

QUEUES

→ a kind of list where insertion is done on one side called the rear & deletion is done at the front

REAR → INSERTION

FRONT → DELETION

→ think of the line at the cashier or any other service where its "first come, first serve"

→ First in First out (FIFO)

→ insertLast() & deleteFirst()

QUEUE IMPLEMENTATIONS

① POINTER IMPLEMENTATION

② ARRAY IMPLEMENTATION

③ CURSOR BASED

QUEUE OPERATIONS

1) ENQUEUE (x, Q) inserts element at the rear of Q (insertLast())

2) DEQUEUE (Q) deletes the element at the front of Q (deleteFirst())

3) FRONT (Q) returns the element at the front of Q

4) EMPTY (s) returns non-zero value if empty

5) INITIALIZE (s) initialize the queue to be NULL to be used for the first time.

QUEUE - POINTER IMPLEMENTATION

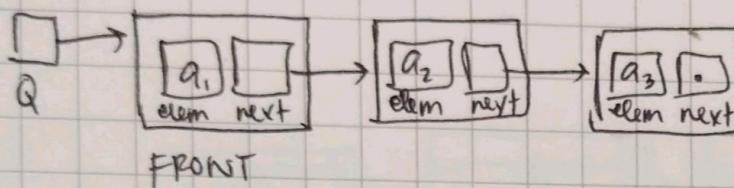
VERSION 1 - QUEUE is a pointer to a self referencing structure

Two views:

- The front element is stored at a cell pointed to be Q

ENQUEUE
insertlast()

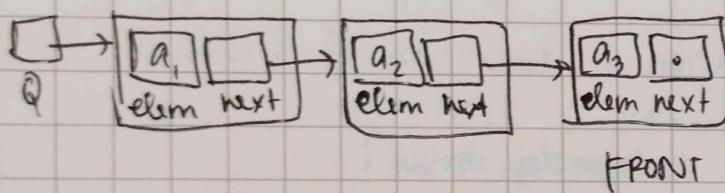
DEQUEUE
deletefirst()



$O(n)$

$O(1)$

- Front element is stored in a cell whose field is NULL



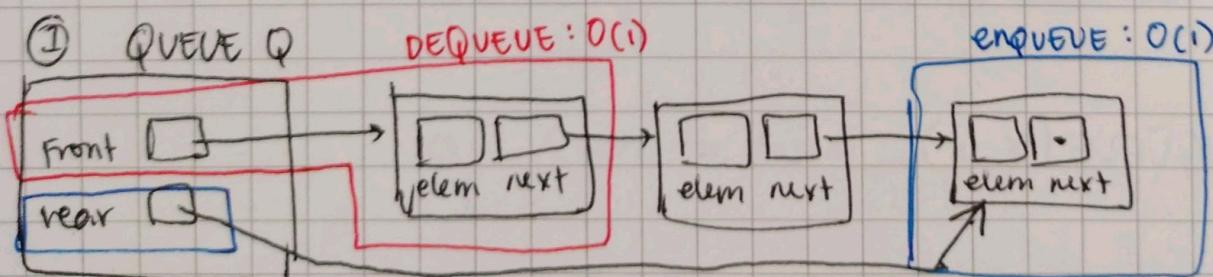
$O(1)$

$O(n)$

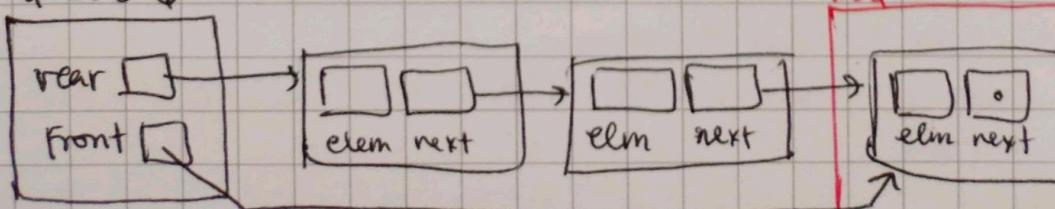
Both versions have the same running time.

VERSION 2 - QUEUE is a structure containing both front & rear pointers.

TWO VIEWS:



② QUEUE Q



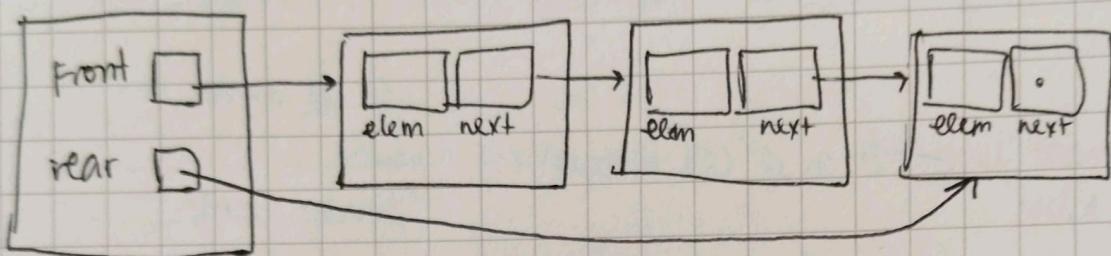
view 1: only need to insertLast() at rear and deleteFirst()
at front. ✓

view 2: ~~The node pointed to be front will be deleted,
needs to traverse in order to reach front, which will
be deleted - making the previous node inaccessible~~

X

PRACTICE EXERCISE

QUEUE Q



Q Write the appropriate declaration & definition of QUEUE Q.

ANS.

```
typedef struct node {  
    char elem;  
    struct node * next;  
} node;
```

```
typedef struct {  
    node * Front, * rear;  
} QUEUE;
```

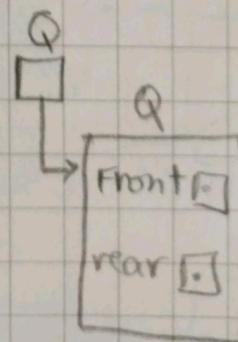
QUEUE Q;

Q WRITE the code of the queue operations.

ANS.

A] initQueue()

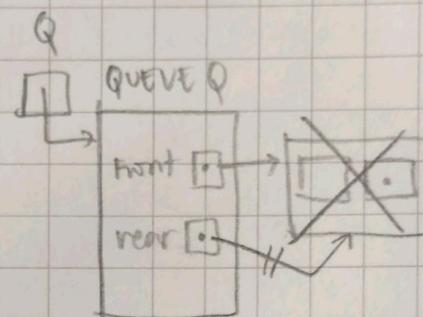
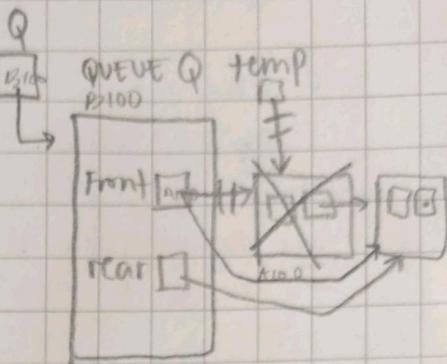
```
void initQueue(QUEUE * Q){  
    Q->Front = NULL;  
    Q->rear = NULL;  
}  
// code so that the queue  
can be used for the first  
time
```



C] DEQUEUE(Q) ≈ delete from the front

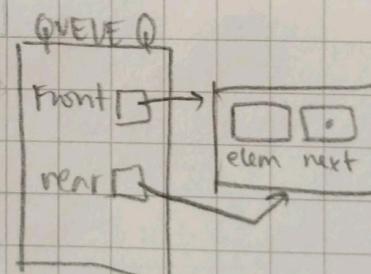
```
void dequeue(QUEUE *Q){  
    node temp;  
    if(Q->front != NULL){  
        temp = Q->front;  
        Q->front = temp->next;  
        free(temp);  
    }  
}
```

```
}  
if(Q->front == NULL){  
    Q->rear = NULL;  
}  
}
```



D] FRONT(Q) return the element at the front of queue

```
char front(QUEUE Q){  
    return (Q.front != NULL)?  
        (Q.front)->elem : '\0';  
}
```



E] EMPTY(Q) return nonzero value if empty

```
int isEmpty(QUEUE Q){  
    return (Q.front == NULL && Q.rear == NULL)? 1 : 0;
```

QUEUE - ARRAY IMPLEMENTATION

VARIATION 1

QUEUE Q

	Elem	
0	H	Front
1	O	
2	P	
3	E	
4	Y	Front
5		rear
6		
7		

For instance,

Enqueue 'y':

- ① check for available space
- ② increment rear
- ③ insert the element

QUEUE Q

	Elem	
0	H	Front
1	O	
2	P	
3	E	
4	Y	Front
5	Y	rear
6		
7		

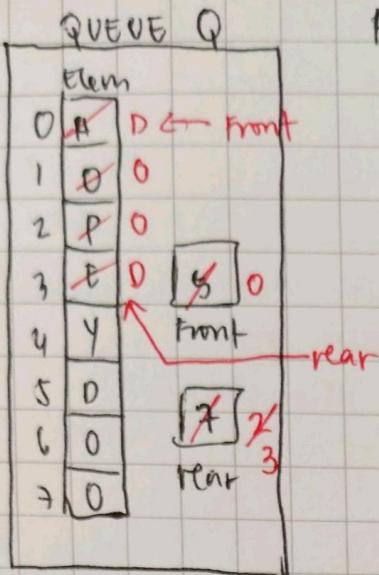
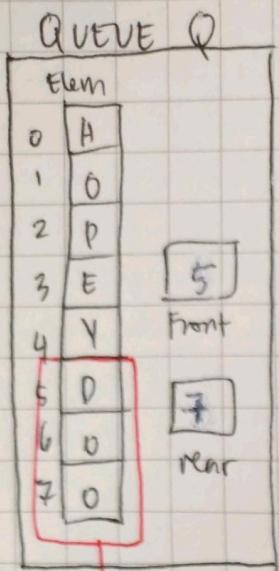
Now,

Dequeue (Q):

- ① check if the queue is not empty
- ② shift elements
- ③ decrement rear

Still physically at index
4 but it is no longer part
of the logical queue

VARIATION 2



For instance,

Enqueue 'D':

- ① check for available space
(no space)
- ② if rear = MAX - 1 & front != 0
then shift the elements
- ③ Adjust front & rear
- ④ increment rear
- ⑤ insert the element

→ the elements that are in the logical queue.

CIRCULAR ARRAY IMPLEMENTATION

- a solution to avoid shifting in array implementation of queues.

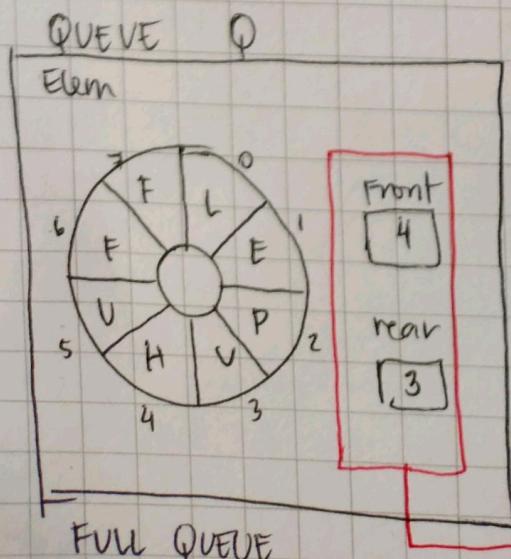
* declared like any other array in C
* "circular orientation"

↳ referring to the way we manipulate the array

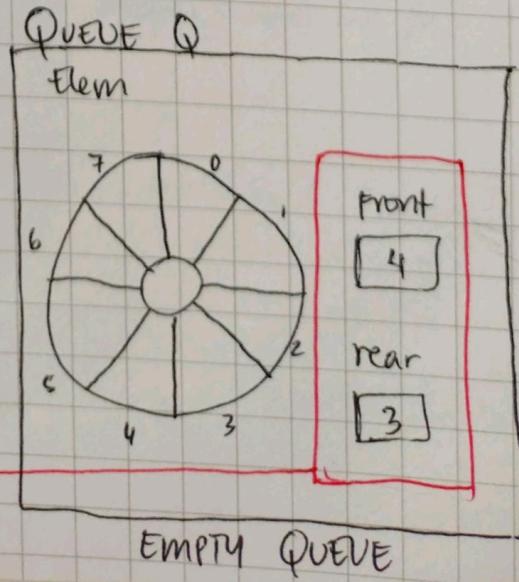
* "circular" → the array has no definite beginning nor end.

The First element can be stored anywhere.

* COUNTER CLOCKWISE or CLOCKWISE direction of insertion are both possible.



Both FULL & EMPTY have the same values for front & rear.



Front & rear can't be the same in both situations.

How can we differentiate between FULL & EMPTY?

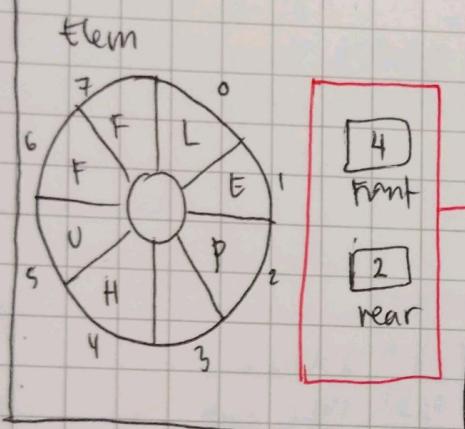
2 Solutions:

① Counter variable

② sacrifice 1 cell ($\text{full} = \text{MAX} - 1$ elements instead of $\text{full} = \text{MAX}$ elements)

So, a full queue will look like this,

QUEUE Q

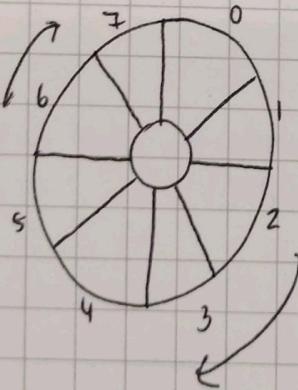


FULL QUEUE

EMPTY

REAR	FRONT
0	1
1	2
2	3
3	4
4	5
5	6
6	7
7	0

MAX = 8



FULL

REAR	FRONT
0	2
1	3
2	4
3	5
4	6
5	7
6	0
7	1

To move:

$$(rear + 1) \% \text{ MAX} \\ = \text{Front}$$

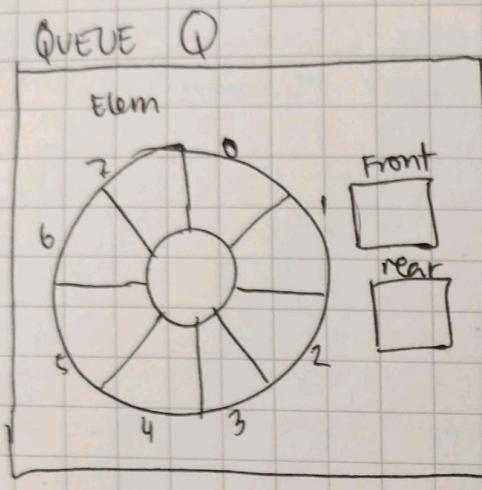
$$\text{Front} = (\text{front} + 1) \% \text{ MAX}$$

$$(rear + 2) \% \text{ MAX} = \text{front}$$

PRACTICE PROBLEM

- Q) 1) Write the appropriate declaration of the circular array
 2) Write the code of the queue operations.

ANS.



#define MAX 8

```
typedef struct {
    char Elem[MAX];
    int front, rear;
} QUEUE;
```

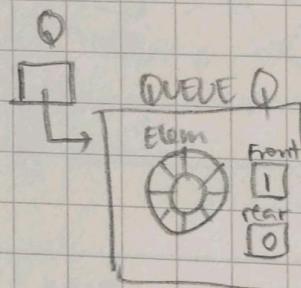
QUEUE Q;

A] initQueue()

```
void initQueue(QUEUE *Q) {
    Q->front = 1;
    Q->rear = 0;
}
```

* going CLOCKWISE

* EMPTY QUEUE = front is ahead
of rear by 1.



is Empty & is Full () are both needed to check the state of the queue

isFull()

```
int isEmpty(QUEUE Q) {
    return ((Q.rear + 1) % MAX
            == Q.front) ?
        1 : 0;
}
```

EMPTY

↳ front is ahead of
rear by one cell

int isFull(QUEUE Q) {

```
return ((Q.rear + 2) % MAX
        == Q.front) ? 1 : 0;
}
```

FULL

↳ Front is ahead of rear
by two cells

C] ENQUEUE (Q, x)

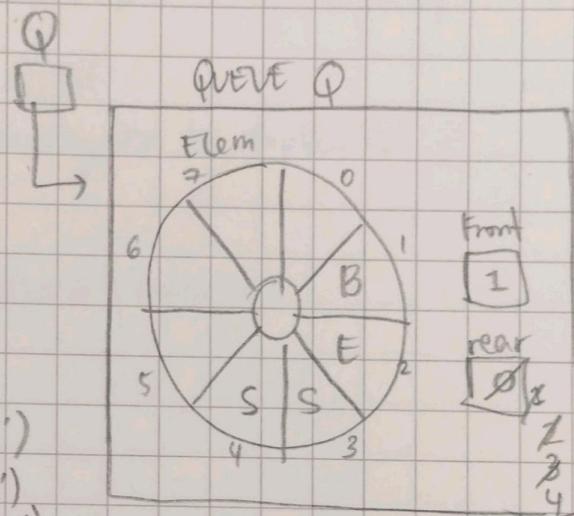
```
void enqueue (QUEUE *Q, char elem)
if (isFull (*Q) != 1) {
    Q->rear = (Q->rear + 1) % MAX;
    Q->Elem [Q->rear] = elem;
```

{ } { }

SUBTASKS

- ① check if Queue is full
- ② increment rear
- ③ Insert the element

```
enqueue (&Q, 'B')
enqueue (&Q, 'E')
enqueue (&Q, 'S')
enqueue (&Q, 'S')
```



D] DEQUEUE (Q)

```
void dequeue (QUEUE *Q) {
    if (isEmpty (*Q) != 1) {
        Q->Front = (Q->Front + 1) % MAX; // incrementing front
                                            // removes the 1st index
                                            // of the queue from the
                                            // logical list.
```

E] FRONT (Q)

```
void front (QUEUE Q) {
    return (isEmpty (Q) != 1) ? Q.Elem [Q.Front] : '\0';
```

F] display Queue (Q)

```
void displayQueue (QUEUE Q) {  
    int ndx;  
    if (isEmpty (Q) != 1) {  
        for (ndx = Q.front; ndx != (Q.rear + 1) % MAX;  
             ndx = (ndx + 1) % MAX)  
            printf ("%c", Q.elem[ndx]);  
    }  
}
```