))*(1.)^clock - 0.1/(1.-1)) + 0.1
<= 200000040.938
```

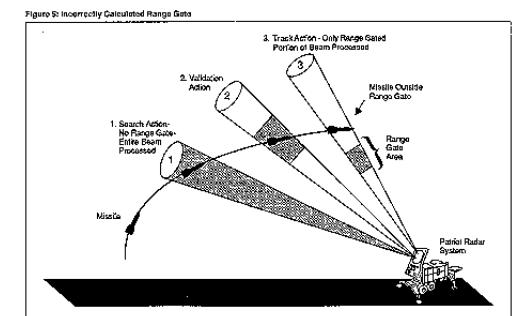
The Patriot missile failure

- “On February 25th, 1991, a Patriot missile . . . failed to track and intercept an incoming Scud ^(*). ”
- The **software failure** was due to accumulated rounding error ^(†)



^(*) This Scud subsequently hit an Army barracks, killing 28 Americans.

- ^(†) – “Time is kept continuously by the system’s internal clock in tenths of seconds”
- “The system had been in operation for over 100 consecutive hours”
 - “Because the system had been on so long, the resulting inaccuracy in the time calculation caused the range gate to shift so much that the system could not track the incoming Scud”



Scaling

Static Analysis of Scaling with ASTRÉE

```
% cat -n scale.c                                % gcc scale.c
 1 int main () {                               % ./a.out
 2   float x; x = 0.70000001;                  x = 0.699999988079071
 3   while (1) {
 4     x = x / 3.0;
 5     x = x * 3.0;
 6     __ASTREE_log_vars((x));
 7     __ASTREE_wait_for_clock();
 8   }
 9 }
```



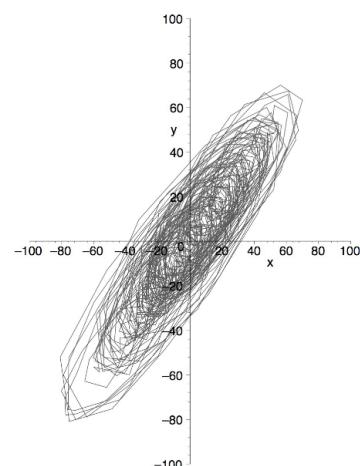
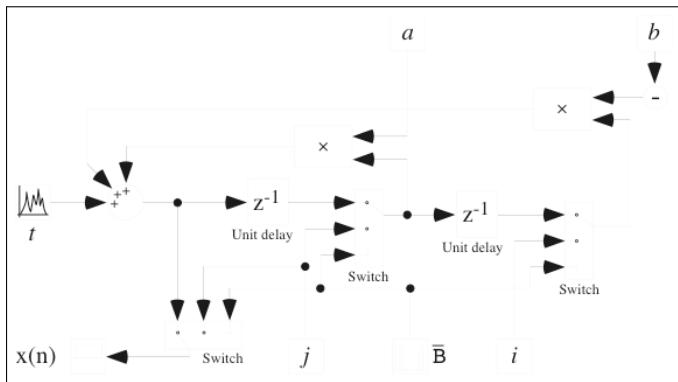
```
% cat scale.config
__ASTREE_max_clock((1000000000));
```



```
% astree -exec-fn main -config-sem scale.config -unroll 0 scale.c \
|& grep "x in" | tail -1
direct = <float-interval: x in [0.69999986887, 0.700000047684] >
%
```

Filtering

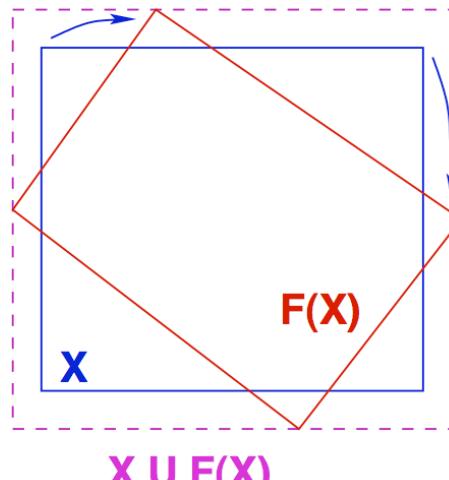
2^d Order Digital Filter:



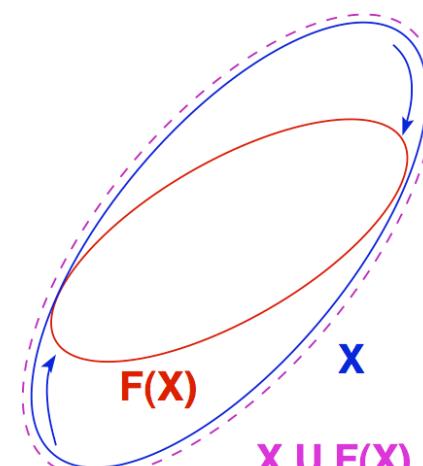
execution trace

Ellipsoid Abstract Domain for Filters

- Computes $X_n = \begin{cases} \alpha X_{n-1} + \beta X_{n-2} + Y_n \\ I_n \end{cases}$
- The concrete computation is bounded, which must be proved in the abstract.
- There is no stable interval or octagon.
- The simplest stable surface is an ellipsoid.



unstable interval



stable ellipsoid

Filter Example [Fer04]

```
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
BOOLEAN INIT; float P, X;

void filter () {
    static float E[2], S[2];
    if (INIT) { S[0] = X; P = X; E[0] = X; }
    else { P = (((((0.5 * X) - (E[0] * 0.7)) + (E[1] * 0.4))
                  + (S[0] * 1.5)) - (S[1] * 0.7)); }
    E[1] = E[0]; E[0] = X; S[1] = S[0]; S[0] = P;
    /* S[0], S[1] in [-1327.02698354, 1327.02698354] */
}

void main () { X = 0.2 * X + 5; INIT = TRUE;
    while (1) {
        X = 0.9 * X + 35; /* simulated filter input */
        filter (); INIT = FALSE; }
}
```

Time Dependence

Arithmetic-Geometric Progressions (Example 1)

```
% cat count.c
typedef enum {FALSE = 0, TRUE = 1} BOOLEAN;
volatile BOOLEAN I; int R; BOOLEAN T;
void main() {

    R = 0;
    while (TRUE) {
        __ASTREE_log_vars((R));
        if (I) { R = R + 1; }           ← potential overflow!
        else { R = 0; }
        T = (R >= 100);
        __ASTREE_wait_for_clock();
    }
}

% cat count.config
__ASTREE_volatile_input((I [0,1]));
__ASTREE_max_clock((3600000));
% astree -exec-fn main -config-sem count.config count.c|grep '|R|'
|R| <= 0. + clock *1. <= 3600001.
```

Arithmetic-Geometric Progressions: Example 2

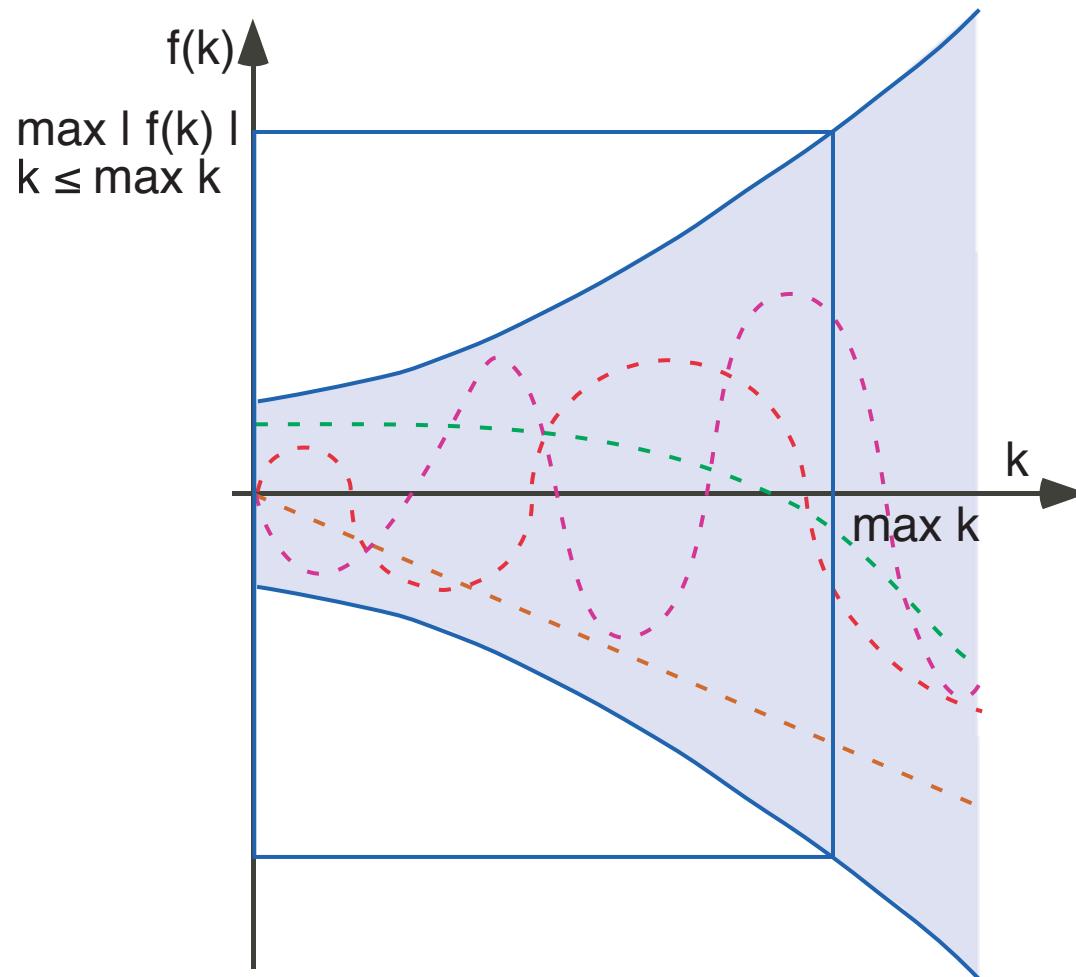
```
% cat retro.c
typedef enum {FALSE=0, TRUE=1} BOOL;
BOOL FIRST;
volatile BOOL SWITCH;
volatile float E;
float P, X, A, B;

void dev( )
{ X=E;
  if (FIRST) { P = X; }
  else
    { P =  (P - (((2.0 * P) - A) - B)
              * 4.491048e-03)); }
  B = A;
  if (SWITCH) {A = P;}
  else {A = X;}
}

void main()
{ FIRST = TRUE;
  while (TRUE) {
    dev( );
    FIRST = FALSE;
    __ASTREE_wait_for_clock();
  }
}

% cat retro.config
__ASTREE_volatile_input((E [-15.0, 15.0]));
__ASTREE_volatile_input((SWITCH [0,1]));
__ASTREE_max_clock((3600000));
|P| <= (15. + 5.87747175411e-39
/ 1.19209290217e-07) * (1
+ 1.19209290217e-07)^clock
- 5.87747175411e-39 /
1.19209290217e-07 <= 23.0393526881
```

Overapproximation with an Arithmetic-Geometric Progression



Arithmetic-geometric progressions¹⁴ [Fer05]

- Abstract domain: $(\mathbb{R}^+)^5$
- Concretization:

$$\gamma \in (\mathbb{R}^+)^5 \longmapsto \wp(\mathbb{N} \mapsto \mathbb{R})$$

$$\gamma(M, a, b, a', b') =$$

$$\{f \mid \forall k \in \mathbb{N} : |f(k)| \leq (\lambda x \cdot ax + b \circ (\lambda x \cdot a'x + b')^k)(M)\}$$

i.e. any function bounded by the arithmetic-geometric progression.

Reference

- [1] J. Feret. The arithmetic-geometric progression abstract domain. In VMCAI'05, Paris, LNCS 3385, pp. 42–58, Springer, 2005.

¹⁴ here in \mathbb{R}

4. The industrial use of ASTRÉE

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Example application

- Primary flight control software of the Airbus A340 family/A380 fly-by-wire system



- C program, automatically generated from a proprietary high-level specification (à la Simulink/SCADE)
- A340 family: 132,000 lines, 75,000 LOCs after preprocessing, 10,000 global variables, over 21,000 after expansion of small arrays, now $\times 2$
- A380: $\times 3/7$

Digital Fly-by-Wire Avionics¹⁵



¹⁵ The electrical flight control system is placed between the pilot's controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.

Benchmarks (Airbus A340 Primary Flight Control Software)

- V1¹⁶, 132,000 lines, 75,000 LOCs after preprocessing
- Comparative results (commercial software):
4,200 (false?) alarms, 3.5 days;
- Our results:
0 alarms,
40mn on 2.8 GHz PC, 300 Megabytes
→ A world première in Nov. 2003!

¹⁶ “Flight Control and Guidance Unit” (FCGU) running on the “Flight Control Primary Computers” (FCPC). The three primary computers (FCPC) and two secondary computers (FCSC) which form the A340 and A330 electrical flight control system are placed between the pilot’s controls (sidesticks, rudder pedals) and the control surfaces of the aircraft, whose movement they control and monitor.

The main loop invariant for the A340 V1

A textual file over 4.5 Mb with

- 6,900 boolean interval assertions ($x \in [0; 1]$)
- 9,600 interval assertions ($x \in [a; b]$)
- 25,400 clock assertions ($x + \text{clk} \in [a; b] \wedge x - \text{clk} \in [a; b]$)
- 19,100 additive octagonal assertions ($a \leq x + y \leq b$)
- 19,200 subtractive octagonal assertions ($a \leq x - y \leq b$)
- 100 decision trees
- 60 ellipse invariants, etc . . .

involving over 16,000 floating point constants (only 550 appearing in the program text) \times 75,000 LOCs.

(Airbus A380 Primary Flight Control Software)

- 0 alarms (Nov. 2004), after some additional parametrization and simple abstract domains developments
- Now at 1,000,000 lines!

34h,

8 Gigabyte

→ A world grand première!

Possible origins of imprecision and how to fix it

In case of false alarm, the imprecision can come from:

- **Abstract transformers** (not best possible) → improve algorithm;
- **Automatized parametrization** (e.g. variable packing) → improve pattern-matched program schemata;
- **Iteration strategy** for fixpoints → fix widening¹⁷;
- **Inexpressivity** i.e. indispensable local inductive invariant are inexpressible in the abstract → add a **new abstract domain** to the reduced product (e.g. filters).

¹⁷ This can be very hard since at the limit only a precise infinite iteration might be able to compute the proper abstract invariant. In that case, it might be better to design a more refined abstract domain.

5. Conclusion

Characteristics of the ASTRÉE Analyzer

- Sound: – ASTRÉE is a **bug eradicator**: finds all bugs in a well-defined class (runtime errors)
- ASTRÉE is not a **bug hunter**: finding some bugs in a well-defined class (e.g. by *bug pattern detection* like FindBugs™, PREfast or PMD)
 - ASTRÉE is **exhaustive**: covers the whole state space (\neq MAGIC, CBMC)
 - ASTRÉE is **comprehensive**: never omits potential errors (\neq UNO, CMC from coverity.com) or sort most probable ones to avoid overwhelming messages (\neq Splint)

Characteristics of the ASTRÉE Analyzer (Cont'd)

Static: compile time analysis (\neq run time analysis Rational Purify, Parasoft Insure++)

Program Analyzer: analyzes programs not micromodels of programs (\neq PROMELA in SPIN or Alloy in the Alloy Analyzer)

Automatic: no end-user intervention needed (\neq ESC Java, ESC Java 2), or PREfast (annotate functions with intended use)

Characteristics of the ASTRÉE Analyzer (Cont'd)

Multiabstraction: uses many numerical/symbolic abstract domains (\neq symbolic constraints in Bane or the canonical abstraction of TVLA)

Infinitary: all abstractions use infinite abstract domains with widening/narrowing (\neq model checking based analyzers such as Bandera, Bogor, Java PathFinder, Spin, VeriSoft)

Efficient: always terminate (\neq counterexample-driven automatic abstraction refinement BLAST, SLAM)

Characteristics of the ASTRÉE Analyzer (Cont'd)

Extensible/Specializable: can easily incorporate new abstractions (and reduction with already existing abstract domains) (\neq general-purpose analyzers PolySpace Verifier)

Domain-Aware: knows about control/command (e.g. digital filters) (as opposed to specialization to a mere programming style in C Global Surveyor)

Parametric: the precision/cost can be tailored to user needs by options and directives in the code

Characteristics of the ASTRÉE Analyzer (Cont'd)

Automatic Parametrization: the generation of parametric directives in the code can be programmed (to be specialized for a specific application domain)

Modular: an analyzer instance is built by selection of OCAML modules from a collection each implementing an abstract domain

Precise: very few or no false alarm when adapted to an application domain → it is a **VERIFIER!**

The Future of the ASTRÉE Analyzer

- ASTRÉE has shown **usable** and **useful** in one industrial context (*electric flight control*):
 - as a R & D tool for A340 V2 and A380,
 - as a production tool for the A350;
- **More applications** are forthcoming (ES_PASS project);
- **Industrialization** is simultaneously under consideration.

THE END, THANK YOU

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