

# MBA@772

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# Week 1 - Time Value of Money

## Present & Future Values

Present value of future cash flow at time  $t$

$$PV_0 = \frac{FV_t}{(1+r)^t}$$

Present value of annuity with growth

$$PV_0 = PMT_1 \times ADF(t, r, g)$$
$$ADF(t, r, g) = \left[ \frac{1 - \left(\frac{1+g}{1+r}\right)^t}{r - g} \right]$$

Future value of annuity with growth

$$FV_t = PMT_1 \times ACF(t, r, g)$$
$$ACF(t, r, g) = \left[ \frac{(1+r)^t - (1+g)^t}{r - g} \right]$$

Present value of perpetuity with growth

$$PV_0 = \frac{PMT_1}{r - g}$$

## APR, EAR & Converting Rates

The stated annual rate (also known as the APR) is the rate that is stated. It is a fake rate because it does not include the effects of compounding interest. It must be converted to a true rate. The APR is written as \_\_\_\_\_% per year compounded \_\_\_\_\_. You can only divide the APR by the compounding frequency (semi-annual, quarterly, weekly, etc.).

The Effective Annual Yield (EAR) is a true rate and includes the effects of compounding interest. You can NOT divide EAR by 2, 4, 12 to get the semi-annual, quarterly, monthly rate.

If your cash flows are at a different frequency than the compounding frequency, then you need to calculate the EAR and then convert the EAR into the rate that aligns with the frequency that matches the cash flows.

Example:

Your bank offers you a loan of \$100 at an annual rate of 12%, compounded monthly. How much interest would you pay in one year?

Note that the stated rate is 12%. This is our fake rate, i.e. APR=12%.

Since the compounded frequency is monthly, we must calculate the true monthly rate. Our generic formulas are:

$$1 + APR = 1 + \text{monthly rate} \times 12$$
$$1 + EAR = (1 + \text{monthly rate})^{12}$$

Using the APR formula, we have

$$monthly\ rate = \frac{APR}{12} = \frac{12\%}{12} = 1\%$$

The monthly rate of 1% is a true rate that incorporates compounding of interest. We could calculate the interest paid over the course of a year (i.e. over the next 12 1-month periods) as

$$\$100 \times (1 + 1\%)^{12} = \$112.68$$

and we see that we would pay \$12.68 in interest over the course of a year. We could also calculate the EAR using the EAR formula

$$EAR = (1 + monthly\ rate)^{12} - 1 = (1 + 1\%)^{12} - 1 = 12.68\%$$

We could also calculate the interest paid over the course of a year as

$$\$100 \times (1 + 12.68\%)^1 = \$112.68$$

We see that the interest is again \$12.68. We see that the monthly rate and EAR both take into compounding of interest.

## Valuation

Price any asset by discounting its expected future cash flows back at an appropriate, risk adjusted discounted rate

$$Price = \sum_{t=0}^{\infty} \frac{CF_t}{(1+r)^t}$$

## Excel Formulas

$$\begin{aligned} PV &= CF_0 + NPV(r, CF_t) \\ PV &= PV(r, n, PMT, FV) \\ FV &= FV(r, n, PMT, PV) \\ PMT &= PMT(r, n, PV, FV) \\ r &= IRR(CF) \\ r &= RATE(n, PMT, PV) \end{aligned}$$

## Week 2 - Bond Valuation

### Cash flows

- Coupons
  - Payments over time
  - Coupon rate determines the coupon payments
  - $\text{Coupon} = \text{Coupon Rate} \times \text{Face}$
- Face (or par) value
  - Single lump sum payment at bond's maturity
- Coupons & face do not change

### Discount rate

- Yield to maturity (ytm)
- Market rate and can change over time

Note that both the coupon rate and ytm should be treated as stated rates. So if we have a bond with \$1000 face that makes semi-annual payments with a stated annual coupon rate of 6% and annual yield to maturity of 10% then

- 6-month coupon payment =  $\frac{6\%}{2} \times \$1000 = \$30$
- 6-month discount rate for cash flows =  $\frac{10\%}{2} = 5\%$

### Time to maturity

- How long the bond lives

### Price

$$\begin{aligned} \text{Price} &= PV(\text{Cash Flows}) \\ &= PV(\text{Coupons}) + PV(\text{Face}) \\ &= \text{Coupon} \times \left[ \frac{1 - \frac{1}{(1+r)^n}}{r} \right] + \frac{\text{Face}}{(1+r)^n} \end{aligned}$$

- Note we use annuity formula to price coupons and single cash flow formula to price face
- If coupon rate goes up, price goes up (you like getting more future cash flows)
- If ytm goes up, price goes down (you dislike more risk)

### Spot Rates

The  $n$ -year spot rate  $r_n$  is found from a  $n$ -year, zero-coupon bond

$$\text{Price} = \frac{\text{Par}}{(1 + r_n)^n}$$

### Yield Curve

The yield curve plots the spot rates (y-axis) against the time to maturity (x-axis). Shows evolution of spot rates across time.

## Week 3 - Stock Valuation

### Cash flows

- Dividends
  - Payments over time
  - Can be irregular
- Future stock price if sell stock
  - Known as capital gains

### Discount rate

- Cost of equity (sometimes denote  $k_e$ )
- Can decompose total return = capital gains + dividend yield
- $r = g + \frac{D_1}{P_0}$

### Price

Ex-dividend price is the present value today of future dividends paid at time 1, 2, 3, ...

$$\begin{aligned} Price &= PV(\text{Cash Flows}) \\ &= PV(D_1, D_2, D_3, \dots) \\ &= \frac{D_1}{(1+r)^1} + \frac{D_2}{(1+r)^2} + \frac{D_3}{(1+r)^3} + \dots \end{aligned}$$

Note that we cannot write down the infinite summation, so we must make assumptions about the dividends to use our perpetuity formulas

### Constant Growth Model

- Assume dividends grow at a constant rate of  $g$
- $D_{t+1} = D_t \times (1 + g)$
- Note the timing difference in our formula (price today, dividend tomorrow)

$$P_0 = \frac{D_1}{r - g}$$

### Differential Growth Model

- Assume short run dividends followed by long run dividends following constant growth
- To value stock, we need to:
  1. Estimate future dividends in the foreseeable future
  2. Estimate the future stock price when the stock becomes a constant growth stock

Compute the total present value of the estimated future dividends and future stock price at the appropriate discount rate

## Week 4 - Portfolio Theory

### Center

- Mean, average and expected return are synonymous in this section
- Expected Return of an Asset

$$E[R] = \sum_{j=1}^s \text{Prob}_j \times R_j$$

- Expected Return Portfolio

$$E[R_P] = \sum_{i=1}^n w_i \times E[R_i]$$

### Dispersion

- Variance of an Asset

$$\text{Var}(R) = \sigma^2 = \sum_{j=1}^s \text{Prob}_j \times (R_j - E[R])^2$$

- Variance of a Portfolio of Two Assets

$$\sigma_P^2 = w_1^2 \cdot \sigma_1^2 + w_2^2 \cdot \sigma_2^2 + 2 \cdot w_1 \cdot w_2 \cdot \sigma_{1,2}$$

- Standard Deviation

$$\text{SD}(R) = \sigma = \sqrt{\text{Var}(R)} = \sqrt{\sigma^2}$$

### Comovement

- Covariance

$$\text{Cov}(R_1, R_2) = \sigma_{1,2} = \sum_{j=1}^s \text{Prob}_j \times (R_{1,j} - E[R_1]) \times (R_{2,j} - E[R_2])$$

- Correlation
  - Bounded between -1 and 1

$$\text{Corr}(R_1, R_2) = \rho_{1,2} = \frac{\sigma_{1,2}}{\sigma_1 \sigma_2}$$

## Week 5 - CAPM

### CAPM

$$R_i = R_f + \beta_i \times (R_M - R_f)$$

- Required return for asset  $i$ :  $R_i$
- Risk-free asset:  $R_f$
- Asset  $i$ 's beta:  $\beta_i$
- Risk Premium:  $R_M - R_f$

### Security's $\beta$

$$\beta_i = \frac{\text{Cov}(R_i, R_M)}{\text{Var}(R_M)} = \frac{\sigma_{iM}}{\sigma_M^2} = \frac{\sigma_i \sigma_M \rho_{iM}}{\sigma_M^2} = \frac{\sigma_i}{\sigma_M} \rho_{iM}$$

If efficient portfolio (i.e. on CML), then  $\rho_{iM} = 1$  and hence

$$\beta_i = \frac{\sigma_i}{\sigma_M} \rho_{iM} = \frac{\sigma_i}{\sigma_M}$$

Portfolio  $\beta_P$

$$\beta_P = \sum_{i=1}^n w_i \times \beta_i$$

### Capital Market Line

CML: Plot  $R$  vs  $\sigma$

- Slope: Sharpe  $\frac{R_M - R_f}{\sigma_M}$
- An efficient portfolio falls on the CML and hence

$$\begin{aligned} R_i &= R_f + \beta_i \times (R_M - R_f) \\ &= R_f + \frac{\sigma_i}{\sigma_M} \times (R_M - R_f) \\ &= R_f + \sigma_i \times \frac{R_M - R_f}{\sigma_M} \end{aligned}$$

### Security Market Line

SML: Plot  $R$  vs  $\beta$

- Slope:  $RP_M = R_M - R_f$
- $R_i = R_f + \beta_i \times (R_M - R_f)$

Holdings : 13 F / D / G

Sec Ret CRSP

Identify / AUM : ADV

Fund Returns : Com + PP

Activist Lists

Fund Name

Firm Name

Return AUM Monthly

AUM ADV Yearly

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$\boxed{ADV \wedge 13D} = HFAU$

$ADV - AUM$   
 $Com + PP - Ret$

Compare : HFAU vs Com + PP

Coverage : Count, AUM

Performance : Ret (EW, VW) Com vs PP



2,300,000,000,000

6,500,000,000

65 B / 76 B

Blumberg

SG7 Fund, ADV

347 Com

46 PP

10% PP #3,

$$p_{SO} = \frac{val}{mcap} = \frac{p \cdot \overset{2}{shr}}{p \cdot shr}$$

$$adv = \frac{val}{adv} = \frac{p \cdot shr}{p \cdot vol}$$

$$L_1 R_1 + L_2 R_2 = R$$