

## -STACK & QUEUE -

### • Kinds of List

- 1.) Stack
- 2.) Queue
- 3.) Deque (double-ended queue)

### \* Stack

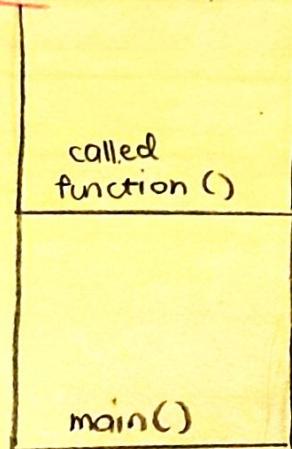
"Last in, First Out"

- special kind of list in which all insertions & deletions take place at one place: **top**
- pushdown list

### \* Operations

- 1.) PUSH ( $x, s$ ) - insert element  $x$  at the top of the stack
- 2.) POP ( $s$ ) - delete top element of stack  $s$
- 3.) TOP ( $s$ ) - returns element at the top of stack  $s$
- 4.) EMPTY ( $s$ ) - returns TRUE if stack is empty, otherwise
- 5.) FULL ( $s$ ) - returns TRUE if stack is full
- 6.) INITIALIZE ( $s$ ) & MAKENULL ( $s$ )

\* fn() A.R. is added  
last but will be removed  
first when fn. terminates.



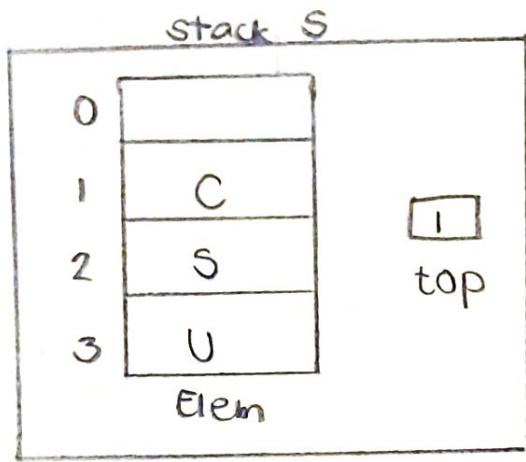
Execution Stack

### \* Implementations

- 1.) Array
- 2.) Linked List
- 3.) CB List

# - ARRAY IMPLEMENTATION - (STACK)

DATE:



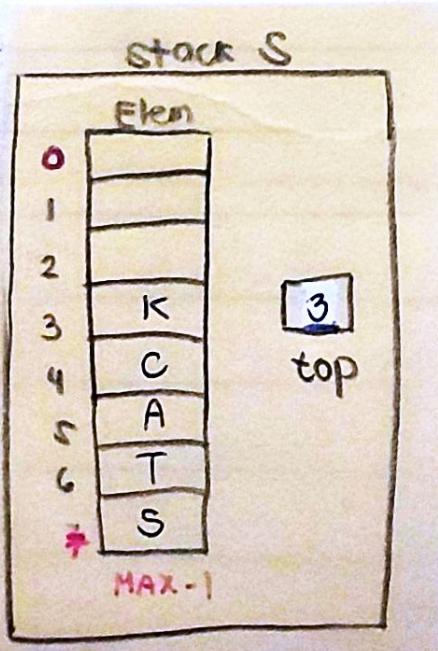
## \* Definition

```
#define MAX 4
```

```
typedef struct {  
    char Elem [MAX];  
    int top;  
} Stack;
```

## \* Two Views

- View 1 - Stack will grow from MAX-1 to 0.



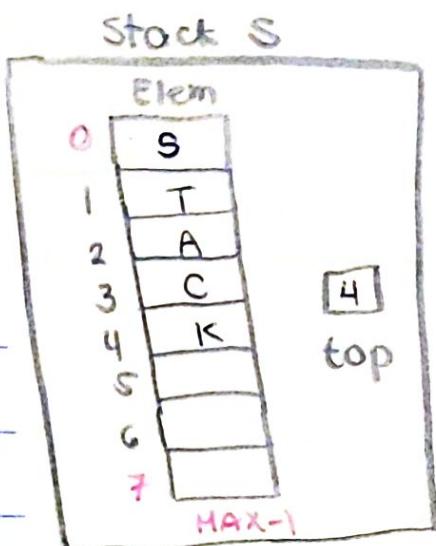
- scenario:

- 1.) Empty stack  $\rightarrow$  top is MAX
- 2.) Full stack  $\rightarrow$  top is 0
- 3.) PUSH(x, s)  $\rightarrow$  top decreases
- 4.) POP(s)  $\rightarrow$  top increases

$$[7] = \text{MAX}$$

\* this view starts with top at MAX  
\* will increase/decrease from there.

• VIEW 2 - stack will grow from 0 to MAX-1 ↓



• scenario:

1.) Empty Stack → top is -1

2.) Full Stack → top is MAX-1

3.) PUSH (X, S) → top increases,

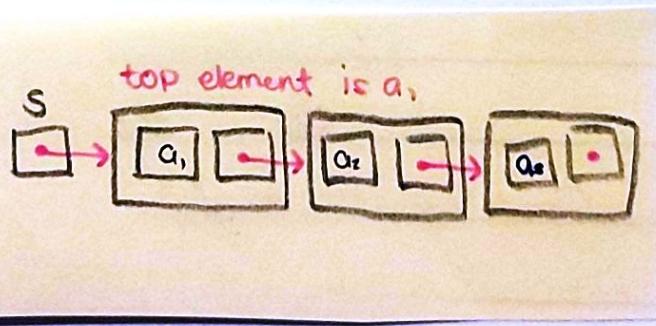
4.) POP (S) → top decreases

\* top starts at 0 & increases/decreases  
from there.

\* the whole point of stack is to AVOID SHIFTING!

## -LINKED LIST IMPLEMENTATION- (STACK)

\* Top element is stored in the cell pointed to by,  
Stack pointer S.



-This orientation is O(1) because it does not  
require traversing to access the top element.

So, all insertion & deletion (PUSH, POP),  
happens at the START of the list.

## - STACK OPERATIONS -

NO. \_\_\_\_\_  
DATE: \_\_\_\_\_

### // initialize (S)

(MAX-1 to 0) ↑

(ARRAY LIST)

void initialize (stack \*S){

S → top = MAX;

}

Definition:

typedef struct {

char elem [MAX];

int top;

} Stack;

### // PUSH (x, S)

void PUSH (stack \*S, char elem) {

if (isFull (\*S) == 0) {

S → top --;

}

S → elem [S → top] = elem; \* increase top &

insert element

}

### // POP (S)

void POP (stack \*S) {

if (isEmpty (\*S) == 0) {

S → top ++;

}

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\* POP the stack by  
decrementing top.

no need to return anything  
unless specifically required.

### // TOP (S)

char TOP (stack \*S) {

return (isEmpty (\*S) == 0)? elem [S → top] : '0';

\* if stack is empty,  
return a sentinel char value!

//isEmpty()

\*should be BEFORE all other fns. since you use it later

```
int isEmpty (Stack S) {
```

```
    return (S.top == MAX)? 1: 0;
```

}

\*return 0 if stack  
IS NOT full.

(3) H264

//isFull()

```
int isFull (Stack S) {
```

```
    return (S.top == -1)? 1: 0;
```

}

\*return 1 if stack IS FULL.  
since stack is from MAX-1 to 0,  
going past 0 means stack is full.

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//displayStack()

```
void displayStack (Stack S) {
```

```
    Stack temp;
```

```
    initialize (&temp);
```

\*since its just pass by

copy, the actual OG  
stack is left untouched

```
    if (isEmpty (S) == 0) {
```

```
        while (isEmpty (S) == 0) {
```

after dumping its

```
        printf ("%c", top (S));
```

contents in temp!

```
        push (&temp, top (S));
```

```
        pop (&S);
```

① Declare & initialize temp variable.

- this will hold the values of stack S  
after we "dump" the contents  
since we CAN'T traverse.

② Check if stack is empty.

③ While its not empty, print the top  
element, one by one.

- store it inside temp after printing.

- Decrement S<sup>(top)</sup> to move to next  
element.

push (&temp, top is )

## //insertBottom() - insert new element at bottom of stack

void insertBottom (Stack \*S, char elem) {

    Stack temp;

    initialize (&temp);

    if (isFull (\*S) == 0) {

        while (isEmpty (\*S) == 0) {

            push (&temp, top (\*S)); } DUMPING

            pop (S);

}

    push (S, elem); → INSERT

    while (isEmpty (temp) == 0) {

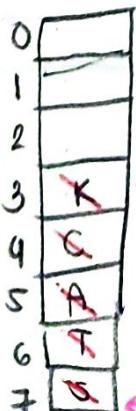
        push (S, top (temp)); } RETURN

        pop (&temp); } VALUES

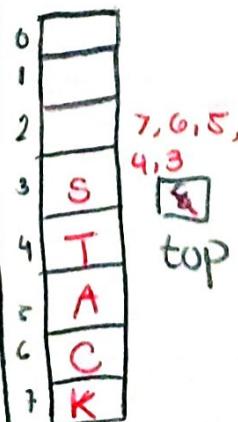
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Stack S



Stack temp



Simulation:

① Dumping (push & pop)

(1)  $\text{temp} \rightarrow \text{top} = 7$   
 $\text{temp}[7] = \text{K}$

$S \rightarrow \text{top} = 4$

(2)  $\text{temp} \rightarrow \text{top} = 6$   
 $\text{temp}[6] = \text{C}$

$S \rightarrow \text{top} = 5$

(3)  $\text{temp} \rightarrow \text{top} = 5$   
 $\text{temp}[5] = \text{A}$   
 $S \rightarrow \text{top} = 6$

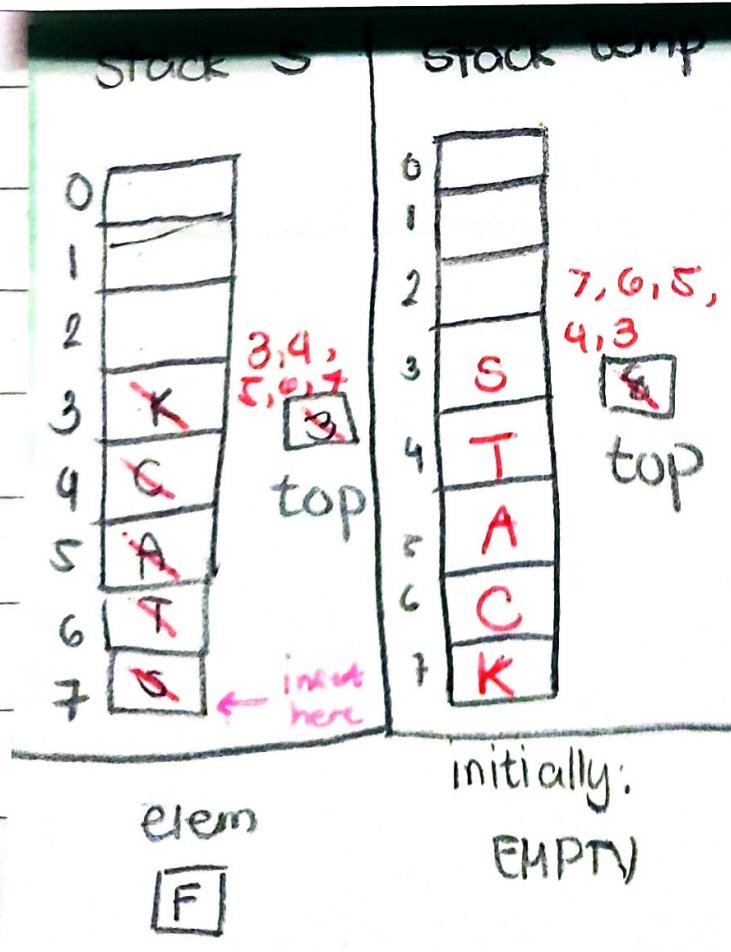
(4)  $\text{temp} \rightarrow \text{top} = 4$   
 $\text{temp}[4] = \text{T}$   
 $S \rightarrow \text{top} = 7$

initially:

EMPTY

elem  
 F

- ① Declare & initialize temp variable to hold 'dumped' values from S.
  - ② Check if S is full (check if there is space available for insertion).
  - ③ while S is NOT empty, dump each element into temp list/variable and decrement S as you go.
  - ④ When list is empty, insert new elem. This is now at the bottom.



Simulation:  
④ Dumping (push & pop)

- (1) temp  $\rightarrow$  top = 7  
temp[7] = R

S  $\rightarrow$  top = 4

(2) temp  $\rightarrow$  top = 6  
temp[6] = C

S  $\rightarrow$  top = 5

(3) temp  $\rightarrow$  top = 5  
temp[5] = A

S  $\rightarrow$  top = C

(4) temp  $\rightarrow$  top = 4  
temp[4] = T

S  $\rightarrow$  top = 7

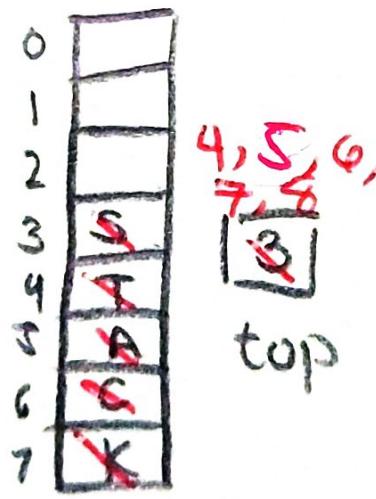
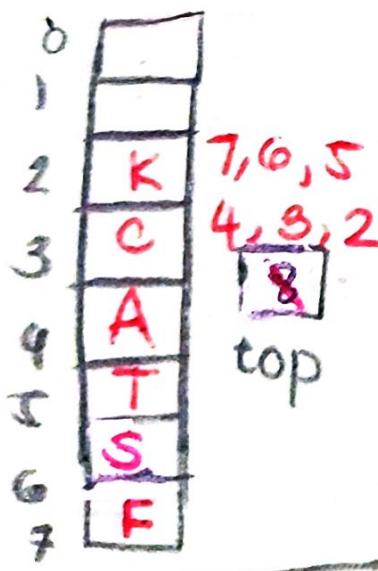
⑤ Reinsert values back into S from temp.

⑥ → DONE.

Stack S		Stack temp	Simulation:
0		0	① Dumping (push & pop)
1		1	(1) $\text{temp} \rightarrow \text{top} = 7$
2		2	$\text{temp}[7] = R$
3	X	3	$S \rightarrow \text{top} = 4$
4	C	4	(2) $\text{temp} \rightarrow \text{top} = 6$
5	A	5	$\text{temp}[6] = C$
6	T	6	$S \rightarrow \text{top} = 5$
7	K	7	(3) $\text{temp} \rightarrow \text{top} = 5$
			$\text{temp}[5] = A$
			$S \rightarrow \text{top} = 4$
			(4) $\text{temp} \rightarrow \text{top} = 4$
			$\text{temp}[4] = T$
			$S \rightarrow \text{top} = 3$

elem  
F

initially:  
EMPTY



initially  
EMPTY

(5)  $\text{temp} \rightarrow \text{top} = 3$   
 $\text{temp}[s] = 5$   
 $s \rightarrow \text{top} = 8$

(6)  $s \rightarrow \text{top} = \text{MAX}(8)$   
so STOP! List is empty.

④ Insert Element

$s \rightarrow \text{top} = 7$   
 $s[7] = 'F'$

⑤ Reinsert values

final: 5 [2] temp [8]

## - STACK OPERATIONS -

(0 to MAX-1)

(LINKED LIST)

NO:

DATE:

### // initialize (s)

```
void initialize (Stack *S){
```

```
*S = NULL;
```

}

### Definition:

```
typedef struct node{  
    char data;  
    struct node *link;  
} *stack;
```

### // PUSH (s, x)

```
void PUSH (stack *S, char elem) {
```

```
    Stack temp;
```

```
    temp = (stack) malloc (sizeof (struct node));
```

\* basically insertFirst()

```
    if (temp != NULL) {
```

```
        temp->data = elem;
```

```
        temp->link = S;
```

```
*S = temp;
```

}

① Declare & malloc temp node.

- Holds new data-

② Check if malloc is successful & no need to check for available space in list since its linked list.

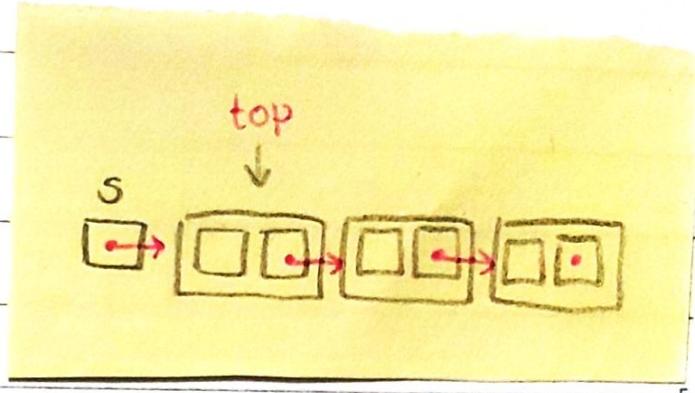
③ Store data in temp.

④ Update temp's link to → to node pointed to by s.

⑤ Update S.

// POP (S)

```
void POP(stack *S) {
    Stack temp;
```



```
if (isEmpty (*S) == 0) {
```

\*basically deleteFirst();

```
    temp = *S;
```

```
*S = temp->link;
```

```
    free (temp);
```

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// TOP (S)

```
char TOP (stack S) {
```

```
return (isEmpty (S) == 0)? S->data : '\0';
```

3

// isEmpty (S)

```
int isEmpty (stack S) {
```

```
return (S == NULL)? 1 : 0;
```

3

// isFull (S)

```
int isFull (stack S) {
```

\*list will never be full, so  
just return 0.

## - QUEUE -

DATE:

### \* Queue

"First In, First Out"

- insertion is done at the **rear**
- deletion is done at the **front**

### \* Operations

1.) ENQUEUE ( $x, Q$ ) - insert element  $x$  at **rear** of queue

2.) DEQUEUE ( $Q$ ) - delete element at **front** of queue

3.) FRONT ( $Q$ ) - returns element at **front** of queue

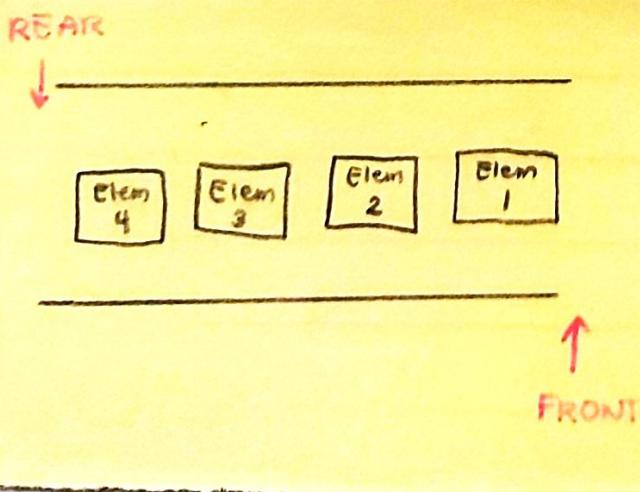
4.) EMPTY ( $Q$ ) - returns 0 if queue IS NOT empty

TRUE (nonzero value) IF EMPTY

5.) FULL ( $Q$ ) - returns 0 if queue IS NOT full

TRUE (nonzero value) IF FULL

6.) INITIALIZE ( $Q$ ) & MAKENULL ( $Q$ )



### \* Implementations

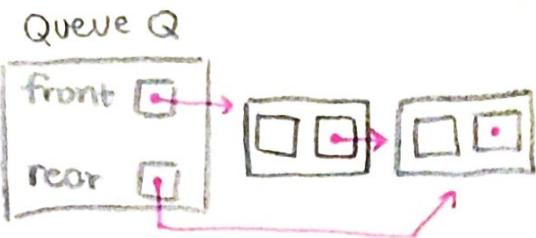
1.) Linked List

2.) Array

3.) CB List

NO: \_\_\_\_\_ DATE: \_\_\_\_\_

## - LINKED LIST IMPLEMENTATION (QUEUE)



Enqueue = rear

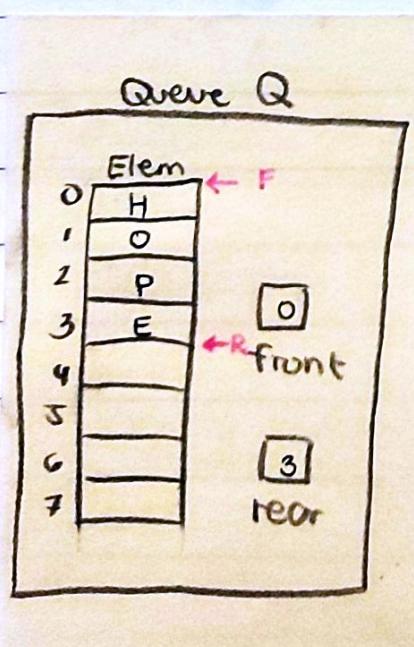
Dequeue = front

5

- By having TWO POINTERS (front/rear) we can minimize the need for traversing. Since our operations take place at the FRONT and END of the list, it makes these operations  $O(1)$ .

## - ARRAY IMPLEMENTATION (QUEUE)

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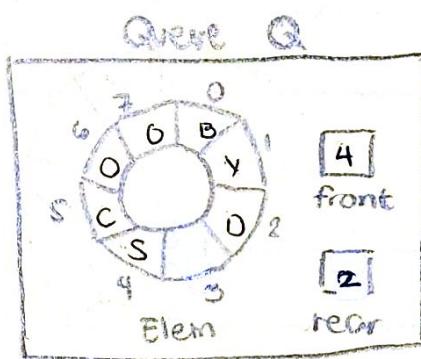
### • ENQUEUE (steps)

- 1.) Check if there is available space.
- 2.) If rear is MAX-1 & front != 0 then SHIFT.
- 3.) Adjust front & rear.
- 4.) Increment rear.
- 5.) Insert element.

\* BUT this implementation still involves SHIFTING! which is a problem and makes it  $O(N)$ .

# \* Circular Array Implementation

- solution to the problem of shifting
- declared as any array in C
- circular: orientation/manner in which array is manipulated
- no beginning/no end
- CLOCKWISE or COUNTERCLOCKWISE



\* USE MODULO (%)  
operator to move  
F & R.

## \* Enqueuing: spell check amg

- 1 element - Relative position of F & R: EQUAL
- Full Queue - Relative position of F & R: F ahead of R by 2 cells
- Empty Queue - Relative position of F & R: F ahead of R by 1 cell

\* Queue is FULL if there is MAX-1 elements, since we sacrificed 1 cell to distinguish a Full Queue & Empty Queue.

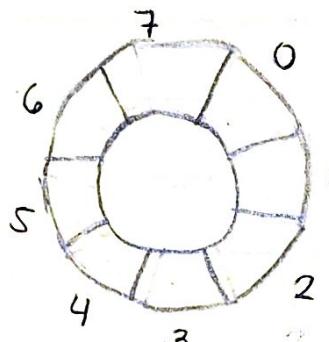
## \* Checking FULL or EMPTY

### • EMPTY

$\text{if}((\text{rear}+1) \% \text{ MAX} == \text{front})$

Front is ahead  
by 1 cell

rear	front
0	1
1	2
2	3
3	4
4	5
5	6
6	7
7	0



### • FULL

$\text{if}(\text{rear}+2 \% \text{ MAX} == \text{front})$

Front is ahead  
By 2 cells

rear	front
0	2
1	3
2	4
3	5
4	6
5	7
6	0
7	1

\* to move Front/Rear by 1 cell:

$$\text{front/rear} = (\text{front}+1) \% \text{ MAX}$$

# - QUEUE OPERATIONS - (LINKED LIST)

NO:  
DATE:

## // initialize (Q)

```
void initialize (Queue * Q) {  
    Q->front = NULL;  
    Q->rear = NULL;
```

}

## // ENQUEUE (Q, x)

```
void Enqueue (Queue * Q, char elem) {
```

Nodetype \* temp;

temp = (Nodetype \*) malloc (sizeof (struct node));

```
if (temp != NULL) {
```

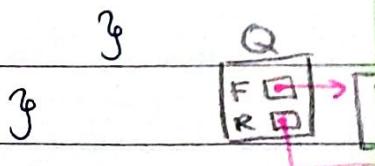
temp->data = elem;

temp->link = NULL;

\*no need to check if list  
is full bcs its linked  
list

```
Q->rear->link = temp;
```

}



## Definition

```
typedef struct node {
```

char data;

struct node \* link;

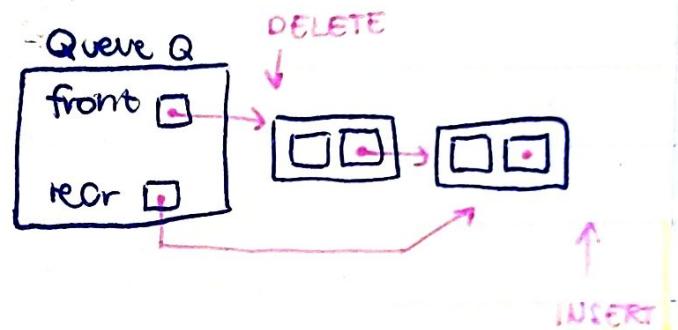
} Nodetype;

```
typedef struct {
```

Nodetype \* front,

\* rear;

} Queue;



STEPS

① Allocate & declare temp node.

- assign new elem
- set link to NULL since this will be the LAST node in the list

② Assign rear's link field to point to temp node to connect it back to list.

## // DEQUEUE (Q)

void dequeue (Queue \*Q) {

    Nodetype \*temp;

    if (isEmpty (Q) == 0) {

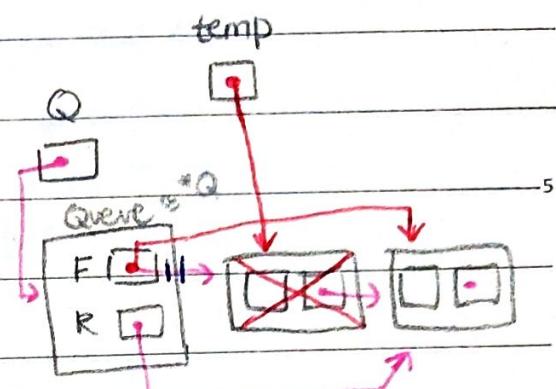
        temp = (\*Q) → front;

        (\*Q) → front = temp → link;

        free (temp);

}

}

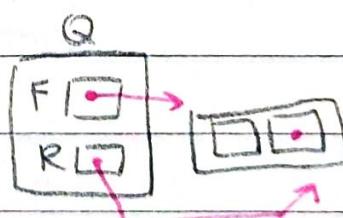


## // FRONT (Q)

char front (Queue Q) {

    return (isEmpty (Q) == 0) ? '\0' : (Q.front) → Elem;

}



## // EMPTY

int isEmpty (Queue Q) {

    return (Q.front == NULL)? 1: 0;

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# - QUEUE OPERATIONS - (CIRCULAR ARRAY)

NO: \_\_\_\_\_

DATE: \_\_\_\_\_

## //initialize(Q)

```
void initialize (Queue *Q){
```

    Q->front = 1;

    Q->rear = 0;

\* remember that in an  
EMPTY QUEUE, Front is  
ahead by 1 cell!

## //ENQUEUE(Q, elem)

```
void enqueue (Queue *Q, char
```

```
if (isFull (*Q) == 0) {
```

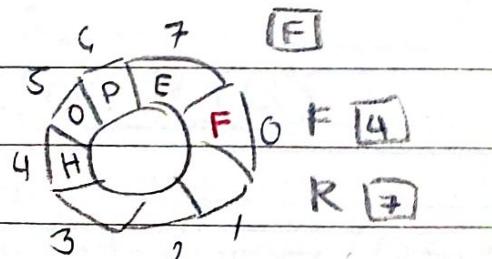
```
    Q->rear = (Q->rear + 1) % MAX;
```

```
    Q->Elem [Q->rear] = elem;
```

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Elem



① Check if Queue has space for new element.

② Increment rear by 1;

③ With new rear index, insert new element.

Front remains stationary!

## ④ Simulation

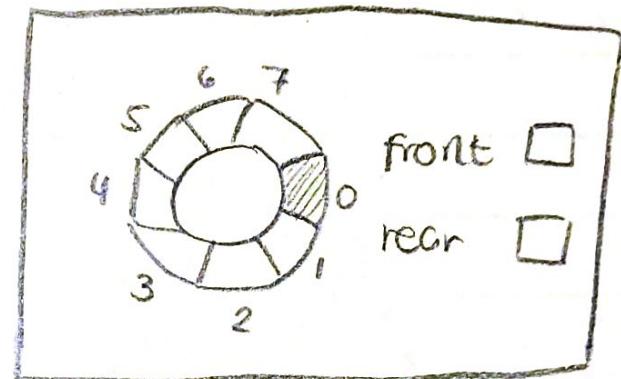
Q->rear = \*0

Elem[0] = 'F'

## Definition:

```
typedef struct {  
    char Elem [MAX];  
    int front, rear;  
} Queue;
```

\* declared like any array.



Queue Q

## - REMEMBER -

\* insert at REAR

\* delete at FRONT

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## // DEQUEUE (Q)

void dequeue (Queue \* Q) {

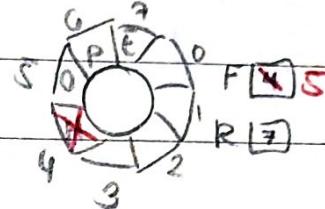
if (isEmpty == 0) {

Q->front = (Q->front + 1) % MAX;

}

}

\* just move front by 1 to  
'delete' element.



## // FRONT (Q)

char front (Queue Q) {

return (isEmpty (Q) != 0) ? Q->elem [Q->front] : '0';

}

## // FULL (Q)

int isFull (Queue Q) {

return ((Q->rear + 2) % MAX == Q->front) ? 1 : 0;

}

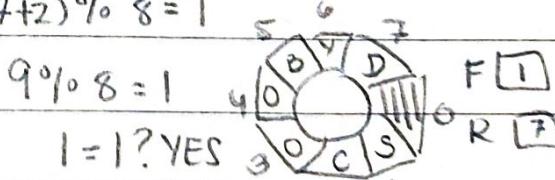
$$(7+2) \% 8 = 1$$

$$9 \% 8 = 1$$

1 = 1?

YES

ITS FULL



## // EMPTY (Q)

int isEmpty (Queue Q) {

return ((Q->rear + 1) % MAX == Q->front) ? 1 : 0;

}

$$(4+1) \% 8 = 1$$

IDEAS COME FROM SONG

NOT EMPTY? 3 = 1? NO

