

Marked Graph Compression

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Chapter 1

Main Page

This is a test

Chapter 2

Namespace Index

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Chapter 3

Class Index

3.1 Class List

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| b_graph_decoder | Decodes a simple unmarked bipartite graph | 18 |
| b_graph_encoder | Encodes a simple unmarked bipartite graph | 24 |
| bit_pipe | A sequence of arbitrary number of bits | 30 |
| colored_graph | This class defines a colored graph, which is obtained from a simple marked graph and the color of edges come from the type of edges | 37 |
| fenwick_tree | Fenwick tree class | 44 |
| graph | Simple unmarked graph | 47 |
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| graph_encoder | Encodes a simple unmarked graph | 58 |
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| obitstream | Handles writing bitstreams to binary files | 123 |
| reverse_fenwick_tree | Similar to the fenwick_tree class, but instead of prefix sums, this class computes suffix sums | 128 |
| time_series_decoder | Decodes a time series which is basically an array of arbitrary nonnegative integers | 131 |

| | |
|---|---------------------|
| time_series_encoder | |
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Chapter 5

Namespace Documentation

5.1 helper_vars Namespace Reference

Variables

- mpz_class [mul_1](#)
- mpz_class [mul_2](#)
helper variables in order to avoid initialization
- vector< mpz_class > [return_stack](#)
- vector< mpz_class > [mpz_vec](#)
- vector< mpz_class > [mpz_vec2](#)

5.1.1 Variable Documentation

5.1.1.1 mpz_vec

```
vector< mpz_class > helper_vars::mpz_vec
```

5.1.1.2 mpz_vec2

```
vector< mpz_class > helper_vars::mpz_vec2
```

5.1.1.3 mul_1

```
mpz_class helper_vars::mul_1
```

5.1.1.4 mul_2

```
mpz_class helper_vars::mul_2
```

helper variables in order to avoid initialization

5.1.1.5 return_stack

```
vector< mpz_class > helper_vars::return_stack
```

Chapter 6

Class Documentation

6.1 b_graph Class Reference

simple unmarked bipartite graph

```
#include <bipartite_graph.h>
```

Public Member Functions

- [b_graph \(\)](#)
default constructor
- [b_graph](#) (const vector< vector< int > > &list, const vector< int > &left_deg, const vector< int > &right_deg)
a fast constructor getting adjacency list and both left and right degree sequences
- [b_graph](#) (const vector< vector< int > > &list, const vector< int > &right_deg)
a constructor
- [b_graph](#) (const vector< vector< int > > &list)
a constructor
- vector< int > [get_adj_list](#) (int v) const
returns the adjacency list of a given left vertex
- int [get_right_degree](#) (int v) const
returns the degree of a right vertex v
- int [get_left_degree](#) (int v) const
returns the degree of a right vertex v
- vector< int > [get_right_degree_sequence](#) () const
return the right degree sequence
- vector< int > [get_left_degree_sequence](#) () const
return the left degree sequence
- int [nu_left_vertices](#) () const
returns the number of left vertices
- int [nu_right_vertices](#) () const
returns the number of right vertices

Private Attributes

- `int n`
the number of left vertices
- `int np`
the number of right vertices
- `vector< vector< int > > adj_list`
adjacency list for left vertices, where for $0 \leq v < n$, `adj_list[v]` is a sorted list of right vertices connected to v .
- `vector< int > left_deg_seq`
degree sequence for left vertices, where `left_deg_seq[v]` is the degree of the left node v
- `vector< int > right_deg_seq`
degree sequence for right vertices, where `right_deg_seq[v]` is the degree of the right node v

Friends

- `ostream & operator<< (ostream &o, const b_graph &G)`
printing the graph to the output
- `bool operator== (const b_graph &G1, const b_graph &G2)`
comparing two graphs for equality
- `bool operator!= (const b_graph &G1, const b_graph &G2)`
comparing for inequality

6.1.1 Detailed Description

simple unmarked bipartite graph

A simple unmarked bipartite graph with n left nodes and np right nodes. There are two ways to define such an object.

1. through adjacency list which is a `vector<vector<int> >` of size n (number of left nodes) where each element is a vector of adjacent right vertices (does not have to be sorted). Note that both left and right vertex indices are 0 based. For instance, (in c++11 notation), if `list = {{0},{1},{0,1}}`, the graph has 3 left nodes and 2 right nodes, left node 0 is connected to right node 0, left node 1 is connected to right node 1, and left node 2 is connected to right nodes 0 and 1.

```
vector<vector<int> > list = {{0},{1},{0,1}};
b_graph G(list);
```

2. through adjacency list and right degree vector. Adjacency list is as explained above, and the extra information of right degree vector is just to help construct the object more easily. For instance, with `list = {{0},{1},{0,1}}`, we have `right_deg = {1,2}`, which means that the degree of the right node 0 is 1 while the degree of the right node 1 is 2.

```
vector<vector<int> > list = {{0},{1},{0,1}};
vector<int> right_deg = {1,2};
b_graph G(list, right_deg);
```

6.1.2 Constructor & Destructor Documentation

6.1.2.1 b_graph() [1/4]

```
b_graph::b_graph ( ) [inline]
```

default constructor

```
33 : n(0), np(0) {}
```

6.1.2.2 b_graph() [2/4]

```
b_graph::b_graph (
    const vector< vector< int > > & list,
    const vector< int > & left_deg,
    const vector< int > & right_deg )
```

a fast constructor getting adjacency list and both left and right degree sequences

This constructor takes the adjacency list of left vertices assuming it is sorted, together with left and right degree sequences.

Parameters

| | |
|------------------|---|
| <i>list</i> | list[v] is an increasingly sorted list of right nodes adjacent to the left node v |
| <i>left_deg</i> | left_deg[v] is the degree of the left node v |
| <i>right_deg</i> | right_deg[w] is the degree of the right node w |

```
4 {
5   n = left_deg.size();
6   np = right_deg.size();
7   adj_list = list;
8   left_deg_seq = left_deg;
9   right_deg_seq = right_deg;
10 }
```

6.1.2.3 b_graph() [3/4]

```
b_graph::b_graph (
    const vector< vector< int > > & list,
    const vector< int > & right_deg )
```

a constructor

This constructor takes the list of adjacent vertices and the right degree sequence, and constructs an object.

Parameters

| | |
|------------------|---|
| <i>list</i> | list[v] for a left node v is the list of right nodes w connected to v. This list does not have to be sorted |
| <i>right_deg</i> | right_deg[v] is the degree of the right node v |

```

13 {
14     n = list.size();
15     np = right_deg.size(); // the number of right nodes
16     adj_list = list;
17     left_deg_seq.resize(n);
18     // sorting the list
19     for (int v=0; v<n; v++){
20         sort(adj_list[v].begin(), adj_list[v].end());
21         left_deg_seq[v] = adj_list[v].size();
22     }
23     right_deg_seq = right_deg;
24 }

```

6.1.2.4 b_graph() [4/4]

```

b_graph::b_graph (
    const vector< vector< int > > & list )

```

a constructor

This constructor takes the list of adjacent vertices

Parameters

| | |
|-------------|---|
| <i>list</i> | list[v] for a left node v is the list of right nodes w connected to v. This list does not have to be sorted |
|-------------|---|

```

27 {
28     // goal: finding right degrees and calling the above constructor
29     // first, we find the number of right nodes
30     np = 0; // the number of right nodes
31     n = list.size();
32     adj_list = list;
33     left_deg_seq.resize(n);
34     for (int v=0; v<adj_list.size(); v++){
35         //cerr << " v " << v << endl;
36         sort(adj_list[v].begin(), adj_list[v].end());
37         if (adj_list[v].size() > 0 and adj_list[v][adj_list[v].size()-1] >
            np)
38             np = adj_list[v][adj_list[v].size()-1];
39         left_deg_seq[v] = adj_list[v].size();
40     }
41     np++; // node indexing is zero based
42
43     right_deg_seq.resize(np);
44     fill(right_deg_seq.begin(), right_deg_seq.end(), 0); // make all elements 0
45     for (int v=0; v<list.size(); v++)
46         for (int i=0; i<list[v].size(); i++)
47             right_deg_seq[list[v][i]]++;
48 }

```

6.1.3 Member Function Documentation

6.1.3.1 get_adj_list()

```

vector< int > b_graph::get_adj_list (
    int v ) const

```

returns the adjacency list of a given left vertex

```
51 {  
52     if (v < 0 or v >= n)  
53         cerr << "b_graph::get_adj_list, index v out of range" << endl;  
54     return adj_list[v];  
55 }
```

6.1.3.2 get_left_degree()

```
int b_graph::get_left_degree (  
    int v ) const
```

returns the degree of a right vertex v

```
66 {  
67     if (v < 0 or v >= n)  
68         cerr << "b_graph::get_left_degree, index v out of range" << endl;  
69     return left_deg_seq[v];  
70 }
```

6.1.3.3 get_left_degree_sequence()

```
vector< int > b_graph::get_left_degree_sequence ( ) const
```

return the left degree sequence

```
78 {  
79     return left_deg_seq;  
80 }
```

6.1.3.4 get_right_degree()

```
int b_graph::get_right_degree (  
    int v ) const
```

returns the degree of a right vertex v

```
59 {  
60     if (v < 0 or v >= n)  
61         cerr << "b_graph::get_right_degree, index v out of range" << endl;  
62     return right_deg_seq[v];  
63 }
```

6.1.3.5 get_right_degree_sequence()

```
vector< int > b_graph::get_right_degree_sequence ( ) const
```

return the right degree sequence

```
73 {  
74     return right_deg_seq;  
75 }
```

6.1.3.6 nu_left_vertices()

```
int b_graph::nu_left_vertices ( ) const
```

returns the number of left vertices

```
84 {  
85     return n;  
86 }
```

6.1.3.7 nu_right_vertices()

```
int b_graph::nu_right_vertices ( ) const
```

returns the number of right vertices

```
89 {  
90     return np;  
91 }
```

6.1.4 Friends And Related Function Documentation

6.1.4.1 operator!=

```
bool operator!= (   
                    const b_graph & G1,  
                    const b_graph & G2 ) [friend]
```

comparing for inequality

```
131 {  
132     return !(G1 == G2);  
133 }
```

6.1.4.2 operator<<

```
ostream& operator<< (
    ostream & o,
    const b_graph & G ) [friend]
```

printing the graph to the output

```
95 {
96     int n = G.nu_left_vertices();
97     vector<int> list;
98     for (int i=0;i<n;i++){
99         list = G.get_adj_list(i);
100         o << i << " -> ";
101         for (int j=0;j<list.size();j++){
102             o << list[j];
103             if (j < list.size()-1)
104                 o << ", ";
105         }
106         o << endl;
107     }
108     return o;
109 }
```

6.1.4.3 operator==

```
bool operator== (
    const b_graph & G1,
    const b_graph & G2 ) [friend]
```

comparing two graphs for equality

```
112 {
113     int n1 = G1.nu_left_vertices();
114     int n2 = G2.nu_left_vertices();
115
116     int np1 = G1.nu_right_vertices();
117     int np2 = G2.nu_right_vertices();
118     if (n1!= n2 or np1 != np2)
119         return false;
120     vector<int> list1, list2;
121     for (int v=0; v<n1; v++){
122         list1 = G1.get_adj_list(v);
123         list2 = G2.get_adj_list(v);
124         if (list1 != list2)
125             return false;
126     }
127     return true;
128 }
```

6.1.5 Member Data Documentation

6.1.5.1 adj_list

```
vector<vector<int>> > b_graph::adj_list [private]
```

adjacency list for left vertices, where for $0 \leq v < n$, `adj_list[v]` is a sorted list of right vertices connected to v .

6.1.5.2 left_deg_seq

```
vector<int> b_graph::left_deg_seq [private]
```

degree sequence for left vertices, where left_deg_seq[v] is the degree of the left node v

6.1.5.3 n

```
int b_graph::n [private]
```

the number of left vertices

6.1.5.4 np

```
int b_graph::np [private]
```

the number of right vertices

6.1.5.5 right_deg_seq

```
vector<int> b_graph::right_deg_seq [private]
```

degree sequence for right vertices, where left_deg_seq[v] is the degree of the right node v

The documentation for this class was generated from the following files:

- [bipartite_graph.h](#)
- [bipartite_graph.cpp](#)

6.2 b_graph_decoder Class Reference

Decodes a simple unmarked bipartite graph.

```
#include <bipartite_graph_compression.h>
```

Public Member Functions

- [b_graph_decoder](#) (vector< int > a_, vector< int > b_)
constructor
- void [init](#) ()
initializes x as empty list of size n, beta as b, U with b and W with a
- pair< mpz_class, mpz_class > [decode_node](#) (int i, mpz_class tN)
decodes the connectivity list of a left node $0 \leq i < n$ given $\tilde{N}_{i,i}$
- pair< mpz_class, mpz_class > [decode_interval](#) (int i, int j, mpz_class tN)
decodes the connectivity list of left vertices $i \leq v \leq j$ given $\tilde{N}_{i,j}$
- [b_graph_decode](#) (mpz_class f)
decodes the bipartite graph given the encoded integer

Private Attributes

- int [n](#)
number of left vertices
- int [np](#)
number of right vertices
- vector< int > [a](#)
left degree sequence
- vector< int > [b](#)
right degree sequence
- vector< vector< int > > [x](#)
the adjacency list of left nodes for the decoded graph
- [reverse_fenwick_tree](#) U
reverse Fenwick tree initialized with the right degree sequence b, and after decoding vertex i, for $0 \leq v < n'$, we have $U_v = \sum_{k=v}^{n'-1} b_k(i)$
- [reverse_fenwick_tree](#) W
keeping partial sums for the degree sequence a. More precisely, for $0 \leq v < n$, we have $W_v = \sum_{k=v}^{n-1} a_k$
- vector< int > [beta](#)
the sequence $\vec{\beta}$, where before decoding vertex i, for $0 \leq v < n'$, we have $\beta_v = b_v(i)$

6.2.1 Detailed Description

Decodes a simple unmarked bipartite graph.

Decodes a simple bipartite graph given its encoded integer. We assume that the decoder knows the left and right degree sequences of the encoded graph, hence these sequences must be given when a decoder object is being constructed. For instance, borrowing the degree sequences of the example we used to explain the [b_graph_encoder](#) class:

```
vector<int> a = {1,1,2};
vector<int> b = {2,2};
b_graph_decoder D(a,b);
```

Then, if variable f of type mpz_class is obtained from a [b_graph_encoder](#) class, we can reconstruct the graph using f:

```
b_graph Ghat = D.decode(f);
```

Then, the graph Ghat will be equal to the graph G. Here is a full example showing the procedure of compression and decompression together:

```
vector<int> a = {1,1,2}; // left degree sequence
vector<int> b = {2,2}; // right degree sequence

b_graph G({{0},{1},{0,1}}); // defining the graph

b_graph_encoder E(a,b); // constructing the encoder object
mpz_class f = E.encode(G);

b_graph_decoder D(a, b);
b_graph Ghat = D.decode(f);

if (Ghat == G)
    cout << " we successfully reconstructed the graph! " << endl;
```

6.2.2 Constructor & Destructor Documentation

6.2.2.1 b_graph_decoder()

```
b_graph_decoder::b_graph_decoder (
    vector< int > a_,
    vector< int > b_ )
```

constructor

```
188 {
189     a = a_;
190     b = b_;
191     n = a.size();
192     np = b.size();
193     init();
194 }
```

6.2.3 Member Function Documentation

6.2.3.1 decode()

```
b_graph b_graph_decoder::decode (
    mpz_class f )
```

decodes the bipartite graph given the encoded integer

Parameters

| | |
|-----|--|
| f | which is $\lceil N(G) / \prod b_v! \rceil$ |
|-----|--|

Returns

the decoded bipartite graph G

```

270 {
271     mpz_class prod_b_factorial = prod_factorial(b, 0, np-1);
272     mpz_class tN = f * prod_b_factorial;
273     decode_interval(0,n-1,tN);
274     return b_graph(x, b);
275 }
```

6.2.3.2 decode_interval()

```

pair< mpz_class, mpz_class > b_graph_decoder::decode_interval (
    int i,
    int j,
    mpz_class tN )
```

decodes the connectivity list of left vertices $i \leq v \leq j$ given $\tilde{N}_{i,j}$

Parameters

| | |
|-------|---------------------------|
| i,j | endpoints of the interval |
| tN | $\tilde{N}_{i,j}$ |

Returns

decodes the connectivity list of vertices in the range and updated member x. Furthermore, returns a pair where the first component is $N_{i,j}(G)$ and the second is $l_{i,j}(G)$

```

241 {
242     if (i==j)
243         return decode_node(i,tN);
244     int k = (i+j)/ 2; // midpoint to break
245     int Wk = W.sum(k+1);
246     int Wj = W.sum(j+1);
247     mpz_class rkj = compute_product(Wk, Wk - Wj, 1) /
248         prod_factorial(a, k+1, j); // r_{t+1, j}
249     mpz_class tNik = tN / rkj; // \tilde{N}_{i,k}
250     pair<mpz_class, mpz_class> ans; // to keep the return for each subinterval
251     // calling the left subinterval
252     ans = decode_interval(i,k,tNik);
253     // preparing for the right subinterval
254     mpz_class Nik = ans.first;
255     mpz_class lik = ans.second;
256     mpz_class tNkj = (tN - Nik * rkj) / lik; // \tilde{N}_{k+1, j}
257     // calling the right subinterval
258     ans = decode_interval(k+1, j, tNkj);
259     mpz_class Nkj = ans.first;
260     mpz_class lkj = ans.second;
261     mpz_class Nij = Nik * rkj + lik * Nkj;
262     mpz_class lij = lik * lkj;
263     return pair<mpz_class, mpz_class> (Nij, lij);
264 }
```

6.2.3.3 decode_node()

```
pair< mpz_class, mpz_class > b_graph_decoder::decode_node (
    int i,
    mpz_class tN )
```

decodes the connectivity list of a left node $0 \leq i < n$ given $\tilde{N}_{i,i}$

Parameters

| | |
|------|--------------------------|
| i | the vertex to be decoded |
| tN | $\tilde{N}_{i,i}$ |

Returns

decodes the connectivity list and updates the x member, and returns a pair, where the first component is $N_{i,i}(G)$ and the second component is $l_i(G)$

```
207 {
208     mpz_class li = 1;
209     mpz_class Ni = 0;
210     int f, g; // endpoints of the interval for binary search
211     int v;
212     mpz_class y; // helper
213     x[i].clear(); // make sure nothing is in the list to be decoded
214     for (int k=0; k<a[i]; k++){
215         // finding x[i][k]
216         if (k==0)
217             f = 0;
218         else
219             f = 1 + x[i][k-1];
220         g = np-1;
221         while (g > f){
222             v = (f+g)/2;
223             if (binomial(U.sum(1+v), a[i] - k) <= tN)
224                 g = v;
225             else
226                 f = v + 1;
227         }
228         x[i].push_back(f); // decoded the kth connection of vertex i
229         y = binomial(U.sum(1+x[i][k]), a[i] - k);
230         tN = (tN - y) / beta[x[i][k]];
231         Ni += li * y;
232         li *= beta[x[i][k]];
233         beta[x[i][k]]--;
234         U.add(x[i][k], -1);
235     }
236     return pair<mpz_class, mpz_class>(Ni, li);
237 }
```

6.2.3.4 init()

```
void b_graph_decoder::init ( )
```

initializes x as empty list of size n, beta as b, U with b and W with a

```
197 {
198     x.clear();
199     x.resize(n);
200     beta = b;
201     U = reverse_fenwick_tree(b);
202     W = reverse_fenwick_tree(a);
203 }
204 }
```

6.2.4 Member Data Documentation

6.2.4.1 a

```
vector<int> b_graph_decoder::a [private]
```

left degree sequence

6.2.4.2 b

```
vector<int> b_graph_decoder::b [private]
```

right degree sequence

6.2.4.3 beta

```
vector<int> b_graph_decoder::beta [private]
```

the sequence $\vec{\beta}$, where before decoding vertex i , for $0 \leq v < n'$, we have $\beta_v = b_v(i)$

6.2.4.4 n

```
int b_graph_decoder::n [private]
```

number of left vertices

6.2.4.5 np

```
int b_graph_decoder::np [private]
```

number of right vertices

6.2.4.6 U

```
reverse_fenwick_tree b_graph_decoder::U [private]
```

reverse Fenwick tree initialized with the right degree sequence b , and after decoding vertex i , for $0 \leq v < n'$, we have $U_v = \sum_{k=v}^{n'-1} b_k(i)$

6.2.4.7 W

```
reverse_fenwick_tree b_graph_decoder::W [private]
```

keeping partial sums for the degree sequence a . More precisely, for $0 \leq v < n$, we have $W_v = \sum_{k=v}^{n-1} a_k$

6.2.4.8 x

```
vector<vector<int> > b_graph_decoder::x [private]
```

the adjacency list of left nodes for the decoded graph

The documentation for this class was generated from the following files:

- [bipartite_graph_compression.h](#)
- [bipartite_graph_compression.cpp](#)

6.3 b_graph_encoder Class Reference

Encodes a simple unmarked bipartite graph.

```
#include <bipartite_graph_compression.h>
```

Public Member Functions

- [b_graph_encoder](#) (vector< int > a_, vector< int > b_)
constructor
- void [init](#) (const [b_graph](#) &G)
initializes beta and U
- pair< mpz_class, mpz_class > [compute_N](#) (const [b_graph](#) &G)
computes $N(G)$
- mpz_class [encode](#) (const [b_graph](#) &G)
encodes the given bipartite graph G and returns an integer in the specified range

Private Attributes

- `vector< int > beta`
when compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $\beta[v] = b_v(i)$
- `vector< int > a`
the degree sequence for the left nodes
- `vector< int > b`
the degree sequence for the right nodes
- `reverse_fenwick_tree U`
a Fenwick tree which encodes the degree of right nodes. When compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $U.sum[v] = \sum_{k=v}^n b_k(i)$.

6.3.1 Detailed Description

Encodes a simple unmarked bipartite graph.

Encodes a simple bipartite graph in the set of bipartite graphs with given left degree sequence `a` and right degree sequence `b`. Therefore, to construct an encoder object, we need to specify these two degree sequences as vectors of `int`. For instance (in c++11)

```
vector<int> a = {1,1,2};
vector<int> b = {2,2};
b_graph_encoder E(a,b);
```

constructs an encode object `E` which is capable of encoding bipartite graphs having 3 left nodes with degrees 1, 1, 2 (in order) and 2 right nodes with degrees 2,2 (in order). Hence, assume that we have defined such a bipartite graph by giving adjacency list:

```
b_graph G({{0},{1},{0,1}});
```

Note that `G` has left and right degree sequences which are equal to `a` and `b`, respectively. Then, we can use `E` to encode `G` as follows:

```
mpz_class f = E.encode(G);
```

In this way, the encode converts `G` to an integer stored in `f`. Later on, we can use `f` to decode `G`.

6.3.2 Constructor & Destructor Documentation

6.3.2.1 b_graph_encoder()

```
b_graph_encoder::b_graph_encoder (
    vector< int > a_,
    vector< int > b_ ) [inline]
```

constructor

```
46 : a(a_), b(b_) {}
```

6.3.3 Member Function Documentation

6.3.3.1 compute_N()

```
pair< mpz_class, mpz_class > b_graph_encoder::compute_N (
    const b_graph & G )
```

computes $N(G)$

Parameters

| | |
|---|---|
| G | reference to the bipartite graph for which we compute N |
|---|---|

Returns

A pair, where the first component is $N(G)$, and the second component is $l(G)$

```

26                                     {
27     //logger::item_start("bip init");
28     int n_l = G.nu_left_vertices(); // number of left vertices
29     int n_bits = 0;
30     int n_copy = n_l;
31     while (n_copy > 0){
32         n_bits++;
33         n_copy >>= 1;
34     }
35     n_bits += 2;
36
37     vector<pair<int, int> > call_stack(2 * n_bits);
38     vector<pair<mpz_class, mpz_class> > return_stack(2 * n_bits); // first = N, second = l
39     vector<mpz_class> r_stack(2 * n_bits); // stack of r values
40
41     vector<int> status_stack(2 * n_bits);
42     //vector<int> St_stack(2 * n_bits); // stack to store values of St
43
44     call_stack[0] = pair<int, int> (0,n_l-1); // i j
45     status_stack[0] = 0; // newly added
46
47     int call_size = 1; // the size of the call stack
48     int return_size = 0; // the size of the return stack
49
50     int i, j, t, Sj;
51     int status;
52
53     vector<int> gamma; // forward list of the graph
54
55     mpz_class rtj, prod_afac, Nit_rtj, lit_Ntj, bin;
56     //logger::item_stop("bip init");
57     while(call_size > 0){
58         //cerr << " call_size " << call_size << endl;
59         i = call_stack[call_size-1].first;
60         j = call_stack[call_size-1].second;
61         if (i==j){
62             //logger::item_start("bip enc i = j");
63             return_stack[return_size].first = 0; // N_{i,j} is initialized with 0
64             return_stack[return_size].second = 1; // l_{i,j} is initialized with 1
65             r_stack[return_size] = binomial(U.sum(0), a[i]); // r_i = \binom{S_i}{a_i}, s_i =
        U.sum(0)
66             gamma = G.get_adj_list(i);
67             for (int k=0;k<a[i];k++){
68                 //logger::item_start("bip enc i = j binomial");
69                 bin = binomial(U.sum(1+gamma[k]), a[i] - k);
70                 //logger::item_stop("bip enc i = j binomial");
71
72                 //logger::item_start("bip enc i = j arithmetic");
73                 return_stack[return_size].first += return_stack[return_size].second * bin;
74                 return_stack[return_size].second *= beta[gamma[k]];
75                 //logger::item_start("bip enc i = j arithmetic");
76                 beta[gamma[k]]--;
77                 U.add(gamma[k],-1);
78             }
79             return_size++;
80             call_size--;
81             //logger::item_stop("bip enc i = j");
82         }else{
83             //logger::item_start("bip enc i neq j");
84             t = (i+j)/2;
85             status = status_stack[call_size - 1];
86             //logger::item_start("bip enc stacking 0 1");
87             if (status == 0){
88                 // newly added, left node must be called
89                 call_stack[call_size].first = i;
90                 call_stack[call_size].second = t;
91                 status_stack[call_size-1] = 1; // left is called
92                 status_stack[call_size] = 0; // newly added
93                 call_size++;
94             }
95             if (status == 1){
96                 // left is returned
97                 //St_stack[call_size-1] = U.sum(0);

```

```

98         // call the right child
99         call_stack[call_size].first = t+1;
100         call_stack[call_size].second = j;
101         status_stack[call_size-1] = 2; //right is called
102         status_stack[call_size] = 0; // newly called
103         call_size ++;
104     }
105     //logger::item_stop("bip enc stacking 0 1");
106     if (status == 2){
107         //Sj = U.sum(0);
108         //logger::item_start("bip enc i neq j prod_factorial");
109         //prod_afac = prod_factorial(a, t+1, j); // the product of a_k! for t + 1 <= k <= j
110         //logger::item_stop("bip enc i neq j prod_factorial");
111
112         //logger::item_start("bip enc i neq j compute_product");
113         //rtj = compute_product(St_stack[call_size-1], St_stack[call_size-1] - Sj, 1) / prod_afac;
114         //logger::item_stop("bip enc i neq j compute_product");
115
116         //logger::item_start("bip enc i neq j arithmetic");
117         Nit_rtj = return_stack[return_size-2].first * r_stack[return_size-1];
118         lit_Ntj = return_stack[return_size-2].second * return_stack[return_size-1].
first;
119         return_stack[return_size-2].first = Nit_rtj + lit_Ntj; // Ni j
120         return_stack[return_size-2].second = return_stack[return_size-2].second *
return_stack[return_size-1].second; // li j
121         r_stack[return_size - 2] = r_stack[return_size-2] * r_stack[return_size-1];
122         //logger::item_stop("bip enc i neq j arithmetic");
123         return_size --; // pop 2 add 1
124         call_size --;
125     }
126     //logger::item_stop("bip enc i neq j");
127 }
128
129 }
130 if (return_size != 1){
131     cerr << " error: bip compute_N return_size is not 1 it is " << return_size << endl;
132 }
133 return return_stack[0];
134 }

```

6.3.3.2 encode()

```

mpz_class b_graph_encoder::encode (
    const b_graph & G )

```

encodes the given bipartite graph G and returns an integer in the specified range

```

138 {
139     if (a != G.get_left_degree_sequence() or b != G.
get_right_degree_sequence())
140         cerr << " WARNING b_graph_encoder::encoder : vectors a and/or b do not match with the degree sequences
of the given bipartite graph " << endl;
141
142     //init(G); // initialize U and beta for G
143     //pair<mpz_class, mpz_class> ans = compute_N(0,G.nu_left_vertices()-1, G);
144     //init(G);
145     //logger::item_start("bip enc compute N");
146     //pair<mpz_class, mpz_class> ans = compute_N_new(G);
147     //logger::item_stop("bip enc compute N");
148
149     init(G);
150     //logger::item_start("bip enc compute N new r");
151     pair<mpz_class, mpz_class> ans = compute_N(G);
152     //logger::item_stop("bip enc compute N new r");
153     // if (ans.first == ans2.first and ans.second == ans2.second){
154     //     cout << " = " << endl;
155     // }else{
156     //     cout << " != " << endl;
157     // }
158     //if (ans.first!= ans2.first or ans.second != ans2.second){
159     //     cerr << " bip ans != ans2 ans = (" << ans.first << " , " << ans.second << " ) ans2 = (" <<
ans2.first << " , " << ans2.second << " ) " << endl;
160     //}else{
161     //cerr << " the same! ans = (" << ans.first << " , " << ans.second << " ) ans2 = (" << ans2.first << "
, " << ans2.second << " ) " << endl;

```



```

162  //}
163  //mpz_class prod_b_factorial = prod_factorial(b, 0, b.size()-1); // \prod_{i=0}^{n-1} b_i
164
165  //if (prod_b_factorial != ans.second)
166  //  cerr << "EEEEEEEEEEEEEEEEEEEEEEEEEEEE prod_b_factorial != ans.second" << endl;
167
168  bool ceil = false;
169  //logger::item_start("bip enc ceil");
170  if (ans.first % ans.second != 0)
171    ceil = true;
172  //logger::item_stop("bip enc ceil");
173
174  //logger::item_start("bip enc final div");
175  ans.first /= ans.second;
176  //logger::item_stop("bip enc final div");
177  if (ceil)
178    ans.first ++;
179  return ans.first;
180 }

```

6.3.3.3 init()

```

void b_graph_encoder::init (
    const b_graph & G )

```

initializes beta and U

```

9 {
10  // initializing beta
11  beta = G.get_right_degree_sequence();
12
13  // initializing the Fenwick tree
14  U = reverse_fenwick_tree(beta);
15
16  if (a != G.get_left_degree_sequence() or b != G.
    get_right_degree_sequence())
17    cerr << " WARNING b_graph_encoder::init : vectors a and/or b do not match with the degree sequences of
    the given bipartite graph " << endl;
18
19 }

```

6.3.4 Member Data Documentation

6.3.4.1 a

```
vector<int> b_graph_encoder::a [private]
```

the degree sequence for the left nodes

6.3.4.2 b

```
vector<int> b_graph_encoder::b [private]
```

the degree sequence for the right nodes

6.3.4.3 beta

```
vector<int> b_graph_encoder::beta [private]
```

when compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $\text{beta}[v] = b_v(i)$

6.3.4.4 U

```
reverse_fenwick_tree b_graph_encoder::U [private]
```

a Fenwick tree which encodes the degree of right nodes. When compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $U.\text{sum}[v] = \sum_{k=v}^n b_k(i)$.

The documentation for this class was generated from the following files:

- [bipartite_graph_compression.h](#)
- [bipartite_graph_compression.cpp](#)

6.4 bit_pipe Class Reference

A sequence of arbitrary number of bits.

```
#include <bitstream.h>
```

Public Member Functions

- [bit_pipe](#) ()
- [bit_pipe](#) (const unsigned int &n)
constructor given an integer
- [bit_pipe](#) (const mpz_class &n)
constructor given an mpz_class object
- void [shift_right](#) (int n)
shifts n bits to the right.
- void [shift_left](#) (int n)
shift everything n bits to the left
- int [size](#) () const
return the number of chunks
- int [residue](#) () const
returns the number of residual bits in the last chunk
- const vector< unsigned int > & [chunks](#) () const
returns const reference to the bit sequence (object bits)
- void [append_left](#) (const [bit_pipe](#) &B)
append B to the left of me
- unsigned int & [operator\[\]](#) (int n)
returns a reference to the nth chunk
- const unsigned int & [operator\[\]](#) (int n) const
returns a (const) reference to the nth chunk (const)

Private Attributes

- vector< unsigned int > `bits`
a vector of chunks, each of size 4 bytes. This represents an arbitrary sequence of bits
- int `last_bits`
the number of bits in the last chunk (the last chunk starts from MSB, so the `BIT_INT` - `last_bits` many bits to the right (LSB) are empty and should be zero)

Friends

- class `obitstream`
- class `ibitstream`
- ostream & `operator<<` (ostream &o, const `bit_pipe` &B)
write to the output
- `bit_pipe operator<<` (const `bit_pipe` &B, int n)
shifts bits in B n bits to the left
- `bit_pipe operator>>` (const `bit_pipe` &B, int n)
shifts bits in B n bits to the right

6.4.1 Detailed Description

A sequence of arbitrary number of bits.

The `bit_pipe` class implements an arbitrary sequence of bits. This is useful for example when we want to use Elias delta code to write some integer to the output. This can lead to storage efficiencies, since in such cases we will need to work with incomplete bytes.

The bits vector stores an array of chunks, each having 4 bytes (32 bits). For instance the sequence of bits `<11001100110011>` is stored as a single chunk `<11001100110011|000000000000000000>` of size 32 where the | sign shows that the remaining zeros are residuals (not part of data). This is stored as the `last_bits` variable. In this example, `last_bits` is 14 because there are 14 bits of data in the last chunk.

6.4.2 Constructor & Destructor Documentation

6.4.2.1 `bit_pipe()` [1/3]

```
bit_pipe::bit_pipe ( ) [inline]
```

```
26 {bits.resize(0); last_bits = 0;}
```

6.4.2.2 bit_pipe() [2/3]

```
bit_pipe::bit_pipe (
    const unsigned int & n )
```

constructor given an integer

Some examples: $n = 1$, bits = 1|0000000 (followed by 3 zero bytes) $n = 12$, bits = 1100|0000 (followed by 3 zero bytes) $n = 255633$, bits = 11111001 10100100 01|000000 (followed by a zero byte)

```
8                                     {
9  bits.resize(1);
10  bits[0] = n;
11  last_bits = nu_bits(n);
12  bits[0] <=<= BIT_INT - last_bits; // so that n appears in the MSB place
13 }
```

6.4.2.3 bit_pipe() [3/3]

```
bit_pipe::bit_pipe (
    const mpz_class & n )
```

constructor given an mpz_class object

```
15                                     {
16  size_t n_bits = mpz_sizeinbase(n.get_mpz_t(), 2);
17  size_t size = n_bits / BIT_INT + 1; // how many unsigned int chunks we need
18  bits.resize(size);
19  mpz_export(&bits[0],
20            &size,
21            1, // order can be 1 for most significant word first or -1 for least significant first
22            BYTE_INT, // size: each word will be size bytes and
23            0, // Within each word endian can be 1 for most significant byte first, -1 for least
                significant first, or 0 for the native endianness of the host CPU.
24            0, // The most significant nails bits of each word are unused and set to zero, this can be 0
                to produce full words.
25            n.get_mpz_t());
26  bits.resize(size);
27  last_bits = BIT_INT; // at the moment LSB of n is the LSB bit of the rightmost chunk
28  // but we need the MSB of n to be the MSB of the leftmost chunk
29  // in order to do this, we must shift left
30  // but how much? it is related to the remainder of bit count in n with respect to BIT_INT
31  int rem = n_bits % BIT_INT; // the remainder
32  if (rem != 0){
33  // if remainder is zero, nothing should be done
34  // otherwise, shift left BIT_INT - rem bits
35  shift_left(BIT_INT - rem);
36  }
37
38 }
```

6.4.3 Member Function Documentation

6.4.3.1 append_left()

```
void bit_pipe::append_left (
    const bit_pipe & B )
```

append B to the left of me

Example: if this is <1100|0000> and B is <11110000 1111|0000> then this becomes <11110000 11111100> (trailing zero bytes not shown in example)

```
144                                     {
145     if (B.size() == 0) // nothing should be done, B is empty
146         return;
147     int B_res = B.residue(); // number of incomplete bits in B
148     if (B_res == BIT_INT){
149         // B has complete chunks, so I just need to insert chunks of B at the beginning of my chunks
150         bits.insert(bits.begin(), B.chunks().begin(), B.chunks().end());
151         return; // all set!
152     }
153     // B has a residue
154     // so I need to shift myself to the right and then append
155     shift_right(B_res);
156     // then, my leftmost chunk must be combined with the rightmost chunk of B:
157     bits[0] |= B[B.size()-1];
158     // then insert all but the rightmost chunk of B at my left
159     bits.insert(bits.begin(), B.chunks().begin(), B.chunks().end()-1);
160 }
```

6.4.3.2 chunks()

```
const vector<unsigned int>& bit_pipe::chunks ( ) const [inline]
```

returns const reference to the bit sequence (object bits)

```
50 {return bits;}
```

6.4.3.3 operator[]() [1/2]

```
unsigned int & bit_pipe::operator[] (
    int n )
```

returns a reference to the nth chunk

```
176                                     {
177     if (n < 0 or n >= bits.size()){
178         cerr << " ERROR: bit_pipe::operator [] called for value out of range " << n << " the range is [0, " <<
179         bits.size()-1 << "]" << endl;
180     }
181     return bits[n];
182 }
```

6.4.3.4 operator[]() [2/2]

```
const unsigned int & bit_pipe::operator[] (
    int n ) const
```

returns a (const) reference to the nth chunk (const)

```
184                                     {
185     if (n < 0 or n >= bits.size()){
186         cerr << " ERROR: bit_pipe::operator [] called for value out of range " << n << " the range is [0, " <<
187         bits.size()-1 << "]" << endl;
188     }
189     return bits[n];
190 }
```

6.4.3.5 residue()

```
int bit_pipe::residue ( ) const [inline]
```

returns the number of residual bits in the last chunk

```
47 {return last_bits;}
```

6.4.3.6 shift_left()

```
void bit_pipe::shift_left (
    int n )
```

shift everything n bits to the left

```
74                                     {
75     if (n < 0){
76         cerr << " ERROR: bit_pipe::shift_left called for negative value " << n << endl;
77         return;
78     }
79     if (n >= BIT_INT){
80         // we need to remove a number of bytes
81         int bytes_to_remove = n / BIT_INT; // these many bytes must be remove
82         bits.erase(bits.begin(), bits.begin() + bytes_to_remove);
83         n = n % BIT_INT;
84     }
85     if (n == 0)
86         return;
87
88     // when we reach at this line, we have 1 <= n <= 7
89     unsigned int mask = mask_gen(n) << (BIT_INT-n); // n bits in MSB for carryover masking
90     unsigned int carry; // carryover to the left byte
91     for (int i=0; i<bits.size(); i++){
92         carry = (mask & bits[i]) >> (BIT_INT-n); // bring it to the right
93         if ( i > 0)
94             bits[i-1] |= carry; // add carry to the left guy
95         bits[i] <<= n;
96     }
97
98     // now, deal with last_bits
99     last_bits -= n;
100     if (last_bits <= 0){
101         // means that the rightmost byte must vanish
102         last_bits += BIT_INT;
103         bits.pop_back(); // remove the last byte
104     }
105 }
```

6.4.3.7 shift_right()

```
void bit_pipe::shift_right (
    int n )
```

shifts n bits to the right.

Example: if bits is 11111111 11111000 and n = 5, then bits becomes 00000111 11111111 11000000 (trailing zero bytes are not shown in this example)

```
43         {
44     if (n == 0)
45         return; // nothing to do
46     if (n >= BIT_INT){
47         bits.insert(bits.begin(), n / BIT_INT, 0); // n/BIT_INT bytes each zero will be added
48         shift_right(n%BIT_INT);
49         return;
50     }
51     // when we arrive at this line, n must be strictly less than BIT_INT and strictly bigger than zero, i.e.
52     // 0 < n < BIT_INT
53     unsigned int mask = mask_gen(n); // mask is going to be n many ones (in LSB), e.g. if n = 3, mask
54     // is 00000111, this is useful in carrying over LSB of left bytes to the right bytes
55     unsigned int carry_current = 0; // carry over of left bytes to the right. For instance, if we want to
56     // shift 11111111 3 bits to the right, it becomes 00011111 but a carry over 111 must be added to the byte to the
57     // right. This is initially zero
58     unsigned int carry_prev = 0; // the same concept, but for the previous byte (to the left of me).
59     for (int i=0;i<bits.size();i++){
60         carry_current = bits[i] & mask; // find carryover bits for current byte
61         bits[i] >>= n; // shift the current byte
62         carry_prev <= (BIT_INT-n); // put the previous carryover bits in place to be added to the
63         // current byte
64         bits[i] |= carry_prev; // add the carryover to the current byte
65         carry_prev = carry_current; // the current byte is the previous byte for the next byte
66     }
67     if (n > (BIT_INT - last_bits)){
68         // the LSB bits of the last chunk must fall into a new chunk, so I should push_back a new chunk, which
69         // is zero for now
70         carry_prev <= (BIT_INT-n);
71         bits.push_back(carry_prev); // the last byte is the last carryover shifted to the left
72     }
73     last_bits += n;
74     if (last_bits > BIT_INT)
75         last_bits -= BIT_INT;
```

6.4.3.8 size()

```
int bit_pipe::size ( ) const [inline]
```

return the number of chunks

```
44 {return bits.size();}
```

6.4.4 Friends And Related Function Documentation

6.4.4.1 ibitstream

```
friend class ibitstream [friend]
```

6.4.4.2 obitstream

```
friend class obitstream [friend]
```

6.4.4.3 operator<< [1/2]

```
ostream& operator<< (
    ostream & o,
    const bit_pipe & B ) [friend]
```

write to the output

```
110                                     {
111     if (B.bits.size()==0){
112         o << "<>";
113         return o;
114     }
115     o << "<";
116     for (int i=0;i<(B.bits.size()-1); i++){ // the last byte requires special handling
117         bitset<BIT_INT> b(B.bits[i]);
118         o << b << " ";
119     }
120     unsigned int last_byte = B.bits[B.bits.size()-1];
121
122     for (int k=BIT_INT;k>(BIT_INT-B.last_bits);k--){ // starting from MSB bit to LSB
123         for existing bits
124             if (last_byte & (1<<(k-1)))
125                 o << "1";
126             else
127                 o << "0";
128     }
129     o << "|"; // to show the place of the last bit
130     for (int k=BIT_INT-B.last_bits; k>=1; k--){
131         if (last_byte & (1<<(k-1)))
132             o << "1";
133         else
134             o << "0";
135     }
136     o << ">";
137     return o;
138 }
```

6.4.4.4 operator<< [2/2]

```
bit_pipe operator<< (
    const bit_pipe & B,
    int n ) [friend]
```

shifts bits in B n bits to the left

```
163                                     {
164     bit_pipe ans = B;
165     ans.shift_left(n);
166     return ans;
167 }
```


6.4.4.5 operator>>

```
bit_pipe operator>> (
    const bit_pipe & B,
    int n ) [friend]
```

shifts bits in B n bits to the right

```
169                                     {
170     bit_pipe ans = B;
171     ans.shift_right(n);
172     return ans;
173 }
```

6.4.5 Member Data Documentation

6.4.5.1 bits

```
vector<unsigned int> bit_pipe::bits [private]
```

a vector of chunks, each of size 4 bytes. This represents an arbitrary sequence of bits

6.4.5.2 last_bits

```
int bit_pipe::last_bits [private]
```

the number of bits in the last chunk (the last chunk starts from MSB, so the BIT_INT - last_bits many bits to the right (LSB) are empty and should be zero)

The documentation for this class was generated from the following files:

- [bitstream.h](#)
- [bitstream.cpp](#)

6.5 colored_graph Class Reference

this class defines a colored graph, which is obtained from a simple marked graph and the color of edges come from the type of edges

```
#include <graph_message.h>
```

Public Member Functions

- [colored_graph](#) (const [marked_graph](#) &graph, int depth, int max_degree)
constructor from a graph, depth and maximum degree parameters
- [colored_graph](#) ()
default constructor
- void [init](#) (const [marked_graph](#) &G)
initializes other variables. Here, G is the reference to the marked graph based on which this object is being created

Public Attributes

- int [h](#)
the depth up to which look at edge types
- int [Delta](#)
the maximum degree threshold
- [graph_message](#) M
we use the message passing algorithm of class [graph_message](#) to find out edge types
- int [nu_vertices](#)
the number of vertices in the graph.
- vector< vector< pair< int, pair< int, int > > > > [adj_list](#)
adj_list[i] is the list of edges connected to vertex i, each of the format (other endpoint, color component towards i, color component towards other endpoint). Therefore, the color of an edge between v and its ith neighbor is of the form (adj_list[v][i].second.first, adj_list[v][i].second.second)
- vector< vector< int > > [index_in_neighbor](#)
index_in_neighbor[v][i] is the index of vertex v in the adjacency list of the ith neighbor of v
- vector< map< pair< int, int >, int > > [deg](#)
deg[v] for a vertex v is a map, where deg[v][(m, m')] for a pair of non star types m, m' is the number of edges connected to v with type m towards v and type m' towards the other endpoint. Note that only non star types appear in this map.
- vector< vector< int > > [ver_type](#)
for a vertex v, ver_type[v] is a vector<int> and encodes the mark of v and its colored degree in the following way: ver_type[v][0] is the ver_mark of v, ver_type[v][3k+1], ver_type[v][3k+2] and ver_type[3k+3] are m, m' and n_{m,m'}, where m and m' are edge types, and n_{m,m'} denotes the number of edges connected to v with type (m, m'). The list of m, m' is sorted (lexicographically) to ensure unique representation. Since we only represent types with nonzero n_{m,m'}, we are effectively giving the nonzero entries of the colored degree matrix, resulting in an improvement over storing the whole degree matrix.
- map< vector< int >, int > [ver_type_dict](#)
the dictionary mapping vertex types to integers, obtained from the ver_type array defined above
- vector< vector< int > > [ver_type_list](#)
the list of all distinct vertex types, obtained from the ver_type array.
- vector< int > [ver_type_int](#)
vertex type converted to integers, using the ver_type_dict map, i.e. ver_type_int[v] = ver_type_dict[ver_type[v]]
- vector< bool > [is_star_vertex](#)
for $0 \leq v < n$, is_star_vertex[v] is true if vertex v has at least one star typed edge connected to it
- vector< int > [star_vertices](#)
the (sorted) list of star_vertices, where a star vertex is the one which has at least one star type vertex connected to it.

6.5.1 Detailed Description

this class defines a colored graph, which is obtained from a simple marked graph and the color of edges come from the type of edges

quick member overview:

- `h` and `Delta` are parameters that determine depth and maximum degree to form edge types,
- `M` is a member with type `graph_message` that is used to form edge types,
- `nu_vertices`: number of vertices in the graph
- `adj_list`: the adjacency list of vertices, which also includes edge colors
- `adj_location`: map for finding where neighbors of vertices are in the adjacency list
- `ver_type`: a vector for each vertex, containing mark + vectorized degree matrix
- `ver_type_dict`: dictionary mapping vertex mark + degree matrix to integer
- `ver_type_list`: list of "distinct" vertex types
- `ver_type_int`: vertex types converted to integers

Sample Usage

```
marked_graph G;
... //define G
int h = 10;
int Delta = 5;
colored_graph C(G, h, Delta);
```

6.5.2 Constructor & Destructor Documentation

6.5.2.1 colored_graph() [1/2]

```
colored_graph::colored_graph (
    const marked_graph & graph,
    int depth,
    int max_degree ) [inline]
```

constructor from a graph, depth and maximum degree parameters

```
148                                     : M(graph, depth, max_degree),
149 {
150     init(graph); // initialize other variables
151 }
```

6.5.2.2 colored_graph() [2/2]

```
colored_graph::colored_graph ( ) [inline]
```

default constructor

```
154 {}
```

6.5.3 Member Function Documentation

6.5.3.1 init()

```
void colored_graph::init (
    const marked_graph & G )
```

initializes other variables. Here, G is the reference to the marked graph based on which this object is being created

- updates messages for M
- updates adj_list
- updates ver_type, ver_type_dict, ver_type_list, ver_type_int
- to make sure, checks whether the sum of degree matrices is symmetric

```
531 {
532     logger::add_entry("colored_graph::init init", "");
533     nu_vertices = G.nu_vertices;
534     //adj_location = G.adj_location; // neighborhood structure is the same as the given graph
535     index_in_neighbor = G.index_in_neighbor;
536
537     // assigning edge colors based on the messages given by M
538     //M.update_messages();
539     adj_list.resize(nu_vertices);
540
541     // updating adj_list
542     logger::add_entry("updating adj_list", "");
543     int w, my_location, color_v, color_w;
544     for (int v=0; v<nu_vertices; v++){
545         adj_list[v].resize(G.adj_list[v].size()); // the same number of neighbors here
546         for (int i=0; i<G.adj_list[v].size(); i++){
547             w = G.adj_list[v][i].first; // the ith neighbor, the same as in G
548             //my_location = G.adj_location[w].at(v); // where v stands among the neighbors of w
549             my_location = index_in_neighbor[v][i];
550             color_v = M.messages[v][i]; // the color towards v corresponds to the message v sends to w
551             color_w = M.messages[w][my_location]; // the color towards w is the message w sends towards
552             v
553             adj_list[v][i] = pair<int, pair<int, int>>>(w, pair<int, int>(color_v, color_w)); // add w as
554             a neighbor, in the same order as in G, and add the colors towards v and w
555         }
556     }
557
558     // updating the vertex type sequence, dictionary and list, i.e. variables ver_type, ver_type_dict and
559     ver_type_list
560     // we also update ver_type_int
561
562     // implement and update deg and type_vertex_list
563
564     int m, mp; // pair of types
565
566     logger::add_entry("Find deg and ver_types", "");
567     deg.resize(nu_vertices);
568     is_star_vertex.resize(nu_vertices);
569     ver_type.resize(nu_vertices);
570     ver_type_int.resize(nu_vertices);
```

```

568
569 for (int v=0;v<nu_vertices;v++){
570     is_star_vertex[v] = false; // it is false unless we figure out otherwise, see below
571     for (int i=0;i<adj_list[v].size(); i++){
572         m = adj_list[v][i].second.first;
573         mp = adj_list[v][i].second.second;
574         if (M.is_star_message[m] == false and M.is_star_message[mp] == false)
575         {
576             // this edge is not star type
577             if (deg[v].find(pair<int, int>(m, mp)) == deg[v].end()){
578                 // this does not exist, so create it, since this is the first edge, its value must be 1
579                 deg[v][pair<int, int>(m, mp)] = 1;
580                 //type_vertex_list[pair<int, int>(m, mp)].push_back(v); // this must be done when we see the type
581                 (m, mp) for the first time here, so as to avoid multiple placing of v in the list
582             }else{
583                 // the edge exists, we only need to increase it by one
584                 deg[v][pair<int, int>(m, mp)] ++;
585             }
586         }else{
587             // this is a star type vertex
588             is_star_vertex[v] = true;
589         }
590     }
591     // check if it was star vertex
592     if (is_star_vertex[v] == true)
593         star_vertices.push_back(v);
594
595     // now, we form the type of this vertex
596     // the type of a vertex is a vector x as follows:
597     // x[0] is the vertex mark of v
598     // x[3k+1], x[3k+2], x[3k+3] = (m_k, mp_k, deg[v][(m_k, mp_k)]) where (m_k, mp_k) is the kt key present
599     // in the map deg[v]. Since deg[v] is a map, we read its elements in increasing order (lexicographic order for
600     // pairs (m, mp)), hence this list is on a 1-1 correspondence with the pair (\theta(v), D(v)) in the paper.
601     vector<int> vt; // type of v
602     vt.resize(1+3 * deg[v].size()); // motivated by the above explanation
603     vt[0] = G.ver_mark[v]; // mark of v
604     int k = 0; // current index of vt
605     for (map<pair<int, int>, int>::iterator it = deg[v].begin(); it != deg[v].end(); it++){
606         vt[++k] = it->first.first; // m
607         vt[++k] = it->first.second; // mp
608         vt[++k] = it->second;
609     }
610     ver_type[v] = vt;
611     // find ver_type_int[v]
612     if (ver_type_dict.find(vt) == ver_type_dict.end()){
613         // this is a new type, so add it to the dictionary and the list
614         ver_type_dict[vt] = ver_type_list.size();
615         ver_type_list.push_back(vt);
616     }
617     ver_type_int[v] = ver_type_dict[vt];
618 }

```

6.5.4 Member Data Documentation

6.5.4.1 adj_list

vector<vector<pair<int, pair<int, int> > > > colored_graph::adj_list

adj_list[i] is the list of edges connected to vertex i, each of the format (other endpoint, color component towards i, color component towards other endpoint). Therefore, the color of an edge between v and its ith neighbor is of the form (adj_list[v][i].second.first, adj_list[v][i].second.second)

6.5.4.2 deg

```
vector<map<pair<int, int> , int> > colored_graph::deg
```

deg[v] for a vertex v is a map, where deg[v][(m, m')] for a pair of non star types m, m' is the number of edges connected to v with type m towards v and type m' towards the other endpoint. Note that only non star types appear in this map.

6.5.4.3 Delta

```
int colored_graph::Delta
```

the maximum degree threshold

6.5.4.4 h

```
int colored_graph::h
```

the depth up to which look at edge types

6.5.4.5 index_in_neighbor

```
vector<vector<int> > colored_graph::index_in_neighbor
```

index_in_neighbor[v][i] is the index of vertex v in the adjacency list of the ith neighbor of v

6.5.4.6 is_star_vertex

```
vector<bool> colored_graph::is_star_vertex
```

for $0 \leq v < n$, is_star_vertex[v] is true if vertex v has at least one star typed edge connected to it

6.5.4.7 M

```
graph_message colored_graph::M
```

we use the message passing algorithm of class [graph_message](#) to find out edge types

6.5.4.8 nu_vertices

```
int colored_graph::nu_vertices
```

the number of vertices in the graph.

6.5.4.9 star_vertices

```
vector<int> colored_graph::star_vertices
```

the (sorted) list of star_vertices, where a star vertex is the one which has at least one star type vertex connected to it.

6.5.4.10 ver_type

```
vector<vector<int> > colored_graph::ver_type
```

for a vertex v , $\text{ver_type}[v]$ is a $\text{vector}<\text{int}>$ and encodes the mark of v and its colored degree in the following way: $\text{ver_type}[v][0]$ is the ver_mark of v , $\text{ver_type}[v][3k+1]$, $\text{ver_type}[v][3k+2]$ and $\text{ver_type}[v][3k+3]$ are m , m' and $n_{m,m'}$, where m and m' are edge types, and $n_{m,m'}$ denotes the number of edges connected to v with type (m, m') . The list of m, m' is sorted (lexicographically) to ensure unique representation. Since we only represent types with nonzero $n_{m,m'}$, we are effectively giving the nonzero entries of the colored degree matrix, resulting in an improvement over storing the whole degree matrix.

6.5.4.11 ver_type_dict

```
map<vector<int>, int > colored_graph::ver_type_dict
```

the dictionary mapping vertex types to integers, obtained from the ver_type array defined above

6.5.4.12 ver_type_int

```
vector<int> colored_graph::ver_type_int
```

vertex type converted to integers, using the ver_type_dict map, i.e. $\text{ver_type_int}[v] = \text{ver_type_dict}[\text{ver_type}[v]]$

6.5.4.13 ver_type_list

```
vector<vector<int> > colored_graph::ver_type_list
```

the list of all distinct vertex types, obtained from the ver_type array.

The documentation for this class was generated from the following files:

- [graph_message.h](#)
- [graph_message.cpp](#)

6.6 fenwick_tree Class Reference

Fenwick tree class.

```
#include <fenwick.h>
```

Public Member Functions

- [fenwick_tree](#) ()
default constructor
- [fenwick_tree](#) (vector< int >)
constructor, which takes a vector of values and initializes
- int [size](#) ()
the size of the array, which is sums.size()-1, since sums is one based
- void [add](#) (int k, int val)
- int [sum](#) (int k)

Private Attributes

- vector< int > [sums](#)
a one based vector containing sum of values

6.6.1 Detailed Description

Fenwick tree class.

this class computes the partial sums of an array. More precisely, we feed it a vector of integers, and it can compute the sum of values up to a certain index efficiently. Moreover, we can change the value of an index. Both these operations are done in $O(\log n)$ where n is the size of the array.

6.6.2 Constructor & Destructor Documentation

6.6.2.1 fenwick_tree() [1/2]

```
fenwick_tree::fenwick_tree ( ) [inline]
```

default constructor

```
23     {
24         sums.resize(0);
25     }
```

6.6.2.2 fenwick_tree() [2/2]

```
fenwick_tree::fenwick_tree (
    vector< int > vals )
```

constructor, which takes a vector of values and initializes

```
9 {
10     int n = vals.size();
11     sums.resize(n+1);
12     // initializes at zero
13     for (int i=1;i<=n;i++)
14         sums[i] = 0;
15     for (int i=0;i<n;i++)
16         add(i,vals[i]); // add values one by one
17 }
```

6.6.3 Member Function Documentation

6.6.3.1 add()

```
void fenwick_tree::add (
    int k,
    int val )
```

gets a (zero based) index k, and add to that value

Parameters

| | |
|------------|--|
| <i>k</i> | the index to be modified, this is zero based |
| <i>val</i> | the value to be added to the above index |

```
20 {
21     k = k +1; // the sums vector is one based while the index k was zero based
22     while (k < sums.size()){
23         sums[k] += val;
24         k += (k & -k);
25     }
26 }
```

6.6.3.2 size()

```
int fenwick_tree::size ( ) [inline]
```

the size of the array, which is sums.size()-1, since sums is one based

```
32 {
33     return sums.size() - 1;
34 }
```

6.6.3.3 sum()

```
int fenwick_tree::sum (
    int k )
```

returns the sum of values from 0 to k

Parameters

| | |
|----------|---|
| <i>k</i> | the index up to which (including) the sum is computed |
|----------|---|

```
30 {
31     k = k + 1; // the sums vector is one based while the index k was zero based
32     int sum_computed = 0;
33     while (k > 0){
34         sum_computed += sums[k];
35         k -= (k & -k); // reduce the lsb bit
36     }
37     return sum_computed;
38 }
```

6.6.4 Member Data Documentation

6.6.4.1 sums

```
vector<int> fenwick_tree::sums [private]
```

a one based vector containing sum of values

sums[k] contains the sum of values in the interval (k-lsb(k), k]. Here lsb(k) denotes the rightmost one in k.

The documentation for this class was generated from the following files:

- [fenwick.h](#)
- [fenwick.cpp](#)

6.7 graph Class Reference

simple unmarked graph

```
#include <simple_graph.h>
```

Public Member Functions

- [graph](#) ()
default constructor
- [graph](#) (const vector< vector< int > > &list, const vector< int > °)
a constructor
- [graph](#) (const vector< vector< int > > &list)
constructor, given only the forward adjacency list
- vector< int > [get_forward_list](#) (int v) const
returns the forward adjacency list of a given vertex
- int [get_forward_degree](#) (int v) const
returns the forward degree of a vertex v
- int [get_degree](#) (int v) const
returns the overall degree of a vertex
- vector< int > [get_degree_sequence](#) () const
returns the whole degree sequence
- int [nu_vertices](#) () const
the number of vertices in the graph

Private Attributes

- int [n](#)
the number of vertices in the graph
- vector< vector< int > > [forward_adj_list](#)
for a vertex $0 \leq v < n$, [forward_adj_list\[v\]](#) is a vector containing vertices w such that are adjacent to v and also $w > v$, i.e. the adjacent vertices in the forward direction. For such v , [forward_adj_list\[v\]](#) is sorted increasing.
- vector< int > [degree_sequence](#)
the degree sequence of the graph, where the degree of a vertex is the number of all edges connected to it (not just the ones with greater index).

Friends

- ostream & [operator<<](#) (ostream &o, const [graph](#) &G)
printing the graph to the output
- bool [operator==](#) (const [graph](#) &G1, const [graph](#) &G2)
comparing two graphs for equality
- bool [operator!=](#) (const [graph](#) &G1, const [graph](#) &G2)
comparing for inequality

6.7.1 Detailed Description

simple unmarked graph

6.7.2 Constructor & Destructor Documentation

6.7.2.1 graph() [1/3]

```
graph::graph ( ) [inline]
```

default constructor

```
16 : n(0) {}
```

6.7.2.2 graph() [2/3]

```
graph::graph (
    const vector< vector< int > > & list,
    const vector< int > & deg )
```

a constructor

This constructor takes the list of adjacent vertices and the degree sequence, and constructs an object.

Parameters

| | |
|-------------|--|
| <i>list</i> | list[v] is the list of vertices w adjacent to v such that $w > v$. However, this list does not have to be sorted. |
| <i>deg</i> | deg[v] is the overall degree of the vertex (not only the ones with greater index). |

```
9
10                                     {
11     n = list.size();
12     forward_adj_list = list;
13     // sorting the list
14     for (int v=0; v<n; v++)
15         sort(forward_adj_list[v].begin(), forward_adj_list[v].end());
16     degree_sequence = deg;
17 }
```

6.7.2.3 graph() [3/3]

```
graph::graph (
    const vector< vector< int > > & list )
```

constructor, given only the forward adjacency list

This constructor only takes the forward adjacency list and computes the degree sequence itself

```

22 {
23     n = list.size();
24     forward_adj_list = list;
25
26
27     // sorting the list
28     for (int v=0; v<n; v++)
29         sort(forward_adj_list[v].begin(), forward_adj_list[v].end());
30
31     // finding the degree sequence
32     // first, removing and resize it
33     degree_sequence.clear();
34     degree_sequence.resize(n);
35
36     for (int v=0; v<n; v++){
37         degree_sequence[v] += forward_adj_list[v].size(); // degree to the right
38
39         for (int i=0; i<forward_adj_list[v].size(); i++) // modifying degree of vertices to the
40             degree_sequence[forward_adj_list[v][i]]++;
41     }
42 }

```

6.7.3 Member Function Documentation

6.7.3.1 get_degree()

```

int graph::get_degree (
    int v ) const

```

returns the overall degree of a vertex

```

55     {
56     return degree_sequence[v];
57 }

```

6.7.3.2 get_degree_sequence()

```

vector< int > graph::get_degree_sequence ( ) const

```

returns the whole degree sequence

```

59     {
60     return degree_sequence;
61 }

```

6.7.3.3 get_forward_degree()

```
int graph::get_forward_degree (
    int v ) const
```

returns the forward degree of a vertex v

```
49                                     {
50     if (v < 0 or v >= n)
51         cerr << "graph::get_forward_degree, index v out of range" << endl;
52     return forward_adj_list[v].size();
53 }
```

6.7.3.4 get_forward_list()

```
vector< int > graph::get_forward_list (
    int v ) const
```

returns the forward adjacency list of a given vertex

```
43                                     {
44     if (v < 0 or v >= n)
45         cerr << "graph::get_forward_list, index v out of range" << endl;
46     return forward_adj_list[v];
47 }
```

6.7.3.5 nu_vertices()

```
int graph::nu_vertices ( ) const
```

the number of vertices in the graph

```
64                                     {
65     return n;
66 }
```

6.7.4 Friends And Related Function Documentation

6.7.4.1 operator!=

```
bool operator!= (
    const graph & G1,
    const graph & G2 ) [friend]
```

comparing for inequality

```
102 {
103     return !(G1 == G2);
104 }
```

6.7.4.2 operator<<

```
ostream& operator<< (
    ostream & o,
    const graph & G ) [friend]
```

printing the graph to the output

```
69 {
70     int n = G.nu_vertices();
71     vector<int> list;
72     for (int i=0;i<n;i++){
73         list = G.get_forward_list(i);
74         o << i << " -> ";
75         for (int j=0;j<list.size();j++){
76             o << list[j];
77             if (j < list.size()-1)
78                 o << ", ";
79         }
80         o << endl;
81     }
82     return o;
83 }
```

6.7.4.3 operator==

```
bool operator== (
    const graph & G1,
    const graph & G2 ) [friend]
```

comparing two graphs for equality

```
86 {
87     int n1 = G1.nu_vertices();
88     int n2 = G2.nu_vertices();
89     if (n1!= n2)
90         return false;
91     vector<int> list1, list2;
92     for (int v=0; v<n1; v++){
93         list1 = G1.get_forward_list(v);
94         list2 = G2.get_forward_list(v);
95         if (list1 != list2)
96             return false;
97     }
98     return true;
99 }
```

6.7.5 Member Data Documentation

6.7.5.1 degree_sequence

```
vector<int> graph::degree_sequence [private]
```

the degree sequence of the graph, where the degree of a vertex is the number of all edges connected to it (not just the ones with greater index).

6.7.5.2 forward_adj_list

```
vector<vector<int> > graph::forward_adj_list [private]
```

for a vertex $0 \leq v < n$, `forward_adj_list[v]` is a vector containing vertices w such that are adjacent to v and also $w > v$, i.e. the adjacent vertices in the forward direction. For such v , `forward_adj_list[v]` is sorted increasing.

6.7.5.3 n

```
int graph::n [private]
```

the number of vertices in the graph

The documentation for this class was generated from the following files:

- [simple_graph.h](#)
- [simple_graph.cpp](#)

6.8 graph_decoder Class Reference

Decodes a simple unmarked graph.

```
#include <simple_graph_compression.h>
```

Public Member Functions

- [graph_decoder](#) (vector< int > a_)
constructor given the degree sequence
- void [init](#) ()
initializes x to be empty vector of size n , and U and β by a
- [graph decode](#) (mpz_class f, vector< int > tS_)
given \tilde{N} and a vector \tilde{S} , decodes the graph and returns an object of type `graph`
- pair< mpz_class, mpz_class > [decode_node](#) (int i, mpz_class tN)
decode the node i
- pair< mpz_class, mpz_class > [decode_interval](#) (int i, int j, int I, mpz_class tN, int Sj)
decodes the interval $[i, j]$ with interval index I .

Private Attributes

- vector< int > [a](#)
the degree sequence of the graph.
- int [n](#)
the number of vertices, which is $a.size()$
- int [logn2](#)
 $\lceil \log_2 n \rceil^2$
- vector< vector< int > > [x](#)
the forward adjacency list of the decoded graph
- vector< int > [beta](#)
the sequence $\vec{\beta}$, where after decoding vertex i , for $i \leq v \leq n$ we have $\beta_v = d_v(i)$.
- [reverse_fenwick_tree](#) [U](#)
a Fenwick tree initialized with the degree sequence a , and after decoding vertex i , for $i \leq v$, we have $U_v = \sum_{k=v}^{n-1} d_k(i)$.
- vector< int > [tS](#)
the \tilde{S} vector, which stores the partial sums for the midpoints of intervals with length more than $\log^2 n$.

6.8.1 Detailed Description

Decodes a simple unmarked graph.

Decodes a simple graph given its encoded version. We assume that the decoder knows the degree sequences of the encoded graph, hence these sequences must be given when a decoder object is being constructed. For instance, borrowing the degree sequence of the example we used to explain the [graph_encoder](#) class:

```
vector<int> a = {3,2,2,3};
b_graph_decoder D(a);
```

Then, if variable `f` of type `pair<mpz_class, vector<int> >` is obtained from a [graph_encoder](#) class, we can reconstruct the graph using `f`:

```
graph Ghat = D.decode(f.first, f.second);
```

Then, the graph `Ghat` will be equal to the graph `G`. Here is a full example showing the procedure of compression and decompression together:

```
vector<int> a = {3,2,2,3}; // degree sequence
graph G({1,2,3},{3},{3},{}); // defining the graph
graph_encoder E(a); // constructing the encoder object
pair<mpz_class, vector<int> > f = E.encode(G);

graph_decoder D(a);
graph Ghat = D.decode(f.first, f.second);

if (Ghat == G)
    cout << " we successfully reconstructed the graph! " << endl;
```

6.8.2 Constructor & Destructor Documentation

6.8.2.1 graph_decoder()

```
graph_decoder::graph_decoder (
    vector< int > a_ )
```

constructor given the degree sequence

```
224 {
225     a = a_;
226     n = a.size();
227
228     int log2n = 0; // log of n in base 2
229     int nn = n; // a copy of n
230     while (nn>0){
231         log2n ++;
232         nn = nn >> 1; // divide by 2
233     } // eventually, we count the number of bits in n
234     log2n --; // we count extra, e.g. when n = 1, we end up having 1, rather than 0
235     logn2 = log2n * log2n;
236
237     init(); // init x, beta and U
238 }
```

6.8.3 Member Function Documentation

6.8.3.1 decode()

```
graph graph_decoder::decode (
    mpz_class f,
    vector< int > tS_ )
```

given \tilde{N} and a vector \tilde{S} , decodes the graph and returns an object of type graph

```
249 {
250     init(); // make x, U and beta ready for decoding
251     tS = tS_;
252     //mpz_class prod_a_factorial = 1; // \prod_{i=1}^n a_i!
253     //for (int i=0; i<a.size();i++)
254     //    prod_a_factorial *= compute_product(a[i], a[i], 1);
255
256     mpz_class prod_a_factorial = prod_factorial(a, 0,a.size()-1); // \prod_{i=0}^{n-1} a_i!
257     mpz_class tN = f * prod_a_factorial;
258     decode_interval(0,n-1,1,tN,0);
259     return graph(x, a);
260 }
```

6.8.3.2 decode_interval()

```
pair< mpz_class, mpz_class > graph_decoder::decode_interval (
    int i,
    int j,
    int I,
    mpz_class tN,
    int Sj )
```

decodes the interval $[i, j]$ with interval index I .

Parameters

| | |
|--------|---------------------------|
| i, j | intervals endpoints |
| I | the index of the interval |
| tN | $\tilde{N}_{i,j}$ |
| S_j | S_{j+1} |

Returns

a pair $N_{i,j}, l_{i,j}$ where $N_{i,j} = N_{i,j}(G)$ and $l_{i,j} = l_{i,j}(G)$

```
315 {
316     //cerr << " decode interval " << i << " " << j << " tN " << tN << endl;
317     if (i == j)
318         return decode_node(i, tN);
319
320     // sweeping for zero nodes
```

```

321
322 int t; // place to break
323 int St; // S_{t+1}
324 if ((j-i) > logn2){
325     //cerr << " long interval I = " << I << endl;
326     t = (i+j) / 2; // break at middle, since we have \tilde{S}
327     St = tS[I]; // looking at the \f$\tilde{S}$\f$ vector
328 }else{
329     //cerr << " short interval " << endl;
330     t = i;
331     St = U.sum(i) - 2 * beta[i];
332 }
333
334 //cerr << " decode interval " << i << " " << j << " t " << t << " St " << St << " Sj " << Sj << endl;
335 mpz_class rtj; // \f$t_{t+1, j}\f$
336 mpz_class tNit; // \f$\tilde{N}_{i,t}\f$ for the left decoder
337 mpz_class tNtj; // \f$\tilde{N}_{t+1, j}\f$ for the right decoder
338 mpz_class Nit; // the true N_{i,t} returned by the left decoder
339 mpz_class lit; // the true l_{i,t} returned by the left decoder
340 mpz_class Ntj; // the true N_{t+1, j} returned by the right decoder
341 mpz_class ltj; // the true l_{t+1, j} returned by the right decoder
342 mpz_class Nij; // the true N_{i,j} to return
343 mpz_class lij; // the true l_{i,j} to return
344
345 pair<mpz_class, mpz_class> ans; // returned by subintervals
346
347
348 rtj = compute_product(St - 1, (St - Sj)/2, 2);
349 //cerr << " interval " << i << " " << j << " t " << t << " St " << St << " rtj " << rtj << endl;
350 tNit = tN / rtj;
351
352 // calling the left decoder
353 ans = decode_interval(i, t, 2*I, tNit, St);
354 Nit = ans.first;
355 lit = ans.second;
356
357 // reducing the contribution of the left decoder to prepare for the right decoder
358 tNtj = (tN - Nit * rtj) / lit;
359
360 // calling the right decoder
361 ans = decode_interval(t+1, j, 2*I + 1, tNtj, Sj);
362 Ntj = ans.first;
363 ltj = ans.second;
364
365 // preparing Nij and lij to return
366 Nij = Nit * rtj + lit * Ntj;
367 lij = lit * ltj;
368 return pair<mpz_class, mpz_class> (Nij, lij);
369 }

```

6.8.3.3 decode_node()

```

pair< mpz_class, mpz_class > graph_decoder::decode_node (
    int i,
    mpz_class tN )

```

decode the node i

Parameters

| | |
|------|-------------------|
| i | the vertex index |
| tN | $\tilde{N}_{i,i}$ |

Returns

a pair $(N_{i,i}, l_i)$ where $l_i = l_i(G)$ and $N_{i,i} = N_{i,i}(G)$

```

263 {

```

```

264 //cerr << " decode node " << i << " tN " << tN << endl;
265 //cerr << " beta[i] " << beta[i] << endl;
266 //cerr << " beta " << endl;
267 //for (int k = i; k < n; k++)
268 // cerr << k << " " << beta[k] << endl;
269 //cerr << " U " << endl;
270 //for (int k=i;k<n;k++)
271 // cerr << k << " " << U.sum(k) << endl;
272
273 if (beta[i] == 0)
274     return pair<mpz_class, mpz_class> (0,1);
275
276 mpz_class li = 1; // l_i(G)
277 mpz_class Ni = 0; // N_{i,i}(G)
278 int f, g; // endpoints for the binary search
279 int t; // midpoint for the binary search
280 mpz_class zik, lik;
281 for (int k=0;k<beta[i];k++){
282     if (k==0)
283         f = i+1;
284     else
285         f = x[i][k-1]+1;
286     g = n-1;
287     while(g > f){
288         //cerr << " f , g " << f << " " << g << endl;
289         t = (f+g)/2;
290         // binary search:
291         if(compute_product(U.sum(t+1), beta[i] - k, 1) <= tN)
292             g = t;
293         else
294             f = t+1;
295     }
296     x[i].push_back(f);
297     zik = compute_product(U.sum(x[i][k]+1), beta[i] - k, 1);
298     Ni += li * zik;
299     lik = (beta[i] - k) * beta[x[i][k]];
300     li *= lik;
301     tN -= zik;
302     tN /= lik;
303     U.add(x[i][k],-1);
304     beta[x[i][k]] --;
305 }
306 //cerr << " decoded for " << i << " x: " << endl;
307 //for (int j=0;j<x[i].size(); j++)
308 // cerr << x[i][j] << " ";
309 //cerr << endl;
310 return pair<mpz_class, mpz_class> (Ni, li);
311 }

```

6.8.3.4 init()

```
void graph_decoder::init ( )
```

initializes x to be empty vector of size n, and U and beta by a

```

241 {
242     x.clear();
243     x.resize(n);
244     beta = a;
245     U = reverse_fenwick_tree(a);
246 }

```

6.8.4 Member Data Documentation

6.8.4.1 a

```
vector<int> graph_decoder::a [private]
```

the degree sequence of the graph.

6.8.4.2 beta

```
vector<int> graph_decoder::beta [private]
```

the sequence $\vec{\beta}$, where after decoding vertex i , for $i \leq v \leq n$ we have $\beta_v = d_v(i)$.

6.8.4.3 logn2

```
int graph_decoder::logn2 [private]
```

$\lfloor \log_2 n \rfloor^2$

6.8.4.4 n

```
int graph_decoder::n [private]
```

the number of vertices, which is `a.size()`

6.8.4.5 tS

```
vector<int> graph_decoder::tS [private]
```

the \tilde{S} vector, which stores the partial sums for the midpoints of intervals with length more than $\log^2 n$.

6.8.4.6 U

```
reverse_fenwick_tree graph_decoder::U [private]
```

a Fenwick tree initialized with the degree sequence `a`, and after decoding vertex i , for $i \leq v$, we have $U_v = \sum_{k=v}^{n-1} d_k(i)$.

6.8.4.7 x

```
vector<vector<int> > graph_decoder::x [private]
```

the forward adjacency list of the decoded graph

The documentation for this class was generated from the following files:

- [simple_graph_compression.h](#)
- [simple_graph_compression.cpp](#)

6.9 graph_encoder Class Reference

Encodes a simple unmarked graph.

```
#include <simple_graph_compression.h>
```

Public Member Functions

- [graph_encoder](#) (const vector< int > &a_)
constructor
- void [init](#) (const [graph](#) &G)
initializes beta and U, clears Stilde for a fresh use
- pair< mpz_class, mpz_class > [compute_N](#) (const [graph](#) &G)
computes $N(G)$
- pair< mpz_class, vector< int > > [encode](#) (const [graph](#) &G)
Encodes the graph and returns N together with Stilde.

Private Attributes

- int [n](#)
the number of vertices
- vector< int > [a](#)
the degree sequence
- vector< int > [beta](#)
When compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $\beta_v = d_v(i)$.
- [reverse_fenwick_tree](#) U
a Fenwick tree which encodes the forward degrees to the right. When compute_N is called for $i \leq j$, for $i \leq v$, we have $U_v = \sum_{k=v}^n d_k(i)$.
- vector< int > [Stilde](#)
Summation of forward degrees at $n / \log^2 n$ many points.
- int [logn2](#)
 $\lceil \log_2 n \rceil^2$ where n is the number of vertices

6.9.1 Detailed Description

Encodes a simple unmarked graph.

Encodes a simple graph in the set of graphs with a given degree sequence a . Therefore, to construct an encoder object, we need to specify this degree sequence as a vector of int. For instance (in c++11)

```
vector<int> a = {3,2,2,3};
graph_encoder E(a);
```

constructs an encode object E which is capable of encoding graphs having 4 nodes with degrees 3, 2, 2, 3 (in order). Hence, assume that we have defined such a graph by giving forward adjacency list:

```
graph G({1,2,3},{3},{3},{});
```

Note that G has a degree sequences which is equal to a. Then, we can use E to encode G as follows:

```
pair<mpz_class, vector<int> > f = E.encode(G);
```

In this way, the encode converts G to a pair stored in f, where its first part is an integer, and the second part is the array of integers \hat{S} . Later on, we can use f to decode G.

6.9.2 Constructor & Destructor Documentation

6.9.2.1 graph_encoder()

```
graph_encoder::graph_encoder (
    const vector< int > & a_ )
```

constructor

initializes the degree sequence to $a_$, sets n and logn2, and resizes the Stilde vector

```
11                                     {
12     a = a_;
13     n = a.size();
14     int log2n = 0; // log of n in base 2
15     int nn = n; // a copy of n
16     while (nn>0){
17         log2n ++;
18         nn = nn >> 1; // divide by 2
19     } // eventually, we count the number of bits in n
20     log2n --; // we count extra, e.g. when n = 1, we end up having 1, rather than 0
21     logn2 = log2n * log2n;
22
23     Stilde.clear();
24     Stilde.resize(4 * n / logn2); // look at the explanation of the algorithm, before deriving
        the bound  $16n$ , that  $4n / \lfloor \log_2 n \rfloor^2$  is also an upper bound. After this point, we have used
         $\lfloor \log_2 n \rfloor^2 \geq \log n / 2$  to derive the  $16n$  bound.
25     Stilde[0] = 0;
26 }
```

6.9.3 Member Function Documentation

6.9.3.1 compute_N()

```
pair< mpz_class, mpz_class > graph_encoder::compute_N (
    const graph & G )
```

computes $N(G)$

Parameters

| | |
|---|-------------------------------------|
| G | the reference to the simple graph G |
|---|-------------------------------------|

Returns

A pair, where the first component is $N(G)$ and the second component is $l(G)$.

```

53 {
54
55     int n = G.nu_vertices();
56     int n_bits = 0;
57     int n_copy = n;
58     while (n_copy > 0) {
59         n_bits++;
60         n_copy >>= 1;
61     }
62     n_bits += 2;
63
64     vector<pair<pair<int, int>, int>> call_stack(2 * n_bits);
65     vector<pair<mpz_class, mpz_class>> return_stack(2 * n_bits); // first = N, second = 1
66     vector<mpz_class> r_stack(2 * n_bits); // stack of r values
67     vector<int> status_stack(2 * n_bits);
68     //vector<int> St_stack(2 * n_bits); // stack to store values of St
69
70     call_stack[0].first = pair<int, int> (0,n-1); // i j
71     call_stack[0].second = 1; // I
72     status_stack[0] = 0; // newly added
73
74     int call_size = 1; // the size of the call stack
75     int return_size = 0; // the size of the return stack
76
77     int i, j, I, t, Sj;
78     int status;
79
80     vector<int> gamma; // forward list of the graph
81     mpz_class zik, lik, rtj; // intermediate variables
82     mpz_class Nit_rtj; // result of Nit * rtj
83     mpz_class lit_Ntj; // result of lit * Ntj
84     while (call_size > 0) {
85         // cerr << " printing the whole stack " << endl;
86         // for (int k = 0; k<call_size; k++){
87         //     cerr << k << " : " << call_stack[k].first.first << " " << call_stack[k].first.second << " I " <<
88         //     call_stack[k].second << "s= " << status_stack[k] << endl;
89         // }
90         // cerr << " return stack " << endl;
91         // for (int k=0;k<return_size;k++)
92         //     cerr << k << ": " << return_stack[k].first << " " << return_stack[k].second << endl;
93         i = call_stack[call_size-1].first.first;
94         j = call_stack[call_size-1].first.second;
95         I = call_stack[call_size-1].second;
96         if (i==j){
97             //logger::item_start("sim enc i = j");
98             return_stack[return_size].first = 0; // z_i is initialized with 0
99             return_stack[return_size].second = 1; // l_i is initialize with 1
100             gamma = G.get_forward_list(i); // the forward adjacency list of vertex i
101             r_stack[return_size] = compute_product(U.sum(i) - 1,
102             beta[i], 2); // this is r_i
103             // cerr << " i " << i << " j " << j << " gamma: " << endl;
104             // for (int k=0;k<gamma.size();k++){
105             //     cerr << gamma[k] << " ";
106             //     cerr << endl;
107             //     cerr << " beta " << endl;
108             //     for (int k=0; k<n; k++)
109             //         cerr << beta[k] << " ";
110             //     cerr << endl;
111             for (int k=0;k<gamma.size();k++){
112                 zik = compute_product(U.sum(1+gamma[k]), beta[i] - k, 1); // we are zero
113                 based here, so instead of -k + 1, we have -k
114                 //zik = helper_vars::return_stack[0];
115                 //cerr << " zik " << zik << endl;
116                 return_stack[return_size].first += return_stack[return_size].second * zik;
117                 lik = (beta[i] - k) * beta[gamma[k]]; // we are zero based here, so instead of -k + 1, we
118                 have -k
119                 //cerr << " lik " << lik << endl;
120                 return_stack[return_size].second *= lik;
121                 beta[gamma[k]] -- ;
122                 U.add(gamma[k],-1);
123             }
124             return_size++; // establish the return

```



```

122     call_size--;
123     //logger::item_stop("sim enc i = j");
124 }else{
125     status = status_stack[call_size-1];
126     if (status == 0){
127         // newly added node, we should call its left child
128         t = (i+j) / 2;
129         call_stack[call_size].first.first = i;
130         call_stack[call_size].first.second = t;
131         call_stack[call_size].second = 2*I;
132         status_stack[call_size-1] = 1; // left is called
133         status_stack[call_size] = 0; // newly added
134         call_size++;
135     }
136     if (status == 1){
137         // left is returned
138         t = (i+j) / 2;
139         //St_stack[call_size-1] = U.sum(t+1);
140         if (j - i > logn2)
141             Stilde[I] = U.sum(t+1); //St_stack[call_size-1];
142         // prepare to call right
143
144         call_stack[call_size].first.first = t + 1;
145         call_stack[call_size].first.second = j;
146         call_stack[call_size].second = 2*I + 1;
147         status_stack[call_size-1] = 2; // right is called
148         status_stack[call_size] = 0; // newly called
149         call_size++;
150     }
151
152     if (status == 2){
153         // both are returned, and results can be accessed by the top two elements in return stack
154         //Sj = U.sum(j+1);
155         //logger::item_start("sim enc i neq j compute_product");
156         //rtj = compute_product(St_stack[call_size-1]-1, (St_stack[call_size-1] - Sj)/2, 2);
157         //logger::item_stop("sim enc i neq j compute_product");
158         //rtj = helper_vars::return_stack[0];
159         //cerr << " rtj " << rtj << endl;
160         //Nij = Nit * rtj + lit * Ntj ;
161         //logger::item_start("sim enc i neq j arithmetic");
162         Nit_rtj = return_stack[return_size-2].first * r_stack[return_size-1];
163         lit_Ntj = return_stack[return_size-2].second * return_stack[return_size-1].
first;
164         return_stack[return_size-2].first = Nit_rtj + lit_Ntj; // Nij
165         return_stack[return_size-2].second = return_stack[return_size-2].second *
return_stack[return_size-1].second; // lij
166         r_stack[return_size-2] = r_stack[return_size-2] * r_stack[return_size-1];
167         //logger::item_stop("sim enc i neq j arithmetic");
168         return_size--; // pop 2 add 1
169         call_size--;
170     }
171 }
172 }
173 }
174
175 if (return_size != 1){
176     cerr << " error: return_size is not 1 it is " << return_size << endl;
177 }
178 return return_stack[0];
179 }

```

6.9.3.2 encode()

```

pair< mpz_class, vector< int > > graph_encoder::encode (
    const graph & G )

```

Encodes the graph and returns N together with Stilde.

Parameters

| | |
|-----|----------------------------------|
| G | reference to the graph to encode |
|-----|----------------------------------|

Returns

A pair, where the first component is $\lceil N(G) / \prod_{i=1}^n a_i! \rceil$ where $N(G) = N_{0,n-1}(G)$ and a is the degree sequence of the graph, and the second component is the vector `Stilde` which stores partial mid sum of intervals and has length roughly $n / \log^2 n$

```

181                                     {
182     if (G.get_degree_sequence() != a)
183         cerr << " WARNING graph_encoder::encode : vector a does not match with the degree sequence of the given
            graph ";
184     //init(G); // initialize U and beta
185     //pair<mpz_class, mpz_class> N_ans = compute_N(0,G.nu_vertices()-1,1, G);
186     init(G); // re initializing U abd beta for the second test
187     pair<mpz_class, mpz_class> N_ans = compute_N(G);
188     // init(G);
189     // pair<mpz_class, mpz_class> N_ans_2 = compute_N(G);
190     // if (N_ans.first == N_ans_2.first and N_ans.second == N_ans_2.second){
191     //     cerr << " = " << endl;
192     // }else{
193     //     cerr << " error N_ans and N_ans_2 are not the same, " << endl << "N_ans = (" << N_ans.first << " ,
            " << N_ans.second << ") " << endl << "N_ans_2 = (" << N_ans_2.first << " , " << N_ans_2.second << ") " <<
            endl;
194     // }
195     //if (N_ans.first != N_ans_2.first or N_ans.second != N_ans_2.second)
196     //     cerr << " error N_ans and N_ans_2 are not the same, " << endl << "N_ans = (" << N_ans.first << " , "
            << N_ans.second << ") " << endl << "N_ans_2 = (" << N_ans_2.first << " , " << N_ans_2.second << ") " <<
            endl;
197     //else
198     //     cerr << " N_ans = N_ans_2 " << endl;
199     //mpz_class prod_a_factorial = prod_factorial(a, 0,a.size()-1); // \prod_{i=1}^n a_i!
200     //if (prod_a_factorial != N_ans.second)
201     //     cerr << " ERROR: not equal " << endl;
202     // N_ans.second = \prod_{i=1}^n a_i!
203     // we need the ceiling of the ratio of N_ans.first and prod_a_factorial
204     bool ceil = false; // if true, we will add one to the integer division
205     //logger::item_start("simple_ar");
206     if (N_ans.first % N_ans.second != 0)
207         ceil = true;
208     N_ans.first /= N_ans.second;
209     if (ceil)
210         N_ans.first ++;
211     //logger::item_stop("simple_ar");
212     return pair<mpz_class, vector<int> > (N_ans.first, Stilde);
213 }

```

6.9.3.3 init()

```

void graph_encoder::init (
    const graph & G )

```

initializes beta and U, clears `Stilde` for a fresh use

```

29 {
30     // initializing the beta sequence
31     beta = a;
32
33     //beta.resize(G.nu_vertices());
34     //for (int v=0;v<G.nu_vertices();v++)
35     //     beta[v] = G.get_degree(v);
36
37     // initializing the Fenwick Tree
38     U = reverse_fenwick_tree(beta);
39
40
41     //initializing the partial sum vector Stilde
42     Stilde.clear();
43     Stilde.resize(4 * n / logn2); // TO CHECK,
        2018-10-18_self-compression_Stilde-size-required-2nlogn2.pdf
44     Stilde[0] = 0;
45 }

```

6.9.4 Member Data Documentation

6.9.4.1 a

```
vector<int> graph_encoder::a [private]
```

the degree sequence

6.9.4.2 beta

```
vector<int> graph_encoder::beta [private]
```

When compute_N is called for $i \leq j$, for $i \leq v \leq n$, we have $\beta_v = d_v(i)$.

6.9.4.3 logn2

```
int graph_encoder::logn2 [private]
```

$\lceil \log_2 n \rceil^2$ where n is the number of vertices

6.9.4.4 n

```
int graph_encoder::n [private]
```

the number of vertices

6.9.4.5 Stilde

```
vector<int> graph_encoder::Stilde [private]
```

Summation of forward degrees at $n / \log^2 n$ many points.

6.9.4.6 U

```
reverse_fenwick_tree graph_encoder::U [private]
```

a Fenwick tree which encodes the forward degrees to the right. When `compute_N` is called for $i \leq j$, for $i \leq v$, we have $U_v = \sum_{k=v}^n d_k(i)$.

The documentation for this class was generated from the following files:

- [simple_graph_compression.h](#)
- [simple_graph_compression.cpp](#)

6.10 graph_message Class Reference

this class takes care of message passing on marked graphs.

```
#include <graph_message.h>
```

Public Member Functions

- [graph_message](#) (const [marked_graph](#) &[graph](#), int depth, int max_degree)
constructor, given reference to a graph
- [graph_message](#) ()
default constructor

Public Attributes

- `vector< vector< int > >` [messages](#)
messages[v][i] is the integer version of the message from vertex v towards its ith neighbor (in the order given by adj_list of vertex i in graph G). The message is at any given step that update_messages is running, so after finishing update_message, the messages are at step (depth) h-1.
- `unordered_map< vector< int >, int, vint_hash >` [message_dict](#)
message_dict is the message dictionary at any step that update_messages is running, which maps each message to its corresponding index in the dictionary. When update_messages is over, this corresponds to step (depth) h-1
- `vector< int >` [message_mark](#)
for an integer message m, message_mark[m] is the mark component associated to the message m at any step that update_messages is working. This is basically the last index in the vector message associate to m. When update_messages is over, this corresponds to step (depth) h-1.
- `vector< bool >` [is_star_message](#)
for an integer message m, is_star_message[m] is true if m is a star message and false otherwise. Note that m is star type iff the first index in the vector message corresponding to m is -1. This is updated at step of update_messages, so when it is over, it corresponds to step (depth) h-1.

Private Member Functions

- `void` [update_messages](#) (const [marked_graph](#) &)
performs the message passing algorithm and updates the messages array accordingly
- `void` [send_message](#) (const `vector< int >` &m, int v, int i)
update message_dict and message_list

Private Attributes

- int `h`
the depth up to which we do message passing (the type of edges go through depth h-1)
- int `Delta`
the maximum degree threshold

6.10.1 Detailed Description

this class takes care of message passing on marked graphs.

This graph has a reference to a [marked_graph](#) object for which we perform message passing to find edge types. The edge types are discovered up to depth h-1, and with degree parameter Delta, where h and Delta are member objects. Star type messages (which roughly speaking corresponds to places where there is a vertex in the h neighborhood has degree more than delta) are vectors of size 2, first coordinate being -1, and the second being the edge mark component (towards the 'me' vertex).

Sample Usage

```
marked_graph G;
... //define G
int h = 10;
int Delta = 5;
graph_message M(G, h, Delta);
```

6.10.2 Constructor & Destructor Documentation

6.10.2.1 graph_message() [1/2]

```
graph_message::graph_message (
    const marked_graph & graph,
    int depth,
    int max_degree ) [inline]
```

constructor, given reference to a graph

```
69                                     {
70     h = depth;
71     Delta = max_degree;
72     update_messages(graph); // do message passing
73 }
```

6.10.2.2 graph_message() [2/2]

```
graph_message::graph_message ( ) [inline]
```

default constructor

```
76 {}
```

6.10.3 Member Function Documentation

6.10.3.1 send_message()

```
void graph_message::send_message (
    const vector< int > & m,
    int v,
    int i ) [inline], [private]
```

update message_dict and message_list

send the message m from vertex v towards its ith neighbor. Updates message_dict, message_mark and is_star↔ message_star

sends a message by setting messages, and puts it in the message hash table message_dict. It also updates message_mark and is_star_message corresponding to step s and the input message.

Parameters

| | |
|----------|---|
| <i>m</i> | the message to be sent |
| <i>v</i> | the vertex from which the message is originated |
| <i>i</i> | the message is sent to the ith neighbor of v |

```
487
488 unordered_map<vector<int>, int, vint_hash>::iterator it;
489 /*
490 cerr << " send message ";
491 for (int k=0;k<m.size();k++){
492     cerr << m[k];
493     if (k<m.size()-1)
494         cerr << ", ";
495 }
496 cerr << "): " << v << " -> " << i;
497 */
498
499 it = message_dict.find(m);
500 if (it == message_dict.end()){
501     // this is a new message
502     message_dict.insert(pair<vector<int>, int> (m, message_mark.size())); // insert
503     // the message into the hash table, message_mark[s].size() is in fact the number of registered marks at step s
504     messages[v][i] = message_mark.size(); // set the message
505     message_mark.push_back(m.back()); // register m by adding its mark component (which is
506     // m.back() the last element in m) to the list of marks at step s
507     is_star_message.push_back(m[0]==-1); // check if m is star type, and add this
508     // information to the list
509 }else{
510     // the message already exists, just use the registered integer value corresponding to m and send the
511     // message
512     messages[v][i] = it->second;
513 }
514 //cerr << " message = " << messages[v][i] << endl;
515 }
```

6.10.3.2 update_messages()

```
void graph_message::update_messages (
    const marked_graph & G ) [private]
```

performs the message passing algorithm and updates the messages array accordingly

The structure of messages is as follows. To simplify the notation, we use $M_k(v, w)$ to denote the message sent from v towards w at time step k , this is in fact `messages[v][i][t]` where i is the index of w among neighbors of v .

- For $k = 0$, we have $M_0(v, w) = (\tau_G(v), 0, \xi_G(w, v))$ where $\tau_G(v)$ is the mark of vertex v and $\xi_G(w, v)$ denotes the mark of the edge between v and w towards v .
- For $k > 0$, if the degree of v is bigger than Delta, we have $M_k(v, w) = (-1, \xi_G(w, v))$.
- Otherwise, we form the list $(s_u : u \sim_G v, u \neq w)$, where for $u \sim_G v, u \neq w$, we set $s_u = (M_{k-1}(u, v), \xi_G(u, v))$.
- If for some $u \sim_G v, u \neq w$, the sequence s_u starts with a -1, we set $M_k(v, w) = (-1, \xi_G(w, v))$.
- Otherwise, we sort the sequences s_u nondecreasingly with respect to the lexicographic order and set s to be the concatenation of the sorted list. Finally, we set $M_k(v, w) = (\tau_G(v), \deg_G(v) - 1, s, \xi_G(w, v))$.

```

24 {
25     logger::current_depth++;
26     logger::add_entry("graph_message::update_message init", "");
27     int nu_vertices = G.nu_vertices;
28     int w;
29     int my_location;
30     messages.resize(nu_vertices);
31     //inward_message.resize(nu_vertices);
32     //message_dict.resize(h);
33     //message_list.resize(h);
34     //message_mark.resize(h);
35     //is_star_message.resize(h);
36
37
38     // initialize the messages
39
40     logger::add_entry("resizing messages", "");
41     for (int v=0;v<nu_vertices;v++){
42         messages[v].resize(G.adj_list[v].size());
43         //inward_messages[v].resize(G.adj_list[v].size());
44         //for (int i=0;i<G.adj_list[v].size();i++){
45             //messages[v][i].resize(h);
46             //inward_messages[v][i].resize(h);
47         //}
48     }
49
50     logger::add_entry("initializing messages","", "");
51     vector<int> m(3);
52     unordered_map<vector<int>, int, vint_hash>::iterator it;
53     //map<vector<int>, int>::iterator it;
54
55     for (int v=0;v<nu_vertices;v++){
56
57         for (int i=0;i<G.adj_list[v].size();i++){
58             // the message from v towards the ith neighbor (lets call it w) at time 0 has a mark component which
59             // is \xi(v,w) and a subtree component which is a single root with mark \tau(v). This is encoded as a message
60             // vector with size 3 of the form (\tau(v), 0, \xi(v,w)) where the last 0 indicates that there is no offspring.
61
62             //vector<int> m;
63             //m.clear();
64             //m.push_back(G.ver_mark[v]);
65             //m.push_back(0);
66             //m.push_back(G.adj_list[v][i].second.first);
67
68             m[0] = G.ver_mark[v];
69             m[1] = 0;
70             m[2] = G.adj_list[v][i].second.first;
71             send_message(m, v, i);
72
73             // adding this message to the message dictionary
74             //it = message_dict[0].find(m);
75             //w = G.adj_list[v][i].first;
76
77             /*
78             if (it == message_dict[0].end()){
79                 message_dict[0][m] = message_list[0].size();
80                 messages[v][i][0] = message_list[0].size();
81                 message_list[0].push_back(m);
82             }else{

```

```

83         messages[v][i][0] = it->second;
84     }
85     */
86     //messages[v][i][0] = message_dict[0][m]; // the message at time 0
87 }
88 }
89
90 // these are copies of message_dict, message_mark and is_star_message at the previous step, which are
    used to update messages at the current step.
91
92 //unordered_map<vector<int>, int, vint_hash> message_dict_old;
93 //vector<int> message_mark_old;
94 vector<bool> is_star_message_old;
95 vector<vector<int>> > messages_old;
96
97 // updating messages
98 logger::add_entry("updating messages", "");
99 m.reserve(5+ 2 * Delta);
100 vector<int> m2;
101 m2.reserve(5 + 2*Delta); // an auxiliary message when we need to work with two types of messages
    simultaneously
102 duration<float> diff;
103 high_resolution_clock::time_point t1, t2;
104 float agg_search = 0;
105 float agg_insert = 0;
106 float agg_m = 0;
107 float agg_sort = 0;
108 float agg_neigh_message = 0;
109
110 vector<pair<pair<int, int>, int> > neighbor_messages; // the first component is the message and the
    second is the name of the neighbor
111 // the second component is stored so that after sorting, we know the owner of the message
112 neighbor_messages.reserve(5+2*Delta);
113
114 int nu_star_neigh; // number of star neighbors, i.e. neighbors of a vertex v whose message towards v are
    star type
115 int star_neigh_index; // the index of the star neighbor of v, this is only useful when there is one star
    neighbor, if there are more than one star neighbor, then the message sent from v towards all other neighbors
    are star typed
116 int star_neigh; // the label of the star neighbor, i.e. star_neigh =
    G.adj_list[v][star_neigh_index].first;
117 int previous_message; // the message from the previous step
118 int mark_to_v; // mark towards the current vertex directed from its neighbor
119 vector<int> neighbors_list; // the list of neighbors of a vertex in the order after sorting with respect
    to their corresponding messages
120 neighbors_list.reserve(Delta + 3);
121 int deg_v; // the degree of vertex v
122
123
124
125 for (int s=1; s<h;s++){ // s stands for step
126     //cerr << endl << endl<< " depth " << s << endl;
127     // store variables corresponding to the previous step in their old version, and clearing the variables
    for this step:
128     //message_dict_old = message_dict;
129     messages_old = messages;
130     //message_mark_old = message_mark;
131     is_star_message_old = is_star_message;
132     message_dict.clear();
133     message_mark.clear();
134     is_star_message.clear();
135     // we do not clear messages since we need its size to be the same, and we only modify its content
136
137
138     for (int v=0;v<nu_vertices;v++){
139         deg_v = G.adj_list[v].size();
140         if (deg_v==1){
141             // no need to collect messages, there is only one message towards the one neighbor, which is known
142             m.resize(3); // there is only one message which is of the form  $\backslash f_{\theta}(\theta, 0, x)\backslash f$ , where
             $\backslash f_{\theta}$  is the mark of v, and  $\backslash f_x = \backslash x_i G(w,v)\backslash f$  where  $\backslash f_w\backslash f$  is the only neighbor of v
143             m[0] = G.ver_mark[v];
144             m[1] = 0;
145             m[2] = G.adj_list[v][0].second.first;
146             send_message(m, v, 0);
147         }else{
148             if (deg_v <= Delta){
149                 neighbor_messages.clear();
150                 nu_star_neigh = 0;
151                 for (int i=0;i<deg_v;i++){
152                     w = G.adj_list[v][i].first; // neighbor label
153                     my_location = G.index_in_neighbor[v][i];
154                     previous_message = messages_old[w][my_location]; // the message sent from this neighbor towards
                    v at time t-1
155                     // check if previous message is star
156                     if (is_star_message_old[previous_message]){
157                         nu_star_neigh ++;
158                         star_neigh_index = i;

```



```

159         star_neigh = w;
160     }
161     if (nu_star_neigh >= 2)
162         break; // then message towards all neighbors will be star, no need to collect messages
163     mark_to_v = G.adj_list[v][i].second.first;
164     neighbor_messages.push_back(pair<pair<int, int>, int> (pair<int,int>(previous_message,
mark_to_v), i));
165 }
166 if (nu_star_neigh == 2){
167     // message towards all the neighbors will be star
168     m.resize(2);
169     m[0] = -1;
170     for (int i=0;i<G.adj_list[v].size();i++){
171         m[1] = G.adj_list[v][i].second.first;
172         send_message(m, v, i); // send message m from v towards its ith neighbor at step
s
173     }
174 }
175 if (nu_star_neigh == 1){
176     // the message towards all the neighbors except for that star neighbor is star
177     // let m be the message towards that neighbor and m2 be the star messages
178
179     // sorting neighbor messages
180     sort(neighbor_messages.begin(), neighbor_messages.end());
181
182     // preparing m
183     m.resize(0);
184     m.push_back(G.ver_mark[v]);
185     m.push_back(G.adj_list[v].size()-1);
186
187
188
189     for (int i=0;i<neighbor_messages.size();i++){
190         if (neighbor_messages[i].second != star_neigh_index){
191             // collect the messages of non star neighbors
192             m.push_back(neighbor_messages[i].first.first);
193             m.push_back(neighbor_messages[i].first.second);
194         }
195     }
196     // finalize m by inserting its mark component
197     m.push_back(G.adj_list[v][star_neigh_index].second.first);
198
199     // prepare star messages
200     m2.resize(2);
201     m2[0] = -1;
202     for (int i=0;i<deg_v;i++){
203         if (i==star_neigh_index){
204             // send the prepared message m
205             send_message(m, v, i);
206         }else{
207             // prepare a star message and send it
208             m2[1] = G.adj_list[v][i].second.first;
209             send_message(m2, v, i);
210         }
211     }
212 }
213
214 if (nu_star_neigh == 0){
215     // no star neighbor, so we can prepare messages to all neighbors comfortably as none of them
are star type
216     // we do this by a masking technique
217     // sorting neighbor messages
218     sort(neighbor_messages.begin(), neighbor_messages.end());
219     if (neighbor_messages.size() != deg_v){
220         cerr << " Error: no star messages and yet neighbor_messages does not have a size equal to the
deg of v, step " << s << " v= " << v << " deg_v= " << deg_v << " neighbor_messages.size() " <<
neighbor_messages.size() << endl;
221     }
222     m.resize(1 + 1 + 2*(G.adj_list[v].size()-1) +1); // 1 for vertex mark, 1 for deg -1,
for (deg-1) many neighbors, each we have 2 values, and finally 1 for the mark component
223     m[0] = G.ver_mark[v];
224     m[1] = G.adj_list[v].size()-1;
225     neighbors_list.resize(deg_v);
226     for (int i=0;i<neighbor_messages.size();i++){
227         m[2*(i+1)] = neighbor_messages[i].first.first;
228         m[2*(i+1)+1] = neighbor_messages[i].first.second;
229         neighbors_list[i] = neighbor_messages[i].second;
230     }
231     // swapping the last message so that its mark component comes first, so that we can treat m as
a valid message in our standard
232     swap(m[2*deg_v], m[2*deg_v+1]);
233
234     for (int i=neighbor_messages.size()-1;i>=0;i--){
235         if (i < neighbor_messages.size()-1){
236             swap(m[2*deg_v], m[2*(i+1)+1]);
237             swap(m[2*deg_v+1], m[2*(i+1)]);
238             swap(neighbors_list[deg_v-1], neighbors_list[i]);

```

```

239         }
240         send_message(m,v,neighbors_list[deg_v-1]);
241     }
242 }
243 }
244 if (deg_v > Delta){ // the message towards all neighbors is star
245     m.resize(2);
246     m[0] = -1;
247     for(int i=0;i<deg_v;i++){
248         m[1] = G.adj_list[v][i].second.first;
249         send_message(m,v,i);
250     }
251 }
252 }
253 }
254 }
255
256
257 logger::add_entry(" symmetrizing", "");
258 bool star1, star2;
259 m.resize(2); // prepare for star message
260 m[0] = -1;
261 for (int v=0;v<nu_vertices;v++){
262     for (int i=0;i<G.adj_list[v].size();i++){
263         w = G.adj_list[v][i].first;
264         my_location = G.index_in_neighbor[v][i];
265         if (w > v){ // to avoid going over edges twice
266             star1 = is_star_message[messages[v][i]];
267             star2 = is_star_message[messages[w][my_location]];
268             if (star1 and !star2){
269                 // message[w][my_location] should be star
270                 m[1] = G.adj_list[v][i].second.second;
271                 send_message(m,w,my_location);
272             }
273             if (!star1 and star2){
274                 // messages[v][i] should also become star
275                 m[1] = G.adj_list[v][i].second.first;
276                 send_message(m,v,i);
277             }
278             if ((!star1 and !star2) and (G.adj_list[v].size() > Delta or G.
adj_list[w].size()>Delta)){ // this activates only when h = 1, ensures truncation of degrees
bigger than delta
279                 // message[w][my_location] should be star
280                 m[1] = G.adj_list[v][i].second.second;
281                 send_message(m,w,my_location);
282                 // messages[v][i] should also become star
283                 m[1] = G.adj_list[v][i].second.first;
284                 send_message(m,v,i);
285             }
286         }
287     }
288 }
289 logger::current_depth--;
290
291
292
293
294 // =====
295 // =====
296 // =====
297 // =====
298 // =====
299 // =====
300 // =====
301 // =====
302
303 /*
304 for (int t=1;t<h;t++){
305     for (int v=0;v<nu_vertices;v++){
306         //cerr << " vertex " << v << endl;
307         if (G.adj_list[v].size() <= Delta){
308             // the degree of v is no more than Delta
309             // do the standard message passing by aggregating messages from neighbors
310             // stacking all the messages from neighbors of v towards v
311             neighbor_messages.clear();
312
313             // the message from each neighbor of v, say w, towards v is considered, the mark of the edge
between w and v towards v is added to it, and then all these objects are stacked in neighbor_messages to be
sorted and used afterwards
314             //t1 = high_resolution_clock::now();
315             for (int i=0;i<G.adj_list[v].size();i++){
316                 w = G.adj_list[v][i].first; // what is the name of the neighbor I am looking at now, which is the
ith neighbor of vertex v
317                 //my_location = G.adj_location[w].at(v); <--- the inefficient way
318                 my_location = G.index_in_neighbor[v][i];
319                 // where is the place of node v among the list of neighbors of the ith neighbor of v
320                 int previous_message = messages[w][my_location][t-1]; // the message sent from this neighbor

```

```

    towards v at time t-1
321     int mark_to_v = G.adj_list[v][i].second.first;
322     neighbor_messages.push_back(pair<pair<int, int> , int> (pair<int,int>(previous_message,
mark_to_v), w));
323 }
324 //t2 = high_resolution_clock::now();
325 //diff = t2 - t1;
326 //agg_neigh_message += diff.count();
327
328 //t1 = high_resolution_clock::now();
329 sort(neighbor_messages.begin(), neighbor_messages.end()); // sorts lexicographically
330 //t2 = high_resolution_clock::now();
331 //diff = t2 - t1;
332 //agg_sort += diff.count();
333
334 for (int i=0;i<G.adj_list[v].size();i++){
335     // let w be the current ith neighbor of v
336     int w = G.adj_list[v][i].first;
337     // first, start with the mark of v and the number of offsprings in the subgraph component of the
message
338     //vector<int> m; // the message that v is going to send to w
339     //t1 = high_resolution_clock::now();
340     m.clear();
341     m.push_back(G.ver_mark[v]); // mark of v
342     m.push_back(G.adj_list[v].size()-1); // the number of offsprings in the subgraph component of the
message
343     //t2 = high_resolution_clock::now();
344     //diff = t2 - t1;
345     //agg_m += diff.count();
346
347     // stacking messages from all neighbors of v expect for w towards v at time t-1
348     for (int j=0;j<G.adj_list[v].size();j++){
349         if (neighbor_messages[j].second != w){
350             if (message_list[t-1][neighbor_messages[j].first.first][0] == -1){
351                 // this means that one of the messages that should be aggregated is * typed, therefore the
outgoing messages should also be * typed
352                 // i.e. the message has only two entries: (-1, \xi(w,v)) where \xi(w,v) is the mark of the
edge between v and w towards v
353                 // since after this loop, the mark \xi(w,v) is added to the message (after the comment
starting with 'finally'), we only add the initial -1 part
354                 //t1 = high_resolution_clock::now();
355                 m.resize(0);
356                 m.push_back(-1);
357                 //t2 = high_resolution_clock::now();
358                 //diff = t2 - t1;
359                 //agg_m += diff.count();
360                 break; // the message is decided, we do not need to go over any of the other neighbor
messages, hence break
361             }
362             // this message should be added to the list of messages
363             //t1 = high_resolution_clock::now();
364             m.push_back(neighbor_messages[j].first.first); // message part
365             m.push_back(neighbor_messages[j].first.second); // mark part towards v
366             //t2 = high_resolution_clock::now();
367             //diff = t2 - t1;
368             //agg_m += diff.count();
369
370         }
371     }
372     // if we break, we reach at this point and message is (-1), otherwise the message is of the form
(\tau(v), \deg(v) - 1, ...) where ... is the list of all neighbor messages towards v except for w.
373     // finally, the mark of the edge between v and w towards v, \xi(w,v), should be added to this
list
374     //t1 = high_resolution_clock::now();
375     m.push_back(G.adj_list[v][i].second.first);
376     //t2 = high_resolution_clock::now();
377     //diff = t2 - t1;
378     //agg_m += diff.count();
379
380     // set the current message
381     //t1 = high_resolution_clock::now();
382     it = message_dict[t].find(m);
383     //t2 = high_resolution_clock::now();
384     //diff = t2 - t1;
385     //agg_search += diff.count();
386
387     if (it == message_dict[t].end()){
388         //t1 = high_resolution_clock::now();
389         //message_dict[t][m] = message_list[t].size();
390         message_dict[t].insert(pair<vector<int>, int> (m, message_list[t].size()));
391         //t2 = high_resolution_clock::now();
392         //diff = t2 - t1;
393         //agg_insert += diff.count();
394
395         messages[v][i][t] = message_list[t].size();
396         message_list[t].push_back(m);
397     }else{

```

```

398         messages[v][i][t] = it->second;
399     }
400 }
401 }else{
402     // if the degree of v is bigger than Delta, the message towards all neighbors is of the form *
403     // i.e. message of v towards a neighbor w is of the form (-1, \xi(w,v)) where \xi(w,v) is the mark
of the edge between v and w towards v
404     for (int i=0;i<G.adj_list[v].size();i++){
405         //vector<int> m; // the current message from v to ith neighbor
406         //t1 = high_resolution_clock::now();
407         m.clear();
408         m.resize(2);
409         m[0] = -1;
410         m[1] = G.adj_list[v][i].second.first;
411         //t2 = high_resolution_clock::now();
412         //diff = t2 - t1;
413         //agg_m += diff.count();
414
415         // set the current message
416         //t1 = high_resolution_clock::now();
417         it = message_dict[t].find(m);
418         //t2 = high_resolution_clock::now();
419         //diff = t2 - t1;
420         //agg_search += diff.count();
421
422         if (it == message_dict[t].end()){
423             //t1 = high_resolution_clock::now();
424             //message_dict[t][m] = message_list[t].size();
425             message_dict[t].insert(pair<vector<int>, int> (m, message_list[t].size()));
426             //t2 = high_resolution_clock::now();
427             //diff = t2 - t1;
428             //agg_insert += diff.count();
429             messages[v][i][t] = message_list[t].size();
430             message_list[t].push_back(m);
431         }else{
432             messages[v][i][t] = it->second;
433         }
434     }
435 }
436 }
437 }
438 cerr << " total time to search in hash table: " << agg_search << endl;
439 cerr << " total time to insert in hash table: " << agg_insert << endl;
440 cerr << " total time to modify vector m " << agg_m << endl;
441 cerr << " total time to sort " << agg_sort << endl;
442 cerr << " total time to collect neighbor messages " << agg_neigh_message << endl;
443 // now, we should update messages at time h-1 so that if the message from v to w is *, i.e. is of the
form (-1,x), then the message from w to v is also of the similar form, i.e. it is (-1,x') where x' = \xi(v,w)
444 logger::add_entry("symmetrizing", "");
445 for (int v=0;v<nu_vertices;v++){
446     for (int i=0;i<G.adj_list[v].size();i++){
447         if (message_list[h-1][messages[v][i][h-1]][0] == -1){
448             // it is of the form *
449             w = G.adj_list[v][i].first; // the other endpoint of the edge
450             //my_location = G.adj_location[w].at(v); // so that adj_list[w][my_location].first = v
451             my_location = G.index_in_neighbor[v][i];
452
453             //vector<int> m;
454             m.clear();
455             m.resize(2);
456             m[0] = -1;
457             m[1] = G.adj_list[v][i].second.second; // the mark towards w
458             if (message_dict[h-1].find(m) == message_dict[h-1].end()){
459                 message_dict[h-1][m] = message_list[h-1].size();
460                 message_list[h-1].push_back(m);
461             }
462             messages[w][my_location][h-1] = message_dict[h-1][m];
463         }
464     }
465 }
466
467 // setting message_mark and is_star_message
468 logger::add_entry("setting message_mark and is_star_message", "");
469 message_mark.resize(message_list[h-1].size());
470 is_star_message.resize(message_list[h-1].size());
471 for (int i=0;i<message_list[h-1].size();i++){
472     message_mark[i] = message_list[h-1][i].back(); // the last element is the mark component
473     is_star_message[i] = (message_list[h-1][i][0] == -1); // message is star type when the first element is
-1
474 }
475 logger::current_depth--;
476 */
477 }

```

6.10.4 Member Data Documentation

6.10.4.1 Delta

```
int graph_message::Delta [private]
```

the maximum degree threshold

6.10.4.2 h

```
int graph_message::h [private]
```

the depth up to which we do message passing (the type of edges go through depth h-1)

6.10.4.3 is_star_message

```
vector<bool> graph_message::is_star_message
```

for an integer message m , `is_star_message[m]` is true if m is a star message and false otherwise. Note that m is star type iff the first index in the vector message corresponding to m is -1. This is updated at step of `update_messages`, so when it is over, it corresponds to step (depth) $h-1$.

6.10.4.4 message_dict

```
unordered_map<vector<int>, int, vint_hash> graph_message::message_dict
```

`message_dict` is the message dictionary at any step that `update_messages` is running, which maps each message to its corresponding index in the dictionary. When `update_messages` is over, this corresponds to step (depth) $h-1$

6.10.4.5 message_mark

```
vector<int> graph_message::message_mark
```

for an integer message m , `message_mark[m]` is the mark component associated to the message m at any step that `update_messages` is working. This is basically the last index in the vector message associate to m . When `update_messages` is over, this corresponds to step (depth) $h-1$.

6.10.4.6 messages

```
vector<vector<int > > graph_message::messages
```

`messages[v][i]` is the integer version of the message from vertex `v` towards its `i`th neighbor (in the order given by `adj_list` of vertex `i` in graph `G`). The message is at any given step that `update_messages` is running, so after finishing `update_message`, the messages are at step (depth) `h-1`.

The documentation for this class was generated from the following files:

- [graph_message.h](#)
- [graph_message.cpp](#)

6.11 ibitstream Class Reference

deals with reading bit streams from binary files, this is the reverse of obitstream

```
#include <bitstream.h>
```

Public Member Functions

- void [read_chunk](#) ()
reads one chunk (4 bytes) from the input file and stores it in buffer
- unsigned int [read_bits](#) (unsigned int k)
read k bits from the input, interpret it as integer (first bit read is MSB) and return its value. Here, k must be in the range $1 \leq k \leq \text{BIT_INT}$
- void [read_bits](#) (int k, [bit_pipe](#) &B)
reads k bits from input and stores in the given [bit_pipe](#). $k \geq 1$ is arbitrary. The bits are stored in the [bit_pipe](#) so that can be interpreted as integer (e.g. [mpz_class](#)) so the LSB is located in the rightmost bit of the rightmost chunk (unlike the usual [bit_pipe](#) situation). We assume that the B given here is an empty [bit_pipe](#)
- void [read_bits_append](#) (int k, [bit_pipe](#) &B)
similar to [read_bits](#), but B does not have to be empty and the result will be appended to B (this is used in order to recursively implement [read_bits](#))
- bool [read_bit](#) ()
read one bit from input and return true if its value is 1 and false otherwise.
- [ibitstream](#) (string file_name)
- [ibitstream](#) & [operator>>](#) (unsigned int &n)
reads an unsigned int from the input using Elias delta decoding and saves it in the reference given
- [ibitstream](#) & [operator>>](#) (mpz_class &n)
reads a nonnegative [mpz_class](#) integer using Elias delta decoding and stores in the reference given
- void [bin_inter_decode](#) (vector< int > &a, int b)
uses binary interpolative coding algorithm to decode for an array of increasing nonnegative integers. Caution: we do not sort the decoding vector for efficiency purposes and return elements in the order they were encoded (mid point first left subinterval then subinterval)
- void [bin_inter_decode](#) (vector< int > &a, int i, int j, int low, int high)
using bit interpolative coding algorithm to decode for a subinterval of an array
- void [close](#) ()
closes the session by closing the input file

Private Attributes

- FILE * `f`
pointer to input binary file
- unsigned int `buffer`
the last chunk read from the input
- unsigned int `head_mask`
the place of the head bit in buffer, represented in terms of mask. So if we are in the LSB, head_mask is one, if we are in two bit left of LSB, this is 4 so on. When this is zero, it means the buffer is expired and we should probably read one more chunk from the input file
- unsigned int `head_place`
the place of head represented in terms of integer, LSB is 1, left of LSB is 2, 2 left of LSB is 3 and so on. head_place is effectively the number of unread bits remaining in the buffer.

6.11.1 Detailed Description

deals with reading bit streams from binary files, this is the reverse of obitstream

6.11.2 Constructor & Destructor Documentation

6.11.2.1 ibitstream()

```

ibitstream::ibitstream (
    string file_name ) [inline]

140
141     {
142     f = fopen(file_name.c_str(), "rb+");
143     buffer =0;
144     head_mask = 0;
145     head_place = 0;
146     }

```

6.11.3 Member Function Documentation

6.11.3.1 bin_inter_decode() [1/2]

```

void ibitstream::bin_inter_decode (
    vector< int > & a,
    int b )

```

uses binary interpolative coding algorithm to decode for an array of increasing nonnegative integers. Caution: we do not sort the decoding vector for efficiency purposes and return elements in the order they were encoded (mid point first left subinterval then subinterval)

Parameters

| | |
|----------|--|
| <i>b</i> | The number of bits used in the compression phase to encode size of array and lower and upper values (for graph compression, it is number of bits in the number of vertices). |
| <i>a</i> | reference to the array to add elements to. Here, we do not erase a, so you need to make sure a is empty. |

```

530                                     {
531     unsigned int a_size;
532     a_size = read_bits(b); // size of the vector
533     //cout << "a_size " << a_size << endl;
534
535     if (a_size == 0)
536         return;
537     if (a_size == 1){
538         a.push_back(read_bits(b));
539         return;
540     }
541
542     // read low and high values
543     unsigned int low, high;
544     low = read_bits(b);
545     high = read_bits(b);
546     //cout << " low " << low << " high " << high << endl;
547     bin_inter_decode(a, 0, a_size - 1, low, high);
548     return;
549 }
```

6.11.3.2 bin_inter_decode() [2/2]

```

void ibitstream::bin_inter_decode (
    vector< int > & a,
    int i,
    int j,
    int low,
    int high )
```

using bit interpolative coding algorithm to decode for a subinterval of an array

Parameters

| | |
|-------------|---|
| <i>a</i> | reference to the array to add elements to |
| <i>i,j</i> | the endpoints of the interval to be decoded (with respect to the encoded array) |
| <i>low</i> | lower bound on the elements of the encoded array in the interval [i,j] |
| <i>high</i> | lower bound on the elements of the encoded array in the interval [i,j] |

```

559                                     {
560     // cout << " i " << i << " j " << j << " low " << low << " high " << high << endl;
561     if (j < i)
562         return;
563     if (i==j){
564         if(low == high)
565             a.push_back(low); // the element must be low = high, no other change, nothing to read
566         else
567             a.push_back(read_bits(nu_bits(high-low)) + low);
568         return;
569     }
570
571     int m = (i+j)/2;
572     unsigned int L = low + m - i; // lower bound on a[m]
573     unsigned int H = high - (j - m); // upper bound on a[m]
```



```

574 unsigned int a_m; // the value of the intermediate point
575 if (L == H)
576     a_m = L; // there will be no bits to read
577 else
578     a_m = read_bits(nu_bits(H-L)) + L;
579
580 a.push_back(a_m);
581
582 bin_inter_decode(a, i, m-1, low, a_m - 1);
583 bin_inter_decode(a, m+1, j, a_m + 1, high);
584 }

```

6.11.3.3 close()

```
void ibitstream::close ( ) [inline]
```

closes the session by closing the input file

```
163 {fclose(f);}
```

6.11.3.4 operator>>() [1/2]

```
ibitstream & ibitstream::operator>> (
    unsigned int & n )
```

reads an unsigned int from the input using Elias delta decoding and saves it in the reference given

```

442                                     {
443     // implement Elias delta decoding
444     //bitset<32> B(buffer);
445     //cerr << " buffer " << B << endl;
446     //cerr << " head " << bitset<32>(head_mask) << endl;
447     //cerr << " head position " << head_place << endl;
448
449     unsigned int L = 0;
450     while (!read_bit()){
451         // read until reach one
452         L++;
453     }
454     //cerr << " L " << L << endl;
455
456     unsigned int N;
457     if (L == 0){ // special case, avoid going over further calculations
458         n = 0; // we had subtracted one when encoding
459         return *this;
460     }
461     N = read_bits(L); // read L digits
462
463     N += (1<<L); // we must add 2^L
464     N--; // this was N + 1
465
466     n = read_bits(N); // read N digits
467     n += (1 << N); // we must add 2^N
468     n--; // when we encoded, in order to get a positive integer, we added one, now we subtract one
469     return *this;
470 }

```

6.11.3.5 operator>>() [2/2]

```
ibitstream & ibitstream::operator>> (
    mpz_class & n )
```

reads a nonnegative `mpz_class` integer using Elias delta decoding and stores in the reference given

```
472                                     {
473     unsigned int L = 0;
474     //cout << "head_place " << head_place << endl;
475     //cout << "head_mask " << head_mask << endl;
476     while (!read_bit()){
477         // read until reach one
478         L++;
479     }
480
481     //cout << " L = " << L << endl;
482     unsigned int N;
483     if (L == 0){ // special case, avoid going over further calculations
484         n = 0; // we had subtracted one when encoding
485         return *this;
486     }
487
488     N = read_bits(L); // read L digits
489
490     N += (1<<L); // we must add 2^L
491     N --; // this was N + 1
492
493     // we must read N bits and form n based on that
494
495     bit_pipe B;
496     //cout << " N " << N << endl;
497     read_bits(N, B);
498     //cout << " B first " << B << endl;
499     // we should add a leading 1 to B
500     // in order to do so, we should consider 2 cases:
501     if (N % BIT_INT == 0){
502         // this is the tricky case, since B now contains full chunks and there is no room to add the leading 1
503         // so we need to insert a chunk at the beginning and place the leading bit there
504         // since the leading bit will be in the rightmost bit in this case, the value of the initial chunk is 1
505         // in this case
506         B.bits.insert(B.bits.begin(), 1);
507     }else{
508         // in this case, the lading bit will be placed in the first chunk of B
509         B.bits[0] |= (1 << (N % BIT_INT));
510     }
511     //cout << " B " << B << endl;
512     //cout << B.bits[0] << endl;
513
514     // construct the mpz_clas
515     mpz_import(n.get_mpz_t(),
516         B.bits.size(), // the number of words
517         1, // order: 1 means first significant word first
518         sizeof(unsigned int), // each word is this many bytes
519         0, // endian can be 1 for most significant byte first, -1 for least significant first, or 0
520         for the native endianness of the host CPU.
521         0, // nails
522         &B.bits[0]); //&B.bits[0]);
523     n --; // when encoding, we added 1 to make sure it is positive
524     return *this;
525 }
```

6.11.3.6 read_bit()

```
bool ibitstream::read_bit ( )
```

read one bit from input and return true if its value is 1 and false otherwise.

```

587     {
588     if (head_mask == 0){ // nothing is in buffer
589         //cerr << " read a chunk " << endl;
590         read_chunk();
591     }
592     bool ans = head_mask & buffer; // look at the value of buffer at the bit where the
593     head_mask is pointing to
594     head_mask >>= 1; // go one bit to the right
595     head_place --;
596     //cerr << " read bit " << ans << endl;
597     return ans;
598 }

```

6.11.3.7 read_bits() [1/2]

```

unsigned int ibitstream::read_bits (
    unsigned int k )

```

read k bits from the input, interpret it as integer (first bit read is MSB) and return its value. Here, k must be in the range $1 \leq k \leq \text{BIT_INT}$

```

333     {
334
335     //cerr << " read bits with k = " << k << endl;
336     if (k < 1 or k > BIT_INT){
337         cerr << "ERROR: ibitstream::read_bits called with k out of range, k = " << k << endl;
338     }
339     if (head_place == 0){ // no bits left
340         read_chunk();
341     }
342     if (head_place >= k){ // head_place is effectively the number of unread bits remaining in the
343     buffer
344         //cerr << " head_place >= k head_mask = " << head_mask << " head_place = " << head_place << endl;
345         // there are enough number of bits in the current buffer to read
346         // mask the input
347         unsigned int mask = mask_gen(k); // k ones
348         // now we should shift mask to start at head_place
349         mask <<= (head_place - k);
350         unsigned int ans = buffer & mask; // mask out the corresponding bits
351         ans >>= (head_place - k); // bring it back to LSB
352
353         // we need to shift head k bits to the right
354         // in some compilers, >>= 32 does strange things, in fact it does nothing. To avoid that, I shift k - 1
355         bits and then an extra 1 bit
356         head_mask >>= k - 1;
357         head_mask >>= 1;
358         head_place -= k;
359         //cerr << " after head_mask " << head_mask << " head_place = " << head_place << endl;
360         return ans;
361     }else{
362         // there is not enough bits in the current buffer.
363         // So we should read head_place many bits from the current buffer
364         // then read another chunk from input file
365         // and then read k - head_place bits from the new buffer
366         // we do these two steps recursively
367         // but first need to store the number of bits we will have to read in the future, since these variables
368         will be modified later:
369         unsigned int future_bits = k - head_place;
370         unsigned int a = read_bits(head_place); // the bits from the current buffer
371         read_chunk();
372         unsigned int b = read_bits(future_bits); // bits from the next buffer
373         // now we need to combine these
374         // in order to do so, we need to shift a to the left and combine with b
375         // but the number of bits we need to shift a is exactly future bits
376         a <<= future_bits;
377         return a | b;
378     }
379 }

```

6.11.3.8 read_bits() [2/2]

```
void ibitstream::read_bits (
    int k,
    bit_pipe & B )
```

reads k bits from input and stores in the given `bit_pipe`. $k \geq 1$ is arbitrary. The bits are stored in the `bit_pipe` so that can be interpreted as integer (e.g. `mpz_class`) so the LSB is located in the rightmost bit of the rightmost chunk (unlike the usual `bit_pipe` situation). We assume that the `B` given here is an empty `bit_pipe`

```
425 {
426     //cerr << " read_bits " << k << endl;
427     // assumption: B is empty bit_pipe
428     if (B.bits.size() != 0 or B.last_bits != 0){
429         cerr << " ERROR: ibitstream::read_bits(int k, bit_pipe& B) must be called with an empty bit_pipe, a
nonempty bitpipe is given with B.bits.size() = " << B.bits.size() << endl;
430     }
431     read_bits_append(k, B);
432     // there might be a few zero chunks at the beginning of B which are redundant, we remove them here
433     // the number of nonzero chunks is exactly the floor of k / BIT_INT
434     int nonzero_chunks = k / BIT_INT;
435     if (k % BIT_INT != 0)
436         nonzero_chunks++; // take the floor
437     //cerr << " nonzero_chunks " << nonzero_chunks << endl;
438     if (nonzero_chunks < B.bits.size())
439         B.bits.erase(B.bits.begin(), B.bits.begin() + B.bits.size() - nonzero_chunks);
440 }
```

6.11.3.9 read_bits_append()

```
void ibitstream::read_bits_append (
    int k,
    bit_pipe & B )
```

similar to `read_bits`, but `B` does not have to be empty and the result will be appended to `B` (this is used in order to recursively implement `read_bits`)

```
377 {
378     //cout << " read_bits called k = " << k << " head_place = " << head_place << endl;
379     // by assumption, when calling this function, B has full chunks (last_bits is either zero so BIT_INT)
380     if (k == 0)
381         return; // nothing remains to be done
382     if (head_place == 0){
383         // we are over with the current bits in the buffer
384         // so we need to load a few chunks from the input
385         // we should append k / BIT_INT full chunks to B and then k % BIT_INT bits from the next chunk
386         unsigned int full_chunks = k / BIT_INT;
387         if (full_chunks > 0){
388             B.bits.resize(B.bits.size() + full_chunks);
389             fread(&B.bits[B.bits.size() - full_chunks], sizeof(unsigned int), full_chunks,
f); // read full_chunks many chunks
390             B.last_bits = BIT_INT; // the last chunk contains full bits
391         }
392         unsigned int res_bits = k % BIT_INT; // the remaining bits to be read
393         if (res_bits > 0){
394             // we need to read an extra res bits
395             unsigned int res = read_bits (res_bits); // read res many bits
396             // we should shift res_bits so that its MSB is the leftmost bits of the chunk
397             res <<= (BIT_INT - res_bits);
398             B.bits.push_back(res);
399             B.last_bits = res_bits;
400         }
401     }else{
402         if (k <= head_place){
403             // there are enough bits to read
404             unsigned int a = read_bits(k);
405             // no need to shift a since we need LSB of a to be in the rightmost bit
406             B.bits.push_back(a);
```

```

407     B.last_bits = BIT_INT;
408 }else{
409     // read head_place bits and call again
410     unsigned int future_read; // number of bits to read in future after calling the read_bits function
    below
411     future_read = k - head_place;
412     unsigned int a = read_bits(head_place);
413     B.bits.push_back(a);
414     B.last_bits = BIT_INT;
415     read_bits_append(future_read, B); // read the remaining bits
416 }
417 }
418
419 B.shift_right(BIT_INT - B.last_bits); // so that LSB of B is the rightmost bit
    of the lats chunk.
420
421 // this is important to make sure that B is correctly representing an integer and can be converted to
    mpz_class
422 // TODO issue of 2^k - 1 correct
423 }

```

6.11.3.10 read_chunk()

```
void ibitstream::read_chunk ( )
```

reads one chunk (4 bytes) from the input file and stores it in buffer

```

325     {
326     fread(&buffer, sizeof(unsigned int), 1, f);
327     //cout << " in read chunk  buffer = " << bitset<32>(buffer) << endl;
328     head_mask = 1 << (BIT_INT - 1); // pointing to the MSB which is the first bit to consider
329     head_place = BIT_INT;
330 }

```

6.11.4 Member Data Documentation

6.11.4.1 buffer

```
unsigned int ibitstream::buffer [private]
```

the last chunk read from the input

6.11.4.2 f

```
FILE* ibitstream::f [private]
```

pointer to input binary file

6.11.4.3 head_mask

```
unsigned int ibitstream::head_mask [private]
```

the place of the head bit in buffer, represented in terms of mask. So if we are in the LSB, head_mask is one, if we are in two bit left of LSB, this is 4 so on. When this is zero, it means the buffer is expired and we should probably read one more chunk from the input file

6.11.4.4 head_place

```
unsigned int ibitstream::head_place [private]
```

the place of head represented in terms of integer, LSB is 1, left of LSB is 2, 2 left of LSB is 3 and so on. head_place is effectively the number of unread bits remaining in the buffer.

The documentation for this class was generated from the following files:

- [bitstream.h](#)
- [bitstream.cpp](#)

6.12 log_entry Class Reference

```
#include <logger.h>
```

Public Member Functions

- [log_entry](#) (string [name](#), string [description](#), int [depth](#))

Public Attributes

- string [name](#)
- string [description](#)
- int [depth](#)
- high_resolution_clock::time_point [t](#)
- system_clock::time_point [sys_t](#)

6.12.1 Constructor & Destructor Documentation

6.12.1.1 log_entry()

```
log_entry::log_entry (
    string name,
    string description,
    int depth )

16
17     name = name_;
18     description = description_;
19     depth = depth_;
20     t = high_resolution_clock::now();
21     sys_t = system_clock::now();
22 }
```

6.12.2 Member Data Documentation

6.12.2.1 depth

```
int log_entry::depth
```

6.12.2.2 description

```
string log_entry::description
```

6.12.2.3 name

```
string log_entry::name
```

6.12.2.4 sys_t

```
system_clock::time_point log_entry::sys_t
```

6.12.2.5 t

```
high_resolution_clock::time_point log_entry::t
```

The documentation for this class was generated from the following files:

- [logger.h](#)
- [logger.cpp](#)

6.13 logger Class Reference

```
#include <logger.h>
```

Static Public Member Functions

- static void [add_entry](#) (string name, string description)
- static void [start](#) ()
- static void [stop](#) ()
- static void [log](#) ()
- static void [item_start](#) (string name)
- static void [item_stop](#) (string name)

Static Public Attributes

- static bool [verbose](#) = true
if true, every entry is printed at the time of its report, default is false
- static bool [stat](#) = false
if true, statistics will be displayed, e.g. number of star vertices / edges or the number of partition graphs etc
- static ostream * [verbose_stream](#) = &cout
the stream for printing entries at the time of arrival, default is cout
- static bool [report](#) = true
if true, at the end of the program, a hierarchical report is printed
- static ostream * [report_stream](#) = &cout
the stream to report the final report. Default is cout
- static ostream * [stat_stream](#) = &cout
the stream to report the statistics. Default is cout
- static vector< [log_entry](#) > [logs](#)
- static int [current_depth](#) = 1
- static map< string, float > [item_duration](#)
- static map< string, high_resolution_clock::time_point > [item_last_start](#)
the last time each item was started

6.13.1 Member Function Documentation

6.13.1.1 add_entry()

```
void logger::add_entry (
    string name,
    string description ) [static]

26 {
27     //cerr << " adding entry current_depth " << current_depth << endl;
28     log_entry new_entry(name, description, current_depth);
29     logger::logs.push_back(new_entry);
30     if (logger::verbose){
31         string s = "";
32         time_t tt = system_clock::to_time_t(new_entry.sys_t);
33         char buffer[80];
34         strftime(buffer, 80, "%F %r", localtime(&tt));
35         for (int i=1;i<(current_depth-1);i++)
36             s += "|---";
37         string buffer_str(buffer);
38         s += name + " (" + description + ") ";
39         s += buffer_str;
40         *verbose_stream << s << endl;
41     }
42 }
```


6.13.1.2 item_start()

```

void logger::item_start (
    string name ) [static]

128         {
129     item_last_start[name] = high_resolution_clock::now();
130 }

```

6.13.1.3 item_stop()

```

void logger::item_stop (
    string name ) [static]

132         {
133     high_resolution_clock::time_point t = high_resolution_clock::now();
134     duration<float> diff = t - item_last_start[name];
135     item_duration[name] += diff.count();
136 }

```

6.13.1.4 log()

```

void logger::log ( ) [static]

45         {
46     //cerr << " log started " << endl;
47     int max_depth = 0;
48     for (int i=0;i<logs.size(); i++){
49         if (logs[i].depth > max_depth)
50             max_depth = logs[i].depth;
51     }
52
53     vector<int> parent(logs.size()); // for a log L, parent[L] is the max index i < L such that depth[i]
    < depth[L], this shows in what block we are in
54     vector<int> next(logs.size()); // for a log L, next[L] is the min index i > L such that depth[i] >=
    depth[L], this is the index right after L in its block, or if L is the last entry in its block, it is the
    start of the next block. The diff between L and next[L] shows the duration of running L
55     for (int i=1;i<(logs.size()-1);i++){
56         // finding parent[i]
57         //cerr << " finding parent " << i << endl;
58         for (int j=(i-1); j>=0 ;j--){
59             if (logs[j].depth < logs[i].depth){
60                 parent[i] = j;
61                 break;
62             }
63         }
64         //cerr << " parent[" << i << "] = " << parent[i] << endl;
65         //cerr << " finding next " << i << endl;
66         for (int j=(i+1); j<logs.size();j++){
67             if (logs[j].depth <= logs[i].depth){
68                 next[i] = j;
69                 break;
70             }
71         }
72         //cerr << " next[" << i << "] = " << next[i] << endl;
73     }
74     next[0] = logs.size()-1; // next of start entry is the finish entry
75
76     vector<float> dur(logs.size()); // dur[L] is the duration that entry L takes, meaning the difference
    between L and next[L]
77     vector<float> block_dur(logs.size()); // the duration of the whole block for each entry, which is the
    difference between

```

```

78  vector<float> block_percent(logs.size()); // the percentage of time each entry takes inside a block
79  duration<float> diff;
80  string s;
81  //cerr << " logs.size() " << logs.size() << endl;
82  *report_stream << endl;
83  for (int i=1;i<(logs.size()-1); i++){
84      //cerr << " i " << i << endl;
85      // finding duration[i]
86      diff = logs[next[i]].t - logs[i].t;
87      dur[i] = diff.count();
88      //cerr << " dur[i] " << dur[i] << endl;
89      // finding block_duration
90      diff = logs[next[parent[i]]].t - logs[parent[i]].t;
91      block_dur[i] = diff.count();
92      //cerr << " block_dur[i] " << block_dur[i] << endl;
93      block_percent[i] = dur[i] / block_dur[i] * 100;
94      //cerr << " block_percent[i] " << block_percent[i] << endl;
95      s = "";
96      //cerr << " logs[i].depth " << logs[i].depth << endl;
97      for (int j=1;j<(logs[i].depth-1); j++)
98          s += "|---";
99      s += logs[i].name + " (" + logs[i].description + "): " + to_string(dur[i]) + "s " + "[" +
to_string(block_percent[i]) + "%]" + " ";
100     *report_stream << s << endl;
101 }
102
103 *report_stream << endl << " itemized log " << endl;
104 for (map<string, float>::iterator it = item_duration.begin(); it!=
item_duration.end(); it++)
105     *report_stream << it->first << " : " << it->second << endl;
106 }

```

6.13.1.5 start()

```
void logger::start ( ) [static]
```

```

109     {
110     log_entry new_log("Start", "", 0);
111     //cerr << " started " << endl;
112     logs.push_back(new_log);
113     //cerr << logger::logs.size() << endl;
114 }

```

6.13.1.6 stop()

```
void logger::stop ( ) [static]
```

```

117     {
118     log_entry new_log("Finish", "", 0);
119     //cerr << " finished " << endl;
120     logs.push_back(new_log);
121     //cerr << logs.size() << endl;
122     if (report)
123         log();
124
125 }

```

6.13.2 Member Data Documentation

6.13.2.1 current_depth

```
int logger::current_depth = 1 [static]
```

6.13.2.2 item_duration

```
map< string, float > logger::item_duration [static]
```

6.13.2.3 item_last_start

```
map< string, high_resolution_clock::time_point > logger::item_last_start [static]
```

the last time each item was started

6.13.2.4 logs

```
vector< log_entry > logger::logs [static]
```

6.13.2.5 report

```
bool logger::report = true [static]
```

if true, at the end of the program, a hierarchical report is printed

6.13.2.6 report_stream

```
ostream * logger::report_stream = &cout [static]
```

the stream to report the final report. Default is cout

6.13.2.7 stat

```
bool logger::stat = false [static]
```

if true, statistics will be displayed, e.g. number of star vertices / edges or the number of partition graphs etc

6.13.2.8 stat_stream

```
ostream * logger::stat_stream = &cout [static]
```

the stream to report the statistics. Default is cout

6.13.2.9 verbose

```
bool logger::verbose = true [static]
```

if true, every entry is printed at the time of its report, default is false

6.13.2.10 verbose_stream

```
ostream * logger::verbose_stream = &cout [static]
```

the stream for printing entries at the time of arrival, default is cout

The documentation for this class was generated from the following files:

- [logger.h](#)
- [logger.cpp](#)

6.14 marked_graph Class Reference

simple marked graph

```
#include <marked_graph.h>
```

Public Member Functions

- [marked_graph](#) ()
default constructor
- [marked_graph](#) (int n, vector< pair< pair< int, int >, pair< int, int > > > edges, vector< int > vertex_marks)
constructs a marked graph based on edges lists and vertex marks.

Public Attributes

- int [nu_vertices](#)
number of vertices in the graph
- vector< vector< pair< int, pair< int, int > > > > [adj_list](#)
adj_list[i] is the list of edges connected to vertex i, each of the format (other endpoint, mark towards i, mark towards other endpoint)
- vector< vector< int > > [index_in_neighbor](#)
index_in_neighbor[v][i] is the index of vertex v in the adjacency list of the ith neighbor of v
- vector< int > [ver_mark](#)
ver_mark[i] is the mark of vertex i

Friends

- bool `operator==` (const `marked_graph` &G1, const `marked_graph` &G2)
checks whether two marked graphs are the same.
- bool `operator!=` (const `marked_graph` &G1, const `marked_graph` &G2)
checks whether two marked graphs are not equal
- ostream & `operator<<` (ostream &o, const `marked_graph` &G)
prints a marked graph to the output

6.14.1 Detailed Description

simple marked graph

This class stores a simple marked graph where each vertex carries a mark, and each edge carries two marks, one towards each of its endpoints. The mark of each vertex and each edge is a nonnegative integer.

6.14.2 Constructor & Destructor Documentation

6.14.2.1 `marked_graph()` [1/2]

```
marked_graph::marked_graph ( ) [inline]
```

default constructor

```
27     {
28         nu_vertices = 0;
29     }
```

6.14.2.2 `marked_graph()` [2/2]

```
marked_graph::marked_graph (
    int n,
    vector< pair< pair< int, int >, pair< int, int > > > edges,
    vector< int > vertex_marks )
```

constructs a marked graph based on edges lists and vertex marks.

Parameters

| | |
|---------------------|--|
| <i>n</i> | the number of vertices in the graph |
| <i>edges</i> | a vector, where each element is of the form $((i, j), (x, y))$ where $i \neq j$ denotes the endpoints of the edge, x is the mark towards i and y is the mark towards j |
| <i>vertex_marks</i> | is a vector of size n, where <code>vertex_marks[i]</code> is the mark of vertex i |

```

4 {
5     nu_vertices = n;
6     adj_list.resize(n);
7     //adj_location.resize(n);
8     index_in_neighbor.resize(n);
9     // modify the edges if necessary so that in each element of the form ((i,j), (x, x')), we have i < j.
    This is important when forming adjacency lists so that the list of each vertex is sorted
10    for (int i=0; i<edges.size(); i++){
11        if (edges[i].first.first > edges[i].first.second){
12            // swap the edge endpoints and represent it in the other direction
13            swap(edges[i].first.first, edges[i].first.second);
14            // also, we should swap the mark components
15            swap(edges[i].second.first, edges[i].second.second);
16        }
17    }
18    sort(edges.begin(), edges.end()); // so that the adjacency list is sorted
19    for (int k=0; k<edges.size(); k++){
20        // (i,j) are endpoints if the edge
21        // (x,y) are marks, x towards i and y towards j
22        int i = edges[k].first.first;
23        int j = edges[k].first.second;
24        int x = edges[k].second.first;
25        int y = edges[k].second.second;
26        if (i < 0 || i >= n || j < 0 || j >= n || i == j)
27            cerr << " ERROR: graph::graph(n, edges) received an invalid pair of edges with n = " << n << " : (" <
            < i << " , " << j << " )" << endl;
28        adj_list[i].push_back(pair<int, int> > (j, pair<int, int> (x,y)));
29        //adj_location[i][j] = adj_list[i].size() - 1;
30        adj_list[j].push_back(pair<int, pair<int, int> > (i, pair<int, int> (y,x)));
31        //adj_location[j][i] = adj_list[j].size() - 1;
32        index_in_neighbor[i].push_back(adj_list[j].size()-1);
33        index_in_neighbor[j].push_back(adj_list[i].size()-1);
34    }
35 }
36
37 ver_mark = vertex_marks;
38 }

```

6.14.3 Friends And Related Function Documentation

6.14.3.1 operator"!="

```

bool operator!= (
    const marked_graph & G1,
    const marked_graph & G2 ) [friend]

```

checks whether two marked graphs are not equal

```

88 {
89     return !(G1 == G2);
90 }

```

6.14.3.2 operator<<

```

ostream& operator<< (
    ostream & o,
    const marked_graph & G ) [friend]

```

prints a marked graph to the output

```

99 {
100     o << G.nu_vertices << endl;
101     for (int v=0;v<G.nu_vertices;v++){
102         o << G.ver_mark[v];
103         if (v < G.nu_vertices-1)
104             o << " ";
105     }
106     o << endl;
107
108     vector<pair<pair<int, int>, pair<int, int> > > edges;
109     pair<pair<int, int>, pair<int, int> > edge; // the current edge to be added to the list
110     for (int v=0;v<G.nu_vertices;v++){
111         for (int i=0;i<G.adj_list[v].size();i++){
112             if (G.adj_list[v][i].first > v) { // avoid duplicate in edge list, only add edges where the
113                 other endpoint has a greater index
114                 edge.first.first = v;
115                 edge.first.second = G.adj_list[v][i].first;
116                 edge.second = G.adj_list[v][i].second;
117                 edges.push_back(edge);
118             }
119         }
120     }
121     sort(edges.begin(), edges.end());
122     o << edges.size() << endl;
123     for(int i=0;i<edges.size();i++){
124         o << edges[i].first.first << " " << edges[i].first.second << " " << edges[i].second.first << " " <<
125         edges[i].second.second << endl;
126     }
127     return o;
128 }
129 /*
130 o << " number of vertices " << G.nu_vertices << endl;
131 vector<pair<int, pair<int, int> > > l; // the adjacency list of a vertex
132 for (int v=0; v<G.nu_vertices; v++){
133     o << " vertex " << v << " mark " << G.ver_mark[v] << endl;
134     //o << " adj list (connections to vertices with greater index): format (j, (x,y))" << endl;
135     o << " adj list " << endl;
136     l = G.adj_list[v];
137     sort(l.begin(), l.end(), edge_compare);
138     for (int i=0;i<l.size();i++){
139         if (l[i].first > v)
140             o << " (" << l[i].first << ", (" << l[i].second.first << ", " << l[i].second.second << ")) ";
141     }
142     o << endl << endl;
143 }
144 return o;
145 */
146 }

```

6.14.3.3 operator==

```

bool operator== (
    const marked_graph & G1,
    const marked_graph & G2 ) [friend]

```

checks whether two marked graphs are the same.

two marked graphs are said to be the same if: 1) they have the same number of vertices, 2) vertex marks match and 3) each vertex has the same set of neighbors with matching marks.

```

66 {
67     if (G1.nu_vertices != G2.nu_vertices)
68         return false;
69     return G1.adj_list == G2.adj_list;
70     int n = G1.nu_vertices; // number of vertices of the two graphs
71     vector<pair<int, pair<int, int> > > l1, l2; // the adjacency list of a vertex in two graphs for
72     comparison.
73     for (int v=0;v<n;v++){
74         if (G1.ver_mark[v] != G2.ver_mark[v]) // mark of each vertex should be the same
75             return false;
76         if (G1.adj_list[v].size() != G2.adj_list[v].size()) // each vertex must have the same
77             degree in two graphs
78             return false;
79         l1 = G1.adj_list[v];

```

```

78     l2 = G2.adj_list[v];
79     sort(l1.begin(), l1.end(), edge_compare); // sort with respect to the other endpoint
80     sort(l2.begin(), l2.end(), edge_compare);
81     if (l1 != l2) // after sorting, the lists must match
82         return false;
83 }
84 return true;
85 }

```

6.14.4 Member Data Documentation

6.14.4.1 adj_list

`vector<vector<pair<int, pair<int, int> > > > marked_graph::adj_list`

`adj_list[i]` is the list of edges connected to vertex `i`, each of the format (other endpoint, mark towards `i`, mark towards other endpoint)

6.14.4.2 index_in_neighbor

`vector<vector<int> > marked_graph::index_in_neighbor`

`index_in_neighbor[v][i]` is the index of vertex `v` in the adjacency list of the `i`th neighbor of `v`

6.14.4.3 nu_vertices

`int marked_graph::nu_vertices`

number of vertices in the graph

6.14.4.4 ver_mark

`vector<int> marked_graph::ver_mark`

`ver_mark[i]` is the mark of vertex `i`

The documentation for this class was generated from the following files:

- [marked_graph.h](#)
- [marked_graph.cpp](#)

6.15 marked_graph_compressed Class Reference

```
#include <marked_graph_compression.h>
```

Public Member Functions

- void [clear](#) ()
- void [binary_write](#) (FILE *f)
writes the compressed data to a binary file
- void [binary_write](#) (string s)
- void [binary_read](#) (FILE *f)
read the compressed data from a binary file
- void [binary_read](#) (string s)

Public Attributes

- int [n](#)
the number of vertices
- int [h](#)
the depth up to which the compression was performed
- int [delta](#)
the degree threshold used when compression was performed
- pair< vector< int >, mpz_class > [star_vertices](#)
the compressed form of the star_vertices list
- map< pair< int, int >, vector< vector< int > > > [star_edges](#)
for each pair of edge marks x, x' , and integer k , $star_edges[pair<int,int>(x,x')][k]$ is a list of neighbors w of the k th star vertex (say v) so that v shares a star edge with w so that the mark towards v is x and the mark towards w is x' .
- vector< int > [type_mark](#)
for an edge type t , $type_mark[t]$ denotes the mark component of t
- vector< vector< int > > [ver_type_list](#)
the list of all vertex types that appear in the graph, where the type of a vertex is a vector of integers, where its index 0 is the mark of the vertex, and indices $3k + 1, 3k + 2, 3k + 3$ are m, m' and $n_{m,m'}$, where (m, m') is a type pair, and $n_{m,m'}$ is the number of edges connected to the vertex with that type. The list is sorted lexicographically to ensure unique representation.
- pair< vector< int >, mpz_class > [ver_types](#)
the compressed form of vertex types, where the type of a vertex is the index with respect to ver_type_list of the list of integers specifying the type of the vertex (mark of the vertex followed by the number of edges of each type connected to that vertex)
- map< pair< int, int >, mpz_class > [part_bgraph](#)
compressed form of partition bipartite graphs corresponding to colors in $C_{<}$. For a pair $0 \leq t < t' < L$ of half edge types, $part_bgraph[pair<int,int>(t,t')]$ is the compressed form of the bipartite graph with n left and right nodes, where a left node i is connected to a right node j if there is an edge connecting i to j with type t towards i and type t' towards j
- map< int, pair< mpz_class, vector< int > > > [part_graph](#)
compressed form of partition graphs corresponding to colors in $C_{=}$. For a half edge type t , $part_graph[t]$ is the compressed form of the simple unmarked graph with n vertices, where a node i is connected to a node j where there is an edge between i and j in the original graph with color (t,t)

6.15.1 Member Function Documentation

6.15.1.1 `binary_read()` [1/2]

```
void marked_graph_compressed::binary_read (
    FILE * f )
```

read the compressed data from a binary file

Parameters

| | |
|----------------|--|
| <code>f</code> | a <code>FILE*</code> object which is the address of the binary file to write |
|----------------|--|

```
510                                     {
511     clear(); // to make sure nothing is stored inside me before reading
512
513     // ==== read n, h, delta
514     fread(&n, sizeof n, 1, f);
515     fread(&h, sizeof h, 1, f);
516     fread(&delta, sizeof delta, 1, f);
517
518     int int_in; // auxiliary input integer
519     // ===== read type_mark
520     // read number of types
521     fread(&int_in, sizeof int_in, 1, f);
522     type_mark.resize(int_in);
523     for (int i=0; i<type_mark.size(); i++){
524         fread(&int_in, sizeof int_in, 1, f);
525         type_mark[i] = int_in;
526     }
527
528     // ==== read star_vertices
529     // first, read the frequency.
530     star_vertices.first = vector<int>(2); // frequency,
531     // we read its first index which is number of zeros, and the second is n - the first.
532     fread(&int_in, sizeof int_in, 1, f);
533     star_vertices.first[0] = int_in;
534     star_vertices.first[1] = n - int_in;
535
536     // the integer representation which is star_vertices.second
537     mpz_inp_raw(star_vertices.second.get_mmpz_t(), f);
538
539     // ==== read star_edges
540
541     int log2n = 0; // the ceiling of log (n+1) in base 2 (which is equal to 1 + the floor of log_2 n), which
                    // is the number of bits to encode vertices
542     int n_copy = n;
543     while(n_copy > 0){
544         n_copy >>= 1;
545         log2n ++;
546     }
547     bitset<8*sizeof(int)> B; // a bit stream with maximum length of int to store a vertex index
548
549     string s;
550     stringstream ss;
551     int sp; // the index of the string s we are studying
552
553     // read the size of star_edges
554
555     int star_edges_size;
556     fread(&star_edges_size, sizeof star_edges_size, 1, f);
557
558     int x, xp; // edge marks
559     int nu_star_vertices = star_vertices.first[1];
560
561     vector<vector<int>> V; // the list of star edges corresponding to each mark pair
562     V.resize(nu_star_vertices);
563
564     for (int i=0; i<star_edges_size; i++){
565         fread(&x, sizeof x, 1, f);
566         fread(&xp, sizeof xp, 1, f);
567
568         s = bit_string_read(f);
569         //cerr << " read x " << x << " xp " << xp << " s " << s << endl;
570         sp = 0; // starting from zero
571         for (int j=0; j<nu_star_vertices; j++){ //
572             V[j].clear(); // make it fresh
573             while(s[sp++] == '1'){ // there is still some edge connected to this vertex
574                 // read log2n many bits
575                 //cerr << " s substr " << s.substr(sp, log2n);
```

```

576         //ss << s.substr(sp, log2n);
577         B = bitset<8*sizeof(int)>(s.substr(sp, log2n));
578         //cerr << " ss " << ss.str() << endl;
579         sp += log2n;
580         //ss >> B;
581
582         V[j].push_back(B.to_ulong());
583     }
584     //for (int k=0;k<V[j].size();k++)
585     // cerr << " , " << V[j][k];
586     //cerr << endl;
587 }
588
589
590 star_edges.insert(pair< pair<int, int> , vector<vector<int> > > (pair<int, int>(x, xp), V));
591 }
592
593 // ==== read vertex_types
594
595 // read ver_type_list
596 fread(&int_in, sizeof int_in, 1, f); // size of ver_type_list
597 ver_type_list.resize(int_in);
598 for (int i=0; i<ver_type_list.size();i++){
599     fread(&int_in, sizeof int_in, 1, f); // size of ver_type_list[i]
600     ver_type_list[i].resize(int_in);
601     for (int j=0;j<ver_type_list[i].size();j++){
602         fread(&int_in, sizeof int_in, 1, f);
603         ver_type_list[i][j] = int_in;
604     }
605 }
606
607 // ver_types
608 // ver_types.first
609 // ver_types.first.size()
610 fread(&int_in, sizeof int_in, 1, f);
611 ver_types.first.resize(int_in);
612 for (int i=0;i<ver_types.first.size();i++){
613     fread(&int_in, sizeof int_in, 1, f);
614     ver_types.first[i] = int_in;
615 }
616 // ver_types.second
617 mpz_inp_raw(ver_types.second.get_mpz_t(), f);
618
619
620 // === part bgraphs
621 int part_bgraph_size;
622 int t, tp;
623 pair<int, int> type;
624 mpz_class part_g;
625 fread(&part_bgraph_size, sizeof part_bgraph_size, 1, f);
626 for (int i=0;i<part_bgraph_size;i++){
627     // read t, t'
628     fread(&t, sizeof t, 1, f);
629     fread(&tp, sizeof tp, 1, f);
630     type = pair<int, int>(t, tp);
631     mpz_inp_raw(part_g.get_mpz_t(), f);
632     part_bgraph.insert(pair<pair<int, int>, mpz_class> (type, part_g));
633 }
634
635 // === part graphs
636
637 // first, the size
638 int part_graph_size;
639 int v_size;
640 vector<int> W;
641 fread(&part_graph_size, sizeof part_graph_size, 1, f);
642 for (int i=0;i<part_graph_size; i++){
643     // first, the type
644     fread(&t, sizeof t, 1, f);
645     // then, the mpz part
646     mpz_inp_raw(part_g.get_mpz_t(), f);
647     // then, the vector size
648     fread(&v_size, sizeof v_size, 1, f);
649     W.resize(v_size);
650     for (int j=0;j<v_size; j++){
651         fread(&int_in, sizeof int_in, 1, f);
652         W[j] = int_in;
653     }
654     part_graph.insert(pair<int, pair< mpz_class, vector< int > > >(t, pair<mpz_class, vector<int>
655 >(part_g, W)));
656 }

```

6.15.1.2 binary_read() [2/2]

```
void marked_graph_compressed::binary_read (
    string s )
```

read the compressed data from a binary file

Parameters

| | |
|---|---|
| s | string containing the name of the binary file |
|---|---|

```
659                                     {
660     clear(); // to make sure nothing is stored inside me before reading
661     ibitstream inp(s);
662
663     // ==== read n, h, delta
664     unsigned int int_in; // auxiliary input integer
665     inp >> int_in;
666     n = int_in; // I need to do this, since ibitstream::operator >> gets unsigned int& and the compile can
        not cast int& to unsigned int&
667     inp >> int_in;
668     h = int_in;
669     inp >> int_in;
670     delta = int_in;
671
672     //fread(&n, sizeof n, 1, f);
673     //fread(&h, sizeof h, 1, f);
674     //fread(&delta, sizeof delta, 1, f);
675
676
677     // ===== read type_mark
678     // read number of types
679     inp >> int_in;
680     //fread(&int_in, sizeof int_in, 1, f);
681     type_mark.resize(int_in);
682     for (int i=0; i<type_mark.size(); i++){
683         inp >> int_in;
684         type_mark[i] = int_in;
685         //fread(&int_in, sizeof int_in, 1, f);
686         //type_mark[i] = int_in;
687     }
688
689     // ==== read star_vertices
690     // first, read the frequency.
691     star_vertices.first = vector<int>(2); // frequency,
692     // we read its first index which is number of zeros, and the second is n - the first.
693     inp >> int_in;
694     //fread(&int_in, sizeof int_in, 1, f);
695     star_vertices.first[0] = int_in;
696     star_vertices.first[1] = n - int_in;
697
698     // the integer representation which is star_vertices.second
699     inp >> star_vertices.second;
700     //mpz_inp_raw(star_vertices.second.get_mmpz_t(), f);
701
702     // ==== read star_edges
703
704     //int log2n = 0; // the ceiling of log (n+1) in base 2 (which is equal to 1 + the floor of log_2 n),
        which is the number of bits to encode vertices
705     //int n_copy = n;
706     //while(n_copy > 0){
707     //n_copy >>= 1;
708     //log2n++;
709     //}
710     //bitset<8*sizeof(int)> B; // a bit stream with maximum length of int to store a vertex index
711
712     //string s;
713     //stringstream ss;
714     //int sp; // the index of the string s we are studying
715
716     // read the size of star_edges
717
718     unsigned int star_edges_size;
719     inp >> star_edges_size;
720     //fread(&star_edges_size, sizeof star_edges_size, 1, f);
721
722     unsigned int x, xp; // edge marks
723     int nu_star_vertices = star_vertices.first[1];
```

```

724
725 vector<vector<int>> > V; // the list of star edges corresponding to each mark pair
726 V.resize(nu_star_vertices);
727
728 unsigned int n_bits = nu_bits(n); // the number of bits in n, i.e.  $\lceil \log_2 n \rceil$ 
729
730 for (int i=0; i<star_edges_size; i++) {
731     inp >> x;
732     inp >> xp;
733     //fread(&x, sizeof x, 1, f);
734     //fread(&xp, sizeof xp, 1, f);
735
736     //s = bit_string_read(f);
737     //cerr << " read x " << x << " xp " << xp << " s " << s << endl;
738     //sp = 0; // starting from zero
739     for (int j=0; j<nu_star_vertices; j++) { //
740         V[j].clear(); // make it fresh
741         inp.bin_inter_decode(V[j], n_bits); // use binary interpolative decoding
742         // while(inp.read_bit()){ // there is still some edge connected to this vertex
743         //     // read log2n many bits
744         //     //cerr << " s substr " << s.substr(sp, log2n);
745         //     //ss << s.substr(sp, log2n);
746         //     //B = bitset<8*sizeof(int)>(s.substr(sp, log2n));
747         //     //cerr << " ss " << ss.str() << endl;
748         //     //sp += log2n;
749         //     //ss >> B;
750         //     //inp >> int_in;
751         //     int_in = inp.read_bits(n_bits);
752         //     V[j].push_back(int_in);
753         // }
754         //for (int k=0; k<V[j].size(); k++)
755         //    cerr << " , " << V[j][k];
756         //cerr << endl;
757     }
758
759     star_edges.insert(pair< pair<int, int> , vector<vector<int>> > > (pair<int, int>(x, xp), V));
760 }
761
762 // ==== read vertex_types
763
764 // read ver_type_list
765 inp >> int_in;
766 //fread(&int_in, sizeof int_in, 1, f); // size of ver_type_list
767 ver_type_list.resize(int_in);
768 for (int i=0; i<ver_type_list.size(); i++) {
769     inp >> int_in;
770     //fread(&int_in, sizeof int_in, 1, f); // size of ver_type_list[i]
771     ver_type_list[i].resize(int_in);
772     for (int j=0; j<ver_type_list[i].size(); j++) {
773         //fread(&int_in, sizeof int_in, 1, f);
774         inp >> int_in;
775         ver_type_list[i][j] = int_in;
776     }
777 }
778
779 // ver_types
780 // ver_types.first
781 // ver_types.first.size()
782 inp >> int_in;
783 //fread(&int_in, sizeof int_in, 1, f);
784 ver_types.first.resize(int_in);
785 for (int i=0; i<ver_types.first.size(); i++) {
786     //fread(&int_in, sizeof int_in, 1, f);
787     inp >> int_in;
788     ver_types.first[i] = int_in; // = int_in;
789 }
790
791 // ver_types.second
792 inp >> ver_types.second;
793 //mpz_inp_raw(ver_types.second.get_mpz_t(), f);
794
795 // === part bgraphs
796 unsigned int part_bgraph_size;
797 unsigned int t, tp;
798 pair<int, int> type;
799 mpz_class part_g;
800 inp >> part_bgraph_size;
801 //fread(&part_bgraph_size, sizeof part_bgraph_size, 1, f);
802 for (int i=0; i<part_bgraph_size; i++) {
803     // read t, t'
804     inp >> t;
805     inp >> tp;
806     //fread(&t, sizeof t, 1, f);
807     //fread(&tp, sizeof tp, 1, f);
808     type = pair<int, int>(t, tp);
809 }

```

```

810     inp >> part_g;
811     //mpz_inp_raw(part_g.get_mpz_t(), f);
812     part_graph.insert(pair<pair<int, int>, mpz_class> (type, part_g));
813 }
814
815 // === part graphs
816
817 // first, the size
818 unsigned int part_graph_size;
819 unsigned int v_size;
820 vector<int> W;
821 inp >> part_graph_size;
822 //fread(&part_graph_size, sizeof part_graph_size, 1, f);
823 for (int i=0; i<part_graph_size; i++){
824     // first, the type
825     inp >> t;
826     //fread(&t, sizeof t, 1, f);
827     // then, the mpz part
828     inp >> part_g;
829     //mpz_inp_raw(part_g.get_mpz_t(), f);
830     // then, the vector size
831     inp >> v_size;
832     //fread(&v_size, sizeof v_size, 1, f);
833     W.resize(v_size);
834     for (int j=0; j<v_size; j++){
835         //fread(&int_in, sizeof int_in, 1, f);
836         inp >> int_in;
837         W[j] = int_in; //!= int_in;
838     }
839     part_graph.insert(pair<int, pair< mpz_class, vector< int > > >(t, pair<mpz_class, vector<int>
>(part_g, W)));
840 }
841 inp.close();
842 }

```

6.15.1.3 binary_write() [1/2]

```

void marked_graph_compressed::binary_write (
    FILE * f )

```

writes the compressed data to a binary file

Parameters

| | |
|----------|---|
| <i>f</i> | a FILE* object which is the address of the binary file to write |
|----------|---|

```

15         {
16
17     vector<pair<string, int> > space_log; // stores the number of bits used to store each category. The
        string part is description of the category, and the int part is the number of bits of output used to express that
        part.
18
19     int output_bits; // the number of bits in the output corresponding to the current category under
        investigation, to be zeroed at each step.
20
21     logger::current_depth++;
22     // ==== write n, h, delta
23     output_bits = 0;
24     logger::add_entry("n", "");
25     fwrite(&n, sizeof n, 1, f);
26     output_bits += sizeof n;
27
28     logger::add_entry("h", "");
29     fwrite(&h, sizeof h, 1, f);
30     output_bits += sizeof h;
31
32     logger::add_entry("delta", "");
33     fwrite(&delta, sizeof delta, 1, f);
34     output_bits += sizeof delta;
35
36     space_log.push_back(pair<string, int> ("n, h, delta", output_bits));

```

```

37
38     logger::add_entry("type_mark", "");
39     output_bits = 0;
40
41     int int_out; // auxiliary variable, an integer value to be written to output
42     // ==== write type_mark
43     // first, the number of types
44     int_out = type_mark.size();
45     fwrite(&int_out, sizeof int_out, 1, f);
46     output_bits += sizeof int_out;
47     // then, marks one by one
48     for (int i=0; i<type_mark.size(); i++){
49         int_out = type_mark[i];
50         fwrite(&int_out, sizeof int_out, 1, f);
51         output_bits += sizeof int_out;
52     }
53
54     space_log.push_back(pair<string, int>("type mark", output_bits));
55
56     logger::add_entry("star_vertices", "");
57     output_bits = 0;
58     // ==== write star vertices
59     // first, write the frequency, note that star_vertices.first is a vector of size 2 with the first entry
60     // being the number of zeros, and the second one the number of ones, so it enough to write only one of them
61     int_out = star_vertices.first[0];
62     fwrite(&int_out, sizeof int_out, 1, f);
63     output_bits += sizeof int_out;
64
65     // then, we write the integer representation star_vertices.second
66     output_bits += mpz_out_raw(f, star_vertices.second.get_mpz_t()); // mpz_out_raw returns the
67     // number of bytes written to the output
68
69     space_log.push_back(pair<string, int> ("star vertices", output_bits));
70
71     logger::add_entry("star_edges", "");
72     // ==== write star edges
73     output_bits = 0;
74     int log2n = 0; // the ceiling of log (n+1) in base 2 (which is equal to 1 + the floor of log_2 n), which
75     // is the number of bits to encode vertices
76     int n_copy = n;
77     while(n_copy > 0){
78         n_copy >>= 1;
79         log2n ++;
80     }
81     //cerr << " log2n " << log2n << endl;
82     bitset<8*sizeof(int)> B; // a bit stream with maximum length of int to store a vertex index
83
84     map<pair<int, int>, vector<vector<int> > >::iterator it;
85     int x, xp;
86     string s; // the bit stream
87
88     // first, write the size of star_edges so that the decoder knows how many blocks are coming
89     int_out = star_edges.size();
90     fwrite(&int_out, sizeof int_out, 1, f);
91     output_bits += sizeof int_out;
92
93     int nu_star_edges = 0; // number of star edges
94     for (it = star_edges.begin(); it!= star_edges.end(); it++){
95         x = it->first.first;
96         xp = it->first.second;
97         //write x and xp
98         fwrite(&x, sizeof x, 1, f);
99         fwrite(&xp, sizeof xp, 1, f);
100        output_bits += sizeof x;
101        output_bits += sizeof xp;
102        s = "";
103        for (int i=0; i<it->second.size(); i++){
104            for (int j=0; j<it->second[i].size(); j++){
105                s += "1";
106                B = it->second[i][j]; // convert the index of the other endpoint to binary
107                s += B.to_string().substr(8*sizeof(int) - log2n, log2n); // take only log2n many bits of the
108                // representation (and this should be taken from the least significant bits)
109                nu_star_edges ++;
110            }
111            s += "0"; // to indicate that the neighbor list of this vertex is over now
112        }
113        //cerr << " write  x " << x << " xp " << xp << " s " << s << endl;
114        //for (int i=0; i<it->second.size(); i++){
115        //    for (int j=0; j<it->second[i].size(); j++){
116        //        cerr << " , " << it->second[i][j];
117        //    }
118        //    cerr << endl;
119        //}
120        output_bits += bit_string_write(f, s); // write this bitstream to the output
121    }
122
123     space_log.push_back(pair<string, int> ("star edges", output_bits));

```

```

120
121
122     logger::add_entry("vertex types", "");
123     output_bits = 0;
124
125     // ==== write vertex types
126
127     // first, we need vertex types list (ver_type_list)
128     // size of ver_type_list
129     int_out = ver_type_list.size();
130     fwrite(&int_out, sizeof int_out, 1, f);
131     output_bits += sizeof int_out;
132
133     for (int i=0;i<ver_type_list.size();i++){
134         int_out = ver_type_list[i].size();
135         fwrite(&int_out, sizeof int_out, 1, f);
136         output_bits += sizeof int_out;
137
138         for (int j=0;j<ver_type_list[i].size();j++){
139             int_out = ver_type_list[i][j];
140             fwrite(&int_out, sizeof int_out, 1, f);
141             output_bits += sizeof int_out;
142         }
143     }
144     space_log.push_back(pair<string, int>("vertex type list", output_bits));
145     output_bits = 0;
146
147     // then, write ver_types
148
149     // ver_types.first
150     // ver_types.first.size():
151     int_out = ver_types.first.size();
152     fwrite(&int_out, sizeof int_out, 1, f);
153     output_bits += sizeof int_out;
154
155     for (int i =0;i<ver_types.first.size(); i++){
156         int_out = ver_types.first[i];
157         fwrite(&int_out, sizeof int_out, 1, f);
158         output_bits += sizeof int_out;
159     }
160     // ver_types.second
161     output_bits += mpz_out_raw(f, ver_types.second.get_mpz_t());
162
163     space_log.push_back(pair<string, int> ("vertex types", output_bits));
164
165     logger::add_entry("partition bipartite graphs", "");
166
167
168     // ==== part bgraphs
169     output_bits = 0;
170
171     // part_bgraphs.size
172     int_out = part_bgraph.size();
173     fwrite(&int_out, sizeof int_out, 1, f);
174     output_bits += sizeof int_out;
175
176     map<pair<int, int>, mpz_class>::iterator it2;
177     if (logger::stat){
178         *logger::stat_stream << " ==== statistics ==== " << endl;
179         *logger::stat_stream << " n: " << n << endl;
180         *logger::stat_stream << " h: " << h << endl;
181         *logger::stat_stream << " delta: " << delta << endl;
182         *logger::stat_stream << " No. types " <<
183         type_mark.size() << endl;
184         *logger::stat_stream << " No. * vertices " << n -
185         star_vertices.first[0] << endl;
186         *logger::stat_stream << " No. * edges " << nu_star_edges << endl;
187         *logger::stat_stream << " No. part bgraphs " <<
188         part_bgraph.size() << endl;
189         *logger::stat_stream << " No. part graphs " <<
190         part_graph.size() << endl;
191     }
192
193     for (it2 = part_bgraph.begin(); it2 != part_bgraph.end(); it2++){
194         // first, write t, t'
195         int_out = it2->first.first;
196         fwrite(&int_out, sizeof int_out, 1, f);
197         output_bits += sizeof int_out;
198         int_out = it2->first.second;
199         fwrite(&int_out, sizeof int_out, 1, f);
200         output_bits += sizeof int_out;
201         // then, the compressed integer
202         output_bits += mpz_out_raw(f, it2->second.get_mpz_t());
203     }
204
205     space_log.push_back(pair<string, int> ("partition bipartite graphs", output_bits));
206
207

```



```

203 logger::add_entry("partition graphs", "");
204 output_bits = 0;
205 // === part graphs
206
207 // part_graph.size
208 int_out = part_graph.size();
209 fwrite(&int_out, sizeof int_out, 1, f);
210 output_bits += sizeof int_out;
211
212 map< int, pair< mpz_class, vector< int > > >::iterator it3;
213 for (it3 = part_graph.begin(); it3 != part_graph.end(); it3++) {
214     int_out = it3->first; // the type
215     fwrite(&int_out, sizeof int_out, 1, f);
216     output_bits += sizeof int_out;
217
218     // the mpz part
219     output_bits += mpz_out_raw(f, it3->second.first.get_mpz_t());
220     // the vector part
221     // first its size
222     int_out = it3->second.second.size();
223     fwrite(&int_out, sizeof int_out, 1, f);
224     output_bits += sizeof int_out;
225     // then element by element
226     for(int j=0; j<it3->second.second.size(); j++){
227         int_out = it3->second.second[j];
228         fwrite(&int_out, sizeof int_out, 1, f);
229         output_bits += sizeof int_out;
230     }
231 }
232 space_log.push_back(pair<string, int>("partition graphs", output_bits));
233
234
235 if (logger::stat){
236     *logger::stat_stream << endl << endl;
237     *logger::stat_stream << " Number of bytes used for each part " << endl;
238     *logger::stat_stream << " ----- " << endl << endl;
239
240     int total_bytes = 0;
241     for (int i=0; i < space_log.size(); i++)
242         total_bytes += space_log[i].second;
243
244     for (int i=0; i < space_log.size(); i++){
245         *logger::stat_stream << space_log[i].first << " -> " << space_log[i].second << "
246         ( " << float(100) * float(space_log[i].second) / float(total_bytes) << " % " << endl;
247     }
248     *logger::stat_stream << " Total number of bytes wrote to the output = " <<
249     total_bytes << endl;
250 }
251 logger::current_depth--;
252 }

```

6.15.1.4 binary_write() [2/2]

```

void marked_graph_compressed::binary_write (
    string s )

```

writes the compressed data to a binary file

Parameters

| | |
|---|---|
| s | string containing the name of the binary file |
|---|---|

```

255
256
257 obitstream oup(s);
258
259 vector<pair<string, int> > space_log; // stores the number of bits used to store each category. The
    string part is description of the category, and the int part is the number of bits of output used to express that
    part.
260

```

```

261 //int output_bits; // the number of bits in the output corresponding to the current category under
    investigation, to be zeroed at each step.
262 unsigned int chunks = 0; // number of chunks written to the output. Each chunk is sizeof(unsigned int) =
    32 bits long
263 unsigned int chunks_new = 0; // to take the difference in each step
264
265 logger::current_depth++;
266 // ==== write n, h, delta
267 //output_bits = 0;
268 logger::add_entry("n", "");
269 oup << n; //fwrite(&n, sizeof n, 1, f);
270 //output_bits += sizeof n;
271
272 logger::add_entry("h", "");
273 oup << h; //fwrite(&h, sizeof h, 1, f);
274 //output_bits += sizeof h;
275
276 logger::add_entry("delta", "");
277 oup << delta; //fwrite(&delta, sizeof delta, 1, f);
278 //output_bits += sizeof delta;
279
280 chunks_new = oup.chunks();
281 space_log.push_back(pair<string, int> ("n, h, delta", chunks_new - chunks));
282 chunks = chunks_new;
283
284 logger::add_entry("type_mark", "");
285 //output_bits = 0;
286
287 int int_out; // auxiliary variable, an integer value to be written to output
288 // ==== write type_mark
289 // first, the number of types
290 oup << type_mark.size();
291 //fwrite(&int_out, sizeof int_out, 1, f);
292 //output_bits += sizeof int_out;
293 // then, marks one by one
294 for (int i=0; i<type_mark.size(); i++){
295     oup << type_mark[i];
296     //fwrite(&int_out, sizeof int_out, 1, f);
297     //output_bits += sizeof int_out;
298 }
299
300 chunks_new = oup.chunks();
301 space_log.push_back(pair<string, int> ("type mark", chunks_new - chunks));
302 chunks = chunks_new;
303
304 logger::add_entry("star_vertices", "");
305 //output_bits = 0;
306 // ==== write star vertices
307 // first, write the frequency, note that star_vertices.first is a vector of size 2 with the first entry
    being the number of zeros, and the second one the number of ones, so it enough to write only one of them
308 oup << star_vertices.first[0];
309 //fwrite(&int_out, sizeof int_out, 1, f);
310 //output_bits += sizeof int_out;
311
312 // then, we write the integer representation star_vertices.second
313 oup << star_vertices.second;
314 //output_bits += mpz_out_raw(f, star_vertices.second.get_mpz_t()); // mpz_out_raw returns the number of
    bytes written to the output
315
316 chunks_new = oup.chunks();
317 space_log.push_back(pair<string, int> ("star vertices", chunks_new - chunks));
318 chunks = oup.chunks();
319
320 logger::add_entry("star_edges", "");
321 // ==== write star edges
322 //output_bits = 0;
323 //int log2n = 0; // the ceiling of log (n+1) in base 2 (which is equal to 1 + the floor of log_2 n),
    which is the number of bits to encode vertices
324 //int n_copy = n;
325 //while(n_copy > 0){
326 //    n_copy >>= 1;
327 //    log2n++;
328 //}
329 //cerr << " log2n " << log2n << endl;
330 //bitset<8*sizeof(int)> B; // a bit stream with maximum length of int to store a vertex index
331
332 map<pair<int, int>, vector<vector<int> > >::iterator it;
333 int x, xp;
334 //string s; // the bit stream
335
336 // first, write the size of star_edges so that the decoder knows how many blocks are coming
337 oup << star_edges.size();
338 //fwrite(&int_out, sizeof int_out, 1, f);
339 //output_bits += sizeof int_out;
340
341 int nu_star_edges = 0; // number of star edges
342 unsigned int n_bits = nu_bits(n); // the number of bits in n, i.e. \f$1 + \lfloor \log_2 n

```

```

    \rfloor\rfloor f$
343 for (it = star_edges.begin(); it!= star_edges.end(); it++){
344     x = it->first.first;
345     xp = it->first.second;
346     //write x and xp
347     oup << x;
348     oup << xp;
349     for (int i=0;i<it->second.size();i++){
350         oup.bin_inter_code(it->second[i], n_bits);
351         nu_star_edges += it->second[i].size();
352     }
353 }
354
355 chunks_new = oup.chunks();
356 space_log.push_back(pair<string, int> ("star edges", chunks_new - chunks));
357 chunks = oup.chunks();
358
359 logger::add_entry("vertex types", "");
360 //output_bits = 0;
361
362 // ==== write vertex types
363
364 // first, we need vertex types list (ver_type_list)
365 // size of ver_type_list
366 oup << ver_type_list.size();
367 //fwrite(&int_out, sizeof int_out, 1, f);
368 //output_bits += sizeof int_out;
369
370 for (int i=0;i<ver_type_list.size();i++){
371     oup << ver_type_list[i].size();
372     //fwrite(&int_out, sizeof int_out, 1, f);
373     //output_bits += sizeof int_out;
374
375     for (int j=0;j<ver_type_list[i].size();j++){
376         oup << ver_type_list[i][j];
377         //fwrite(&int_out, sizeof int_out, 1, f);
378         //output_bits += sizeof int_out;
379     }
380 }
381
382 chunks_new = oup.chunks();
383 space_log.push_back(pair<string, int> ("vertex type list", chunks_new - chunks));
384 chunks = chunks_new;
385
386 //output_bits = 0;
387
388 // then, write ver_types
389
390 // ver_types.first
391 // ver_types.first.size():
392 oup << ver_types.first.size();
393 //fwrite(&int_out, sizeof int_out, 1, f);
394 //output_bits += sizeof int_out;
395
396 for (int i =0;i<ver_types.first.size(); i++){
397     oup << ver_types.first[i];
398     //fwrite(&int_out, sizeof int_out, 1, f);
399     //output_bits += sizeof int_out;
400 }
401 // ver_types.second
402 oup << ver_types.second;
403 //output_bits += mpz_out_raw(f, ver_types.second.get_mpz_t());
404
405 chunks_new = oup.chunks();
406 space_log.push_back(pair<string, int> ("vertex types", chunks_new - chunks));
407 chunks = chunks_new;
408
409 logger::add_entry("partition bipartite graphs", "");
410
411 // ==== part bgraphs
412 //output_bits = 0;
413
414 // part_bgraphs.size
415 oup << part_bgraph.size();
416 //fwrite(&int_out, sizeof int_out, 1, f);
417 //output_bits += sizeof int_out;
418
419 map<pair<int, int>, mpz_class>::iterator it2;
420 if (logger::stat){
421     *logger::stat_stream << " ==== statistics ==== " << endl;
422     *logger::stat_stream << " n: " << n << endl;
423     *logger::stat_stream << " h: " << h << endl;
424     *logger::stat_stream << " delta: " << delta << endl;
425     *logger::stat_stream << " No. types " <<
426     type_mark.size() << endl;
427     *logger::stat_stream << " No. * vertices " << n -

```

```

star_vertices.first[0] << endl;
428 *logger::stat_stream << " No. * edges      " << nu_star_edges << endl;
429 *logger::stat_stream << " No. part bgraphs  " <<
part_bgraph.size() << endl;
430 *logger::stat_stream << " No. part graphs   " <<
part_graph.size() << endl;
431 }
432
433 for (it2 = part_bgraph.begin(); it2 != part_bgraph.end(); it2++){
434     // first, write t, t'
435     oup << it2->first.first;
436     //fwrite(&int_out, sizeof int_out, 1, f);
437     //output_bits += sizeof int_out;
438     oup << it2->first.second;
439     //fwrite(&int_out, sizeof int_out, 1, f);
440     //output_bits += sizeof int_out;
441     // then, the compressed integer
442     oup << it2->second;
443     //output_bits += mpz_out_raw(f, it2->second.get_mpz_t());
444 }
445
446 chunks_new = oup.chunks();
447 space_log.push_back(pair<string, int> ("partition bipartite graphs", chunks_new - chunks));
448 chunks = chunks_new;
449
450 logger::add_entry("partition graphs", "");
451 //output_bits = 0;
452 // === part graphs
453
454 // part_graph.size
455 oup << part_graph.size();
456 //fwrite(&int_out, sizeof int_out, 1, f);
457 //output_bits += sizeof int_out;
458
459 map< int, pair< mpz_class, vector< int > >::iterator it3;
460 for (it3 = part_graph.begin(); it3 != part_graph.end(); it3++){
461     oup << it3->first; // the type
462     //fwrite(&int_out, sizeof int_out, 1, f);
463     //output_bits += sizeof int_out;
464
465     // the mpz part
466     oup << it3->second.first;
467     //output_bits += mpz_out_raw(f, it3->second.first.get_mpz_t());
468     // the vector part
469     // first its size
470     oup << it3->second.second.size();
471     //fwrite(&int_out, sizeof int_out, 1, f);
472     //output_bits += sizeof int_out;
473     // then element by element
474     for(int j=0; j<it3->second.second.size(); j++){
475         oup << it3->second.second[j];
476         //fwrite(&int_out, sizeof int_out, 1, f);
477         //output_bits += sizeof int_out;
478     }
479 }
480
481 chunks_new = oup.chunks();
482 space_log.push_back(pair<string, int>("partition graphs", chunks_new - chunks));
483 chunks = chunks_new;
484
485
486 if (logger::stat){
487     *logger::stat_stream << endl << endl;
488     *logger::stat_stream << " Number of bytes used for each part " << endl;
489     *logger::stat_stream << " ----- " << endl << endl;
490
491     int total_chunks = 0;
492     for (int i=0; i < space_log.size(); i++)
493         total_chunks += space_log[i].second;
494
495     for (int i=0; i < space_log.size(); i++){
496         // each chunks is 4 bytes.
497         *logger::stat_stream << space_log[i].first << " -> " << 4 * space_log[i].second <
498         < " ( " << float(100) * float(space_log[i].second) / float(total_chunks) << " % " << endl;
499     }
500
501     *logger::stat_stream << " Total number of bytes wrote to the output = " << 4 *
total_chunks << endl;
501 }
502
503 oup.close();
504 logger::current_depth--;
505 }

```

6.15.1.5 clear()

```
void marked_graph_compressed::clear ( )
```

```
4 {
5   star_edges.clear();
6   type_mark.clear();
7   ver_type_list.clear();
8   part_bgraph.clear();
9   part_graph.clear();
10 }
```

6.15.2 Member Data Documentation

6.15.2.1 delta

```
int marked_graph_compressed::delta
```

the degree threshold used when compression was performed

6.15.2.2 h

```
int marked_graph_compressed::h
```

the depth up to which the compression was performed

6.15.2.3 n

```
int marked_graph_compressed::n
```

the number of vertices

6.15.2.4 part_bgraph

```
map<pair<int, int>, mpz_class> marked_graph_compressed::part_bgraph
```

compressed form of partition bipartite graphs corresponding to colors in $C_{<}$. For a pair $0 \leq t < t' < L$ of half edge types, `part_bgraph[pair<int, int>(t,t')]` is the compressed form of the bipartite graph with `n` left and right nodes, where a left node `i` is connected to a right node `j` if there is an edge connecting `i` to `j` with type `t` towards `i` and type `t'` towards `j`

6.15.2.5 part_graph

```
map<int, pair<mpz_class, vector<int> > > marked_graph_compressed::part_graph
```

compressed form of partition graphs corresponding to colors in C_- . For a half edge type t , `part_graph[t]` is the compressed form of the simple unmarked graph with n vertices, where a node i is connected to a node j where there is an edge between i and j in the original graph with color (t,t)

6.15.2.6 star_edges

```
map<pair<int, int> , vector<vector<int> > > marked_graph_compressed::star_edges
```

for each pair of edge marks x, x' , and integer k , `star_edges[pair<int,int>(x,x')][k]` is a list of neighbors w of the k th star vertex (say v) so that v shares a star edge with w so that the mark towards v is x and the mark towards w is x' .

6.15.2.7 star_vertices

```
pair<vector<int>, mpz_class> marked_graph_compressed::star_vertices
```

the compressed form of the `star_vertices` list

6.15.2.8 type_mark

```
vector<int> marked_graph_compressed::type_mark
```

for an edge type t , `type_mark[t]` denotes the mark component of t

6.15.2.9 ver_type_list

```
vector<vector<int> > marked_graph_compressed::ver_type_list
```

the list of all vertex types that appear in the graph, where the type of a vertex is a vector of integers, where its index 0 is the mark of the vertex, and indices $3k + 1$, $3k + 2$, $3k + 3$ are m , m' and $n_{m,m'}$, where (m, m') is a type pair, and $n_{m,m'}$ is the number of edges connected to the vertex with that type. The list is sorted lexicographically to ensure unique representation.

6.15.2.10 ver_types

```
pair<vector<int>, mpz_class> marked_graph_compressed::ver_types
```

the compressed form of vertex types, where the type of a vertex is the index with respect to ver_type_list of the list of integers specifying the type of the vertex (mark of the vertex followed by the number of edges of each type connected to that vertex)

The documentation for this class was generated from the following files:

- [marked_graph_compression.h](#)
- [marked_graph_compression.cpp](#)

6.16 marked_graph_decoder Class Reference

```
#include <marked_graph_compression.h>
```

Public Member Functions

- [marked_graph_decoder](#) ()
constructor
- [marked_graph decode](#) (const [marked_graph_compressed](#) &)

Private Member Functions

- void [decode_star_vertices](#) (const [marked_graph_compressed](#) &)
- void [decode_star_edges](#) (const [marked_graph_compressed](#) &)
- void [decode_vertex_types](#) (const [marked_graph_compressed](#) &)
- void [find_part_deg_orig_index](#) ()
- void [decode_partition_graphs](#) (const [marked_graph_compressed](#) &)
- void [decode_partition_bgraphs](#) (const [marked_graph_compressed](#) &)

Private Attributes

- int [h](#)
- int [delta](#)
- int [n](#)
number of vertices, this is set when a graph G is given to be encoded
- vector< int > [is_star_vertex](#)
for $0 \leq v < n$, [is_star_vertex](#)[v] is 1 if there is at least one star type edge connected to v and 0 otherwise.
- vector< int > [star_vertices](#)
the list of star vertices
- map< pair< int, int >, [b_graph](#) > [part_bgraph](#)
for $0 \leq t < t' < L$, [part_bgraph](#)[pair<int, int> (t,t')] is a bipartite graph with n left vertex and n right vertex. In this bipartite graph, a left vertex i is connected to a right vertex j iff there is an edge in the graph between vertices i and j with a half edge type towards i equal to t and a half edge type towards j equal to t'.
- map< int, [graph](#) > [part_graph](#)

for $0 \leq t < L$, `part_graph[i]` is a simple unmarked graph with n vertices. In this graph, vertices i and j are connected in the original graph with an edge with half edge types t in both directions i and j .

- `vector< pair< pair< int, int >, pair< int, int > > >` [edges](#)

the list of edges in the decoded graph, each index of the form $((i, j), (x, y))$, where i and j are the endpoints and x and y are the marks (towards i and j , respectively).

- `vector< int >` [vertex_marks](#)

the list of vertex marks of the marked graph to be decoded

- `vector< map< pair< int, int >, int > >` [Deg](#)

for a vertex $0 \leq v < n$, `Deg[v]` is a map such that `Deg[v][t]` is the number of edges connected to v with type (t, t') (if such an edge exists)

- `map< pair< int, int >, vector< int > >` [part_deg](#)

`part_deg[t]` is the degree sequence of the partition graph corresponding to pair of types t and t' , if $t \neq t'$, this is the degree sequence of the side of the graph corresponding to t .

- `map< pair< int, int >, vector< int > >` [origin_index](#)

`origin_index[t][v]` gives the original index in the marked graph corresponding to the vertex v in the (t, t') partition graph. Here, if $t \neq t'$, v is in the side of the bipartite graph corresponding to t

6.16.1 Constructor & Destructor Documentation

6.16.1.1 marked_graph_decoder()

```
marked_graph_decoder::marked_graph_decoder ( ) [inline]
```

constructor

```
149 {}
```

6.16.2 Member Function Documentation

6.16.2.1 decode()

```
marked_graph marked_graph_decoder::decode (
    const marked_graph_compressed & compressed )
```

```
1111 {
1112     logger::current_depth++;
1113     logger::add_entry("Init", "");
1114     n = compressed.n;
1115     h = compressed.h;
1116     delta = compressed.delta;
1117
1118
1119     edges.clear(); // clear the edge list of the marked graph to be decoded
1120     vertex_marks.clear(); // clear the list of vertex marks of the marked graph to be decoded
1121
1122     logger::add_entry("Decode * vertices", "");
1123     decode_star_vertices(compressed);
1124     //cerr << " decoded star vertices " << endl;
1125
1126     logger::add_entry("Decode * edges", "");
```



```

1127 decode_star_edges(compressed);
1128 //cerr << " decoded star edges " << endl;
1129
1130 logger::add_entry("Decode vertex types", "");
1131 decode_vertex_types(compressed);
1132 //cerr << " decoded vertex types " << endl;
1133
1134 logger::add_entry("Decode partition graphs", "");
1135 decode_partition_graphs(compressed);
1136 //cerr << " decoded partition graphs " << endl;
1137
1138 logger::add_entry("Decode partition b graphs", "");
1139 decode_partition_bgraphs(compressed);
1140 //cerr << " decoded partition b graphs " << endl;
1141
1142 // now, reconstruct the original marked graphs by assembling the vertex marks and edge list
1143 logger::add_entry("Construct decoded graph", "");
1144 marked_graph G(n, edges, vertex_marks);
1145
1146 logger::current_depth--;
1147 return G;
1148 }

```

6.16.2.2 decode_partition_bgraphs()

```

void marked_graph_decoder::decode_partition_bgraphs (
    const marked_graph_compressed & compressed ) [private]

1274 {
1275     pair<int, int> c; // the pair of types
1276     int t, tp; // types
1277     int x, xp; // mark components of t and tp
1278
1279     b_graph G; // the decoded partition bipartite graph
1280     int nl_G; // the number of left nodes in the partition graph G
1281     vector<int> adj_list; // adj list of a vertex in a partition bipartite graph
1282     int w; // a right node
1283     int v_orig, w_orig; // the original index of vertices v and w in partition graphs
1284     for (map<pair<int, int>, mpz_class>::const_iterator it = compressed.
part_bgraph.begin(); it!=compressed.part_bgraph.end(); it++){
1285         c = it->first;
1286         t = c.first;
1287         tp = c.second;
1288         x = compressed.type_mark[t]; // the mark component of t
1289         xp = compressed.type_mark[tp]; // the mark component of tp
1290
1291         //cerr << " t " << t << " tp " << tp << endl;
1292
1293         b_graph_decoder D(part_deg.at(pair<int, int>(t,tp)),
part_deg.at(pair<int, int>(tp,t))); // the degree sequence of left nodes is precisely
part_deg.at(pair<int, int>(t,tp)), while that of the right nodes is precisely part_deg.at(pair<int, int>(tp,t))
1294         //cerr << " decoder constructed " << endl;
1295         //cerr << " part graph t = " << t << " t' = " << tp << " nl " << part_deg.at(pair<int,
int>(t,tp)).size() << " nr = " << part_deg.at(pair<int, int>(tp,t)).size() << endl;
1296         G = D.decode(it->second);
1297
1298         //cerr << " G decoded " << endl;
1299         nl_G = part_deg.at(pair<int, int>(t,tp)).size(); // the number of left nodes in G is obtained
from the size of the degree sequence of left nodes
1300
1301         for (int v=0;v<nl_G;v++){
1302             v_orig = origin_index.at(pair<int, int>(t,tp))[v];
1303             //cerr << " v " << v << " v_orig " << v_orig << endl;
1304             adj_list = G.get_adj_list(v);
1305             for (int i=0;i<adj_list.size();i++){
1306                 w = adj_list[i];
1307                 w_orig = origin_index.at(pair<int, int>(tp,t))[w]; // since w is a right node, we
should read its original index through origin_index[(tp,t)]
1308                 //cerr << " w " << w << " w_orig " << w_orig << endl;
1309                 edges.push_back(pair<pair<int, int>, pair<int, int>>(pair<int, int>(v_orig,w_orig), pair<int,
int>(x,xp)));
1310             }
1311         }
1312     }
1313 }

```

6.16.2.3 decode_partition_graphs()

```

void marked_graph_decoder::decode_partition_graphs (
    const marked_graph_compressed & compressed ) [private]

1237 {
1238     int t; // the type corresponding to the partition graph
1239     vector<int> t_message; // the actual message corresponding to t
1240     int x; // the mark component associated to t
1241     pair< mpz_class, vector< int > > G_compressed; // the compressed form of the partition graph
1242     graph G; // the decoded partition graph
1243     vector<int> flist; // the forward adjacency list of a vertex in a partition graph
1244     int w; // vertex in partition graph
1245     int v_orig, w_orig; // the original index of vertices v and w
1246     int n_G; // the number of vertices of the partitioned graph
1247
1248     for(map< int, pair< mpz_class, vector< int > >>::const_iterator it=compressed.
part_graph.begin(); it!=compressed.part_graph.end(); it++){
1249         t = it->first;
1250         x = compressed.type_mark[t]; // the mark component of t
1251
1252         G_compressed = it->second;
1253         // the degree sequence of the graph can be obtained from part_deg.at(pair<int,int>(t,t))
1254         graph_decoder D(part_deg.at(pair<int, int>(t,t)));
1255         //cerr << " part_graph t = " << t << " with " << part_deg.at(pair<int, int>(t,t)).size() << " vertices
" << endl;
1256         n_G = part_deg.at(pair<int, int>(t,t)).size(); // the number of vertices in the partition graph
is read from the size of its degree sequence
1257         G = D.decode(G_compressed.first, G_compressed.second);
1258         // for each edge in G, we should add an edge with mark pair (x,x) to the edge list of the marked graph
1259         for (int v=0;v<n_G;v++){
1260             flist = G.get_forward_list(v);
1261             v_orig = origin_index.at(pair<int, int>(t,t))[v]; // the index of v in the original graph

1262             for (int i=0;i<flist.size();i++){
1263                 w = flist[i]; // the other endpoint in the partition graph
1264                 w_orig = origin_index.at(pair<int, int>(t,t))[w]; // the index of w in the original
graph
1265                 edges.push_back(pair<pair<int, int>, pair<int, int> >(pair<int, int>(v_orig,w_orig), pair<int,
int> (x,x)));
1266             }
1267         }
1268     }
1269 }

```

6.16.2.4 decode_star_edges()

```

void marked_graph_decoder::decode_star_edges (
    const marked_graph_compressed & compressed ) [private]

1162 {
1163     pair<int, int> mark_pair; // the pair of marks
1164     vector<vector<int> > list; // list of edges with this pair of marks
1165     int v; // one endpoint of the star edge
1166     // iterating through the star_edges map
1167     for (map<pair<int, int>, vector<vector<int> > >>::const_iterator it = compressed.
star_edges.begin(); it!=compressed.star_edges.end(); it++){
1168         mark_pair = it->first;
1169         //cerr << " mark_pair " << mark_pair.first << " " << mark_pair.second << endl;
1170         list = it->second;
1171         for (int i=0;i<list.size();i++){
1172             v = star_vertices[i];
1173             for (int j=0;j<list[i].size();j++){
1174                 //cerr << " list[i][j] " << list[i][j] << endl;
1175                 edges.push_back(pair<pair<int, int>, pair<int, int> >(pair<int, int>(v,list[i][j]), mark_pair)
);
1176             }
1177         }
1178     }
1179 }

```

6.16.2.5 decode_star_vertices()

```
void marked_graph_decoder::decode_star_vertices (
    const marked_graph_compressed & compressed ) [private]
```

```
1151 {
1152     time_series_decoder D(n);
1153     is_star_vertex = D.decode(compressed.star_vertices);
1154
1155     star_vertices.clear();
1156     for (int i=0;i<n;i++)
1157         if (is_star_vertex[i] == 1)
1158             star_vertices.push_back(i);
1159 }
```

6.16.2.6 decode_vertex_types()

```
void marked_graph_decoder::decode_vertex_types (
    const marked_graph_compressed & compressed ) [private]
```

```
1182 {
1183     time_series_decoder D(n);
1184     vector<int> ver_type_int = D.decode(compressed.ver_types);
1185
1186     // converting the integer value vertex types to actual vectors using the 'ver_type_list' attribute of
    compressed
1187
1188     vertex_marks.resize(n); // preparing for decoding vertex marks
1189     Deg.clear(); // refresh
1190     Deg.resize(n);
1191
1192     vector<int> x; // auxiliary vector
1193
1194     for (int v=0;v<n;v++){
1195         if (ver_type_int[v] >= compressed.ver_type_list.size())
1196             cerr << " Warning: marked_graph_decoder::decode_vertex_types ver_type_int[" << v << "] is out of
    range" << endl;
1197         x = compressed.ver_type_list[ver_type_int[v]];
1198         vertex_marks[v] =x[0]; // the mark of vertex v is the first element in the type list of
    this vertex
1199         // now, we extract Deg[v] by looking at batches of size 3 in x
1200         for (int i=1;i<x.size();i+=3){
1201             if (i+2 >= x.size())
1202                 cerr << " Error: marked_graph_decoder::decode_vertex_types, the type of vertex " << v << " does not
    obey length constraints, i.e. it does not have length 1 + 3k " << endl;
1203             Deg[v][pair<int, int>(x[i],x[i+1])] = x[i+2]; // x[i] and x[i+1] are types, and x[i+2] is the
    count
1204         }
1205     }
1206
1207     find_part_deg_orig_index(); // find part_deg and orig_index maps
1208 }
```

6.16.2.7 find_part_deg_orig_index()

```
void marked_graph_decoder::find_part_deg_orig_index ( ) [private]
```

```

1211 {
1212     part_deg.clear();
1213     origin_index.clear();
1214     int t, tp; // types
1215
1216     //cerr << " decoded deg : " << endl;
1217     for (int v=0;v<n;v++){
1218         //cerr << " v " << v << endl;
1219         for (map<pair<int, int>, int>::iterator it=Deg[v].begin(); it!=Deg[v].end(); it++){
1220             t = it->first.first;
1221             tp = it->first.second;
1222             //cerr << " t " << t << " tp " << tp << " : " << it->second << endl;
1223             if (part_deg.find(it->first) == part_deg.end()){
1224                 // this is our first encounter with this type pair
1225                 origin_index[it->first] = vector<int>({v}); // v is the first node in the t side of the
(t,t') partition graph
1226                 part_deg[it->first] = vector<int>({it->second}); // the degree in the partition graph is
read from it->second
1227             }else{
1228                 origin_index.at(it->first).push_back(v); // v is the next vertex observed with type
t,t', so the vertex in the partition graph with index origin_index[it->first] has original index v
1229                 // append degree of v, which is it->second
1230                 part_deg.at(it->first).push_back(it->second);
1231             }
1232         }
1233     }
1234 }

```

6.16.3 Member Data Documentation

6.16.3.1 Deg

```
vector<map<pair<int, int>, int> > marked_graph_decoder::Deg [private]
```

for a vertex $0 \leq v < n$, $Deg[v]$ is a map such that $Deg[v][(t,t')]$ is the number of edges connected to v with type (t, t') (if such an edge exists)

6.16.3.2 delta

```
int marked_graph_decoder::delta [private]
```

6.16.3.3 edges

```
vector<pair<pair<int, int>, pair<int, int> > > marked_graph_decoder::edges [private]
```

the list of edges in the decoded graph, each index of the form $((i, j), (x, y))$, where i and j are the endpoints and x and y are the marks (towards i and j , respectively).

6.16.3.4 h

```
int marked_graph_decoder::h [private]
```

6.16.3.5 is_star_vertex

```
vector<int> marked_graph_decoder::is_star_vertex [private]
```

for $0 \leq v < n$, `is_star_vertex[v]` is 1 if there is at least one star type edge connected to v and 0 otherwise.

6.16.3.6 n

```
int marked_graph_decoder::n [private]
```

number of vertices, this is set when a graph G is given to be encoded

6.16.3.7 origin_index

```
map<pair<int, int>, vector<int> > marked_graph_decoder::origin_index [private]
```

`origin_index[(t,t')][v]` gives the original index in the marked graph corresponding to the vertex v in the (t, t') partition graph. Here, if $t \neq t'$, v is in the side of the bipartite graph corresponding to t

6.16.3.8 part_bgraph

```
map<pair<int, int>, b_graph> marked_graph_decoder::part_bgraph [private]
```

for $0 \leq t < t' < L$, `part_bgraph[pair<int, int> (t,t')]` is a bipartite graph with n left vertex and n right vertex. In this bipartite graph, a left vertex i is connected to a right vertex j iff there is an edge in the graph between vertices i and j with a half edge type towards i equal to t and a half edge type towards j equal to t' .

6.16.3.9 part_deg

```
map<pair<int, int>, vector<int> > marked_graph_decoder::part_deg [private]
```

`part_deg[(t,t')]` is the degree sequence of the partition graph corresponding to pair of types t and t' , if $t \neq t'$, this is the degree sequence of the side of the graph corresponding to t .

6.16.3.10 `part_graph`

```
map<int, graph> marked_graph_decoder::part_graph [private]
```

for $0 \leq t < L$, `part_graph[i]` is a simple unmarked graph with n vertices. In this graph, vertices i and j are connected in the original graph with an edge with half edge types t in both directions i and j .

6.16.3.11 `star_vertices`

```
vector<int> marked_graph_decoder::star_vertices [private]
```

the list of star vertices

6.16.3.12 `vertex_marks`

```
vector<int> marked_graph_decoder::vertex_marks [private]
```

the list of vertex marks of the marked graph to be decoded

The documentation for this class was generated from the following files:

- [marked_graph_compression.h](#)
- [marked_graph_compression.cpp](#)

6.17 `marked_graph_encoder` Class Reference

```
#include <marked_graph_compression.h>
```

Public Member Functions

- [marked_graph_encoder](#) (int $h_{_}$, int $\delta_{_}$)
- [marked_graph_compressed encode](#) (const [marked_graph](#) &G)
compresses a simple marked graph G , and returns the compressed form as an object of type [marked_graph_compressed](#)
- void [encode](#) (const [marked_graph](#) &G, FILE $*f$)
compresses a simple marked graph G , and writes the compressed form in a binary file f

Private Member Functions

- void `encode_star_vertices` ()
encodes the star vertices (those vertices with at least one star edge connected to them)
- void `extract_edge_types` (const `marked_graph` &)
Given a marked graph, extracts edge types by updating the `colored_graph` member C.
- void `encode_star_edges` ()
Encodes star edges to the `star_edges` attribute of compressed.
- void `encode_vertex_types` ()
encodes the type of vertices, where the type of a vertex denotes its mark as well as its degree matrix
- void `find_part_index_deg` ()
update `part_index` and `part_deg` members
- void `extract_partition_graphs` ()
by looking at the colored graph C, extract partition graphs (simple and bipartite)
- void `encode_partition_bgraphs` ()
encode partition bipartite graphs
- void `encode_partition_graphs` ()
encodes partition simple graphs

Private Attributes

- int `h`
- int `delta`
- int `n`
number of vertices, this is set when a graph G is given to be encoded
- `colored_graph` C
the auxiliary object to extract edge types
- vector< bool > `is_star_vertex`
for $0 \leq v < n$, `is_star_vertex[v]` is true if there is at least one star type edge connected to v and false otherwise.
- vector< int > `star_vertices`
the list of star vertices
- map< pair< int, int >, `b_graph` > `part_bgraph`
for $0 \leq t < t' < L$, `part_bgraph[pair<int, int> (t,t')]` is a bipartite graph with n left vertex and n right vertex. In this bipartite graph, a left vertex i is connected to a right vertex j iff there is an edge in the graph between vertices i and j with a half edge type towards i equal to t and a half edge type towards j equal to t'.
- vector< map< pair< int, int >, int > > `part_index`
for a vertex $0 \leq v < n$, if v has a (t,t') edge connected to it. `part_index[v][(t,t')]` is the index of vertex v in the partition graph (or bipartite graph) corresponding to the pair (t,t'). If $t < t'$, this is the index of the left vertex corresponding to v in the partition bipartite graph, and if $t > t'$, this is the index of the right node corresponding to v in the bipartite partition graph.
- map< pair< int, int >, vector< int > > `part_deg`
for a pair of types (t,t'), `part_deg[(t,t')]` is the degree sequence of the nodes in the partition graph corresponding to the pair t,t'. If $t < t'$, this is the degree sequence of the left nodes in the (t,t') partition bipartite graph, while if $t > t'$, this is the degree sequence of the right nodes in the (t', t) partition bipartite graph. Moreover, if $t = t'$, this is the degree sequence of the (t,t) partition graph.
- map< int, `graph` > `part_graph`
for $0 \leq t < L$, `part_graph[i]` is a simple unmarked graph with n vertices. In this graph, vertices i and j are connected in the original graph with an edge with half edge types t in both directions i and j.
- `marked_graph_compressed` compressed
the compressed version of the given graph in encode function

6.17.1 Constructor & Destructor Documentation

6.17.1.1 marked_graph_encoder()

```
marked_graph_encoder::marked_graph_encoder (
    int h_,
    int delta_ ) [inline]

105 : h(h_), delta(delta_) {}
```

6.17.2 Member Function Documentation

6.17.2.1 encode() [1/2]

```
marked_graph_compressed marked_graph_encoder::encode (
    const marked_graph & G )
```

compresses a simple marked graph G, and returns the compressed form as an object of type [marked_graph_compressed](#)

```
846 {
847     logger::current_depth++;
848     logger::add_entry("Init compressed", "");
849
850     compressed.clear(); // reset the compressed variable before starting
851
852     n = G.nu_vertices;
853     compressed.n = n;
854     compressed.h = h;
855     compressed.delta = delta;
856
857     logger::add_entry("Extract edge types", "");
858     extract_edge_types(G);
859     //cout << " edge types extracted " << endl;
860
861
862     compressed.ver_type_list = C.ver_type_list; //
863     compressed.type_mark = C.M.message_mark;
864
865     /*
866     cout << " message list " << endl;
867     for (int i=0;i<C.M.message_list.size();i++){
868         cout << i << " : ";
869         for (int j=0;j<C.M.message_list[i].size();j++){
870             cout << C.M.message_list[i][j] << " ";
871         }
872     }
873     */
874
875     logger::add_entry("Encode * vertices", "");
876     encode_star_vertices(); // encode the list of vertices with at least one star edge
      connected to them
877     //cout << " encoded star vertices " << endl;
878
879     logger::add_entry("Encode * edges", "");
880     encode_star_edges(); // encode edges with star types, i.e. those with half edge type L
      or larger
881     //cout << " encoded star edges " << endl;
882
883     logger::add_entry("Encode vertex types", "");
884     encode_vertex_types(); // encode the sequences \f$\vec{\beta}$, \vec{D}\f$, which is
```



```

    encoded in C.ver_type
885 //cout << " encoded vertex types " << endl;
886
887 logger::add_entry("Extract partition graphs", "");
888 extract_partition_graphs(); // for equality types, we form simple unmarked
    graphs, and for inequality types, we form a bipartite graph
889 //cout << " extracted partition graphs " << endl;
890 /*
891     cout << " partition bipartite graphs " << endl;
892     for (map<pair<int, int>, b_graph>::iterator it = part_bgraph.begin(); it!=part_bgraph.end(); it++){
893         cout << " c = " << it->first.first << " , " << it->first.second << endl;
894         cout << it->second << endl;
895     }
896
897     cout << " partition simple graphs " << endl;
898     for (map<int, graph>::iterator it = part_graph.begin(); it!=part_graph.end(); it++){
899         cout << " t = " << it->first << endl;
900         cout << it->second << endl;
901     }
902 */
903
904 logger::add_entry("Encode partition b graphs", "");
905 encode_partition_bgraphs();
906 //cout << " encoded partition bgraphs " << endl;
907
908 logger::add_entry("Encode partition graphs", "");
909 encode_partition_graphs();
910 //cout << " encoded partition graphs " << endl;
911
912 logger::current_depth--;
913 return compressed;
914 }

```

6.17.2.2 encode() [2/2]

```

void marked_graph_encoder::encode (
    const marked_graph & G,
    FILE * f )

```

compresses a simple marked graph G, and writes the compressed form in a binary file f

```

916                                                                 {
917     logger::add_entry("Encode", "");
918     marked_graph_compressed comp = encode(G);
919     logger::add_entry("Write to binary file", "");
920     comp.binary_write(f);
921 }

```

6.17.2.3 encode_partition_bgraphs()

```

void marked_graph_encoder::encode_partition_bgraphs ( ) [private]

```

encode partition bipartite graphs

```

1069 {
1070     int t, tp;
1071
1072     // compressing bipartite graphs
1073     for (map<pair<int, int>, b_graph>::iterator it = part_bgraph.begin(); it!=
    part_bgraph.end(); it++){
1074         // the color components are t, tp
1075         t = it->first.first;
1076         tp = it->first.second;
1077         b_graph_encoder E(part_deg.at(pair<int, int>(t,tp)),
    part_deg.at(pair<int, int>(tp, t)));
1078         compressed.part_bgraph[pair<int, int>(t,tp)] = E.encode(it->second);
1079     }
1080
1081 }

```

6.17.2.4 encode_partition_graphs()

```
void marked_graph_encoder::encode_partition_graphs ( ) [private]
```

encodes partition simple graphs

```
1084 {
1085     int t;
1086
1087     // compressing graphs
1088     for (map<int, graph>::iterator it=part_graph.begin(); it!=part_graph.end(); it++){
1089         t = it->first; // the color is t,t
1090         graph_encoder E(part_deg.at(pair<int, int>(t,t)));
1091         compressed.part_graph[t] = E.encode(it->second);
1092     }
1093 }
```

6.17.2.5 encode_star_edges()

```
void marked_graph_encoder::encode_star_edges ( ) [private]
```

Encodes star edges to the star_edges attribute of compressed.

```
960 {
961     int x, xp; // auxiliary mark variables
962     int w; // auxiliary vertex variable
963     int v; // auxiliary vertex variable
964     for (int k=0; k<star_vertices.size(); k++){ // iterating over star vertices
965         v = star_vertices[k];
966         for (int i=0; i<C.adj_list[v].size(); i++){
967             if (C.M.is_star_message[C.adj_list[v][i].second.first] or
C.M.is_star_message[C.adj_list[v][i].second.second]){ // this is a star edge
968                 x = C.M.message_mark[C.adj_list[v][i].second.first]; // mark towards v
969                 xp = C.M.message_mark[C.adj_list[v][i].second.second]; // mark towards other
endpoint
970                 w = C.adj_list[v][i].first; // the other endpoint of the edge
971                 if (x < xp){ // if x > xp, we only store this edge when visiting the other endpoint (w), since we
do not want to express an edge twice
972                     if (compressed.star_edges.find(pair<int, int>(x,xp)) ==
compressed.star_edges.end()) // this pair does not exist
973                         compressed.star_edges[pair<int, int>(x,xp)].resize(
star_vertices.size()); // open space for all star vertices
974                         compressed.star_edges.at(pair<int, int>(x,xp))[k].push_back(w); // add w to
the position of v (which is k)
975                     }
976                     if (x == xp and w > v){ // if w < v, we store this edge when visiting the other endpoint (w) to
avoid storing and edge twice
977                         if (compressed.star_edges.find(pair<int, int>(x,xp)) ==
compressed.star_edges.end()) // not yet exist
978                             compressed.star_edges[pair<int, int>(x,xp)].resize(
star_vertices.size()); // open space
979                             compressed.star_edges.at(pair<int, int>(x,xp))[k].push_back(w);
980                         }
981                     }
982                 }
983             }
984 }
```

6.17.2.6 encode_star_vertices()

```
void marked_graph_encoder::encode_star_vertices ( ) [private]
```

encodes the star vertices (those vertices with at least one star edge connected to them)

uses `time_series_encode` to encode the 0-1 sequence of star vertices stored in `is_star_vertex` to the `star_vertices` attribute of compressed

```
946 {
947     // compress the is_star_vertex list
948     time_series_encoder star_encoder(n);
949     vector<int> is_star_vertex_int(is_star_vertex.size());
950     for (int i=0;i<is_star_vertex.size();i++){
951         if(is_star_vertex[i] == true)
952             is_star_vertex_int[i] = 1;
953         else
954             is_star_vertex_int[i] = 0;
955     }
956     compressed.star_vertices = star_encoder.encode(is_star_vertex_int);
957 }
```

6.17.2.7 encode_vertex_types()

```
void marked_graph_encoder::encode_vertex_types ( ) [private]
```

encodes the type of vertices, where the type of a vertex denotes its mark as well as its degree matrix

```
924 {
925     time_series_encoder vtype_encoder(n);
926     //cerr << " C.ver_type_int " << endl;
927     //for (int i=0;i<C.ver_type_int.size();i++)
928     //    cerr << C.ver_type_int[i] << " ";
929     //cerr << endl;
930     compressed.ver_types = vtype_encoder.encode(C.ver_type_int);
931 }
```

6.17.2.8 extract_edge_types()

```
void marked_graph_encoder::extract_edge_types (
    const marked_graph & G ) [private]
```

Given a marked graph, extracts edge types by updating the `colored_graph` member C.

```
934 {
935     // extracting edges types (aka colors)
936     logger::current_depth++;
937     logger::add_entry("Extract messages", "");
938     C = colored_graph(G, h, delta);
939     //cerr << " number of types " << C.M.message_mark.size() << endl;
940     is_star_vertex = C.is_star_vertex;
941     star_vertices = C.star_vertices;
942     logger::current_depth--;
943 }
```

6.17.2.9 extract_partition_graphs()

```
void marked_graph_encoder::extract_partition_graphs ( ) [private]
```

by looking at the colored graph C, extract partition graphs (simple and bipartite)

```
1009 {
1010     find_part_index_deg();
1011
1012     // for t \leq t', part_adj_list[(t,t')] is the adjacency list of the partition graph t,t'. If t < t',
    // this is the adjacency list of the left nodes, if t = t', this is the forward adjacency list of the partition
    // graph.
1013
1014     map<pair<int, int>, vector<vector<int> > > part_adj_list;
1015     int t, tp; // types
1016     for (map<pair<int, int>, vector<int> >::iterator it = part_deg.begin(); it!=
    part_deg.end(); it++){
1017         // search over all type pairs in part_deg
1018         t = it->first.first;
1019         tp = it->first.second;
1020         // t < t': bipartite, t = t': simple. In both cases,
1021         if (t <= tp)
1022             part_adj_list[it->first] = vector<vector<int> >(it->second.size());
1023     }
1024
1025     // going over the edges in the graph and forming partition_adj_list
1026     int w, p, q; // auxiliary variables
1027     for (int v = 0; v < n; v++){
1028         for (int i = 0; i < C.adj_list[v].size(); i++){
1029             w = C.adj_list[v][i].first; // the other endpoint
1030             t = C.adj_list[v][i].second.first; // color towards v
1031             tp = C.adj_list[v][i].second.second; // color towards w
1032             if (C.M.is_star_message[t] == false and C.M.
    is_star_message[tp] == false){
1033                 p = part_index[v].at(pair<int, int>(t,tp)); // the index of v in the t part of the t,tp
    partition graph
1034                 //cerr << " p " << p << endl;
1035                 q = part_index[w].at(pair<int, int>(tp, t)); // the index of w in the tp part of the t,tp
    partition graph
1036                 //cerr << " q " << q << endl;
1037                 if (t < tp)
1038                     part_adj_list.at(pair<int, int>(t,tp))[p].push_back(q);
1039                 if ((t == tp) and (q > p))
1040                     part_adj_list.at(pair<int, int>(t,t))[p].push_back(q);
1041             }
1042         }
1043     }
1044
1045     // using partition_adj_list in order to construct partition graphs
1046     //if(logger::stat){
1047     //*logger::stat_stream << " partition graphs size: " << endl;
1048     //*logger::stat_stream << " ===== " << endl;
1049     //}
1050     for (map<pair<int, int>, vector<vector<int> > >::iterator it=part_adj_list.begin(); it!=part_adj_list.end
    (); it++){
1051         t = it->first.first;
1052         tp = it->first.second;
1053         if (t < tp){
1054             part_bgraph[it->first] = b_graph(it->second, part_deg.at(pair<int, int>(t,
    tp)), part_deg.at(pair<int, int>(tp, t))); // left and right degree sequences are read from the
    part_deg map
1055             //if (logger::stat){
1056             //*logger::stat_stream << " bipartite: (" << part_deg.at(pair<int, int>(t,tp)).size() << " , " <<
    part_deg.at(pair<int, int>(tp,t)).size() << ")" << endl;
1057             //}
1058         }
1059         if (t == tp){
1060             part_graph[t] = graph(it->second, part_deg.at(pair<int, int>(t,t)));
1061             //if (logger::stat){
1062             //*logger::stat_stream << " simple: " << part_deg.at(pair<int, int>(t,t)).size() << endl;
1063             //}
1064         }
1065     }
1066 }
```

6.17.2.10 find_part_index_deg()

```
void marked_graph_encoder::find_part_index_deg ( ) [private]
```

update part_index and part_deg members

```

987 {
988     // extracting part_index and part_deg
989     part_index.resize(n);
990     for (int v =0; v<n; v++){
991         for (map< pair< int, int >, int >::iterator it = C.deg[v].begin(); it !=
C.deg[v].end(); it++){
992             if (part_deg.find(it->first) == part_deg.end()){
993                 // this pair has not been observed yet in the graph
994                 // so v is the first index node
995                 part_index[v][it->first] = 0;
996                 // the degree of v in the partition graph is indeed it->second
997                 part_deg[it->first] = vector<int>({it->second});
998             }else{
999                 // there are currently part_deg[it->first].size() many elements there, and v is the last arrival
one, so its index is equal to the number of existing nodes
1000                 part_index[v][it->first] = part_deg.at(it->first).size();
1001                 // append degree of v, which is it->second
1002                 part_deg.at(it->first).push_back(it->second);
1003             }
1004         }
1005     }
1006 }
```

6.17.3 Member Data Documentation

6.17.3.1 C

```
colored_graph marked_graph_encoder::C [private]
```

the auxiliary object to extract edge types

6.17.3.2 compressed

```
marked_graph_compressed marked_graph_encoder::compressed [private]
```

the compressed version of the given graph in encode function

6.17.3.3 delta

```
int marked_graph_encoder::delta [private]
```

6.17.3.4 h

```
int marked_graph_encoder::h [private]
```

6.17.3.5 is_star_vertex

```
vector<bool> marked_graph_encoder::is_star_vertex [private]
```

for $0 \leq v < n$, `is_star_vertex[v]` is true if there is at least one star type edge connected to v and false otherwise.

6.17.3.6 n

```
int marked_graph_encoder::n [private]
```

number of vertices, this is set when a graph G is given to be encoded

6.17.3.7 part_bgraph

```
map<pair<int, int>, b_graph> marked_graph_encoder::part_bgraph [private]
```

for $0 \leq t < t' < L$, `part_bgraph[pair<int, int> (t,t')]` is a bipartite graph with n left vertex and n right vertex. In this bipartite graph, a left vertex i is connected to a right vertex j iff there is an edge in the graph between vertices i and j with a half edge type towards i equal to t and a half edge type towards j equal to t' .

6.17.3.8 part_deg

```
map<pair<int, int>, vector<int> > marked_graph_encoder::part_deg [private]
```

for a pair of types (t,t') , `part_deg[(t,t')]` is the degree sequence of the nodes in the partition graph corresponding to the pair t,t' . If $t < t'$, this is the degree sequence of the left nodes in the (t,t') partition bipartite graph, while if $t > t'$, this is the degree sequence of the right nodes in the (t', t) partition bipartite graph. Moreover, if $t = t'$, this is the degree sequence of the (t,t) partition graph.

6.17.3.9 part_graph

```
map<int, graph> marked_graph_encoder::part_graph [private]
```

for $0 \leq t < L$, `part_graph[t]` is a simple unmarked graph with n vertices. In this graph, vertices i and j are connected in the original graph with an edge with half edge types t in both directions i and j .

6.17.3.10 part_index

```
vector<map<pair<int, int>, int> > marked_graph_encoder::part_index [private]
```

for a vertex $0 \leq v < n$, if v has a (t, t') edge connected to it. `part_index[v][(t, t')]` is the index of vertex v in the partition graph (or bipartite graph) corresponding to the pair (t, t') . If $t < t'$, this is the index of the left vertex corresponding to v in the partition bipartite graph, and if $t > t'$, this is the index of the right node corresponding to v in the bipartite partition graph.

6.17.3.11 star_vertices

```
vector<int> marked_graph_encoder::star_vertices [private]
```

the list of star vertices

The documentation for this class was generated from the following files:

- [marked_graph_compression.h](#)
- [marked_graph_compression.cpp](#)

6.18 obitstream Class Reference

handles writing bitstreams to binary files

```
#include <obitstream.h>
```

Public Member Functions

- [obitstream](#) (string file_name)
constructor
- void [write_bits](#) (unsigned int n, unsigned int nu_bits)
write the bits given as unsigned int to the output
- [obitstream](#) & [operator<<](#) (const unsigned int &n)
uses Elias delta code to write a nonnegative integer to the output. In order to make sure that $n \geq 1$, we effectively encode $n + 1$ instead
- [obitstream](#) & [operator<<](#) (const mpz_class &n)
uses Elias delta code to write a nonnegative mpz_class integer to the output. In order to make sure that $n \geq 1$, we effectively encode $n + 1$ instead
- void [bin_inter_code](#) (const vector< int > &a, int b)
uses binary interpolative coding to encode an increasing sequence of integers
- void [bin_inter_code](#) (const vector< int > &a, int i, int j, int low, int high)
binary interpolative coding for array a, interval [i,j], where values are in the range [low, high]
- unsigned int [chunks](#) ()
returns the number of chunks (each is BIT_INT = 32 bits) to the output.
- void [close](#) ()
closes the session by writing the remaining chunk to the output (if any) and closing the file pointer f

Private Member Functions

- void `write()`
writes complete chunks to the output

Private Attributes

- `bit_pipe` buffer
a `bit_pipe` carrying the buffered data
- `FILE * f`
- unsigned int `chunks_written`
the number of chunks written to the output so far

6.18.1 Detailed Description

handles writing bitstreams to binary files

When trying to write to binary files, we sometimes need to write less than a byte, or a few bytes followed by say 2 bits. This is not possible unless we turn those 2 bits to 8 bits by basically adding 6 zeros. . However, if we want to do a lot of such operations, this can result in space inefficiencies. To avoid this, we can concatenate the bitstreams together and perhaps gain a lot in space. This class also handles Elias delta encoding of unsigned int and mpz↔_class. The way it is done is to buffer the data, write complete bytes to the output, and keeping the residuals for future operations.

In order to make sure that the carry over from the last operation is also written to the output, we should call the `close()` function.

6.18.2 Constructor & Destructor Documentation

6.18.2.1 `obitstream()`

```
obitstream::obitstream (
    string file_name ) [inline]
```

constructor

```
87     {
88         f = fopen(file_name.c_str(), "wb+");
89         chunks_written = 0;
90     }
```

6.18.3 Member Function Documentation

6.18.3.1 `bin_inter_code()` [1/2]

```
void obitstream::bin_inter_code (
    const vector< int > & a,
    int b )
```

uses binary interpolative coding to encode an increasing sequence of integers

We use the binary interpolative coding algorithm introduced by Moffat and Stuiver, reference:

Moffat, Alistair, and Lang Stuiver. "Binary interpolative coding for effective index compression." Information Retrieval 3.1 (2000): 25-47.

Parameters

| | |
|----------|--|
| <i>a</i> | array of nonnegative increasing integers (this function assumes a contains nonnegative increasing integers, and does not check it) |
| <i>b</i> | an upper bound on the number of bits necessary to encode values in a and the size of a |

```

264                                     {
265     // write a.size
266
267     write_bits(a.size(),b);
268     if (a.size() == 0)
269         return;
270     if (a.size()==1){
271         write_bits(a[0],b);
272         return;
273     }
274     // write low and high values in a
275     write_bits(a[0], b);
276     write_bits(a[a.size()-1], b);
277
278     // then, encode recursively
279     bin_inter_code(a, 0, a.size()-1, a[0], a[a.size()-1]);
280 }
```

6.18.3.2 bin_inter_code() [2/2]

```

void obitstream::bin_inter_code (
    const vector< int > & a,
    int i,
    int j,
    int low,
    int high )
```

binary interpolative coding for array a, interval [i,j], where values are in the range [low, high]

Parameters

| | |
|-------------|--|
| <i>a</i> | array of increasing nonnegative integers |
| <i>i,j</i> | endpoints of the interval to be encoded |
| <i>low</i> | lower bound for the integers in the interval [i,j] |
| <i>high</i> | upper bound for the integers in the interval [i,j] |

```

288                                     {
289     if (j < i)
290         return;
291     if (i==j){
292         // we should encode a[i] using the assumption that it is bounded by high - low
293         // therefore low <= a[i] <= high
294         // so 0 <= a[i]-low <= high - low
295         // so we can encode a[i]-low using nu_bits(high - low) bits
296         if (high > low) // otherwise, there will be nothing to be printed
297             write_bits(a[i] - low, nu_bits(high-low));
298         return;
299     }
300     // find the intermediate value
301     int m = (i+j)/ 2;
302     unsigned int L = low + m - i; // lower bound on a[m]
303     unsigned int H = high - (j - m); // upper bound on a[m]
304     // so L <= a[m] <= H
305     // and we can encode a[m] - L using nu_bits(H-L) bits
```

```

306  if (H > L) // otherwise, a[m] is clearly H = L and nothing need to be written
307      write_bits(a[m] - L, nu_bits(H-L));
308
309  // then, we should recursively encode intervals [i,m-1] and [m+1, j]
310  bin_inter_code(a, i, m-1, low, a[m]-1);
311  bin_inter_code(a, m+1, j, a[m]+1, high);
312 }

```

6.18.3.3 chunks()

```
unsigned int obitstream::chunks ( ) [inline]
```

returns the number of chunks (each is BIT_INT = 32 bits) to the output.

```

107      {
108  return chunks_written;
109  }

```

6.18.3.4 close()

```
void obitstream::close ( )
```

closes the session by writing the remaining chunk to the output (if any) and closing the file pointer f

```

315      {
316  if (buffer.bits.size() > 0){
317      fwrite(&buffer.bits[0], sizeof(unsigned int), buffer.bits.size(),
318      f);
319      buffer.bits.clear();
319      buffer.last_bits = 0;
320  }
321  fclose(f);
322 }

```

6.18.3.5 operator<<() [1/2]

```
obitstream & obitstream::operator<< (
    const unsigned int & n )
```

uses Elias delta code to write a nonnegative integer to the output. In order to make sure that $n \geq 1$, we effectively encode $n + 1$ instead

```

222      {
223  if (buffer.bits.size() > 1){
224      cerr << " ERROR: buffer has more than 1 chunk! " << endl;
225  }
226  unsigned int buffer_backup = 0; // the backup of the remaining chunk in
227  int buffer_res = 0;
228  if (buffer.bits.size() != 0){
229      buffer_backup = buffer.bits[0];
230      buffer_res = buffer.last_bits;
231  }
232  elias_delta_encode(n+1, buffer); // find the delta encoded version of n + 1
233  buffer.shift_right(buffer_res); // open up space for the residual of the previous
    operation
234  buffer.bits[0] |= buffer_backup; // add the residual
235  write();
236  return *this;
237 }

```

6.18.3.6 operator<<() [2/2]

```
obitstream & obitstream::operator<< (
    const mpz_class & n )
```

uses Elias delta code to write a nonnegative mpz_class integer to the output. In order to make sure that $n \geq 1$, we effectively encode $n + 1$ instead

```
239                                     {
240     if (buffer.bits.size() > 1){
241         cerr << " ERROR: buffer has more than 1 chunk! " << endl;
242     }
243     unsigned int buffer_backup = 0; // the backup of the remaining chunk in
244     int buffer_res = 0;
245     if (buffer.bits.size() != 0){
246         buffer_backup = buffer.bits[0];
247         buffer_res = buffer.last_bits;
248     }
249     elias_delta_encode(n+1, buffer); // find the delta encoded version of n + 1
250     buffer.shift_right(buffer_res); // open up space for the residual of the previous
        operation
251     buffer.bits[0] |= buffer_backup; // add the residual
252     write();
253     return *this;
254 }
```

6.18.3.7 write()

```
void obitstream::write ( ) [private]
```

writes complete chunks to the output

```
191                                     {
192     if (buffer.bits.size() > 1){
193         // write the first chunks to the output
194         fwrite(&buffer.bits[0], sizeof(unsigned int), buffer.bits.size()-1,
        f);
195         // add the number of chunks written to chunks_written
196         chunks_written += buffer.bits.size() -1;
197         // then, remove the first buffer.bits.size()-1 chunks which were written to the output
198         buffer.bits.erase(buffer.bits.begin(), buffer.bits.begin() +
        buffer.bits.size()-1);
199     }
200 }
```

6.18.3.8 write_bits()

```
void obitstream::write_bits (
    unsigned int n,
    unsigned int nu_bits )
```

write the bits given as unsigned int to the output

Parameters

| | |
|----------------------|--|
| <i>n</i> | bits to be written to the output in the form of an unsigned int (4 bytes of data) |
| <i>nu_bits</i> | number of bits, counted from LSB of <i>n</i> , to write to the output. For instance if $n = 1$ and $nu_bits = 1$, a single bit with value 1 is written |
| Generated by Doxygen | |

```

206                                     {
207     unsigned int buffer_backup = 0; // the backup of the remaining chunk in
208     int buffer_res = 0; // number of bits remaining in the buffer
209     if (buffer.bits.size() != 0){
210         buffer_backup = buffer.bits[0];
211         buffer_res = buffer.last_bits;
212     }
213     buffer.bits.resize(1);
214     buffer.bits[0] = n << (BIT_INT - nu_bits); // shift left so that exactly nu_bits
        many bits are in the buffer
215     buffer.last_bits = nu_bits;
216     buffer.shift_right(buffer_res); // open up space for the residual of the previous
        operation
217     buffer.bits[0] |= buffer_backup; // add the residual
218     write(); // write the buffer to the output
219 }

```

6.18.4 Member Data Documentation

6.18.4.1 buffer

`bit_pipe` obitstream::buffer [private]

a `bit_pipe` carrying the buffered data

6.18.4.2 chunks_written

`unsigned int` obitstream::chunks_written [private]

the number of chunks written to the output so far

6.18.4.3 f

`FILE*` obitstream::f [private]

pointer to the binary output file

The documentation for this class was generated from the following files:

- [bitstream.h](#)
- [bitstream.cpp](#)

6.19 reverse_fenwick_tree Class Reference

similar to the [fenwick_tree](#) class, but instead of prefix sums, this class computes suffix sums.

```
#include <fenwick.h>
```

Public Member Functions

- [reverse_fenwick_tree](#) ()
default constructor
- [reverse_fenwick_tree](#) (vector< int >)
constructor which receives values and initializes
- void [add](#) (int k, int val)
- int [size](#) ()
the number of elements in the original array
- int [sum](#) (int k)

Private Attributes

- [fenwick_tree](#) FT
member of type [fenwick_tree](#), which saves the partial sums for the reversed array.

6.19.1 Detailed Description

similar to the [fenwick_tree](#) class, but instead of prefix sums, this class computes suffix sums.

6.19.2 Constructor & Destructor Documentation

6.19.2.1 reverse_fenwick_tree() [1/2]

```
reverse_fenwick_tree::reverse_fenwick_tree ( ) [inline]
```

default constructor

```
58 {}
```

6.19.2.2 reverse_fenwick_tree() [2/2]

```
reverse_fenwick_tree::reverse_fenwick_tree (
    vector< int > vals )
```

constructor which receives values and initializes

```
47 {
48     reverse(vals.begin(),vals.end()); // reverse the array and then use the previously defined fenwick_tree
    class
49     FT = fenwick_tree(vals);
50 }
```

6.19.3 Member Function Documentation

6.19.3.1 add()

```
void reverse_fenwick_tree::add (
    int k,
    int val )
```

gets a (zero based) index k, and add to that value

Parameters

| | |
|------------|--|
| <i>k</i> | the index to be modified, this is zero based |
| <i>val</i> | the value to be added to the above index |

```

53 {
54     FT.add(FT.size() - 1 - k, val);
55 }

```

6.19.3.2 size()

```
int reverse_fenwick_tree::size ( ) [inline]
```

the number of elements in the original array

```

70     {
71         return FT.size();
72     }

```

6.19.3.3 sum()

```
int reverse_fenwick_tree::sum (
    int k )
```

returns the sum of values from index k until the end of the array

Parameters

| | |
|----------|--|
| <i>k</i> | the index from which (including) the sum is computed |
|----------|--|

```

59 {
60     if (k >= size())
61         return 0;
62     return FT.sum(FT.size() - 1 - k);
63 }

```

6.19.4 Member Data Documentation**6.19.4.1 FT**

```
fenwick_tree reverse_fenwick_tree::FT [private]
```

member of type [fenwick_tree](#), which saves the partial sums for the reversed array.

The documentation for this class was generated from the following files:

- [fenwick.h](#)
- [fenwick.cpp](#)

6.20 time_series_decoder Class Reference

decodes a time series which is basically an array of arbitrary nonnegative integers

```
#include <time_series_compression.h>
```

Public Member Functions

- [time_series_decoder](#) (int n_)
constructor
- `vector< int >` [decode](#) (pair< vector< int >, mpz_class >)
inputs an object of type pair<vector<int>, mpz_class> generated by [time_series_encoder](#) and returns the decoded array.

Private Attributes

- int n
the length
- int [alph_size](#)
the number of distinct integers showing up in the sequence after decoding. Therefore, the sequence would consists of integers in the range [0.alph_size-1].
- `vector< int >` [freq](#)
the frequency of symbols after decoding, so has size alph_size
- [b_graph](#) G
the decoded bipartite graph as in [time_series_encoder](#)

6.20.1 Detailed Description

decodes a time series which is basically an array of arbitrary nonnegative integers

This class is capable of decompressing arrays of nonnegative integers with size n. Upon construction, n must be given. But later, the object is capable of decompressing any sequence with this size, universally. The input would be the output of [time_series_decoder](#) class.

Usage Example

```
vector<int> a = {0,2,3,1,2,1,0,1,0,2,1,0,0,2,1,3,4,5,0};
int n = a.size();
time_series_encoder E(n);
pair<vector<int>, mpz_class > ans = E.encode(a);

time_series_decoder D(n);
vector<int> ahat = D.decode(ans);
if (ahat == a)
    cout << " successfully decoded the original time series! " << endl;
```

6.20.2 Constructor & Destructor Documentation

6.20.2.1 time_series_decoder()

```
time_series_decoder::time_series_decoder (
    int n_ ) [inline]
```

constructor

```
90 : n(n_) {}
```

6.20.3 Member Function Documentation

6.20.3.1 decode()

```
vector< int > time_series_decoder::decode (
    pair< vector< int >, mpz_class > E )
```

inputs an object of type `pair<vector<int>, mpz_class>` generated by `time_series_encoder` and returns the decoded array.

```
77 {
78     freq = E.first;
79     mpz_class f = E.second;
80     vector<int> left_deg(n,1); // the left degree sequence
81     b_graph_decoder D(left_deg, freq); // the bipartite graph decoder to convert f to G
82     G = D.decode(f);
83
84     // reconstructing the original sequence given G
85     vector<int> x(n);
86     vector<int> adj_list;
87     for (int i=0;i<n;i++){
88         adj_list = G.get_adj_list(i);
89         x[i] = adj_list[0];
90     }
91     return x;
92 }
```

6.20.4 Member Data Documentation

6.20.4.1 alph_size

```
int time_series_decoder::alph_size [private]
```

the number of distinct integers showing up in the sequence after decoding. Therefore, the sequence would consists of integers in the range `[0,alph_size-1]`.

6.20.4.2 freq

```
vector<int> time_series_decoder::freq [private]
```

the frequency of symbols after decoding, so has size alph_size

6.20.4.3 G

```
b_graph time_series_decoder::G [private]
```

the decoded bipartite graph as in [time_series_encoder](#)

6.20.4.4 n

```
int time_series_decoder::n [private]
```

the length

The documentation for this class was generated from the following files:

- [time_series_compression.h](#)
- [time_series_compression.cpp](#)

6.21 time_series_encoder Class Reference

encodes a time series which is basically an array of arbitrary nonnegative integers

```
#include <time_series_compression.h>
```

Public Member Functions

- [time_series_encoder](#) (int n_)
constructor
- pair< vector< int >, mpz_class > [encode](#) (const vector< int > &x)
Encodes a vector<int> with size n.

Private Member Functions

- void [init_alph_size](#) (const vector< int > &x)
initializes the alphabet size, i.e. the variable init_alph_size
- void [init_freq](#) (const vector< int > &x)
initializes the freq vector
- void [init_G](#) (const vector< int > &x)
initializes the auxiliary bipartite graph G

Private Attributes

- `int n`
length of the series is assumed to be known
- `int alph_size`
the number of distinct integers showing up in the sequence. Therefore, the sequence would consists of integers in the range $[0, \text{alph_size}-1]$.
- `vector< int > freq`
the frequency of symbols, so has size `alph_size`
- `b_graph G`
the bipartite graph version of the sequence, which has `n` left vertices and `alph_size` right sequence. Left vertex `v` is connected to right vertex `w` if the value of the time series in coordinate `v` is `w`. This way, each vertex on the left has degree 1, and the degree of a right vertex `w` is the frequency of `w`.

6.21.1 Detailed Description

encodes a time series which is basically an array of arbitrary nonnegative integers

This class is capable of compressing arrays of nonnegative integers with size `n`. Upon construction, `n` must be given. But later, the object is capable of compressing any sequence with this size, universally. The output of the compression is an object of type `pair<vector<int>, mpz_class>`.

Usage Example

```
vector<int> a = {0,2,3,1,2,1,0,1,0,2,1,0,0,2,1,3,4,5,0};
int n = a.size();
time_series_encoder E(n);
pair<vector<int>, mpz_class > ans = E.encode(a);
```

See [time_series_decoder](#) for decoding.

6.21.2 Constructor & Destructor Documentation

6.21.2.1 time_series_encoder()

```
time_series_encoder::time_series_encoder (
    int n_ ) [inline]
```

constructor

```
44 : n(n_) {}
```

6.21.3 Member Function Documentation

6.21.3.1 encode()

```
pair< vector< int >, mpz_class > time_series_encoder::encode (
    const vector< int > & x )
```

Encodes a `vector<int>` with size `n`.

Parameters

| | |
|---|--|
| x | const reference to the array to be compressed. |
|---|--|

Returns

an object of type `pair<vector<int>, mpz_class>`. The first part is the corresponding frequency array (`freq` member), and the second is the compressed form of the bipartite graph `G`

```

35 {
36     //check whether x is a compatible sequence
37     if (x.size() != n)
38         cerr << " WARNING: time_series_encoder::encode, called for a vector with size different from n,
39             x.size() = " << x.size() << endl;
40     // initialize alph_size, freq and G
41     //logger::item_start("time series init alph size");
42     init_alph_size(x);
43     //logger::item_stop("time series init alph size");
44     //logger::item_start("time series init freq");
45     init_freq(x);
46     //logger::item_stop("time series init freq");
47
48     //logger::item_start("time series init G");
49     init_G(x);
50     //logger::item_stop("time series init G");
51
52     // initializing a b_graph_encoder
53     vector<int> left_deg(n, 1); // the left degree sequence
54     b_graph_encoder E(left_deg, freq); // the right degree sequence is freq
55     //logger::item_start("time series encode");
56     mpz_class f = E.encode(G);
57     //logger::item_stop("time series encode");
58     pair<vector<int>, mpz_class> ans;
59     ans.first = freq;
60     ans.second = f;
61     return ans;
62 }
```

6.21.3.2 init_alph_size()

```

void time_series_encoder::init_alph_size (
    const vector< int > & x ) [private]
```

initializes the alphabet size, i.e. the variable `init_alph_size`

```

4 {
5     alph_size = 0;
6     for (int i=0; i<x.size(); i++){
7         if (x[i] > alph_size)
8             alph_size = x[i];
9         if (x[i] < 0)
10             cerr << " WARNING: time_series_encoder::encode called for a vector with negative entries " << endl;
11     }
12
13     alph_size ++; // the array is zero based
14 }
```

6.21.3.3 init_freq()

```
void time_series_encoder::init_freq (
    const vector< int > & x ) [private]
```

initializes the freq vector

```
17 {
18     freq.clear();
19     freq.resize(alph_size); //assuming that alph_size is already set
20     for (int i=0;i<x.size();i++)
21         freq[x[i]] ++;
22 }
```

6.21.3.4 init_G()

```
void time_series_encoder::init_G (
    const vector< int > & x ) [private]
```

initializes the auxiliary bipartite graph G

```
25 {
26     //initializing the adjacency list
27     vector<vector<int> > list;
28     list.resize(n);
29     for (int i=0;i<x.size();i++)
30         list[i] = vector<int>({x[i]}); // list[i] has a single member, which is x[i]. In other words, the left
31         // vertex i has only one right neighbor, which is precisely x[i]
32     G = b_graph(list, freq); // construct G based on its adjacency list, and the right degree
33     // sequence which is freq
34 }
```

6.21.4 Member Data Documentation

6.21.4.1 alph_size

```
int time_series_encoder::alph_size [private]
```

the number of distinct integers showing up in the sequence. Therefore, the sequence would consists of integers in the range [0,alph_size-1].

6.21.4.2 freq

```
vector<int> time_series_encoder::freq [private]
```

the frequency of symbols, so has size alph_size

6.21.4.3 G

```
b_graph time_series_encoder::G [private]
```

the bipartite graph version of the sequence, which has n left vertices and alph_size right sequence. Left vertex v is connected to right vertex w if the value of the time series in coordinate v is w . This way, each vertex on the left has degree 1, and the degree of a right vertex w is the frequency of w .

6.21.4.4 n

```
int time_series_encoder::n [private]
```

length of the series is assumed to be known

The documentation for this class was generated from the following files:

- [time_series_compression.h](#)
- [time_series_compression.cpp](#)

6.22 vint_hash Struct Reference

```
#include <graph_message.h>
```

Public Member Functions

- [size_t operator\(\)](#) (vector< int > const &v) const

6.22.1 Member Function Documentation

6.22.1.1 operator>()

```
size_t vint_hash::operator() (
    vector< int > const & v ) const

3
4     return boost::hash_range(v.begin(), v.end());
5 }
```

The documentation for this struct was generated from the following files:

- [graph_message.h](#)
- [graph_message.cpp](#)

Chapter 7

File Documentation

7.1 bipartite_graph.cpp File Reference

```
#include "bipartite_graph.h"
```

Functions

- ostream & [operator<<](#) (ostream &o, const [b_graph](#) &G)
- bool [operator==](#) (const [b_graph](#) &G1, const [b_graph](#) &G2)
- bool [operator!=](#) (const [b_graph](#) &G1, const [b_graph](#) &G2)

7.1.1 Function Documentation

7.1.1.1 [operator!=\(\)](#)

```
bool operator!= (
    const b\_graph & G1,
    const b\_graph & G2 )
```

```
131 {
132     return !(G1 == G2);
133 }
```

7.1.1.2 operator<<()

```
ostream& operator<< (
    ostream & o,
    const b_graph & G )

95 {
96     int n = G.nu_left_vertices();
97     vector<int> list;
98     for (int i=0; i<n; i++){
99         list = G.get_adj_list(i);
100         o << i << " -> ";
101         for (int j=0; j<list.size(); j++){
102             o << list[j];
103             if (j < list.size()-1)
104                 o << ", ";
105         }
106         o << endl;
107     }
108     return o;
109 }
```

7.1.1.3 operator==()

```
bool operator== (
    const b_graph & G1,
    const b_graph & G2 )

112 {
113     int n1 = G1.nu_left_vertices();
114     int n2 = G2.nu_left_vertices();
115
116     int np1 = G1.nu_right_vertices();
117     int np2 = G2.nu_right_vertices();
118     if (n1!= n2 or np1 != np2)
119         return false;
120     vector<int> list1, list2;
121     for (int v=0; v<n1; v++){
122         list1 = G1.get_adj_list(v);
123         list2 = G2.get_adj_list(v);
124         if (list1 != list2)
125             return false;
126     }
127     return true;
128 }
```

7.2 bipartite_graph.h File Reference

```
#include <iostream>
#include <vector>
```

Classes

- class [b_graph](#)
simple unmarked bipartite graph

7.3 bipartite_graph_compression.cpp File Reference

```
#include "bipartite_graph_compression.h"
```

7.4 bipartite_graph_compression.h File Reference

```
#include <iostream>
#include <vector>
#include "compression_helper.h"
#include "bipartite_graph.h"
#include "fenwick.h"
```

Classes

- class [b_graph_encoder](#)
Encodes a simple unmarked bipartite graph.
- class [b_graph_decoder](#)
Decodes a simple unmarked bipartite graph.

7.5 bitstream.cpp File Reference

```
#include "bitstream.h"
```

Functions

- ostream & [operator<<](#) (ostream &o, const [bit_pipe](#) &B)
- [bit_pipe](#) [operator<<](#) (const [bit_pipe](#) &B, int n)
- [bit_pipe](#) [operator>>](#) (const [bit_pipe](#) &B, int n)
- unsigned int [nu_bits](#) (unsigned int n)
returns number of bits in a positive integer n, e.g. 3 has 3 bits, 12 has 4 bits, and 0 has 0 bits.
- unsigned int [mask_gen](#) (int n)
generates a binary mask with n consecutive ones in LSB
- [bit_pipe](#) [elias_delta_encode](#) (const unsigned int &n)
returns the Elias delta representation of an integer in [bit_pipe](#) format
- void [elias_delta_encode](#) (const unsigned int &n, [bit_pipe](#) &B)
performs Elias delta encode for an integer, and stores the results in the given reference to [bit_pipe](#) objects
- [bit_pipe](#) [elias_delta_encode](#) (const mpz_class &n)
returns the Elias delta representation of an mpz_class in [bit_pipe](#) format
- void [elias_delta_encode](#) (const mpz_class &n, [bit_pipe](#) &B)
performs Elias delta encoding on n, and stores the results in the given reference to [bit_pipe](#) objects

7.5.1 Function Documentation

7.5.1.1 `elias_delta_encode()` [1/4]

```
bit_pipe elias_delta_encode (
    const unsigned int & n )
```

returns the Elias delta representation of an integer in `bit_pipe` format

```
631                                     {
632     if (n == 0){
633         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
634     }
635     // first, find number of bits in n
636     int n_bits = nu_bits(n); // or equivalently \f$\lfloor \log_2 n \rfloor + 1\f$
637     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor \log_2 n \rfloor$
638
639     bit_pipe N(n_bits); // binary representation
640     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
641     bit_pipe n_pipe(n); // binary representation of n
642     n_pipe.shift_left(1); // remove the leading 1
643     n_pipe.append_left(N);
644     return n_pipe;
645 }
```

7.5.1.2 `elias_delta_encode()` [2/4]

```
void elias_delta_encode (
    const unsigned int & n,
    bit_pipe & B )
```

performs Elias delta encode for an integer, and stores the results in the given reference to `bit_pipe` objects

```
647                                     {
648     if (n == 0){
649         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
650     }
651     // first, find number of bits in n
652     int n_bits = nu_bits(n); // or equivalently \f$\lfloor \log_2 n \rfloor + 1\f$
653     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor \log_2 n \rfloor$
654
655     bit_pipe N(n_bits); // binary representation
656     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
657     B = bit_pipe(n); // binary representation of n
658     B.shift_left(1); // remove the leading 1
659     B.append_left(N);
660 }
```

7.5.1.3 `elias_delta_encode()` [3/4]

```
bit_pipe elias_delta_encode (
    const mpz_class & n )
```

returns the Elias delta representation of an `mpz_class` in `bit_pipe` format

```
663                                     {
664     if (n == 0){
665         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
666     }
667     // first, find number of bits in n
668     int n_bits = mpz_sizeinbase(n.get_mpz_t(), 2); // number of bits in n
669     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor
        \log_2 n \rfloor$
670
671     bit_pipe N(n_bits); // binary representation
672     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
673     bit_pipe n_pipe(n); // binary representation of n
674     n_pipe.shift_left(1); // remove the leading 1
675     n_pipe.append_left(N);
676     return n_pipe;
677 }
```

7.5.1.4 `elias_delta_encode()` [4/4]

```
void elias_delta_encode (
    const mpz_class & n,
    bit_pipe & B )
```

performs Elias delta encoding on `n`, and stores the results in the given reference to `bit_pipe` objects

```
679                                     {
680     if (n == 0){
681         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
682     }
683     // first, find number of bits in n
684     int n_bits = mpz_sizeinbase(n.get_mpz_t(), 2); // number of bits in n
685     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor
        \log_2 n \rfloor$
686
687     bit_pipe N(n_bits); // binary representation
688     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
689     B = bit_pipe(n); // binary representation of n
690     B.shift_left(1); // remove the leading 1
691     B.append_left(N);
692 }
```

7.5.1.5 `mask_gen()`

```
unsigned int mask_gen (
    int n )
```

generates a binary mask with `n` consecutive ones in LSB

Example: `n = 1` -> 00000001, `n = 7` -> 01111111

```
618                                     {
619     if (n < 1 or n > BIT_INT){
620         cerr << " ERROR: mask_gen called for n outside the range [1,BIT_INT] " << endl;
621         return 0;
622     }
623     unsigned int mask = 1;
624     for (int i=1; i<n; i++){
625         mask <= 1;
626         mask += 1;
627     }
628     return mask;
629 }
```

7.5.1.6 nu_bits()

```
unsigned int nu_bits (
    unsigned int n )
```

returns number of bits in a positive integer n, e.g. 3 has 3 bits, 12 has 4 bits, and 0 has 0 bits.

This is in fact nothing but $\lfloor \log_2 n \rfloor + 1$

```
604                                     {
605     int nu_bits = 0;
606     unsigned int n_copy = n;
607     while (n_copy > 0){
608         nu_bits++;
609         n_copy >>= 1;
610     }
611     return nu_bits;
612 }
```

7.5.1.7 operator<<() [1/2]

```
ostream& operator<< (
    ostream & o,
    const bit_pipe & B )

{
110
111     if (B.bits.size()==0){
112         o << "<>";
113         return o;
114     }
115     o << "<";
116     for (int i=0;i<(B.bits.size()-1); i++){ // the last byte requires special handling
117         bitset<BIT_INT> b(B.bits[i]);
118         o << b << " ";
119     }
120     unsigned int last_byte = B.bits[B.bits.size()-1];
121
122     for (int k=BIT_INT;k>(BIT_INT-B.last_bits);k--){ // starting from MSB bit to LSB
        for existing bits
123         if (last_byte & (1<<(k-1)))
124             o << "1";
125         else
126             o << "0";
127     }
128     o << "|"; // to show the place of the last bit
129     for (int k=BIT_INT-B.last_bits; k>=1; k--){
130         if (last_byte & (1<<(k-1)))
131             o << "1";
132         else
133             o << "0";
134     }
135     o << ">";
136     return o;
137 }
```

7.5.1.8 operator<<() [2/2]

```
bit_pipe operator<< (
    const bit_pipe & B,
    int n )

{
163
164     bit_pipe ans = B;
165     ans.shift_left(n);
166     return ans;
167 }
```

7.5.1.9 operator>>()

```

bit_pipe operator>> (
    const bit_pipe & B,
    int n )

169                                     {
170     bit_pipe ans = B;
171     ans.shift_right(n);
172     return ans;
173 }

```

7.6 bitstream.h File Reference

```

#include <iostream>
#include <gmpxx.h>
#include <vector>

```

Classes

- class `bit_pipe`
A sequence of arbitrary number of bits.
- class `obitstream`
handles writing bitstreams to binary files
- class `ibitstream`
deals with reading bit streams from binary files, this is the reverse of obitstream

Functions

- unsigned int `nu_bits` (unsigned int n)
returns number of bits in a positive integer n, e.g. 3 has 3 bits, 12 has 4 bits, and 0 has 0 bits.
- unsigned int `mask_gen` (int n)
generates a binary mask with n consecutive ones in LSB
- `bit_pipe` `elias_delta_encode` (const unsigned int &n)
returns the Elias delta representation of an integer in `bit_pipe` format
- void `elias_delta_encode` (const unsigned int &n, `bit_pipe` &B)
performs Elias delta encode for an integer, and stores the results in the given reference to `bit_pipe` objects
- `bit_pipe` `elias_delta_encode` (const mpz_class &n)
returns the Elias delta representation of an mpz_class in `bit_pipe` format
- void `elias_delta_encode` (const mpz_class &n, `bit_pipe` &B)
performs Elias delta encoding on n, and stores the results in the given reference to `bit_pipe` objects

Variables

- const unsigned int `BYTE_INT` = sizeof(unsigned int)
- const unsigned int `BIT_INT` = 8 * sizeof(unsigned int)

7.6.1 Function Documentation

7.6.1.1 `elias_delta_encode()` [1/4]

```
bit_pipe elias_delta_encode (
    const unsigned int & n )
```

returns the Elias delta representation of an integer in `bit_pipe` format

```
631                                     {
632     if (n == 0){
633         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
634     }
635     // first, find number of bits in n
636     int n_bits = nu_bits(n); // or equivalently \f$\lfloor \log_2 n \rfloor + 1\f$
637     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor\f$ where \f$N = \lfloor \log_2 n \rfloor\f$
638
639     bit_pipe N(n_bits); // binary representation
640     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
641     bit_pipe n_pipe(n); // binary representation of n
642     n_pipe.shift_left(1); // remove the leading 1
643     n_pipe.append_left(N);
644     return n_pipe;
645 }
```

7.6.1.2 `elias_delta_encode()` [2/4]

```
void elias_delta_encode (
    const unsigned int & n,
    bit_pipe & B )
```

performs Elias delta encode for an integer, and stores the results in the given reference to `bit_pipe` objects

```
647                                     {
648     if (n == 0){
649         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
650     }
651     // first, find number of bits in n
652     int n_bits = nu_bits(n); // or equivalently \f$\lfloor \log_2 n \rfloor + 1\f$
653     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor\f$ where \f$N = \lfloor \log_2 n \rfloor\f$
654
655     bit_pipe N(n_bits); // binary representation
656     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
657     B = bit_pipe(n); // binary representation of n
658     B.shift_left(1); // remove the leading 1
659     B.append_left(N);
660 }
```

7.6.1.3 `elias_delta_encode()` [3/4]

```
bit_pipe elias_delta_encode (
    const mpz_class & n )
```

returns the Elias delta representation of an `mpz_class` in `bit_pipe` format

```
663                                     {
664     if (n == 0){
665         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
666     }
667     // first, find number of bits in n
668     int n_bits = mpz_sizeinbase(n.get_mpz_t(), 2); // number of bits in n
669     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor
        \log_2 n \rfloor$
670
671     bit_pipe N(n_bits); // binary representation
672     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
673     bit_pipe n_pipe(n); // binary representation of n
674     n_pipe.shift_left(1); // remove the leading 1
675     n_pipe.append_left(N);
676     return n_pipe;
677 }
```

7.6.1.4 `elias_delta_encode()` [4/4]

```
void elias_delta_encode (
    const mpz_class & n,
    bit_pipe & B )
```

performs Elias delta encoding on `n`, and stores the results in the given reference to `bit_pipe` objects

```
679                                     {
680     if (n == 0){
681         cerr << " ERROR: elias delta called for 0, input must be a positive integer" << endl;
682     }
683     // first, find number of bits in n
684     int n_bits = mpz_sizeinbase(n.get_mpz_t(), 2); // number of bits in n
685     int L = nu_bits(n_bits) - 1; // this is \f$\lfloor \log_2 (N+1) \rfloor$ where \f$N = \lfloor
        \log_2 n \rfloor$
686
687     bit_pipe N(n_bits); // binary representation
688     N.shift_right(L); // it is as if I write L zeros followed by binary representation of N
689     B = bit_pipe(n); // binary representation of n
690     B.shift_left(1); // remove the leading 1
691     B.append_left(N);
692 }
```

7.6.1.5 `mask_gen()`

```
unsigned int mask_gen (
    int n )
```

generates a binary mask with `n` consecutive ones in LSB

Example: `n = 1` -> 00000001, `n = 7` -> 01111111

```
618                                     {
619     if (n < 1 or n > BIT_INT){
620         cerr << " ERROR: mask_gen called for n outside the range [1,BIT_INT] " << endl;
621         return 0;
622     }
623     unsigned int mask = 1;
624     for (int i=1; i<n; i++){
625         mask <= 1;
626         mask += 1;
627     }
628     return mask;
629 }
```

7.6.1.6 nu_bits()

```
unsigned int nu_bits (
    unsigned int n )
```

returns number of bits in a positive integer n , e.g. 3 has 3 bits, 12 has 4 bits, and 0 has 0 bits.

This is in fact nothing but $\lfloor \log_2 n \rfloor + 1$

```
604                                     {
605     int nu_bits = 0;
606     unsigned int n_copy = n;
607     while (n_copy > 0){
608         nu_bits ++;
609         n_copy >>= 1;
610     }
611     return nu_bits;
612 }
```

7.6.2 Variable Documentation

7.6.2.1 BIT_INT

```
const unsigned int BIT_INT = 8 * sizeof(unsigned int)
```

7.6.2.2 BYTE_INT

```
const unsigned int BYTE_INT = sizeof(unsigned int)
```

7.7 compression_helper.cpp File Reference

```
#include "compression_helper.h"
```


Functions

- `mpz_class compute_product_old` (int N, int k, int s)
This function computes the product of consecutive integers separated by a given iteration. This is the old version which uses standard recursion.
- `mpz_class compute_product_stack` (int N, int k, int s)
This function computes the product of consecutive integers separated by a given iteration. This is the new version which implements recursion via stack.
- `void compute_product_void` (int N, int k, int s)
- `void compute_array_product` (vector< mpz_class > &a)
computes the product of elements in vector a by inline multiplication of adjacent elements recursively. The results will be in a[0].
- `mpz_class compute_product` (int N, int k, int s)
- `mpz_class binomial` (const int n, const int m)
computes the binomial coefficient n choose $m = n! / m! (n-m)!$
- `mpz_class prod_factorial_old` (const vector< int > &a, int i, int j)
computes the product of factorials in a vector given a range
- `mpz_class prod_factorial` (const vector< int > &a, int i, int j)
- `int bit_string_write` (FILE *f, const string &s)
Write a string containing 0 and 1 to a binary file, treating the string as a bit sequence. Returns the number of bytes written to the output.
- `string bit_string_read` (FILE *f)
Reads a bit sequence from a binary file, assuming the bit sequence was generated by the `bit_string_write` function.

7.7.1 Function Documentation

7.7.1.1 binomial()

```
mpz_class binomial (
    const int n,
    const int m )
```

computes the binomial coefficient n choose $m = n! / m! (n-m)!$

Parameters

| | |
|-----|---------|
| n | integer |
| m | integer |

Returns

the binomial coefficient $n! / m! (n-m)!$. If $n \leq 0$, or $m > n$, or $m \leq 0$, returns 0

```
319 {
320     if (n <= 0 or m > n or m <= 0)
321         return 0;
322     return compute_product(n, m, 1) / compute_product(m, m, 1);
323 }
```

7.7.1.2 bit_string_read()

```
string bit_string_read (
    FILE * f )
```

Reads a bit sequence from a binary file, assuming the bit sequence was generated by the `bit_string_write` function.

Parameters

| | |
|----------|----------------|
| <i>f</i> | a file pointer |
|----------|----------------|

Returns

a string of zeros and ones.

```
375                                     {
376     int nu_bytes;
377     int ssize;
378     // read the number of bytes to read
379     fread(&ssize, sizeof(ssize), 1, f);
380     //cerr << " ssize " << ssize << endl;
381     nu_bytes = ssize / 8;
382     if (ssize % 8 != 0)
383         nu_bytes ++;
384
385     int last_byte_size = ssize % 8;
386     if (last_byte_size == 0)
387         last_byte_size = 8;
388
389     unsigned char c;
390     bitset<8> B;
391     string s;
392     for (int i=0;i<nu_bytes;i++){
393         fread(&c, sizeof(c), 1, f);
394         B = c;
395         //cout << B << endl;
396         if (i < nu_bytes -1){
397             s += B.to_string();
398         }else{
399             s += B.to_string().substr(8-last_byte_size, last_byte_size);
400         }
401     }
402     return s;
403 }
```

7.7.1.3 bit_string_write()

```
int bit_string_write (
    FILE * f,
    const string & s )
```

Write a string containing 0 and 1 to a binary file, treating the string as a bit sequence. Returns the number of bytes written to the output.

First, the size of the bit sequence is written to the output, then the input is split into 8 bit chunks, perhaps with some leftover, which are written to the output file as bytes.

Parameters

| | |
|----------|--|
| <i>f</i> | a file pointer |
| <i>s</i> | a string where each character is either 0 or 1 |

Returns

the number of bytes written to the output

```

350                                     {
351     // find out the number of bytes
352     int ssize = s.size();
353     int nu_bytes; // number of bytes wrote to the output
354
355     //if (ssize % 8 != 0) // an incomplete byte is required
356     //nu_bytes++;
357
358     fwrite(&ssize, sizeof(ssize), 1, f); // first, write down how many bytes are coming.
359     nu_bytes += sizeof(ssize);
360
361     stringstream ss;
362     ss << s;
363
364     bitset<8> B;
365     unsigned char c;
366     while (ss >> B){
367         c = B.to_ulong();
368         fwrite(&c, sizeof(c), 1, f);
369         nu_bytes += sizeof(c);
370     }
371     return nu_bytes;
372 }
```

7.7.1.4 compute_array_product()

```

void compute_array_product (
    vector< mpz_class > & a )
```

computes the product of elements in vector a by inline multiplication of adjacent elements recursively. The results will be in a[0].

```

237                                     {
238     //logger::item_start("Compute Array Product");
239     int step_size, to_mul;
240     int k = a.size();
241     for (step_size = 2, to_mul = 1; to_mul < k; step_size <=1, to_mul <=1){
242         for (int i=0; i<k; i+=step_size){
243             if (i+to_mul < k)
244                 a[i] *= a[i+to_mul];
245         }
246     }
247     //logger::item_stop("Compute Array Product");
248 }
```

7.7.1.5 compute_product()

```

mpz_class compute_product (
    int N,
    int k,
    int s )
```

```

251                                     {
252     if (k==1)
253         return N;
254     if (k == 0) // TO CHECK because there are no terms to compute product
255         return 1;
256
257     if (k < 0){
258         cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
259         << endl;
260     }
261     if (N - (k-1) * s <= 0){ // the terms go negative
262         //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
263         return 0;
264     }
265
266     if (k == 2){
267         helper_vars::mul_1 = N;
268         helper_vars::mul_2 = N - s;
269         return helper_vars::mul_1 * helper_vars::mul_2;
270     }
271
272     helper_vars::mpz_vec.resize(k);
273     for (int i=0; i<k; i++){
274         helper_vars::mpz_vec[i] = N - i * s;
275     }
276     compute_array_product(helper_vars::mpz_vec);
277
278     // int step_size, to_mul;
279
280
281     // for (step_size = 2, to_mul = 1; to_mul < k; step_size <=1, to_mul <=1){
282     //     for (int i=0; i<k; i+=step_size){
283     //         if (i+to_mul < k)
284     //             helper_vars::mpz_vec[i] *= helper_vars::mpz_vec[i+to_mul];
285     //     }
286     // }
287     return helper_vars::mpz_vec[0];
288 }

```

7.7.1.6 compute_product_old()

```

mpz_class compute_product_old (
    int N,
    int k,
    int s )

```

This function computes the product of consecutive integers separated by a given iteration. This is the old version which uses standard recursion.

Parameters

| | |
|-----|------------------------------------|
| N | The first term in the product |
| k | the number of terms in the product |
| s | the iteration |

Returns

the product $N \times (N - s) \times (N - 2s) \times \dots \times (N - (k - 1)s)$

```

9                                     {
10     //cerr << " compute_product  N " << N << " k " << k << " s " << s << endl;
11
12     if (k==1)
13         return N;
14     if (k == 0) // TO CHECK because there are no terms to compute product

```

```

15     return 1;
16
17     if (k < 0){
18         cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
19         << endl;
20         return 1;
21     }
22     if (N - (k-1) * s <= 0){ // the terms go negative
23         //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
24         return 0;
25     }
26     if (k == 2)
27         return mpz_class(N) * mpz_class(N-s);
28     // we do this by dividing the terms into two parts
29     int m = k / 2; // the middle point
30     mpz_class left, right; // each of the half products
31     left = compute_product(N, m, s);
32     right = compute_product(N-m * s, k-m, s);
33     //logger::item_start("cp_mul");
34     mpz_class ans = left*right;
35     //logger::item_stop("cp_mul");
36     return ans;
37 }

```

7.7.1.7 compute_product_stack()

```

mpz_class compute_product_stack (
    int N,
    int k,
    int s )

```

This function computes the product of consecutive integers separated by a given iteration. This is the new version which implements recursion via stack.

Parameters

| | |
|-----|------------------------------------|
| N | The first term in the product |
| k | the number of terms in the product |
| s | the iteration |

Returns

the product $N \times (N - s) \times (N - 2s) \times \dots \times (N - (k - 1)s)$

```

39     {
40
41     if (k==1)
42         return N;
43     if (k == 0) // TO CHECK because there are no terms to compute product
44         return 1;
45
46     if (k < 0){
47         cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
48         << endl;
49         return 1;
50     }
51     if (N - (k-1) * s <= 0){ // the terms go negative
52         //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
53         return 0;
54     }
55     if (k == 2){
56         helper_vars::mul_1 = N;
57         helper_vars::mul_2 = N - s;
58         return helper_vars::mul_1 * helper_vars::mul_2;

```

```

59 }
60
61 logger::item_start("CP body");
62
63 int k_bits = 0; // roughly , the number of bits in k, the depth of the stack during run time
64 int k_copy = k;
65 while (k_copy > 0){
66     k_bits ++;
67     k_copy >>= 1;
68 }
69 k_bits += 2;
70 vector<pair<int, int> > call_stack(2 * k_bits);
71 //cout << " 2 * k_bits " << 2 * k_bits << endl;
72 int call_pointer = 0; // size of the call pointer, so the top index is call_pointer - 1
73 vector<int> status_stack(2 * k_bits); // 0: first meet, 1: to return
74 //vector<mpz_class> return_stack(2 * k_bits);
75 helper_vars::return_stack.resize(2*k_bits);
76 int return_pointer = 0;
77
78 call_stack[call_pointer] = pair<int, int> (N, k);
79 status_stack[call_pointer] = 0;
80 call_pointer ++;
81
82 int m;
83 int N_now, k_now; // N and k for the current stack element
84
85 while (call_pointer > 0){
86     N_now = call_stack[call_pointer-1].first;
87     k_now = call_stack[call_pointer-1].second;
88     //cout << "call_pointer = " << call_pointer << " N = " << N_now << " k = " << k_now << " stat = " <<
89     status_stack[call_pointer-1] << endl;
90     //cout << " the whole stack " << endl;
91     //for (int i=0;i<call_pointer; i++){
92     //    cout << call_stack[i].first << " , " << call_stack[i].second << " " << status_stack[i] << endl;
93     //}
94     if (status_stack[call_pointer-1] == 1){ // we should multiply two top elements in the return stack
95         // to collect two top elements in return stack and multiply them
96         logger::item_start("CP arithmetic");
97         helper_vars::return_stack[return_pointer-2] =
98         helper_vars::return_stack[return_pointer-2] *
99         helper_vars::return_stack[return_pointer-1];
100         logger::item_stop("CP arithmetic");
101         return_pointer--; // remove two items, add one item
102         call_pointer --;
103     }else{
104         //cout << " else " << endl;
105         if(k_now == 1){
106             // to return the corresponding N
107             helper_vars::return_stack[return_pointer++] = call_stack[call_pointer-1].
108             first;
109             call_pointer --; // pop this element
110         }
111         if (k_now == 2){
112             helper_vars::mul_1 = N_now;
113             helper_vars::mul_2 = N_now - s;
114             logger::item_start("CP arithmetic");
115             helper_vars::return_stack[return_pointer++] =
116             helper_vars::mul_1 * helper_vars::mul_2;
117             logger::item_stop("CP arithmetic");
118             call_pointer --;
119         }
120         if (k_now > 2){
121             m = k_now / 2;
122             status_stack[call_pointer-1] = 1; // when return to this state, we know that we should aggregate
123             call_stack[call_pointer] = pair<int, int>(N_now, m);
124             status_stack[call_pointer] = 0; // just added
125             call_stack[call_pointer+1] = pair<int, int>(N_now - m*s, k_now - m );
126             status_stack[call_pointer+1] = 0;
127             call_pointer += 2;
128         }
129     }
130 }
131 // make sure there is exactly one element in return stack
132 if (return_pointer != 1){
133     cerr << " return pointer is not zero";
134 }
135 logger::item_stop("CP body");
136 return helper_vars::return_stack[0]; // the top element remaining in the return
137 stack
138 }

```

7.7.1.8 compute_product_void()

```

void compute_product_void (
    int N,
    int k,
    int s )

136
137 //cerr << " void called N " << N << " k " << k << " s " << s << endl;
138 if (k==1){
139     helper_vars::return_stack.resize(1);
140     helper_vars::return_stack[0] = N;//return N;
141     return;
142 }
143 if (k == 0){ // TO CHECK because there are no terms to compute product
144     helper_vars::return_stack.resize(1);
145     helper_vars::return_stack[0] = 1;//return 1;
146     return;
147 }
148
149 if (k < 0){
150     cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
    << endl;
151     helper_vars::return_stack.resize(1);
152     helper_vars::return_stack[0] = 1;//return 1;
153     return;
154 }
155 if (N - (k-1) * s <= 0){ // the terms go negative
156     //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
157     helper_vars::return_stack.resize(1);
158     helper_vars::return_stack[0] = 0; //return 0;
159     return;
160 }
161
162 if (k == 2){
163     helper_vars::mul_1 = N;
164     helper_vars::mul_2 = N - s;
165     helper_vars::return_stack.resize(1);
166     helper_vars::return_stack[0] = helper_vars::mul_1 *
    helper_vars::mul_2;
167     return;
168 }
169
170 int k_bits = 0; // roughly , the number of bits in k, the depth of the stack during run time
171 int k_copy = k;
172 while (k_copy > 0){
173     k_bits ++;
174     k_copy >>= 1;
175 }
176 k_bits += 2;
177 vector<pair<int, int> > call_stack(2 * k_bits);
178 //cout << " 2 * k_bits " << 2 * k_bits << endl;
179 int call_pointer = 0; // size of the call pointer, so the top index is call_pointer - 1
180 vector<int> status_stack(2 * k_bits); // 0: first meet, 1: to return
181 //vector<mpz_class> return_stack(2 * k_bits);
182 helper_vars::return_stack.resize(2*k_bits);
183 int return_pointer = 0;
184
185 call_stack[call_pointer] = pair<int, int> (N, k);
186 status_stack[call_pointer] = 0;
187 call_pointer ++;
188
189 int m;
190 int N_now, k_now; // N and k for the current stack element
191
192 while (call_pointer > 0){
193     N_now = call_stack[call_pointer-1].first;
194     k_now = call_stack[call_pointer-1].second;
195     //cout << "call_pointer = " << call_pointer << " N = " << N_now << " k = " << k_now << " stat = " <<
    status_stack[call_pointer-1] << endl;
196     //cout << " the whole stack " << endl;
197     //for (int i=0;i<call_pointer; i++){
198     //    cout << call_stack[i].first << " , " << call_stack[i].second << " " << status_stack[i] << endl;
199     //}
200     if (status_stack[call_pointer-1] == 1){ // we should multiply two top elements in the return stack
201         // to collect two top elements in return stack and multiply them
202         helper_vars::return_stack[return_pointer-2] =
    helper_vars::return_stack[return_pointer-2] *
    helper_vars::return_stack[return_pointer-1];
203         return_pointer--; // remove two items, add one item
204         call_pointer --;
205     }else{

```

```

206         //cout << " else " << endl;
207         if(k_now == 1){
208             // to return the corresponding N
209             helper_vars::return_stack[return_pointer++] = call_stack[call_pointer-1].
first;
210             call_pointer --; // pop this element
211         }
212         if (k_now == 2){
213             helper_vars::mul_1 = N_now;
214             helper_vars::mul_2 = N_now - s;
215             helper_vars::return_stack[return_pointer++] =
helper_vars::mul_1 * helper_vars::mul_2;
216             call_pointer --;
217         }
218         if (k_now > 2){
219             m = k_now / 2;
220             status_stack[call_pointer-1] = 1; // when return to this state, we know that we should aggregate
221             call_stack[call_pointer] = pair<int, int>(N_now, m);
222             status_stack[call_pointer] = 0; // just added
223             call_stack[call_pointer+1] = pair<int, int>(N_now - m*s, k_now - m );
224             status_stack[call_pointer+1] = 0;
225             call_pointer += 2;
226         }
227     }
228 }
229 // make sure there is exactly one element in return stack
230 if (return_pointer != 1){
231     cerr << " return pointer is not zero";
232 }
233 //return helper_vars::return_stack[0]; // the top element remaining in the return stack
234 }

```

7.7.1.9 prod_factorial()

```

mpz_class prod_factorial (
    const vector< int > & a,
    int i,
    int j )

{
338
339     if (i==j){
340         return compute_product(a[i], a[i], 1);
341     }else{
342         helper_vars::mpz_vec2.resize(j-i+1);
343         for (int k = i; k<=j;k++)
344             helper_vars::mpz_vec2[k- i] = compute_product(a[k], a[k],1);
345         compute_array_product(helper_vars::mpz_vec2);
346         return helper_vars::mpz_vec2[0];
347     }
348 }

```

7.7.1.10 prod_factorial_old()

```

mpz_class prod_factorial_old (
    const vector< int > & a,
    int i,
    int j )

```

computes the product of factorials in a vector given a range

Parameters

| | |
|--------|---------------------------|
| a | vector of integers |
| i, j | endpoints of the interval |

Returns

$$\prod_{v=i}^j a_v!$$

```

327 {
328     if (i == j){
329         return compute_product(a[i], a[i], 1);
330     }else{
331         int k = (i+j)/2;
332         mpz_class x = prod_factorial(a, i, k);
333         mpz_class y = prod_factorial(a, k+1, j);
334         return x * y;
335     }
336 }
```

7.8 compression_helper.h File Reference

```

#include <iostream>
#include <gmpxx.h>
#include <vector>
#include <stdio.h>
#include <bitset>
#include <sstream>
#include "logger.h"
```

Namespaces

- [helper_vars](#)

Functions

- `mpz_class compute_product_old` (int N, int k, int s)
This function computes the product of consecutive integers separated by a given iteration. This is the old version which uses standard recursion.
- `mpz_class compute_product_stack` (int N, int k, int s)
This function computes the product of consecutive integers separated by a given iteration. This is the new version which implements recursion via stack.
- `mpz_class compute_product` (int N, int k, int s)
- `void compute_product_void` (int N, int k, int s)
- `void compute_array_product` (vector< mpz_class > &a)
computes the product of elements in vector a by inline multiplication of adjacent elements recursively. The results will be in a[0].
- `mpz_class binomial` (const int n, const int m)
computes the binomial coefficient n choose m = n! / m! (n-m)!
- `mpz_class prod_factorial_old` (const vector< int > &a, int i, int j)
computes the product of factorials in a vector given a range
- `mpz_class prod_factorial` (const vector< int > &a, int i, int j)
- `int bit_string_write` (FILE *f, const string &s)
Write a string containing 0 and 1 to a binary file, treating the string as a bit sequence. Returns the number of bytes written to the output.
- `string bit_string_read` (FILE *f)
Reads a bit sequence from a binary file, assuming the bit sequence was generated by the bit_string_write function.

Variables

- mpz_class [helper_vars::mul_1](#)
- mpz_class [helper_vars::mul_2](#)
- *helper variables in order to avoid initialization*
- vector< mpz_class > [helper_vars::return_stack](#)
- vector< mpz_class > [helper_vars::mpz_vec](#)
- vector< mpz_class > [helper_vars::mpz_vec2](#)

7.8.1 Function Documentation

7.8.1.1 binomial()

```
mpz_class binomial (
    const int n,
    const int m )
```

computes the binomial coefficient n choose $m = n! / m! (n-m)!$

Parameters

| | |
|----------|---------|
| <i>n</i> | integer |
| <i>m</i> | integer |

Returns

the binomial coefficient $n! / m! (n-m)!$. If $n \leq 0$, or $m > n$, or $m \leq 0$, returns 0

```
319 {
320     if (n <= 0 or m > n or m <= 0)
321         return 0;
322     return compute_product(n, m, 1) / compute_product(m, m, 1);
323 }
```

7.8.1.2 bit_string_read()

```
string bit_string_read (
    FILE * f )
```

Reads a bit sequence from a binary file, assuming the bit sequence was generated by the `bit_string_write` function.

Parameters

| | |
|----------|----------------|
| <i>f</i> | a file pointer |
|----------|----------------|

Returns

a string of zeros and ones.

```

375                                     {
376     int nu_bytes;
377     int ssize;
378     // read the number of bytes to read
379     fread(&ssize, sizeof(ssize), 1, f);
380     //cerr << " ssize " << ssize << endl;
381     nu_bytes = ssize / 8;
382     if (ssize % 8 != 0)
383         nu_bytes ++;
384
385     int last_byte_size = ssize % 8;
386     if (last_byte_size == 0)
387         last_byte_size = 8;
388
389     unsigned char c;
390     bitset<8> B;
391     string s;
392     for (int i=0;i<nu_bytes;i++){
393         fread(&c, sizeof(c), 1, f);
394         B = c;
395         //cout << B << endl;
396         if (i < nu_bytes -1){
397             s += B.to_string();
398         }else{
399             s += B.to_string().substr(8-last_byte_size, last_byte_size);
400         }
401     }
402     return s;
403 }
```

7.8.1.3 bit_string_write()

```

int bit_string_write (
    FILE * f,
    const string & s )
```

Write a string containing 0 and 1 to a binary file, treating the string as a bit sequence. Returns the number of bytes written to the output.

First, the size of the bit sequence is written to the output, then the input is split into 8 bit chunks, perhaps with some leftover, which are written to the output file as bytes.

Parameters

| | |
|----------|--|
| <i>f</i> | a file pointer |
| <i>s</i> | a string where each character is either 0 or 1 |

Returns

the number of bytes written to the output

```

350                                     {
351     // find out the number of bytes
352     int ssize = s.size();
353     int nu_bytes; // number of bytes wrote to the output
354
355     //if (ssize % 8 != 0) // an incomplete byte is required
356     //nu_bytes++;
357
358     fwrite(&ssize, sizeof(ssize), 1, f); // first, write down how many bytes are coming.
```

```

359     nu_bytes += sizeof(ssize);
360
361     stringstream ss;
362     ss << s;
363
364     bitset<8> B;
365     unsigned char c;
366     while (ss >> B){
367         c = B.to_ulong();
368         fwrite(&c, sizeof(c), 1, f);
369         nu_bytes += sizeof(c);
370     }
371     return nu_bytes;
372 }

```

7.8.1.4 compute_array_product()

```

void compute_array_product (
    vector< mpz_class > & a )

```

computes the product of elements in vector a by inline multiplication of adjacent elements recursively. The results will be in a[0].

```

237                                     {
238     //logger::item_start("Compute Array Product");
239     int step_size, to_mul;
240     int k = a.size();
241     for (step_size = 2, to_mul = 1; to_mul < k; step_size <=1, to_mul <=1){
242         for (int i=0; i<k; i+=step_size){
243             if (i+to_mul < k)
244                 a[i] *= a[i+to_mul];
245         }
246     }
247     //logger::item_stop("Compute Array Product");
248 }

```

7.8.1.5 compute_product()

```

mpz_class compute_product (
    int N,
    int k,
    int s )

```

```

251                                     {
252     if (k==1)
253         return N;
254     if (k == 0) // TO CHECK because there are no terms to compute product
255         return 1;
256
257     if (k < 0){
258         cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
259         << endl;
260         return 1;
261     }
262     if (N - (k-1) * s <= 0){ // the terms go negative
263         //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
264         return 0;
265     }
266     if (k == 2){
267         helper_vars::mul_1 = N;
268         helper_vars::mul_2 = N - s;
269         return helper_vars::mul_1 * helper_vars::mul_2;

```

```

270 }
271
272 helper_vars::mpz_vec.resize(k);
273 for (int i=0; i<k; i++){
274     helper_vars::mpz_vec[i] = N - i * s;
275 }
276 compute_array_product(helper_vars::mpz_vec);
277
278 // int step_size, to_mul;
279
280
281 // for (step_size = 2, to_mul = 1; to_mul < k; step_size <=&1, to_mul <=&1){
282 //     for (int i=0; i<k; i+=step_size){
283 //         if (i+to_mul < k)
284 //             helper_vars::mpz_vec[i] *= helper_vars::mpz_vec[i+to_mul];
285 //     }
286 // }
287 return helper_vars::mpz_vec[0];
288 }

```

7.8.1.6 compute_product_old()

```

mpz_class compute_product_old (
    int N,
    int k,
    int s )

```

This function computes the product of consecutive integers separated by a given iteration. This is the old version which uses standard recursion.

Parameters

| | |
|-----|------------------------------------|
| N | The first term in the product |
| k | the number of terms in the product |
| s | the iteration |

Returns

the product $N \times (N - s) \times (N - 2s) \times \dots \times (N - (k - 1)s)$

```

9
10 //cerr << " compute_product  N " << N << " k " << k << " s " << s << endl;
11
12 if (k==1)
13     return N;
14 if (k == 0) // TO CHECK because there are no terms to compute product
15     return 1;
16
17 if (k < 0){
18     cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
19     << endl;
20     return 1;
21 }
22 if (N - (k-1) * s <= 0){ // the terms go negative
23     //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
24     return 0;
25 }
26 if (k == 2)
27     return mpz_class(N) * mpz_class(N-s);
28 // we do this by dividing the terms into two parts
29 int m = k / 2; // the middle point
30 mpz_class left, right; // each of the half products
31 left = compute_product(N, m, s);
32 right = compute_product(N-m * s, k-m, s);
33 //logger::item_start("cp_mul");

```

```

34  mpz_class ans = left*right;
35  //logger::item_stop("cp_mul");
36  return ans;
37 }

```

7.8.1.7 compute_product_stack()

```

mpz_class compute_product_stack (
    int N,
    int k,
    int s )

```

This function computes the product of consecutive integers separated by a given iteration. This is the new version which implements recursion via stack.

Parameters

| | |
|-----|------------------------------------|
| N | The first term in the product |
| k | the number of terms in the product |
| s | the iteration |

Returns

the product $N \times (N - s) \times (N - 2s) \times \dots \times (N - (k - 1)s)$

```

39                                     {
40
41     if (k==1)
42         return N;
43     if (k == 0) // TO CHECK because there are no terms to compute product
44         return 1;
45
46     if (k < 0){
47         cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
48         << endl;
49         return 1;
50     }
51     if (N - (k-1) * s <= 0) { // the terms go negative
52         //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
53         return 0;
54     }
55     if (k == 2){
56         helper_vars::mul_1 = N;
57         helper_vars::mul_2 = N - s;
58         return helper_vars::mul_1 * helper_vars::mul_2;
59     }
60
61     logger::item_start("CP body");
62
63     int k_bits = 0; // roughly , the number of bits in k, the depth of the stack during run time
64     int k_copy = k;
65     while (k_copy > 0){
66         k_bits++;
67         k_copy >>= 1;
68     }
69     k_bits += 2;
70     vector<pair<int, int> > call_stack(2 * k_bits);
71     //cout << " 2 * k_bits " << 2 * k_bits << endl;
72     int call_pointer = 0; // size of the call pointer, so the top index is call_pointer - 1
73     vector<int> status_stack(2 * k_bits); // 0: first meet, 1: to return
74     //vector<mpz_class> return_stack(2 * k_bits);
75     helper_vars::return_stack.resize(2*k_bits);
76     int return_pointer = 0;
77
78     call_stack[call_pointer] = pair<int, int> (N, k);

```

```

79  status_stack[call_pointer] = 0;
80  call_pointer ++;
81
82  int m;
83  int N_now, k_now; // N and k for the current stack element
84
85  while (call_pointer > 0){
86      N_now = call_stack[call_pointer-1].first;
87      k_now = call_stack[call_pointer-1].second;
88      //cout << "call_pointer = " << call_pointer << " N = " << N_now << " k = " << k_now << " stat = " <<
      status_stack[call_pointer-1] << endl;
89      //cout << " the whole stack " << endl;
90      //for (int i=0;i<call_pointer; i++){
91      //  cout << call_stack[i].first << " , " << call_stack[i].second << " " << status_stack[i] << endl;
92      //}
93      if (status_stack[call_pointer-1] == 1){ // we should multiply two top elements in the return stack
94          // to collect two top elements in return stack and multiply them
95          logger::item_start("CP arithmetic");
96          helper_vars::return_stack[return_pointer-2] =
helper_vars::return_stack[return_pointer-2] *
helper_vars::return_stack[return_pointer-1];
97          logger::item_stop("CP arithmetic");
98          return_pointer--; // remove two items, add one item
99          call_pointer --;
100      }else{
101          //cout << " else " << endl;
102          if(k_now == 1){
103              // to return the corresponding N
104              helper_vars::return_stack[return_pointer++] = call_stack[call_pointer-1].
first;
105              call_pointer --; // pop this element
106          }
107          if (k_now == 2){
108              helper_vars::mul_1 = N_now;
109              helper_vars::mul_2 = N_now - s;
110              logger::item_start("CP arithmetic");
111              helper_vars::return_stack[return_pointer++] =
helper_vars::mul_1 * helper_vars::mul_2;
112              logger::item_stop("CP arithmetic");
113              call_pointer --;
114          }
115          if (k_now > 2){
116              m = k_now / 2;
117              status_stack[call_pointer-1] = 1; // when return to this state, we know that we should aggregate
118              call_stack[call_pointer] = pair<int, int>(N_now, m);
119              status_stack[call_pointer] = 0; // just added
120              call_stack[call_pointer+1] = pair<int, int>(N_now - m*s, k_now - m );
121              status_stack[call_pointer+1] = 0;
122              call_pointer += 2;
123          }
124      }
125  }
126  // make sure there is exactly one element in return stack
127  if (return_pointer != 1){
128      cerr << " return pointer is not zero";
129  }
130  logger::item_stop("CP body");
131  return helper_vars::return_stack[0]; // the top element remaining in the return
      stack
132 }

```

7.8.1.8 compute_product_void()

```

void compute_product_void (
    int N,
    int k,
    int s )

{
137  //cerr << " void called N " << N << " k " << k << " s " << s << endl;
138  if (k==1){
139      helper_vars::return_stack.resize(1);
140      helper_vars::return_stack[0] = N; //return N;
141      return;
142  }

```

```

143 if (k == 0){ // TO CHECK because there are no terms to compute product
144     helper_vars::return_stack.resize(1);
145     helper_vars::return_stack[0] = 1; //return 1;
146     return;
147 }
148
149 if (k < 0){
150     cerr << " WARNING: compute_product called for k < 0, returning 1, N " << N << " k " << k << " s " << s
151     << endl;
152     helper_vars::return_stack.resize(1);
153     helper_vars::return_stack[0] = 1; //return 1;
154     return;
155 }
156 if (N - (k-1) * s <= 0){ // the terms go negative
157     //cerr << " WARNING: compute_product called for N - (k-1) * s <= 0 " << endl;
158     helper_vars::return_stack.resize(1);
159     helper_vars::return_stack[0] = 0; //return 0;
160     return;
161 }
162
163 if (k == 2){
164     helper_vars::mul_1 = N;
165     helper_vars::mul_2 = N - s;
166     helper_vars::return_stack.resize(1);
167     helper_vars::return_stack[0] = helper_vars::mul_1 *
168     helper_vars::mul_2;
169     return;
170 }
171
172 int k_bits = 0; // roughly , the number of bits in k, the depth of the stack during run time
173 int k_copy = k;
174 while (k_copy > 0){
175     k_bits++;
176     k_copy >>= 1;
177 }
178 k_bits += 2;
179 vector<pair<int, int>> call_stack(2 * k_bits);
180 //cout << " 2 * k_bits " << 2 * k_bits << endl;
181 int call_pointer = 0; // size of the call pointer, so the top index is call_pointer - 1
182 vector<int> status_stack(2 * k_bits); // 0: first meet, 1: to return
183 //vector<mpz_class> return_stack(2 * k_bits);
184 helper_vars::return_stack.resize(2*k_bits);
185 int return_pointer = 0;
186
187 call_stack[call_pointer] = pair<int, int> (N, k);
188 status_stack[call_pointer] = 0;
189 call_pointer++;
190
191 int m;
192 int N_now, k_now; // N and k for the current stack element
193
194 while (call_pointer > 0){
195     N_now = call_stack[call_pointer-1].first;
196     k_now = call_stack[call_pointer-1].second;
197     //cout << "call_pointer = " << call_pointer << " N = " << N_now << " k = " << k_now << " stat = " <<
198     status_stack[call_pointer-1] << endl;
199     //cout << " the whole stack " << endl;
200     //for (int i=0;i<call_pointer; i++){
201     //    cout << call_stack[i].first << " , " << call_stack[i].second << " " << status_stack[i] << endl;
202     //}
203     if (status_stack[call_pointer-1] == 1){ // we should multiply two top elements in the return stack
204         // to collect two top elements in return stack and multiply them
205         helper_vars::return_stack[return_pointer-2] =
206         helper_vars::return_stack[return_pointer-2] *
207         helper_vars::return_stack[return_pointer-1];
208         return_pointer--; // remove two items, add one item
209         call_pointer--;
210     }else{
211         //cout << " else " << endl;
212         if(k_now == 1){
213             // to return the corresponding N
214             helper_vars::return_stack[return_pointer++] = call_stack[call_pointer-1].
215             first;
216             call_pointer--; // pop this element
217         }
218         if (k_now == 2){
219             helper_vars::mul_1 = N_now;
220             helper_vars::mul_2 = N_now - s;
221             helper_vars::return_stack[return_pointer++] =
222             helper_vars::mul_1 * helper_vars::mul_2;
223             call_pointer--;
224         }
225         if (k_now > 2){
226             m = k_now / 2;
227             status_stack[call_pointer-1] = 1; // when return to this state, we know that we should aggregate
228             call_stack[call_pointer] = pair<int, int>(N_now, m);
229             status_stack[call_pointer] = 0; // just added

```



```

223         call_stack[call_pointer+1] = pair<int, int>(N_now - m*s, k_now - m );
224         status_stack[call_pointer+1] = 0;
225         call_pointer += 2;
226     }
227 }
228 }
229 // make sure there is exactly one element in return stack
230 if (return_pointer != 1){
231     cerr << " return pointer is not zero";
232 }
233 //return helper_vars::return_stack[0]; // the top element remaining in the return stack
234 }

```

7.8.1.9 prod_factorial()

```

mpz_class prod_factorial (
    const vector< int > & a,
    int i,
    int j )

{
338
339     if (i==j){
340         return compute_product(a[i], a[i], 1);
341     }else{
342         helper_vars::mpz_vec2.resize(j-i+1);
343         for (int k = i; k<=j;k++)
344             helper_vars::mpz_vec2[k- i] = compute_product(a[k], a[k],1);
345         compute_array_product(helper_vars::mpz_vec2);
346         return helper_vars::mpz_vec2[0];
347     }
348 }

```

7.8.1.10 prod_factorial_old()

```

mpz_class prod_factorial_old (
    const vector< int > & a,
    int i,
    int j )

```

computes the product of factorials in a vector given a range

Parameters

| | |
|-------|---------------------------|
| a | vector of integers |
| i,j | endpoints of the interval |

Returns

$$\prod_{v=i}^j a_v!$$

```

327 {
328     if (i == j){
329         return compute_product(a[i], a[i], 1);
330     }else{

```

```
331     int k = (i+j)/2;
332     mpz_class x = prod_factorial(a, i, k);
333     mpz_class y = prod_factorial(a, k+1, j);
334     return x * y;
335 }
336 }
```

7.9 fenwick.cpp File Reference

```
#include "fenwick.h"
```

7.10 fenwick.h File Reference

```
#include <vector>
```

Classes

- class [fenwick_tree](#)
Fenwick tree class.
- class [reverse_fenwick_tree](#)
similar to the [fenwick_tree](#) class, but instead of prefix sums, this class computes suffix sums.

7.11 gcomp.cpp File Reference

To compress / decompress simple marked graphs.

```
#include <iostream>
#include <stdio.h>
#include <ctype.h>
#include <stdlib.h>
#include <unistd.h>
#include "marked_graph_compression.h"
```

Functions

- int [main](#) (int argc, char **argv)

7.11.1 Detailed Description

To compress / decompress simple marked graphs.

This code has two functionalities: 1) gets a simple marked graph and compresses it, 2) gets a simple marked graph in its compressed form and decompresses it.

In order to compress a graph, the hyperparameters `h` and `delta` should be given using `-h` and `-d`, respectively. The input graph should be given using `-i` option, followed by the name of the file containing the graph. Also, the compressed graph will be stored in the file specified by `-o` option. A graph must be specified using its edge list in the following format: first, the number of vertices comes, then the mark of vertices in order, then each line contains the information on an edge, which is of the form `i j x y`, meaning there is an edge between vertices `i` and `j`, with mark `x` and `y` towards `i` and `j`, respectively.

In order to decompress, the compressed file should be given after `-i`, the file to store the decompressed graph should be given using `-o`, and an argument `-u` for uncompress should be given.

7.11.2 Function Documentation

7.11.2.1 main()

```
int main (
    int argc,
    char ** argv )

{
    22
    23     int h, delta;
    24     string infile, outfile;
    25     bool uncompress = false; // becomes true if -u option is given (to decompress)
    26     bool quiet = true; // becomes false if -v option is given (verbose)
    27     bool stat = false; // if true, statistics on the properties of the compressed graph, e.g. number of star
                          // vertices / edges or the number of partition graphs will be given
    28     char opt;
    29
    30     string report_file, stat_file;
    31     ofstream report_stream, stat_stream;
    32
    33     while ((opt = getopt(argc, argv, "h:d:i:o:uvsV:S:")) != EOF){
    34         switch(opt){
    35             case 'h':
    36                 h = atoi(optarg);
    37                 break;
    38             case 'd':
    39                 delta = atoi(optarg);
    40                 break;
    41             case 'i':
    42                 infile = string(optarg);
    43                 break;
    44             case 'o':
    45                 outfile = string(optarg);
    46                 break;
    47             case 'u':
    48                 uncompress = true; // in the decompression phase
    49                 break;
    50             case 'v':
    51                 quiet = false;
    52                 break;
    53             case 'V':
    54                 report_file = string(optarg);
    55                 if (report_file != ""){
    56                     report_stream.open(report_file);
    57                     logger::report_stream = &report_stream;
    58                 }
    59                 break;
    60             case 's':
```

```

61     stat = true;
62     break;
63     case 'S':
64         stat_file = string(optarg);
65         if (stat_file != ""){
66             stat_stream.open(stat_file);
67             logger::stat_stream = &stat_stream;
68         }
69         break;
70     case '?':
71         cerr << "Error: option -" << char(optopt) << " requires an argument" << endl;
72         return 1;
73     }
74 }
75 if (uncompress == false and h <= 0){
76     cerr << "Error: parameter h must be a positive integer. Instead, the value " << h << " was given." <<
    endl;
77     return 1;
78 }
79 if (uncompress == false and delta <= 0){
80     cerr << "Error: parameter d (delta) must be a positive integer. Instead, the value " << delta << " was
    given." << endl;
81     return 1;
82 }
83
84 ifstream inp(infile.c_str());
85 ofstream oup(outfile.c_str());
86
87 if (!inp.good()){
88     cerr << "Error: invalid input file <" << infile << "> given " << endl;
89     return 1;
90 }
91
92 if (!oup.good()){
93     cerr << "Error: invalid output file <" << outfile << "> given " << endl;
94     return 1;
95 }
96
97
98 if (quiet == true){
99     // do not log
100     logger::verbose = false; // no run time log
101     logger::report = false; // no final report
102 }
103
104 if (stat == true){
105     logger::stat = true;
106 }
107
108 //cout << " h = " << h << " delta = " << delta << " infile = " << infile << " outfile = " << outfile <<
    endl;
109
110 logger::start();
111 if (uncompress == false){
112     // goal is compression
113     logger::current_depth++;
114     logger::add_entry("Read Graph", "");
115     marked_graph_encoder E(h, delta);
116     marked_graph G; // the input graph to be compressed
117     inp >> G;
118     logger::current_depth--;
119     logger::current_depth++;
120     logger::add_entry("Encode", "");
121     marked_graph_compressed C = E.encode(G);
122     logger::current_depth--;
123     //FILE* f;
124     //f = fopen(outfile.c_str(), "wb+");
125     logger::current_depth++;
126     logger::add_entry("Write to binary", "");
127     //C.binary_write(f);
128     C.binary_write(outfile);
129     //fclose(f);
130     logger::current_depth--;
131 }else{
132     // goal is to decompress
133     //FILE* f;
134     //f = fopen(infile.c_str(), "rb+");
135     marked_graph_compressed C;
136     logger::current_depth++;
137     logger::add_entry("Read from binary", "");
138     //C.binary_read(f);
139     C.binary_read(infile);
140     //fclose(f);
141     logger::current_depth--;
142
143     logger::current_depth++;
144     logger::add_entry("Decode", "");

```

```

145     marked_graph_decoder D;
146     marked_graph G = D.decode(C);
147     logger::current_depth--;
148
149     logger::current_depth++;
150     logger::add_entry("Write decoded graph to output file","");
151     oup << G;
152     logger::current_depth--;
153 }
154 logger::stop();
155 return 0;
156 }

```

7.12 graph_message.cpp File Reference

```
#include "graph_message.h"
```

Functions

- bool [pair_compare](#) (const pair< vector< int >, int > &a, const pair< vector< int >, int > &b)
used for sorting messages

7.12.1 Function Documentation

7.12.1.1 pair_compare()

```

bool pair_compare (
    const pair< vector< int >, int > & a,
    const pair< vector< int >, int > & b )

```

used for sorting messages

```

515                                     {
516     return a.first < b.first;
517 }

```

7.13 graph_message.h File Reference

```

#include <vector>
#include <map>
#include <unordered_map>
#include <boost/functional/hash/hash.hpp>
#include "marked_graph.h"
#include "logger.h"

```

Classes

- struct [vint_hash](#)
- class [graph_message](#)
this class takes care of message passing on marked graphs.
- class [colored_graph](#)
this class defines a colored graph, which is obtained from a simple marked graph and the color of edges come from the type of edges

Functions

- bool [pair_compare](#) (const pair< vector< int >, int > &, const pair< vector< int >, int > &)
used for sorting messages

7.13.1 Function Documentation

7.13.1.1 pair_compare()

```
bool pair_compare (
    const pair< vector< int >, int > & ,
    const pair< vector< int >, int > & )
```

used for sorting messages

```
515                                     {
516     return a.first < b.first;
517 }
```

7.14 logger.cpp File Reference

```
#include "logger.h"
```

7.15 logger.h File Reference

```
#include <iostream>
#include <string>
#include <vector>
#include <chrono>
#include <ctime>
#include <map>
```

Classes

- class [log_entry](#)
- class [logger](#)

Functions

- void [__attribute__](#) ((constructor)) prog_start()
- void [__attribute__](#) ((destructor)) prog_finish()

7.15.1 Function Documentation

7.15.1.1 [__attribute__](#)() [1/2]

```
void __attribute__ (
    (constructor) )
```

7.15.1.2 [__attribute__](#)() [2/2]

```
void __attribute__ (
    (destructor) )
```

7.16 marked_graph.cpp File Reference

```
#include "marked_graph.h"
```

Functions

- istream & [operator>>](#) (istream &inp, [marked_graph](#) &G)
inputs a [marked_graph](#)
- bool [operator==](#) (const [marked_graph](#) &G1, const [marked_graph](#) &G2)
- bool [operator!=](#) (const [marked_graph](#) &G1, const [marked_graph](#) &G2)
- bool [edge_compare](#) (const pair< int, pair< int, int > > &a, pair< int, pair< int, int > > &b)
this is to help comparing two marked graphs. The inputs would resemble two edge information, of the form (j, (x, y)), where j is the other endpoint, and x and y are marks. We want to sort them with respect to the neighbor index j.
- ostream & [operator<<](#) (ostream &o, const [marked_graph](#) &G)

7.16.1 Function Documentation

7.16.1.1 edge_compare()

```
bool edge_compare (
    const pair< int, pair< int, int > > & a,
    pair< int, pair< int, int > > & b )
```

this is to help comparing two marked graphs. The inputs would resemble two edge information, of the form (j, (x, y)), where j is the other endpoint, and x and y are marks. We want to sort them with respect to the neighbor index j.

```
93 {
94     return a.first < b.first;
95 }
```

7.16.1.2 operator!=(())

```
bool operator!= (
    const marked_graph & G1,
    const marked_graph & G2 )
```

```
88 {
89     return !(G1 == G2);
90 }
```

7.16.1.3 operator<<()

```
ostream& operator<< (
    ostream & o,
    const marked_graph & G )
```

```
99 {
100     o << G.nu_vertices << endl;
101     for (int v=0;v<G.nu_vertices;v++){
102         o << G.ver_mark[v];
103         if (v < G.nu_vertices-1)
104             o << " ";
105     }
106     o << endl;
107
108     vector<pair<pair<int, int>, pair<int, int> > > edges;
109     pair<pair<int, int>, pair<int, int> > edge; // the current edge to be added to the list
110     for (int v=0;v<G.nu_vertices;v++){
111         for (int i=0;i<G.adj_list[v].size();i++){
112             if (G.adj_list[v][i].first > v){ // avoid duplicate in edge list, only add edges where the
                other endpoint has a greater index
113                 edge.first.first = v;
114                 edge.first.second = G.adj_list[v][i].first;
115                 edge.second = G.adj_list[v][i].second;
116                 edges.push_back(edge);
117             }
118         }
119     }
120     sort(edges.begin(), edges.end());
121     o << edges.size() << endl;
122     for(int i=0;i<edges.size();i++){
123         o << edges[i].first.first << " " << edges[i].first.second << " " << edges[i].second.first << " " <<
            edges[i].second.second << endl;
124     }
125     return o;
126     /*
```



```

127 o << " number of vertices " << G.nu_vertices << endl;
128 vector<pair<int, pair<int, int> > > l; // the adjacency list of a vertex
129 for (int v=0; v<G.nu_vertices; v++){
130     o << " vertex " << v << " mark " << G.ver_mark[v] << endl;
131     //o << " adj list (connections to vertices with greater index): format (j, (x,y))" << endl;
132     o << " adj list " << endl;
133     l = G.adj_list[v];
134     sort(l.begin(), l.end(), edge_compare);
135     for (int i=0; i<l.size(); i++){
136         if (l[i].first > v)
137             o << " (" << l[i].first << ", (" << l[i].second.first << ", " << l[i].second.second << ")) ";
138     }
139     o << endl << endl;
140 }
141 return o;
142 */
143 }

```

7.16.1.4 operator==()

```

bool operator== (
    const marked_graph & G1,
    const marked_graph & G2 )

```

two marked graphs are said to be the same if: 1) they have the same number of vertices, 2) vertex marks match and 3) each vertex has the same set of neighbors with matching marks.

```

66 {
67     if (G1.nu_vertices != G2.nu_vertices)
68         return false;
69     return G1.adj_list == G2.adj_list;
70     int n = G1.nu_vertices; // number of vertices of the two graphs
71     vector< pair< int, pair< int, int > > > l1, l2; // the adjacency list of a vertex in two graphs for
        comparison.
72     for (int v=0; v<n; v++){
73         if (G1.ver_mark[v] != G2.ver_mark[v]) // mark of each vertex should be the same
74             return false;
75         if (G1.adj_list[v].size() != G2.adj_list[v].size()) // each vertex must have the same
            degree in two graphs
76             return false;
77         l1 = G1.adj_list[v];
78         l2 = G2.adj_list[v];
79         sort(l1.begin(), l1.end(), edge_compare); // sort with respect to the other endpoint
80         sort(l2.begin(), l2.end(), edge_compare);
81         if (l1 != l2) // after sorting, the lists must match
82             return false;
83     }
84     return true;
85 }

```

7.16.1.5 operator>>()

```

istream& operator>> (
    istream & inp,
    marked_graph & G )

```

inputs a [marked_graph](#)

The input format is as follows: 1) number of vertices 2) a list of vertex marks as nonnegative integers 3) number of edges 4) for each edge: write $ijxy$, where i and j are the endpoints (here, $0 \leq i, j \leq n - 1$ with n being the number of vertices), x is the mark towards i and y is the mark towards j (both nonnegative integers) Example: 2 1 2 1 0 1 1 2 which is a graph with 2 vertices, the mark of vertex 0 is 1 and the mark of vertex 1 is 2, there is one edge between these two vertices with mark 1 towards 0 and mark 2 toward s 1

```

41 {
42     logger::current_depth++;
43     logger::add_entry("Read vertex marks and edges","");
44     int nu_vertices;
45     inp >> nu_vertices;
46
47     vector<int> ver_marks;
48     ver_marks.resize(nu_vertices);
49     for (int i=0;i<nu_vertices;i++)
50         inp >> ver_marks[i];
51
52     int nu_edges;
53     inp >> nu_edges;
54     vector<pair< pair<int, int> , pair<int, int> > > edges;
55     edges.resize(nu_edges);
56     for (int i=0;i<nu_edges;i++)
57         inp >> edges[i].first.first >> edges[i].first.second >> edges[i].second.first >> edges[i].second.second
58         ;
59     logger::add_entry("Constructing marked graph", "");
60     G = marked_graph(nu_vertices, edges, ver_marks);
61     logger::current_depth--;
62     return inp;
63 }

```

7.17 marked_graph.h File Reference

```

#include <iostream>
#include <vector>
#include <map>
#include <fstream>
#include "logger.h"

```

Classes

- class [marked_graph](#)
simple marked graph

Functions

- `istream & operator>> (istream &inp, marked_graph &G)`
inputs a [marked_graph](#)
- `bool edge_compare (const pair< int, pair< int, int > > &a, pair< int, pair< int, int > > &b)`
this is to help comparing two marked graphs. The inputs would resemble two edge information, of the form (j, (x, y)), where j is the other endpoint, and x and y are marks. We want to sort them with respect to the neighbor index j.

7.17.1 Function Documentation

7.17.1.1 edge_compare()

```
bool edge_compare (
    const pair< int, pair< int, int > > & a,
    pair< int, pair< int, int > > & b )
```

this is to help comparing two marked graphs. The inputs would resemble two edge information, of the form $(j, (x, y))$, where j is the other endpoint, and x and y are marks. We want to sort them with respect to the neighbor index j .

```
93 {
94     return a.first < b.first;
95 }
```

7.17.1.2 operator>>()

```
istream& operator>> (
    istream & inp,
    marked_graph & G )
```

inputs a [marked_graph](#)

The input format is as follows: 1) number of vertices 2) a list of vertex marks as nonnegative integers 3) number of edges 4) for each edge: write $ijxy$, where i and j are the endpoints (here, $0 \leq i, j \leq n - 1$ with n being the number of vertices), x is the mark towards i and y is the mark towards j (both nonnegative integers) Example: 2 1 2 1 0 1 1 2 which is a graph with 2 vertices, the mark of vertex 0 is 1 and the mark of vertex 1 is 2, there is one edge between these two vertices with mark 1 towards 0 and mark 2 toward s 1

```
41 {
42     logger::current_depth++;
43     logger::add_entry("Read vertex marks and edges", "");
44     int nu_vertices;
45     inp >> nu_vertices;
46
47     vector<int> ver_marks;
48     ver_marks.resize(nu_vertices);
49     for (int i=0; i<nu_vertices; i++)
50         inp >> ver_marks[i];
51
52     int nu_edges;
53     inp >> nu_edges;
54     vector<pair< pair<int, int> , pair<int, int> > > edges;
55     edges.resize(nu_edges);
56     for (int i=0; i<nu_edges; i++)
57         inp >> edges[i].first.first >> edges[i].first.second >> edges[i].second.first >> edges[i].second.second
58         ;
59     logger::add_entry("Constructing marked graph", "");
60     G = marked_graph(nu_vertices, edges, ver_marks);
61     logger::current_depth--;
62     return inp;
63 }
```

7.18 marked_graph_compression.cpp File Reference

```
#include "marked_graph_compression.h"
```

7.19 marked_graph_compression.h File Reference

```
#include <vector>
#include "marked_graph.h"
#include "graph_message.h"
#include "simple_graph.h"
#include "bipartite_graph.h"
#include "simple_graph_compression.h"
#include "bipartite_graph_compression.h"
#include "time_series_compression.h"
#include "logger.h"
#include "bitstream.h"
```

Classes

- class [marked_graph_compressed](#)
- class [marked_graph_encoder](#)
- class [marked_graph_decoder](#)

7.20 random_graph.cpp File Reference

```
#include "random_graph.h"
```

Functions

- [marked_graph marked_ER](#) (int n, double p, int ver_mark, int edge_mark)
generates a marked Erdos Renyi graph
- [marked_graph poisson_graph](#) (int n, double deg_mean, int ver_mark, int edge_mark)
generates a random graph where roughly speaking, the degree of a vertex is Poisson
- [marked_graph near_regular_graph](#) (int n, int half_deg, int ver_mark, int edge_mark)
*generates a random graph which is nearly regular, and the degree of each vertex is close to $2 * half_deg$. Each vertex is uniformly connected to $half_deg$ many other vertices, and multiple edges are dropped. Furthermore, each vertex and edge is randomly assigned marks, where the vertex mark set is $\{0, 1, \dots, ver_mark - 1\}$ and $\{0, 1, \dots, edge_mark - 1\}$.*

7.20.1 Function Documentation

7.20.1.1 marked_ER()

```
marked\_graph marked_ER (
    int n,
    double p,
    int ver_mark,
    int edge_mark )
```

generates a marked Erdos Renyi graph

Parameters

| | |
|------------------|--------------------------------------|
| <i>n</i> | the number of vertices |
| <i>p</i> | probability of an edge being present |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge marks |

Returns

a random marked graph, where each edge is independently present with probability *p*, each vertex has a random integer mark in the range $[0, \text{ver_mark})$, and each edge has two random integers marks in the range $[0, \text{edge_mark})$

```

4 {
5     unsigned seed = chrono::system_clock::now().time_since_epoch().count();
6     default_random_engine generator(seed);
7     uniform_int_distribution<int> ver_mark_dist(0, ver_mark-1); // distribution a vertex mark
8     uniform_int_distribution<int> edge_mark_dist(0, edge_mark-1); // distribution an edge mark
9     uniform_real_distribution<double> unif_dist(0.0, 1.0);
10    double unif;
11    int x, xp; // generated marks
12
13    vector<int> ver_marks(n); // vector of size n
14    vector<pair< pair<int, int>, pair<int, int> > > edges; // the edge list of the graph
15
16    for (int v=0; v<n; v++){
17        ver_marks[v] = ver_mark_dist(generator);
18        for (int w=v+1; w<n; w++){
19            unif = unif_dist(generator);
20            if (unif < p){ // we put an edge between v and w
21                x = edge_mark_dist(generator);
22                xp = edge_mark_dist(generator);
23                edges.push_back(pair<pair<int, int>, pair<int, int> >(pair<int, int>(v,w), pair<int, int>(x,xp)));
24            }
25        }
26    }
27    cout << " marked_ER number of edges " << edges.size() << endl;
28    return marked_graph(n, edges, ver_marks);
29 }

```

7.20.1.2 near_regular_graph()

```

marked_graph near_regular_graph (
    int n,
    int half_deg,
    int ver_mark,
    int edge_mark )

```

generates a random graph which is nearly regular, and the degree of each vertex is close to $2 * \text{half_deg}$. Each vertex is uniformly connected to *half_deg* many other vertices, and multiple edges are dropped. Furthermore, each vertex and edge is randomly assigned marks, where the vertex mark set is $\{0, 1, \dots, \text{ver_mark} - 1\}$ and $\{0, 1, \dots, \text{edge_mark} - 1\}$.

Parameters

| | |
|------------------|--|
| <i>n</i> | the number of vertices |
| <i>half_deg</i> | the number of edges each vertex tries to connect to, so the final average degree is $2 * \text{half_deg}$ |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge_marks |

Returns

a random marked graph as described above.

```

76                                     {
77     unsigned seed = chrono::system_clock::now().time_since_epoch().count();
78     default_random_engine generator(seed);
79
80     uniform_int_distribution<int> neighbor_dist(0,n-1);
81     uniform_int_distribution<int> ver_mark_dist(0,ver_mark-1); // distribution a vertex mark
82     uniform_int_distribution<int> edge_mark_dist(0,edge_mark-1); // distribution an edge mark
83
84     int w;
85     pair<int, int> edge;
86
87     set<pair<int, int> > umarked_edges;
88     vector< pair< pair< int, int >, pair< int, int > > > edges;
89
90     int x, xp; // edge marks
91     vector<int> ver_marks(n);
92
93     for (int i=0;i<n;i++){
94         ver_marks[i] = ver_mark_dist(generator);
95         for (int j=0;j<half_deg;j++){
96             w = neighbor_dist(generator);
97             if (w!= i){
98                 edge = pair<int,int>(i,w);
99                 if (edge.first > edge.second)
100                     swap (edge.first, edge.second); // to make sure pairs are ordered
101                 umarked_edges.insert(edge);
102             }
103         }
104     }
105     for (set<pair<int, int>>::iterator it = umarked_edges.begin(); it!=umarked_edges.end(); it++){
106         x = edge_mark_dist(generator);
107         xp = edge_mark_dist(generator);
108         edges.push_back(pair<pair<int, int>, pair<int, int> >(*it, pair<int, int>(x, xp)));
109     }
110
111
112     return marked_graph(n, edges, ver_marks);
113 }
```

7.20.1.3 poisson_graph()

```

marked_graph poisson_graph (
    int n,
    double deg_mean,
    int ver_mark,
    int edge_mark )
```

generates a random graph where roughly speaking, the degree of a vertex is Poisson

Parameters

| | |
|------------------|-------------------------------------|
| <i>n</i> | the number of vertices |
| <i>deg_mean</i> | mean of Poisson |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge marks |

Returns

A random graph, where each vertex chooses its degree according to Poisson(deg_mean), then picks neighbors uniformly at random, and connects to them (if the neighbors have not already connected to them, if some

of the neighbors I pick are already connected to me, I just don't do anything). Vertex and edge marks are picked independently and uniformly.

```

32                                     {
33     unsigned seed = chrono::system_clock::now().time_since_epoch().count();
34     default_random_engine generator(seed);
35     poisson_distribution<int> deg_dist(deg_mean);
36     uniform_int_distribution<int> neighbor_dist(0,n-1); // distribution for the other endpoint
37
38     vector< pair< pair< int, int >, pair< int, int > > > edges;
39     vector<int> ver_marks(n);
40
41     uniform_int_distribution<int> ver_mark_dist(0,ver_mark-1); // distribution a vertex mark
42     uniform_int_distribution<int> edge_mark_dist(0,edge_mark-1); // distribution an edge mark
43     int x, xp; // edge mark values
44
45     pair< pair< int, int >, pair< int, int > > edge; // the current edge to be added
46     vector<set<int> > neighbors(n); // the list of neighbors of vertices
47     int deg; // the degree of a vertex
48     int w; // the neighbor
49     for (int v=0;v<n;v++){
50         ver_marks[v] = ver_mark_dist(generator);
51         deg = deg_dist(generator);
52         for (int i=0; i<deg; i++){
53             do{
54                 w = neighbor_dist(generator);
55             }while(w == v or neighbors[v].find(w) != neighbors[v].end()); // not myself and not already connected
56             // now, w is a possible neighbor
57             // see if w has picked v as a neighbor
58             if (neighbors[w].find(v) == neighbors[w].end()){
59                 // add w as a neighbors to v
60                 neighbors[v].insert(w);
61                 // marks for the edge
62                 x = edge_mark_dist(generator);
63                 xp = edge_mark_dist(generator);
64                 edge.first.first = v;
65                 edge.first.second = w;
66                 edge.second.first = x;
67                 edge.second.second = xp;
68                 edges.push_back(edge);
69             }
70         }
71     }
72     cerr << " edges size " << edges.size() << endl;
73     return marked_graph(n, edges, ver_marks);
74 }

```

7.21 random_graph.h File Reference

```

#include "marked_graph.h"
#include <random>
#include <chrono>
#include <vector>
#include <set>

```

Functions

- [marked_graph marked_ER](#) (int n, double p, int ver_mark, int edge_mark)
generates a marked Erdos Renyi graph
- [marked_graph poisson_graph](#) (int n, double deg_mean, int ver_mark, int edge_mark)
generates a random graph where roughly speaking, the degree of a vertex is Poisson
- [marked_graph near_regular_graph](#) (int n, int half_deg, int ver_mark, int edge_mark)
*generates a random graph which is nearly regular, and the degree of each vertex is close to $2 * half_deg$. Each vertex is uniformly connected to $half_deg$ many other vertices, and multiple edges are dropped. Furthermore, each vertex and edge is randomly assigned marks, where the vertex mark set is $\{0, 1, \dots, ver_mark - 1\}$ and $\{0, 1, \dots, edge_mark - 1\}$.*

7.21.1 Function Documentation

7.21.1.1 marked_ER()

```
marked_graph marked_ER (
    int n,
    double p,
    int ver_mark,
    int edge_mark )
```

generates a marked Erdos Renyi graph

Parameters

| | |
|------------------|--------------------------------------|
| <i>n</i> | the number of vertices |
| <i>p</i> | probability of an edge being present |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge marks |

Returns

a random marked graph, where each edge is independently present with probability *p*, each vertex has a random integer mark in the range $[0, \text{ver_mark})$, and each edge has two random integers marks in the range $[0, \text{edge_mark})$

```
4 {
5   unsigned seed = chrono::system_clock::now().time_since_epoch().count();
6   default_random_engine generator(seed);
7   uniform_int_distribution<int> ver_mark_dist(0, ver_mark-1); // distribution a vertex mark
8   uniform_int_distribution<int> edge_mark_dist(0, edge_mark-1); // distribution an edge mark
9   uniform_real_distribution<double> unif_dist(0.0, 1.0);
10  double unif;
11  int x, xp; // generated marks
12
13  vector<int> ver_marks(n); // vector of size n
14  vector<pair< pair<int, int>, pair<int, int> > > edges; // the edge list of the graph
15
16  for (int v=0; v<n; v++){
17    ver_marks[v] = ver_mark_dist(generator);
18    for (int w=v+1; w<n; w++){
19      unif = unif_dist(generator);
20      if (unif < p){ // we put an edge between v and w
21        x = edge_mark_dist(generator);
22        xp = edge_mark_dist(generator);
23        edges.push_back(pair<pair<int, int>, pair<int, int> >(pair<int, int>(v,w), pair<int, int>(x,xp)));
24      }
25    }
26  }
27  cout << " marked_ER number of edges " << edges.size() << endl;
28  return marked_graph(n, edges, ver_marks);
29 }
```

7.21.1.2 near_regular_graph()

```
marked_graph near_regular_graph (
    int n,
```



```

    int half_deg,
    int ver_mark,
    int edge_mark )

```

generates a random graph which is nearly regular, and the degree of each vertex is close to $2 * \text{half_deg}$. Each vertex is uniformly connected to half_deg many other vertices, and multiple edges are dropped. Furthermore, each vertex and edge is randomly assigned marks, where the vertex mark set is $\{0, 1, \dots, \text{ver_mark} - 1\}$ and $\{0, 1, \dots, \text{edge_mark} - 1\}$.

Parameters

| | |
|------------------|--|
| <i>n</i> | the number of vertices |
| <i>half_deg</i> | the number of edges each vertex tries to connect to, so the final average degree is $2 * \text{half_deg}$ |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge_marks |

Returns

a random marked graph as described above.

```

76
77 unsigned seed = chrono::system_clock::now().time_since_epoch().count();
78 default_random_engine generator(seed);
79
80 uniform_int_distribution<int> neighbor_dist(0,n-1);
81 uniform_int_distribution<int> ver_mark_dist(0,ver_mark-1); // distribution a vertex mark
82 uniform_int_distribution<int> edge_mark_dist(0,edge_mark-1); // distribution an edge mark
83
84 int w;
85 pair<int, int> edge;
86
87 set<pair<int, int> > umarked_edges;
88 vector< pair< pair< int, int >, pair< int, int > > > edges;
89
90 int x, xp; // edge marks
91 vector<int> ver_marks(n);
92
93 for (int i=0;i<n;i++){
94     ver_marks[i] = ver_mark_dist(generator);
95     for (int j=0;j<half_deg;j++){
96         w = neighbor_dist(generator);
97         if (w!= i){
98             edge = pair<int,int>(i,w);
99             if (edge.first > edge.second)
100                 swap (edge.first, edge.second); // to make sure pairs are ordered
101             umarked_edges.insert(edge);
102         }
103     }
104 }
105 for (set<pair<int, int>>::iterator it = umarked_edges.begin(); it!=umarked_edges.end(); it++){
106     x = edge_mark_dist(generator);
107     xp = edge_mark_dist(generator);
108     edges.push_back(pair<pair<int, int>, pair<int, int> >(*it, pair<int, int>(x, xp)));
109 }
110
111
112 return marked_graph(n, edges, ver_marks);
113 }

```

7.21.1.3 poisson_graph()

```

marked_graph poisson_graph (
    int n,
    double deg_mean,
    int ver_mark,
    int edge_mark )

```

generates a random graph where roughly speaking, the degree of a vertex is Poisson

Parameters

| | |
|------------------|-------------------------------------|
| <i>n</i> | the number of vertices |
| <i>deg_mean</i> | mean of Poisson |
| <i>ver_mark</i> | the number of possible vertex marks |
| <i>edge_mark</i> | the number of possible edge marks |

Returns

A random graph, where each vertex chooses its degree according to `Poisson(deg_mean)`, then picks neighbors uniformly at random, and connects to them (if the neighbors have not already connected to them, if some of the neighbors I pick are already connected to me, I just don't do anything). Vertex and edge marks are picked independently and uniformly.

```

32                                     {
33     unsigned seed = chrono::system_clock::now().time_since_epoch().count();
34     default_random_engine generator(seed);
35     poisson_distribution<int> deg_dist(deg_mean);
36     uniform_int_distribution<int> neighbor_dist(0,n-1); // distribution for the other endpoint
37
38     vector< pair< pair< int, int >, pair< int, int > > > edges;
39     vector<int> ver_marks(n);
40
41     uniform_int_distribution<int> ver_mark_dist(0,ver_mark-1); // distribution a vertex mark
42     uniform_int_distribution<int> edge_mark_dist(0,edge_mark-1); // distribution an edge mark
43     int x, xp; // edge mark values
44
45     pair< pair< int, int >, pair< int, int > > edge; // the current edge to be added
46     vector<set<int> > neighbors(n); // the list of neighbors of vertices
47     int deg; // the degree of a vertex
48     int w; // the neighbor
49     for (int v=0;v<n;v++){
50         ver_marks[v] = ver_mark_dist(generator);
51         deg = deg_dist(generator);
52         for (int i=0; i<deg; i++){
53             do{
54                 w = neighbor_dist(generator);
55             }while(w == v or neighbors[v].find(w) != neighbors[v].end()); // not myself and not already connected
56             // now, w is a possible neighbor
57             // see if w has picked v as a neighbor
58             if (neighbors[w].find(v) == neighbors[w].end()){
59                 // add w as a neighbors to v
60                 neighbors[v].insert(w);
61                 // marks for the edge
62                 x = edge_mark_dist(generator);
63                 xp = edge_mark_dist(generator);
64                 edge.first.first = v;
65                 edge.first.second = w;
66                 edge.second.first = x;
67                 edge.second.second = xp;
68                 edges.push_back(edge);
69             }
70         }
71     }
72     cerr << " edges size " << edges.size() << endl;
73     return marked_graph(n, edges, ver_marks);
74 }
```

7.22 README.md File Reference

7.23 rnd_graph.cpp File Reference

```

#include <iostream>
#include <stdio.h>
#include <ctype.h>
#include <stdlib.h>
#include <unistd.h>
#include "random_graph.h"
```

Functions

- void [print_usage](#) ()
- int [main](#) (int argc, char **argv)

7.23.1 Function Documentation

7.23.1.1 main()

```
int main (
    int argc,
    char ** argv )

43     {
44     int n, edge_mark, ver_mark;
45     double p, deg;
46     string type, outfile;
47     char opt;
48
49     while ((opt = getopt(argc, argv, "t:n:p:d:e:v:o:h")) != EOF){
50         switch(opt){
51             case 't':
52                 type = string(optarg);
53                 break;
54             case 'n':
55                 n = atoi(optarg);
56                 break;
57             case 'p':
58                 p = atof(optarg);
59                 break;
60             case 'd':
61                 deg = atof(optarg);
62                 break;
63             case 'e':
64                 edge_mark = atoi(optarg);
65                 break;
66             case 'v':
67                 ver_mark = atoi(optarg);
68                 break;
69             case 'o':
70                 outfile = string(optarg);
71                 break;
72             case 'h':
73                 print_usage();
74                 break;
75             case '?':
76                 cerr << "Error: option -" << char(optopt) << " requires an argument" << endl;
77                 print_usage();
78                 return 1;
79             }
80         }
81         ofstream oup(outfile.c_str());
82         if (!oup.good()){
83             cerr << "Error: invalid output file <" << outfile << "> given " << endl;
84             return 1;
85         }
86
87         marked_graph G;
88         if (type == "er"){
89             G = marked_ER(n, p, ver_mark, edge_mark);
90             oup << G;
91         }else if(type == "reg"){
92             G = near_regular_graph(n, deg, ver_mark, edge_mark);
93             oup << G;
94         }else if(type == "poi"){
95             G = poisson_graph(n, deg, ver_mark, edge_mark);
96             oup << G;
97         }else{
98             cerr << " ERROR: unknown type " << type << ", type must be either <er> or <reg> or <poi> " << endl;
99             return 1;
100         }
101         return 0;
102     }
```

7.23.1.2 print_usage()

```
void print_usage ( )

10      {
11  cout << " Usage: " << endl;
12  cout << " rnd_graph -t [random graph type] -n [number of vertices] [[options with -p / -d]] -e [number of
    edge marks] -v [number of vertex marks] -o [output file]" << endl;
13  cout << endl;
14  cout << " OPTIONS " << endl;
15  cout << " -n : number of vertices (positive integer) " << endl;
16  cout << " -e : size of edge mark set " << endl;
17  cout << " -v : size of vertex mark set " << endl;
18  cout << " -o : output file to store graph " << endl;
19  cout << " -t : type of random graph: " << endl;
20  cout << "          \\"er\\" for Erdos Renyi " << endl;
21  cout << "          \\"reg\\" for near regular graph " << endl;
22  cout << "          \\"poi\\" for Poisson graph " << endl;
23  cout << endl;
24  cout << " TYPE SPECIFIC OPTIONS " << endl;
25  cout << endl;
26  cout << " Erdos Renyi Graph " << endl;
27  cout << " ----- " << endl;
28  cout << " -p : edge probability " << endl;
29  cout << endl;
30  cout << " Near Regular Graph " << endl;
31  cout << " ----- " << endl;
32  cout << " -d : half degree, generates a random graph which is nearly regular, and the degree of each
    vertex is close to 2 * half_deg. " << endl;
33  cout << endl;
34  cout << " Poisson Graph " << endl;
35  cout << " ----- " << endl;
36  cout << " -d : mean degree, each vertex chooses Poisson neighbors with this mean " << endl;
37  cout << endl;
38
39 }
```

7.24 simple_graph.cpp File Reference

```
#include "simple_graph.h"
```

Functions

- ostream & [operator<<](#) (ostream &o, const [graph](#) &G)
- bool [operator==](#) (const [graph](#) &G1, const [graph](#) &G2)
- bool [operator!=](#) (const [graph](#) &G1, const [graph](#) &G2)

7.24.1 Function Documentation

7.24.1.1 operator!=()

```
bool operator!= (
    const graph & G1,
    const graph & G2 )

102 {
103     return !(G1 == G2);
104 }
```

7.24.1.2 operator<<()

```
ostream& operator<< (
    ostream & o,
    const graph & G )

69 {
70     int n = G.nu_vertices();
71     vector<int> list;
72     for (int i=0;i<n;i++){
73         list = G.get_forward_list(i);
74         o << i << " -> ";
75         for (int j=0;j<list.size();j++){
76             o << list[j];
77             if (j < list.size()-1)
78                 o << ", ";
79         }
80         o << endl;
81     }
82     return o;
83 }
```

7.24.1.3 operator==()

```
bool operator== (
    const graph & G1,
    const graph & G2 )

86 {
87     int n1 = G1.nu_vertices();
88     int n2 = G2.nu_vertices();
89     if (n1!= n2)
90         return false;
91     vector<int> list1, list2;
92     for (int v=0; v<n1; v++){
93         list1 = G1.get_forward_list(v);
94         list2 = G2.get_forward_list(v);
95         if (list1 != list2)
96             return false;
97     }
98     return true;
99 }
```

7.25 simple_graph.h File Reference

```
#include <iostream>
#include <vector>
```

Classes

- class `graph`
simple unmarked graph

7.26 simple_graph_compression.cpp File Reference

```
#include "simple_graph_compression.h"
```

7.27 simple_graph_compression.h File Reference

```
#include <vector>
#include <math.h>
#include "simple_graph.h"
#include "compression_helper.h"
#include "fenwick.h"
#include "logger.h"
```

Classes

- class [graph_encoder](#)
Encodes a simple unmarked graph.
- class [graph_decoder](#)
Decodes a simple unmarked graph.

7.28 test.cpp File Reference

```
#include <iostream>
#include <fstream>
#include <vector>
#include "marked_graph.h"
#include "graph_message.h"
#include "fenwick.h"
#include "simple_graph.h"
#include "simple_graph_compression.h"
#include "bipartite_graph.h"
#include "bipartite_graph_compression.h"
#include "time_series_compression.h"
#include "marked_graph_compression.h"
#include "random_graph.h"
#include "logger.h"
```

Functions

- ostream & [operator<<](#) (ostream &o, const vector< int > &v)
- void [b_graph_test](#) ()
- void [graph_test](#) ()
- void [time_series_compression_test](#) ()
- void [marked_graph_encoder_test](#) ()
- void [random_graph_test](#) ()
- int [main](#) ()

7.28.1 Function Documentation

7.28.1.1 b_graph_test()

```
void b_graph_test ( )

28         {
29     vector<int> a = {1,1,2}; // left degree sequence
30     vector<int> b = {2,2}; // right degree sequence
31
32     b_graph G({{0},{1},{0,1}}); // defining the graph
33
34     b_graph_encoder E(a,b); // constructing the encoder object
35     mpz_class f = E.encode(G);
36
37     b_graph_decoder D(a, b);
38     b_graph Ghat = D.decode(f);
39
40     if (Ghat == G)
41         cout << " successfully decoded the graph! " << endl;
42 }
```

7.28.1.2 graph_test()

```
void graph_test ( )

44         {
45     vector<int> a = {3,2,2,3};
46     vector<vector<int> > list = {{1,2,3},{3},{3},{}};
47
48     graph G(list);
49
50     graph_encoder E(a);
51     pair<mpz_class, vector<int> > f = E.encode(G);
52
53     graph_decoder D(a);
54     graph Ghat = D.decode(f.first, f.second);
55     Ghat = D.decode(f.first, f.second);
56
57     if (Ghat == G)
58         cout << " successfully decoded the graph! " << endl;
59 }
```

7.28.1.3 main()

```
int main ( )
```

```

142     {
143     cout << compute_product(100,100,1) << endl;
144     cout << compute_product_old(100,100,1) << endl;
145     //logger::start();
146     //marked_graph G;
147     //ifstream inp("star_graph.txt");
148     //inp >> G;
149     //graph_message M(G, 10, 2);
150     //M.update_messages();
151     //graph_test();
152     //time_series_compression_test();
153     //marked_graph_encoder_test();
154     //random_graph_test();
155     //logger::stop();
156     return 0;
157     // vector<vector<int> > list = {{}, {}, {}};
158
159     // b_graph G({{0},{1},{0,1}});
160     // // cout << G << endl;
161     // // cout << G.nu_left_vertices() << endl;
162     // // cout << G.nu_right_vertices() << endl;
163     // // cout << G.get_left_degree_sequence() << endl;
164     // // cout << G.get_right_degree_sequence() << endl;
165     // vector<int> a = G.get_left_degree_sequence();
166     // vector<int> b = G.get_right_degree_sequence();
167
168
169     // b_graph_encoder E(a,b);
170     // mpz_class m = E.encode(G);
171     // cout << "encoded: " << m << endl;
172
173     // b_graph_decoder D(a, b);
174     // b_graph Ghat = D.decode(m);
175     // cout << "decoded graph: " << endl << Ghat << endl;
176
177     // if (Ghat == G)
178     //   cout << " equal " << endl;
179     // return 0;
180
181 }

```

7.28.1.4 marked_graph_encoder_test()

```
void marked_graph_encoder_test ( )
```

```

75 {
76     logger::current_depth++;
77
78     logger::add_entry("Construct G", "");
79     marked_graph G;
80     //ifstream inp("test_graphs/ten_node.txt"); //("test_graphs/hexagon_diagonal_marked.txt");
81     //ifstream inp("test_graphs/problem_4.txt");
82     //inp >> G;
83     //G = marked_graph(5, {{0,1}, {0,0}}, {{1,2}, {0,0}}, {{0,3},{0,0}}, {0,0,0,0,0});
84     //int h, delta;
85     //cout << " h " << endl;
86     //cin >> h;
87     //cout << " delta " << endl;
88     //cin >> delta;
89     G = poisson_graph(100000,3, 10, 10);//
90     //G = near_regular_graph(100000,3,1,1);
91     //G = marked_ER(100,0.05,1 ,1);
92     cout << " graph constructed " << endl;
93     //cout << G << endl;
94
95     logger::add_entry("Encode", "");
96
97     marked_graph_encoder E(3,20);
98     //marked_graph_encoder E(1,20);
99     marked_graph_compressed C = E.encode(G);
100     FILE* f;
101     logger::add_entry("write to binary file", "");
102     f = fopen("test.dat", "wb+");
103     C.binary_write(f);
104     fclose(f);
105     //cerr << " graph encoded " << endl;
106

```



```

107 FILE* g;
108 g = fopen("test.dat", "rb+");
109 marked_graph_compressed Chat;
110 logger::add_entry("read from binary file", "");
111 Chat.binary_read(g);
112 fclose(g);
113
114 if (Chat.star_edges != C.star_edges)
115     cerr << " star edges do not match " << endl;
116
117 logger::add_entry("Decode", "");
118 marked_graph_decoder D;
119 marked_graph Ghat = D.decode(Chat);
120
121 //cout << " Ghat " << endl;
122 //cout << Ghat << endl;
123
124 logger::add_entry("compare", "");
125 if (Ghat == G)
126     cout << " successfully decoded the marked graph :D " << endl;
127 else
128     cout << " they do not match :(" << endl;
129
130 logger::current_depth--;
131 //cout << " G " << endl;
132 //cout << G << endl;
133 //cout << " Ghat " << endl;
134 //cout << Ghat << endl;
135 }

```

7.28.1.5 operator<<()

```

ostream& operator<< (
    ostream & o,
    const vector< int > & v )

```

```

19                                     {
20     for (int i=0;i<v.size();i++){
21         o << v[i];
22         if (i < v.size()-1)
23             o << ", ";
24     }
25     return o;
26 }

```

7.28.1.6 random_graph_test()

```

void random_graph_test ( )

```

```

138 {
139     marked_graph G = marked_ER(100,1,3,4);
140     //cout << G << endl;
141 }

```

7.28.1.7 time_series_compression_test()

```
void time_series_compression_test ( )

62 {
63     vector<int> a = {0,2,3,1,2,1,0,1,0,2,1,0,0,2,1,3,4,5,0};
64     int n = a.size();
65     time_series_encoder E(n);
66     pair<vector<int>, mpz_class > ans = E.encode(a);
67
68     time_series_decoder D(n);
69     vector<int> ahat = D.decode(ans);
70     if (ahat == a)
71         cout << " successfully decoded the original time series! " << endl;
72 }
```

7.29 test_mp.cpp File Reference

```
#include <iostream>
#include <fstream>
#include <vector>
#include "marked_graph.h"
#include "graph_message.h"
#include "random_graph.h"
#include "logger.h"
```

Functions

- ostream & [operator<<](#) (ostream &o, const vector< int > &v)
- void [random_graph_test](#) ()
- void [mp_test](#) ()
- int [main](#) ()

7.29.1 Function Documentation

7.29.1.1 main()

```
int main ( )

58     {
59         logger::start();
60         //mp_test();
61         random_graph_test();
62         logger::stop();
63         //random_graph_test ();
64         return 0;
65     }
```

7.29.1.2 mp_test()

```

void mp_test ( )

28     {
29     marked_graph G;
30     ifstream inp("test_graphs/hexagon_diagonal_marked2.txt");
31     inp >> G;
32     //G = marked_ER(10000,0.0003,2 ,2);
33     //G = poisson_graph(100000,3, 10, 10);
34     //cerr << " graph generated " << endl;
35     //cerr << " graph generated " << endl;
36     //cout << " G " << endl << G << endl;
37     colored_graph C(G, 3, 2);
38
39     /*
40     int n = C.nu_vertices;
41     for (int v=0; v<n; v++){
42         cout << v << " : ";
43         for (int i=0;i<C.adj_list[v].size();i++){
44             cout << C.adj_list[v][i].first << " ( " << C.adj_list[v][i].second.first << " , " <<
45             C.adj_list[v][i].second.second << " ) ";
46         }
47         cout << endl;
48     }
49     cout << " message marks " << endl;
50     for (int m=0; m<C.M.message_mark.size(); m++){
51         cout << m << " mark = " << C.M.message_mark[m] << " star " << C.M.is_star_message[m] << endl;
52     }
53     */
54
55 }

```

7.29.1.3 operator<<()

```

ostream& operator<< (
    ostream & o,
    const vector< int > & v )

12                                     {
13     for (int i=0;i<v.size();i++){
14         o << v[i];
15         if (i < v.size()-1)
16             o << ", ";
17     }
18     return o;
19 }

```

7.29.1.4 random_graph_test()

```

void random_graph_test ( )

22     {
23     //marked_graph G = poisson_graph(10, 2, 2, 2);
24     marked_graph G = near_regular_graph(10,2,1,1);
25     cout << G;
26 }

```

7.30 time_series_compression.cpp File Reference

```
#include "time_series_compression.h"
```

7.31 time_series_compression.h File Reference

```
#include <vector>
#include "bipartite_graph.h"
#include "bipartite_graph_compression.h"
```

Classes

- class [time_series_encoder](#)
encodes a time series which is basically an array of arbitrary nonnegative integers
- class [time_series_decoder](#)
decodes a time series which is basically an array of arbitrary nonnegative integers

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