Latent Heating Tendency

- References:
 - o van Heerwaarden, C. C., J. Vilá-Guerau de Arellano, A. Gounou, F. Guichard, and F. Couvreux, 2010: Understanding the daily cycle of evapotranspiration: A method to quantify the influence of forcings and feedbacks. *J. Hydrometeor.*, **11**, 1405–1422, doi: 10.1175/2010JHM1272.1.
 - Stap, L. B., B. J. J. M. van den Hurk, C. C. van Heerwaarden, and R. A. J. Neggers,
 2014: Modeled contrast in the response of the surface energy balance to heat waves for forest and grassland. *J. Hydrometeor.*, 15, 973-989, doi: 10.1175/JHM-D-13-029.1.

• Principle:

o The Penman-Monteith Equation is differentiated in time and decomposed into five main terms; the first two are atmospheric forcings and the remainder are feedbacks:

$$\frac{1}{c_0} \frac{dLE}{dt} = \left\{ \frac{dq_{Sat}}{dT} \left[(1-a) \frac{dS_{\downarrow}}{dt} + \frac{dL_{\downarrow}}{dt} \right] \right\} + \left\{ \left(H \frac{d^2q_{Sat}}{dT^2} + \frac{rc_p}{r_a} \frac{dq_{Sat}}{dT} \right) adv_q - \frac{rc_p}{r_a} adv_q \right\} \\
+ \left\{ \left(H \frac{d^2q_{Sat}}{dT^2} + \frac{rc_p}{r_a} \frac{dq_{Sat}}{dT} \right) \left(\frac{H}{rc_p h} + \frac{w_e Dq}{h} \right) - \frac{rc_p}{r_a} \left(\frac{LE}{rl_v h} + \frac{w_e Dq}{h} \right) \right\} \\
- \left\{ \left(\frac{rc_p}{r_a^2} (q_{Sat} - q) - LE \frac{c_p r_s}{l_v r_a^2} \right) \frac{dr_a}{dt} \right\} - \left\{ \frac{dq_{Sat}}{dT} \frac{dL_{\uparrow}}{dt} + \frac{dq_{Sat}}{dT} \frac{dG}{dt} + LE \frac{c_p}{l_v r_a} \frac{dr_s}{dt} \right\} \\
c_0 = 1 \sqrt{\left[\frac{dq_{Sat}}{dT} + \frac{c_p}{l_v} \left(1 + \frac{r_s}{r_a} \right) \right]}$$

See references for all symbol definitions.

- The five terms, each in {}, are (1) radiative tendency forcings; (2) boundary layer advective forcings; (3) boundary layer feedbacks (surface sensible warming, entrainment warming, surface moistening, and entrainment drying); (4) surface layer feedback; (5) land surface feedbacks (surface OLR, ground heat flux, and stomatal resistance).
- Data needs:
 - o Models often have all needed terms for diagnosis.
- Observational data sources:
 - o Many terms (e.g., r_s , $w_{_{\varrho}}$) are nearly impossible to measure in the field.
- Caveats:
 - o Well suited to SCM or LEM output, possibly GCM or regional model output as well.
 - o Specific terms may be estimated from default model output, but perhaps not all.
 - o If latent heat flux is not calculated in the model using a Penman-Monteith formulation, there will be a discrepancy in the diagnostics.