

STACKS & QUEUES

STACKS

- a kind of list where insertions & deletions take place at the top
- think of a stack of pancakes or an execution stack
- First in, last out / last in, first out
- insertFirst() & deleteFirst()

The challenge of stack is finding where the "top" of our list is located in our datatype.

STACK IMPLEMENTATIONS

- ① ARRAY IMPLEMENTATION
- ② LINKED LIST
- ③ CURSOR BASED

STACK OPERATIONS

1) PUSH (x, s) inserts element at the top of the stack (insertFirst)

2) POP (s) deletes the element at the top of the stack (deleteFirst)

3) TOP (s) returns the element at the top of the stack

4) EMPTY (s)
 FULL (s) returns non-zero value if empty
 returns non-zero value if full

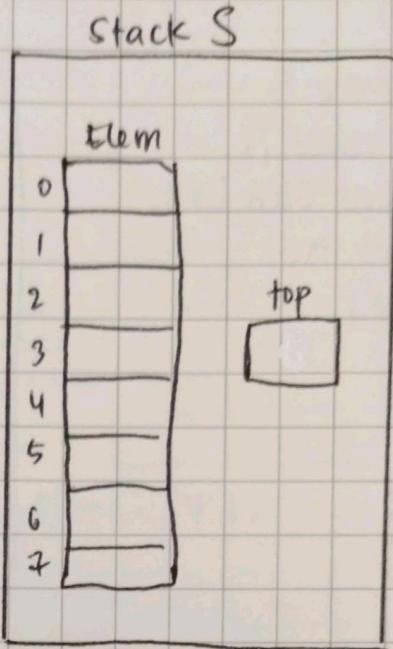
5) INITIALIZE (s) only applicable for array / cursor based implementation initializes the stack to be NULL so it can be used for the first time

STACKS - ARRAY IMPLEMENTATION

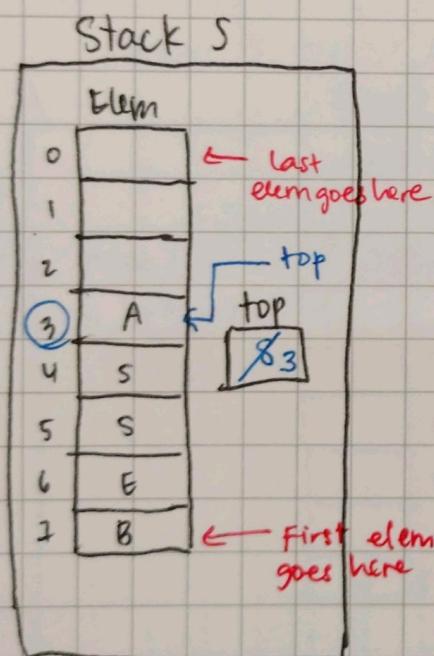
```
#define MAX 8
typedef struct {
    char elem[8];
    int top;
} Stack;
```

* TWO VIEWS

- ① STACK GROWS FROM MAX-1 to 0
- ② STACK GROWS FROM 0 to MAX-1.



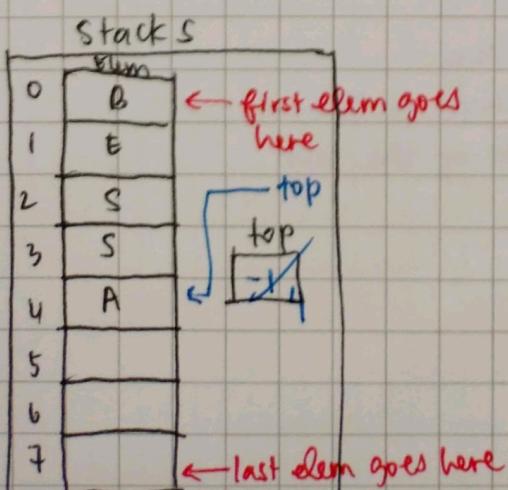
VIEW 1 - STACK GROWS FROM MAX-1 to 0.



Empty stack \rightarrow top = MAX
 Full stack \rightarrow top = 0
 $\text{push}(x, s) \rightarrow$ top decrements
 $\text{insertFirst}(x, s)$
 $\text{pop}(x, s) \rightarrow$ top increments.

STACK GROWS FROM 0 to MAX-1 - VIEW 2

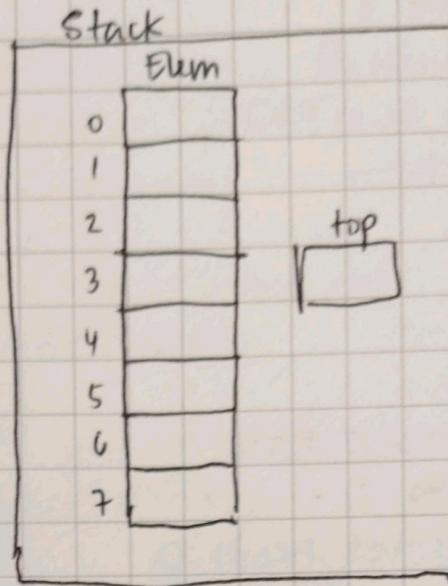
Empty stack \rightarrow top = -1
 Full stack \rightarrow top = MAX-1
 $\text{push}(x, s) \rightarrow$ top increases
 $\text{pop}(x, s) \rightarrow$ top decreases



PRACTICE PROBLEM

Q. WRITE THE CODE OF THE FOLLOWING STACK OPERATIONS ASSUMING
STACK WILL GROW FROM MAX-1 TO 0.

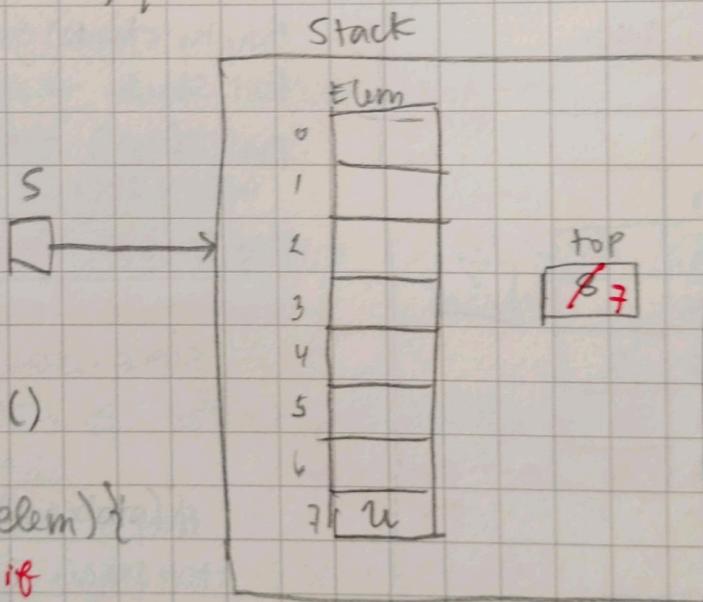
```
#define MAX 8
typedef struct {
    char Elm[8];
    int top;
} stack;
```



ANS

A] INITIALIZE

```
void initializeStack(Stack *S) {
    S -> top = MAX;
}
```



B] PUSH (x,S) ~ insertFirst()

```
void push(Stack *S, char elem) {
    if (S->top != 0){ // checks if
        there is still space
        S -> top--;
        S -> Elm[S -> top] = elem; // assigning
    }
}
```

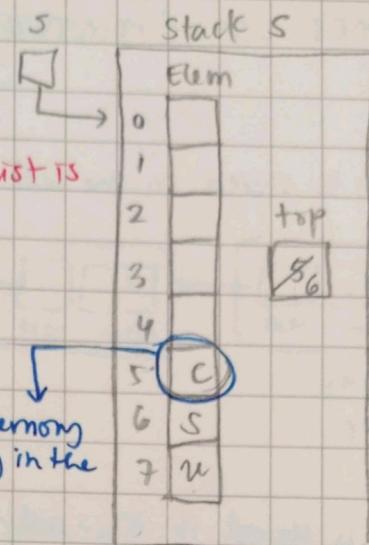
data
u

the element to the
top index of the list

→ when element is inserted,
the top of the list moves up

C] POP (S) ≈ deleteFirst ()

```
void pop(stack *S){  
    if(S->top != MAX)?  
        S->top++;  
    }  
    //checks if list is  
    empty.
```



D] TOP (S)

```
char top(stack S){  
    return (S.top == MAX)? '10', S.Elem[S.top];  
    }  
    // returns a  
    // char sentinel value  
    // if stack is empty
```

E] EMPTY (S)

```
int isEmpty(S){  
    return (S.top == MAX)? 1:0;  
    }
```

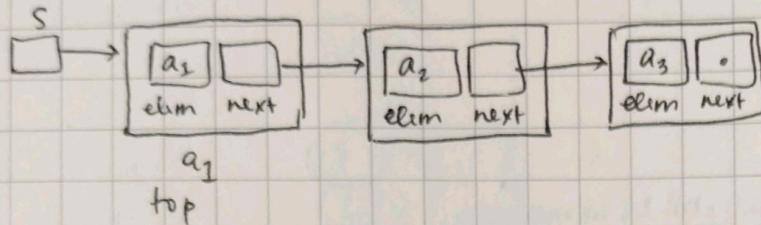
F] FULL (S) ↳ only applicable to array & cursor based.

```
int isFull(S){  
    return (S.top == 0)? 1:0;  
    }
```

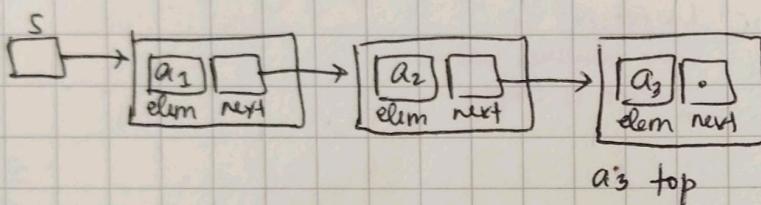
STACK - LINKED LIST (POINTER IMPLEMENTATION)

* TWO VIEWS:

- ① Top elem is stored in the cell pointed to by stack pointer S



- ② top elem is stored in the cell whose field is NULL



The goal is to have $O(1)$ running time. $O(n)$ is worst case scenario.

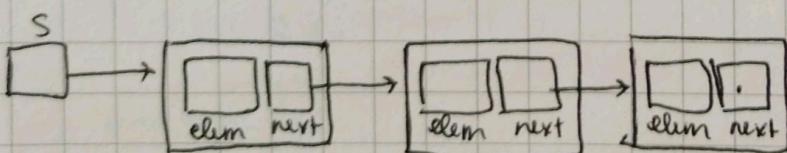
view ①: only need to insert & deleteFirst, no traversal.

Running time = $O(1)$ ✓

view ②: needs traversal first in order to insertFirst & deleteFirst().

Running time = $O(n)$ X

PRACTICE EXERCISE



Q. Write the datatype of Stack S & write the code of the Stack operations.

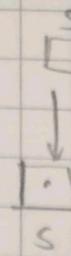
ANS. `typedef struct node {
 char elem;
 struct node * link;
} * Stack;`

Stack operations:

A] INITIALIZE

```
void initialize (Stack *S) {  
    *S = NULL;
```

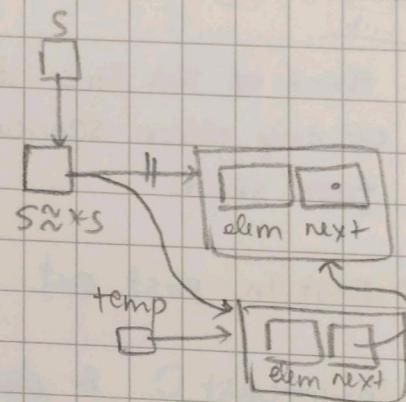
}



B] PUSH (x, S) \approx insertFirst()

```
void push (Stack *S, char data) {  
    Stack temp;  
    temp = (Stack) malloc (sizeof (struct node)); temp  
    if (temp != NULL) {  
        temp->elem = data;  
        temp->link = *S;  
        *S = temp;
```

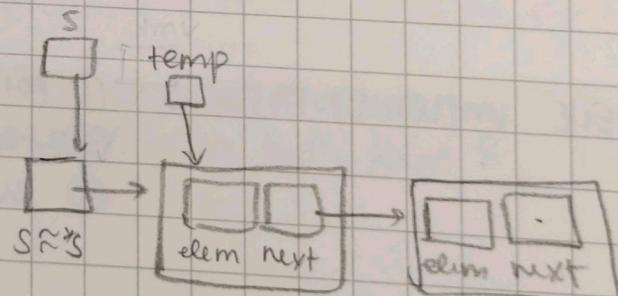
}



C] POP (S) \approx deleteFirst()

```
void pop (Stack *S) {  
    Stack temp;  
    if (*S != NULL) {  
        temp = *S;  
        *S = temp->next;  
        free (temp);
```

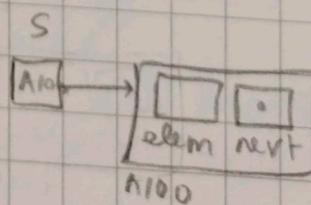
}



D] TOP (S)

```
char top (Stack S) {  
    return (S != NULL)? S->elem : '\0';
```

}



E] empty(s)

```
int isempty (s) {  
    return (*s == NULL)? 1:0;
```