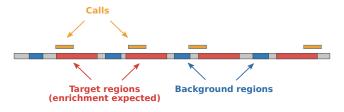
The algorithm of perm-test

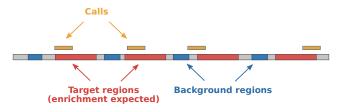
 ${\tt https://github.com/pd3/utils/}$

Enrichment test



Are calls enriched in the target regions?

Enrichment test

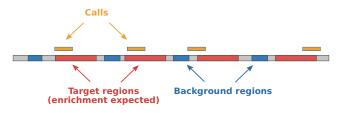


Are calls enriched in the target regions?

Standard permutation test

randomly place the calls on the genome and count how many are placed in the target regions. Repeat many times and count how often the number of calls placed in the target regions matched or exceeded the count observed in the experimental data

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Computational problem

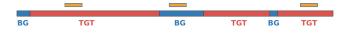
when working with exomes (2% of the genome), calls are placed in inaccessible regions 98% of the time. A huge waste of CPU time!

Enrichment test: naive improvement



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Enrichment test: naive improvement

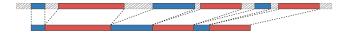


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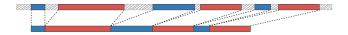
However, if we only permute the labels, we ignore size differences between target and background regions.

Trimmed genome

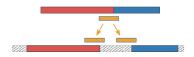


Instead, we splice out inaccessible regions creating a shorter version of the genome. This way every random placement results in a usable call, it can never land in an inaccessible region.

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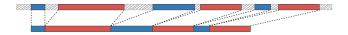


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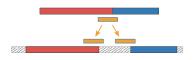


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The trimmed genome must include left overhangs.

Implementation



Be careful with calls that overlap more than one region in the real genome. Also take care at chromosome boundaries. Note that we must build a separate trimmed genome for each call length.

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Be careful with calls that overlap more than one region in the real genome. Also take care at chromosome boundaries. Note that we must build a separate trimmed genome for each call length.

It would require too much memory to keep the genomes for all call lengths at the same time. Instead of updating all calls within a single iteration, iterate calls individually, one at a time, and keep in memory the counters of hits for all iterations.

```
for (iter=0; iter<niters; iter++)
{
   for (call=0; call<ncalls; call++)
      place_call_randomly
   if ( number_of_hits_exceeded )
      increase_pvalue
}</pre>
```

Iterate all calls jointly update P-value in every iteration (the standard way)

```
for (call=0; call<ncalls; call++)
{
    for (iter=0; iter<niter; iter++)
    {
        place_call_randomly
        if (is_a_hit)
            increase_number_of_hits_in_the_iter
    }
}
for (iter=0; iter<niters; iter++)
    if (number_of_hits_exceeded)
    increase_pvalue</pre>
```

Iterate calls invidually, update P-value at the end (perm-test)

Usage

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The regions and calls should be a tab-delimited files with inclusive 1-based coordinates

```
1 69090 70008
1 861321 861496
1 865532 865787
etc
```

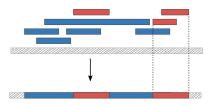
Usage

```
perm-test
    --calls calls.txt
    --target-regs tgt.txt
    --background-regs bg.txt
    --ref-fai ref.fai # required for chr lengths
    --niter 1e9,1e8 # iterations total and per batch
```

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```
1 69090 70008
1 861321 861496
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etc
```

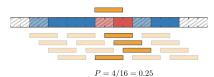
The regions will be correctly merged and spliced when necessary



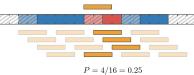
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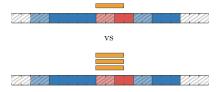


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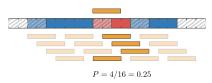


- -, --

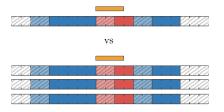
For complex cases we used identities such as $P(c_1, \ldots, c_n) = \prod P(c_i)$



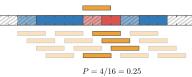
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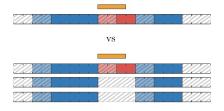


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Performance

- ▶ 4k iterations per call per minute
- \triangleright 255 calls, 10^{11} iterations, 140 hosts ... 400 MB RAM, 5 hours
- ► flexible memory usage (can be lowered by decreasing the number of iterations per batch)