

Lecture 5



Ambiguity – 1/5

Ambiguity implies the possibility of **different interpretation of a source string**

In natural languages, ambiguity may concern the meaning or syntax category of a word, or syntactic structure of a construct

Eg. A word can have multiple meanings or can be both noun and verb, and a sentence can have multiple syntactic structures



Ambiguity – 2/5

Formal language grammars avoid ambiguity at the level of a lexical unit or a syntax category

This is achieved by the **simple rule that identical strings cannot appear on the RHS of more than one production in the grammar**

Existence of ambiguity at the level of the syntactic structure of a string would mean that more parse tree can be built for the string



Ambiguity – 3/5

Example

$$E \rightarrow E + E \mid E * E \mid \text{id}$$

String is **id + id * id**

Ambiguous grammar since we will have two parse trees



Ambiguity – 4/5

First parse tree

$E \rightarrow E + E$
 $\rightarrow E + E * E$
 $\rightarrow id + E * E$
 $\rightarrow id + id * E$
 $\rightarrow id + id * id$



Ambiguity – 5/5

Second parse tree

$E \rightarrow E * E$
 $\rightarrow E * E + E$
 $\rightarrow id * E + E$
 $\rightarrow id * id + E$
 $\rightarrow id * id + id$



Eliminating ambiguity – 1/2

An ambiguous grammar should be rewritten to eliminate ambiguity

$$\begin{aligned} E &\rightarrow E + T \mid T \\ T &\rightarrow T * F \mid F \\ F &\rightarrow \text{id} \end{aligned}$$

Enforce precedence of * over +



Eliminating ambiguity – 2/2

$E \rightarrow E + T$
 $\rightarrow T + T$
 $\rightarrow F + T$
 $\rightarrow \text{id} + T$
 $\rightarrow \text{id} + T * F$
 $\rightarrow \text{id} + F * F$
 $\rightarrow \text{id} + \text{id} * F$
 $\rightarrow \text{id} + \text{id} * \text{id}$

Examples

Find out if these grammars are ambiguous or not. If ambiguous then convert them into unambiguous grammar

1. $E \rightarrow E + E \mid \text{id}$

2. $E \rightarrow E \text{ or } E \mid E \text{ and } E \mid \text{not } E \mid \text{True} \mid \text{False}$

3. $E \rightarrow E + E \mid E * E \mid E \wedge E \mid \text{id}$

