

# L2 REGULARIZED (RIDGE) REGRESSION

WHEN FITTING A MODEL,  
WE CAN "SHRINK" COEFFICIENTS  
TOWARDS ZERO

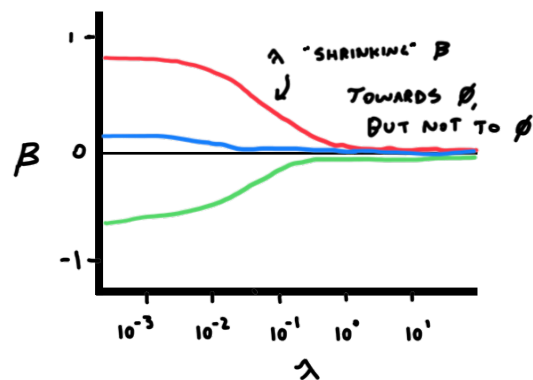
SHRINKING LESS IMPORTANT  
OR REDUNDANT  
FEATURE'S CONTRIBUTIONS

VIA  
 $\lambda \cdot \sum \beta_j^2$   
PENALTY  
ADDED TO  
O.L.S.  
LOSS FUNCTION

LAMDA  
MODULATES  
THE STRENGTH  
OF SHRINKAGE

SUM OF SQUARED  
COEFFICIENTS

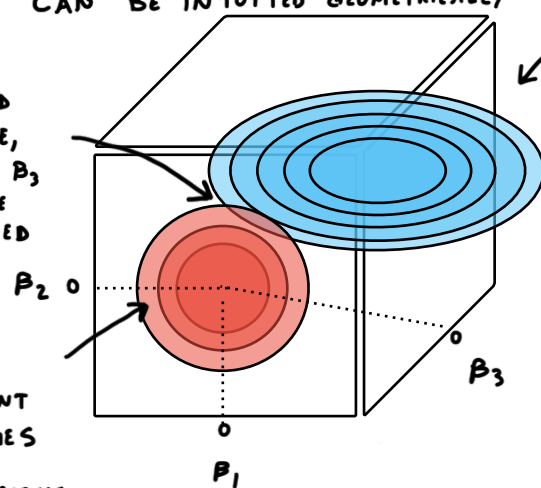
eg. FOR 3 FEATURES



RIDGE REGULARIZATION

CAN BE INTUITED GEOMETRICALLY

MODEL IS SELECTED  
AT THE INTERFACE,  
SUCH THAT  $\beta_1, \beta_2, \beta_3$   
ARE SHRUNK WHILE  
RSS IS MINIMIZED



RIDGE  
CONSTRAINT  
BOUNDARIES  
SMALLER CIRCLE  
= LARGER  $\lambda$

RESIDUAL  
SUM OF (RSS)  
SQUARES  
CONTOURS

SMALLER CIRCLE  
= BETTER MODEL FIT

LASSO HAS A  
TENDENCY TO SELECT  
A "CORNER" OF THE  
POLYHEDRON, INDICATING  
THE SHRINKAGE OF SOME  
 $\beta$  TO 0

# L1 REGULARIZED (LASSO) REGRESSION

WHEN FITTING A MODEL,  
WE CAN "SHRINK" COEFFICIENTS  
TO ZERO

SHRINKING AND/OR ELIMINATING  
LESS IMPORTANT  
OR REDUNDANT  
FEATURE'S CONTRIBUTIONS

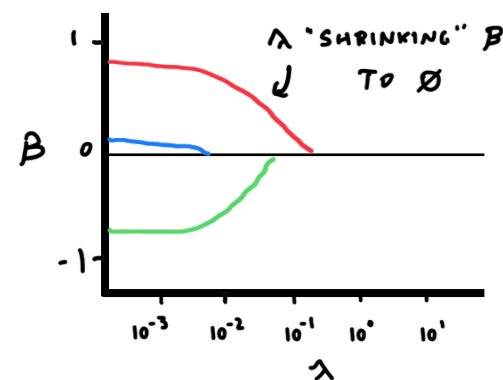
"FEATURE SELECTION"

VIA  
 $\lambda \cdot \sum |\beta_j|$   
PENALTY  
ADDED TO  
O.L.S.  
LOSS FUNCTION

LAMDA  
MODULATES  
THE STRENGTH  
OF SHRINKAGE

SUM OF ABSOLUTE  
COEFFICIENTS

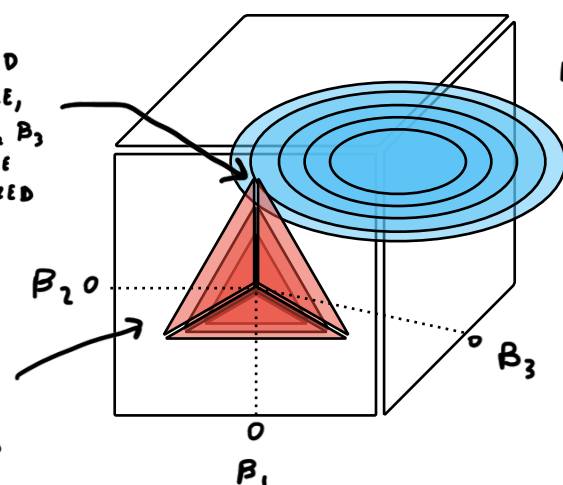
eg. FOR 3 FEATURES



LASSO REGULARIZATION

CAN BE INTUITED GEOMETRICALLY

MODEL IS SELECTED  
AT THE INTERFACE,  
SUCH THAT  $\beta_1, \beta_2, \beta_3$   
ARE SHRUNK WHILE  
RSS IS MINIMIZED



LASSO  
CONSTRAINT  
BOUNDARIES  
SMALLER POLYHEDRON  
= LARGER  $\lambda$

RESIDUAL  
SUM OF (RSS)  
SQUARES  
CONTOURS

SMALLER CIRCLE  
= BETTER MODEL FIT