

Angle measures for an MPT characterisation of a computed toy gun

5th April 2024

Barrel has $\sigma_* = 1.45 \times 10^6$ S/m and μ_r is varied ($\mu_r = 100$ corresponds to carbon steel) and the receiver has 4.5×10^6 S/m and $\mu_r = 1$ and is a stainless steel. The barrel is hollow with a cap at one end. The length of the barrel is 0.2 m, outer and inner radii of the barrel are 0.02 m and 0.01m, respectively. The box representing the receiver is $0.08 \text{ m} \times 0.01 \text{ m} \times 0.15 \text{ m}$. A mesh of 21,132 unstructured tetrahedra, 5,525 prisms and elements of order $p = 0, 1, 2, 3, 4, 5$ are considered. The prisms are chosen to be used as boundary layers in the barrel, which has a smaller skin depth.



Figure 1: Illustration of the toy gun. Barrel has $\sigma_* = 1.45 \times 10^6$ S/m and μ_r is varied ($\mu_r = 100$ corresponds to carbon steel) and the receiver has 4.5×10^6 S/m and μ_r and is a non-magnetic stainless steel.

When the eigenvalue curves cross each other then this indicates the presence of eigenvalues with algebraic multiplicity greater than one. The associated eigenvectors for an eigenvalue with algebraic multiplicity two can be arbitrarily chosen as any two vectors that form a basis for the two-dimensional eigenspace. In numerical computations, the computation of eigenvectors associated with eigenvalues λ_n, λ_m is problematic when $\lambda_n \rightarrow \lambda_m$.

Angles between the computed eigenvectors using the metrics d_R and d_F are considered and the approximations d_E and d_C that do not require knowledge of the eigenvectors. Notice the smooth transition of d_R and d_F in the regions where the eigenvalues are repeated and the associated **peaks**. While we know there are issues with the eigenvectors of repeated eigenvalues, the peaks are interesting as there is a **smooth transition to them**. While d_E and d_C do not capture the peaks well, particularly d_E , the normalising constant involved in the computation do identify the peaks.

Note that d_E and d_C do capture the behaviour of d_R and d_F well for other objects when there are no peaks.

0.1 Barrel with $\mu_r = 20$

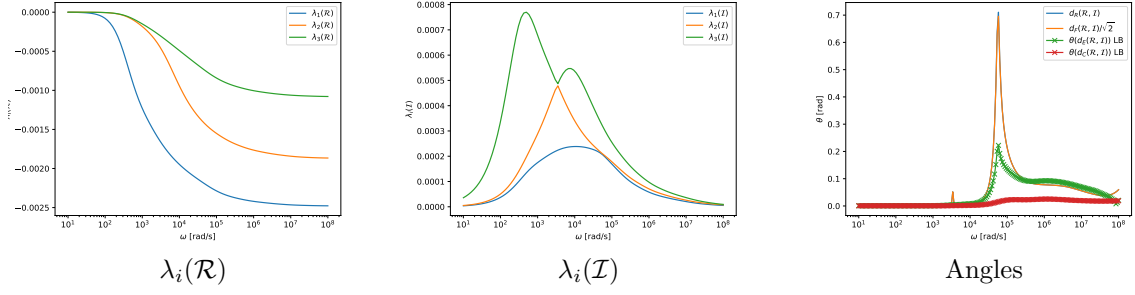


Figure 2: Toy gun with $\mu_r = 20$ in the barrel.

0.2 Barrel with $\mu_r = 40$

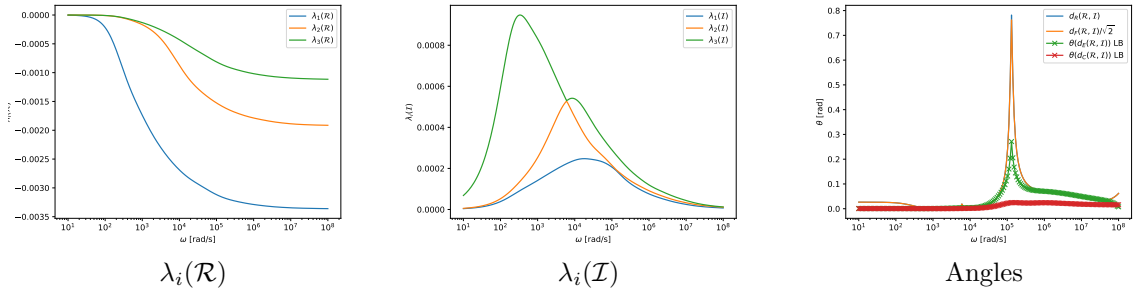


Figure 3: Toy gun with $\mu_r = 40$ in the barrel.

0.3 Barrel with $\mu_r = 80$

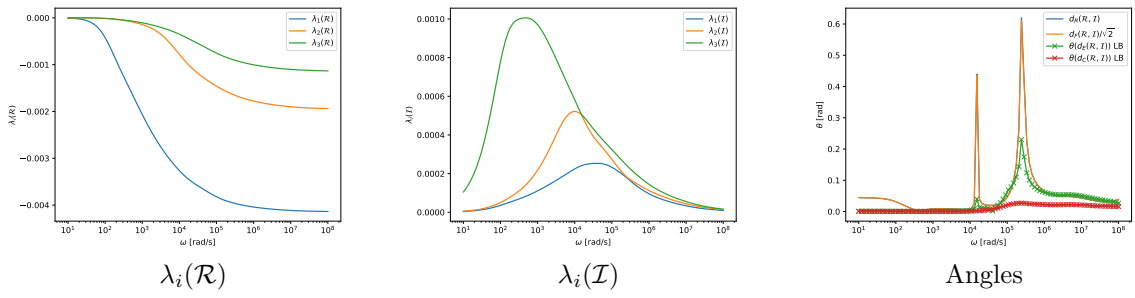


Figure 4: Toy gun with $\mu_r = 80$ in the barrel.

0.4 Barrel with $\mu_r = 100$

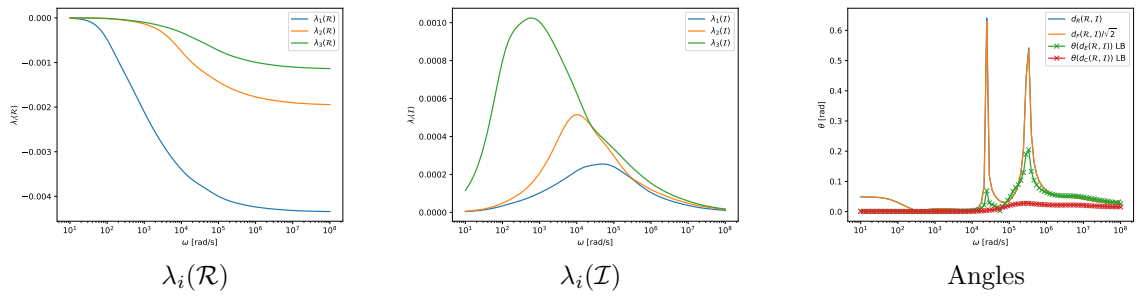


Figure 5: Toy gun with $\mu_r = 100$ in the barrel.