

# Income Taxation, Firing Cost and Insurance within Firms

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People differ in **initial ability** and face **productivity shocks** along the life cycle.

We want to **redistribute income** and **insure risk**. Typically with income tax.

## What is the role of firms?

Can firms insure their workers? How? Is it desirable?

Important clues:

- Firms have more information than the government.
- Firms can fire, workers can quit.
- Firms help their workers to avoid taxes.

This paper: a theory of optimal taxation with endogenous insurance on the labor market.

# Why are firms important for personal income taxation?

## Firms insure workers

- Lifetime employment: Flabbi and Ichino (2001), Watanabe (2000).
- Predictable income: Guiso, Pistaferri, and Schivardi (2005), Watanabe (2000), Lagakos and Ordonez (2011).

## Firms help workers avoid taxes: income shifting

Kreiner, Leth-Petersen, and Skov (2015, 2014): in Jan 2010 Denmark reduced the top tax rate, which affected 1/4 of all employees.

- 10% of affected income was shifted from Nov/Dec 2009 to Jan 2010.
- Top managers shift both bonuses and salaries.

## Key assumptions

- Every worker has an idiosyncratic productivity which evolves stochastically.
- Workers' productivities are observed by firms, but neither by the government nor financial markets.
- Firms can fire, workers can quit.

## Main results

1. A high firing cost enables insurance within firms.
  2. However, a high firing cost also enables tax avoidance within firms.
    - Firms shift incomes to histories with low marginal tax rates.
- Trade-off between insurance and redistribution
- Low productivity workers may end up uninsured, but with higher transfers.
3. Inclusion of private insurance simplifies tax implementation
    - Tax rates as in Mirrlees (1971), tax on consumption expenditures.

### **Optimal taxation with firms / private insurance markets**

Golosov and Tsyvinski (2007); Chetty and Saez (2010); Stantcheva (2014); Attanasio and Rios-Rull (2000); Krueger and Perri (2011); Ábrahám, Koehne, and Pavoni (2016)

Here: private insurance constrained by commitment, not by information.

### **Simple fiscal implementations**

Albanesi and Sleet (2006); Farhi and Werning (2013); Weinzierl (2011); Findeisen and Sachs (2015); Conesa, Kitao, and Krueger (2009)

Here: private insurance makes the optimal non-linear tax very simple.

### **Firing costs, dual labor markets**

Blanchard and Tirole (2008); Cabrales, Dolado, and Mora (2014); García-Pérez, Marinescu, and Castello (2014); Bentolila, Cahuc, Dolado, and Le Barbanchon (2012); Kosior, Rubaszek, and Wierus (2015)

Here: firing costs affect how workers respond to taxes.

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## Workers

A continuum of workers live for  $\bar{t} \in \mathbb{N}$  periods and have a utility function

$$u(c) - v(n),$$

where  $u'' \leq 0$  and  $v'' > 0$ . They discount future with  $\beta$ .

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In every period each worker draws a productivity from the finite set  $\Theta \subset \mathbb{R}_+$ .

A **history** is a sequence of productivity draws

$$\theta^t = (\theta_1, \dots, \theta_t) \in \Theta^t.$$

History  $\theta^t$  happens with probability  $\mu(\theta^t)$ .

History  $\theta^t$ , conditional on sub-history  $\theta^s$ , happens with probability  $\mu(\theta^t \mid \theta^s)$ .

## Useful sets

$\mathcal{H}$	all possible histories	$\equiv \cup_{t=1}^{\bar{t}} \Theta^t$
$\mathcal{H}(\theta^s)$	all histories containing sub-history $\theta^s$	$\equiv \{\theta^s\} \times \cup_{t=1}^{\bar{t}-s} \Theta^t$



A continuum of identical, risk neutral firms with a linear production technology.

They face exogenous interest rate  $R = \beta^{-1}$ .

# Allocation and payoffs

The allocation  $(c, y, n)$  specifies

- consumption  $c : \mathcal{H} \rightarrow \mathbb{R}_+$ ,
- labor income  $y : \mathcal{H} \rightarrow \mathbb{R}$ ,
- labor supply  $n : \mathcal{H} \rightarrow \mathbb{R}_+$ .

Take some allocation  $(c, y, n)$ .

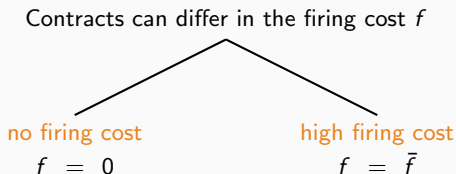
The **expected utility** of the worker with history  $\theta^s$  is

$$U(c, n; \theta^s) \equiv \sum_{\theta^t \in \mathcal{H}(\theta^s)} \mu(\theta^t \mid \theta^s) \beta^{t-s} \left( u(c(\theta^t)) - v(n(\theta^t)) \right). \quad (1)$$

The firm's **expected profit** from hiring the worker with history  $\theta^s$  is

$$\Pi(y, n; \theta^s) \equiv \sum_{\theta^t \in \mathcal{H}(\theta^s)} \mu(\theta^t \mid \theta^s) R^{t-s} \left( \theta_t n(\theta^t) - y(\theta^t) \right). \quad (2)$$

1. Workers enter the labor market after the initial productivity draw.
2. Firms make offers dependent on the initial productivity.
3. Workers observe all offers: a Bertrand competition among firms.



Assumption:  $\bar{f}$  is so high enough s.t. a firm never fires a worker.

Denote by  $f$  the assignment of type of contract to the worker's history

$$f : \mathcal{H} \rightarrow \{0, \bar{f}\}.$$

**Observables:** consumption  $c$ , firing cost  $f$ , labor income  $y$ .

**Unobservables:** individual productivity  $\theta$ , hours worked  $n$ , output  $\theta n$ .

Revelation principle: we can restrict attention to *direct mechanisms*

1. The planner commits to the mechanism  $\{\mathcal{H}, (c, y, f)\}$ .
2. In every period each worker makes a type report  $r \in \mathcal{H}$ .
3. The planner assigns him  $(c(r), y(r), f(r))$ .

The *truthful reporting strategy*  $r^* : \forall_{h \in \mathcal{H}} r^*(h) = h$ .

W.l.o.g. we can restrict attention to pure reporting strategies.

# Labor market equilibrium

Equilibrium consists of reporting strategy  $r$  and labor policy  $n$ .

## Lemma

The set of equilibria of mechanism  $(c, y, f)$  is

$$\mathcal{E}(c, y, f) \equiv \arg \max_{r, n} \sum_{\theta^1 \in \Theta} \mu(\theta^1) U(c \circ r, n; \theta^1)$$

s.t.

$$\text{zero profit:} \quad \forall \theta^1 \in \Theta \quad \Pi(y \circ r, n; \theta^1) = 0$$

$$\text{limited commitment:} \quad \forall \theta^t \in \mathcal{H} \quad -f(r(\theta^t)) \leq \Pi(y \circ r, n; \theta^t) \leq 0$$

Equilibrium policies  $(r, n)$  maximize workers' ex ante utility subject to

1. **zero profit condition**

→ firms cannot redistribute among the initial types.

2. **limited commitment constraints**

→ at no history a worker or a firm have incentives to terminate the contract.

## Social planner's problem

The planner maximizes the social welfare function (with Pareto weights  $\lambda$ )

$$\max_{c, y, f} \sum_{\theta^1 \in \Theta} \lambda(\theta^1) \mu(\theta^1) U(c, n; \theta^1)$$

subject to the **resource constraint**

$$\sum_{\theta^t \in \mathcal{H}} \mu(\theta^t) R^{-t} (y(\theta^t) - c(\theta^t)) \geq 0$$

and the **implementability constraint**

$$(r^*, n) \in \mathcal{E}(c, y, f).$$

The implementability constraint means that:

- there exists an equilibrium with truthful reporting,
- labor supply is determined by the truthful equilibrium.

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### Lemma (Equivalence to NDPF)

*Suppose that the planner sets all firing costs to zero.*

*Firms provide no insurance. The planner's problem is equivalent to New Dynamic Public Finance problem.*

Without firing costs, the limited commitment constraints become

$$\forall_{\theta^t \in \mathcal{H}} \quad \Pi(y, n; \theta^t) = 0 \implies y(\theta^t) = \theta_t n(\theta^t).$$

Income is always equal to output → no insurance within firms.

Conditional on no firing costs, the optimal allocation involves:

- history dependent tax on labor income: Farhi and Werning (2013); Golosov, Troshkin, and Tsyvinski (2016),
- tax on capital income: Golosov, Kocherlakota, and Tsyvinski (2003); Kocherlakota (2005),
- only partial consumption insurance.



### Theorem (High firing costs solve commitment problem)

*With high firing costs, the limited commitment constraints do not restrict the set of implementable allocations of consumption and labor supply.*

Specifically, workers can get full consumption insurance within firms. How?

With high firing costs, limited commitment constraints become

$$\forall_{\theta^t \in \mathcal{H}} \quad \Pi(y \circ r, n; \theta^t) \leq 0.$$

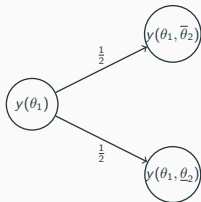
- As long as profits are non-positive,  $y(\theta^t)$  can be  $\neq$  than  $\theta_t n(\theta^t)$ .
- Income payments can be shifted to later periods (backloading).

How to insure workers by backloading income?

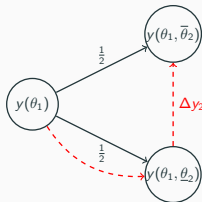
- Pay less today, pay more tomorrow when productivity is low.

# High firing costs: insurance via backloading

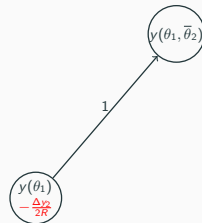
1. Income process without insurance.



2. A firm **shifts** income forward.



3. A deterministic income path.



All this happens without changing the labor supply allocation.

Now income is deterministic, but not constant across time.

How to smooth consumption?

- borrow against future wages: Harris and Holmstrom (1982).
- age/tenure dependent taxation.

### Theorem (High firing costs for top taxpayers)

*An initial type  $\theta^1$  is a top taxpayer if*

$$\theta^1 \in \arg \max_{\theta} \sum_{\theta^t \in \mathcal{H}(\theta)} R^{-t} \mu(\theta^t | \theta) (y(\theta^t) - c(\theta^t)) .$$

*Assigning high firing cost and full consumption insurance to top taxpayers is Pareto improving.*

Assign high firing cost to initial types that pay the highest lifetime taxes.

- Top taxpayers benefit as they are better insured.
- If other types decide to mimic a top taxpayer, they won't be worse off and they will pay higher taxes.

With Markov productivities, result applies to top taxpayers after every history.

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**Conclusion:** It is *never* optimal to set all firing costs to zero.

## Proposition (Redistribution channel)

*Suppose that (i) productivities are iid, (ii)  $u(c) = c^{1-\sigma}/(1-\sigma)$ , (iii) the planner is Rawlsian:  $\lambda(\theta) = 0 \ \forall_{\theta \neq \underline{\theta}}$ .*

*There exists a threshold  $\bar{\sigma} > 0$  such that when  $\bar{\sigma} > \sigma$ , assigning zero firing cost to the initially least productive type  $\underline{\theta}$  is welfare improving.*

Assigning zero firing cost to  $\underline{\theta}$  has two effects:

1. reduces consumption insurance of  $\underline{\theta} \rightarrow$  welfare loss bounded by  $\sigma < \bar{\sigma}$ .
2. relaxes the incentive constraints  $\rightarrow$  strictly positive gain in redistribution.

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## Why are incentive constraints relaxed?

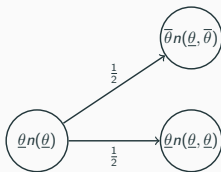
When  $f(\underline{\theta}) = \bar{f}$ , income can be backloaded  $\rightarrow$  mimicker can produce more initially and be paid more than his output in the future.

Mimicker has higher initial productivity, so he likes it!

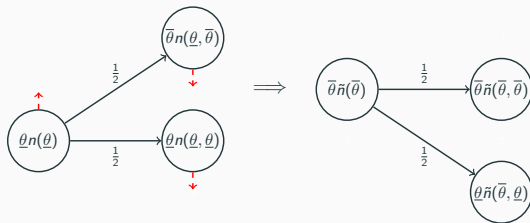
# High firing costs and tax avoidance within firm

$\Theta = \{\underline{\theta}, \bar{\theta}\}, \bar{\theta} > \underline{\theta}$ , two periods.

Allocation of output of  $\underline{\theta}$   
and of mimicker if  $f(\underline{\theta}) = 0$ .



Allocation of output of mimicker when  $f(\underline{\theta}) = \bar{f}$   
Mimicker has incentives to produce more today and less tomorrow



$f(\underline{\theta}) = 0$ : Mimicker has output equal to income at each history.

$f(\underline{\theta}) = \bar{f}$ : Mimicker produces more using higher initial productivity and less in the future. Firm shifts income forward, s.t. income allocation is unchanged.

→ mimicker strictly gains in comparison to  $f(\underline{\theta}) = 0$

# Plan of the presentation

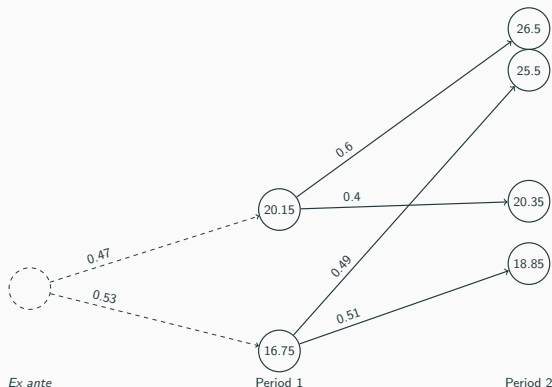
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I estimate a simple income process from Work Histories Italian Panel.



Following Saez (2001), I derive productivities using the actual Italian income tax and the utility function  $u(c) - v(n) = \log(c) - \frac{n^2}{2}$ .



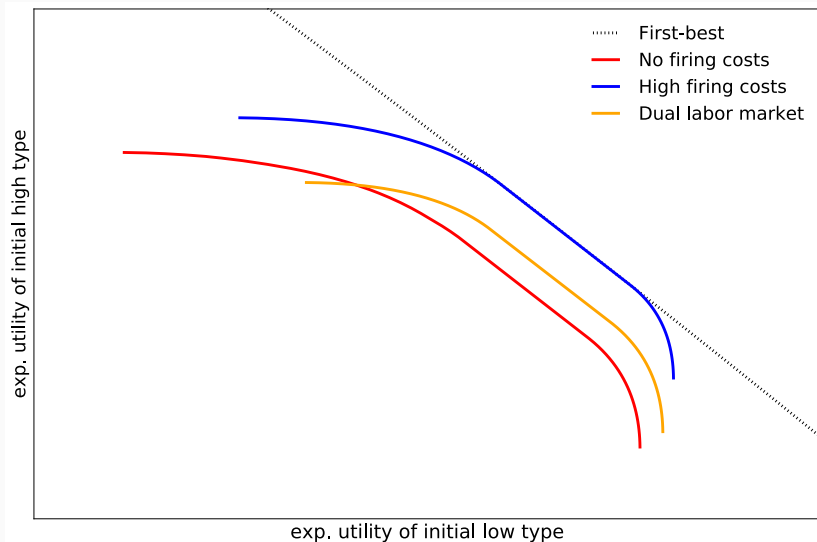
### 3 scenarios

**No firing cost:** both initial types have zero firing cost.

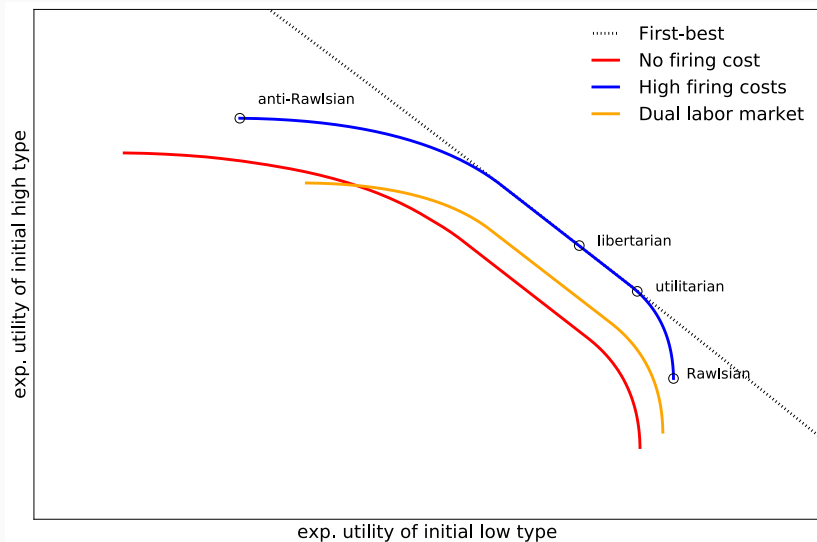
**High firing cost:** both initial types have high firing cost.

**Dual labor market:** Initial high type has high firing cost, initial low type has zero firing cost.

## Pareto frontiers



# Pareto frontiers

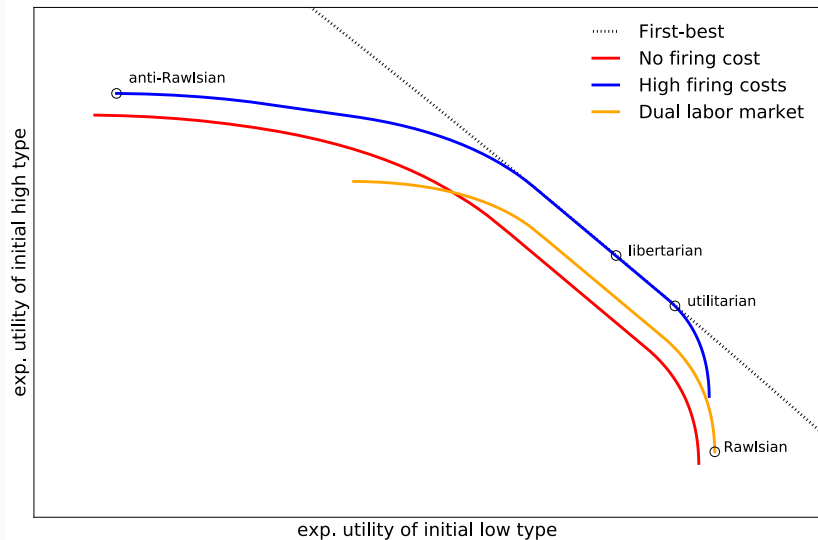


## Large welfare gains from using permanent contracts

Welfare [consumption equivalent]				
	utilitarian	libertarian	Rawlsian	anti-Rawlsian
laissez-faire	100%	100%	100%	100%
no firing costs	102.8%	102.6%	107.2%	105.9%
high firing costs	104.3%	104.1%	108.3%	107.2%
relative gain from high firing costs	53.3%	59.7%	12.9%	20.3%

High firing costs imply large welfare gains especially when the planner is not 'too redistributive'.

## Pareto frontiers with increased initial differences ( $\theta \searrow$ by 5%)



1. Firing costs enable insurance within firms.
2. Firing costs enable tax avoidance within firms as well.
3. Policy implications:
  - high firing costs at high incomes,
  - possibly zero firing costs at low incomes.

Such arrangement maximizes redistribution from high to low incomes.

4. Private insurance simplifies tax implementation: tax rates as in Mirrlees (1971), consumption expenditure tax. [not shown today]