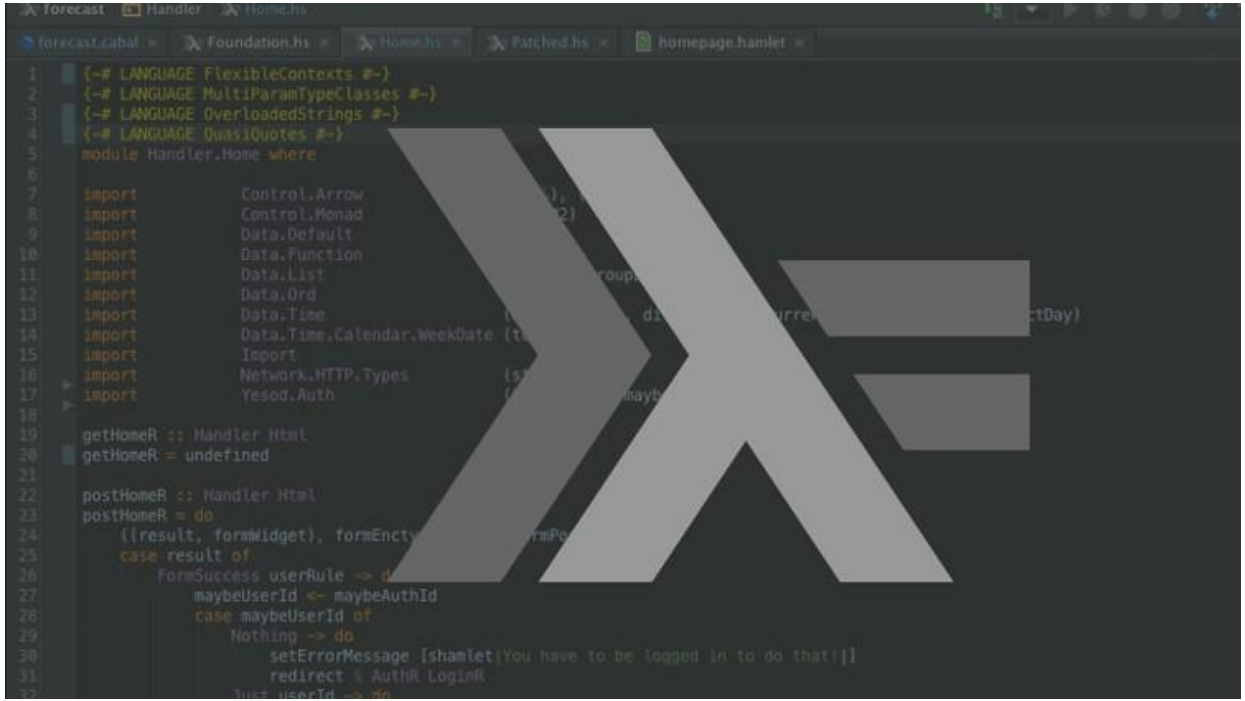
Instantiations of Applicative



Laws of Applicatives

1. Identity:

   `pure id <*> v ≡ v`.

2. Homomorphism:

   `pure f <*> pure x ≡ pure (f x)`.

3. Exchange:

   `u <*> pure y ≡ pure ($ y) <*> u`.

4. Composition:

   `u <*> (v <*> w) ≡ pure (.) <*> u <*> v <*> w`.

5. Relation with the functor:

   `fmap g x ≡ pure g <*> x`.

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```haskell
instance Applicative Maybe where
    pure = Just
    Nothing <*> _ = Nothing
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```haskell
instance Applicative [] where
    pure x = [x]
    fs <*> xs = [f x | f <- fs, x <- xs]
```

Summary

Applicatives allow functions within a container to be applied to objects within the same container.

- `pure` constructs a container with a value.
- `<*>` applies a function inside a container to values inside a container: