Assignment 3

Write a parallel OpenMP program computing the norm of the product of two $n \times n$ dense matrices on a p-processor SMP so that

- p threads are involved in the parallel computations.
- The 1-dimensional parallel algorithm of matrix multiplication is employed:
 - one of the matrices is partitioned in one dimension into p equal slices
 - there is one-to-one mapping between the partitions and threads
 - each thread is responsible for computation of the corresponding slice of the resulting matrix
- Computation of the norm of the resulting matrix employs the mutex synchronization mechanism.

You can use BLAS or ATLAS for local computations. Experiment with the program and build/plot:

- The dependence of the execution time of the program on the matrix size n.
- The speedup over a serial counterpart of the program.

Explain the results.

Variants of the assignment:

- 1. Granularity of the program:
 - (a) Two successive steps:
 - i. Parallel matrix multiplication
 - ii. Parallel computation of the norm of the resulting matrix
 - (b) One-step algorithm. No intermediate resulting matrix.
- 2. Partitioning scheme:
 - (a) Left matrix is horizontally partitioned
 - (b) Right matrix is vertically partitioned
- 3. Matrix norm to be computed:
 - (a) The maximum absolute column sum norm (aka one-norm):

$$||A||_1 = \max_{0 \le j < n} \sum_{i=0}^{n-1} |a_{ij}|$$

(b) The maximum absolute row sum norm (aka infinity-norm):

$$||A||_{\infty} = \max_{0 \le i < n} \sum_{j=0}^{n-1} |a_{ij}|$$