

STACKS

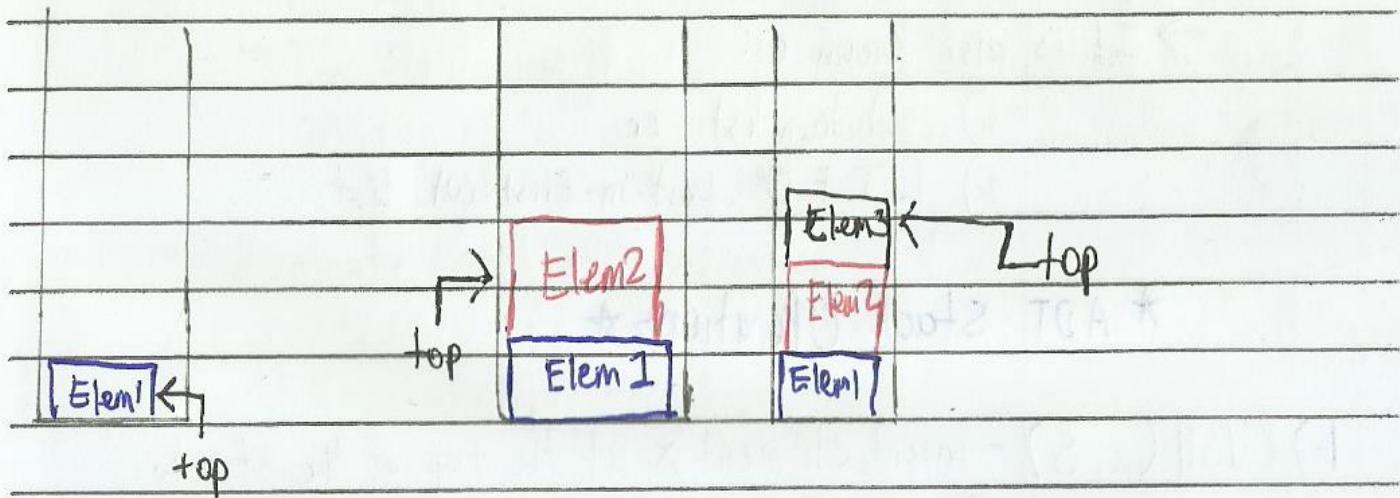
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"First IS Last"

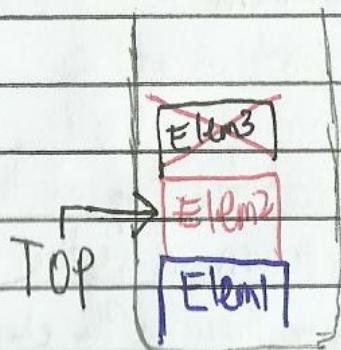
or

"Last Is First"

- Visual Representation of Inserting elements in Stack.



- Visual representation of Deleting elements in Stack.



→ stacks follow the Last In, First Out rule

→ can also be First In, Last Out

• What is a Stack?

→ It is a special kind of list in which all insertions and deletions take place at one end, called the top.

→ It is also known as:

1.) pushdown list or

2.) LIFO (Last-in-First-out) List

* ADT Stack Operations *

1.) PUSH(x, s) - inserts element x at the top of the stack.
 \approx insertFirst()

2.) POP(s) - deletes the top element of the stack s
 \approx deleteFirst()

3.) TOP(s) - returns the element at the top of the stack s
- if empty, it will still return a sentinel value

Note: Sentinel values are the same type as the element but not included in the set of elements.

4.) EMPTY(s) - returns true (nonzero value) if the stack s is empty; otherwise return false (zero).

5.) FULL(s) - returns true (nonzero value) if the stack s is full;
otherwise return false (zero).

NOTE: Only applicable for Array & CB Implementation

> Some Stack Applications

- Execution Stack

- In compiler design, a stack is used to organize the activation records of functions that are invoked or called.
- The activation record of the called function is found on top of the activation record of the calling function.

- Evaluate arithmetic expression

- Stack is used to convert infix expression to postfix Expression
- Evaluate postfix Expression

- Implementations of ADT Stack •

- 1.) Array Implementation

- a.) Static Array

- b.) Dynamic Array

- 2.) Linked List (Using Pointers)

- a.) Singly - Linked

- b.) Doubly - Linked

- 3.) Cursor - Based Implementation

* Array Implementation *

Illustration:

Elem							
0							
1							
2							
3							
4				top			
5							
6							
7							

- Write an appropriate definition of datatype Stack.

→ #define MAX 8

```
typedef struct S
char Elem [MAX];
int top;
```

}

- In Array Implementation, Stack has two views:

1) Stack will grow from max-1 to 0

2) Stack will grow from 0 to max-1 (the usual for Array Inv)

- View 1: Stack will grow from max-1 to 0 Scenarios

Stack S	Stack S	Stack S	Stack S
Elem	Elem	Elem	Elem
0	0 G	0	0
1	1 O	1	1
2	2 P	2	2
3	3 K	3 K	3 K
4	8	4 C	4 C
5	top	top	top
6	5 A	5 A	5 A
7	6 T	6 T	6 T
	7 S	7 S	7 S

1.) Empty Stack

↳ top is max

2.) Full Stack

↳ top is 0

3.) PUSH(x,S);

↓ stack grows

top increases

4.) POP(S);

↑ top decreases

• View 2: Stack will grow from 0 to max-1 Scenarios

Stack S	Stack S	Stack S	Stack S
Elem	Elem	Elem	Elem
0	0 S	0 S	0 S
1	1 T	1 T	1 T
2	2 A	2 A	2 A
3	3 C	3 C	3 C
4	-1 K	4 K	4 K
5	top	5 top	5 top
6	6 O	6 T	6
7	7 G	7	T

1) Empty stack 2) Full stack 3) PUSH(x, s) 4-) POP(s)

↳ top is -1 ↳ top is max-1 ↳ top increases, ↳ top decreases

• Exercise 1 - Write the code the ff. stack operations using the declaration given and assuming that the stack will grow from max-1 to 0.

1.) INITIALIZE(s)

2.) PUSH(x, s)

3.) POP (s)

4.) TOP(s)

5.) EMPTY(s)

6.) FULL(s)

→

Exercise 1 - stack operations if stack grows from ~~no 0~~ max-1

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Data Struct Def (for Guide):

```
#define MAX 8
typedef struct {
    char data[MAX];
    int top;
} Stack;
```

1) Initialize(S);

```
void initStack(Stack *S) {
    S->top = MAX; // is equals to max since view 1
}
```

// pass by address

where an empty set, top = MAX

2) PUSH(x, S); ~~≈ recall:~~ equivalent to insertFirst()

```
void push(char x, Stack *S) {
    if (S->top != 0) { // check if not full stack
        S->top--; // decrement top (or move)
        S->data[S->top] = x; // assign the element to the current position of top
    }
}
```

3) POP(S); ~~≈ recall:~~ equivalent to deleteFirst()

```
void pop(Stack *S) {
    if (S->top != MAX) { // check if not empty stack
        S->top++; // increase top
    }
}
```

Stack Operations for Stack
Exercise 1: grows from max-1 to 0

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4) TOP(s);

Char top (Stack S) { pass by copy since we just return what value is at top

return S.top != MAX ? S.data[S.top] : '\0'; } check if not empty

What value is at top

returns sentinel value if empty

5) EMPTY(s);

int isEmpty (Stack S) {

return S.top == MAX ? 1 : 0; // in this view 1, stack is empty if top == MAX

};

6) FULL(s);

int isFull (Stack S) { Pass by copy

return S.top == 0 ? 1 : 0; // in view 1, stack is full

};

Practice: Stack operations but stack grows from 0 to max-1

1) Initialize(s);

void initStack (Stack *S) {

S → top = -1; // set stack as empty,

}; // stack is empty if top = -1 in View/ver-2

2) Push(x, s);

void push (char x, Stack *S) {

if (S → top != MAX-1) { // check if not Full Stack

S → top++; // move to Vacant space (?)

S → data[S → top] = x; // assign the element to said space

};



Practicing - if Stack grows from
0 to max-1

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3.) POP(S);

void pop(Stack *S) { ↗ Pass by address

if (S->top != -1) { // check if stack is not empty

S->top--; // decrement the top

}

}

4.) TOP(S);

↗ // pass by copy

void top(Stack S) {

return S.top == -1 ? S.data[S.top] : '0';

}

↙ check if not

empty

↙ returns
sentinel value
if empty

5.) EMPTY(S);

Void isEmpty(Stack S) {

return S.top == -1 ? 1 : 0;

}

6.) FULL(S);

void isFull(Stack S) {

return S.top == MAX-1 ? 1 : 0;

}

Stackoverflow

Singly-Linked Implementation

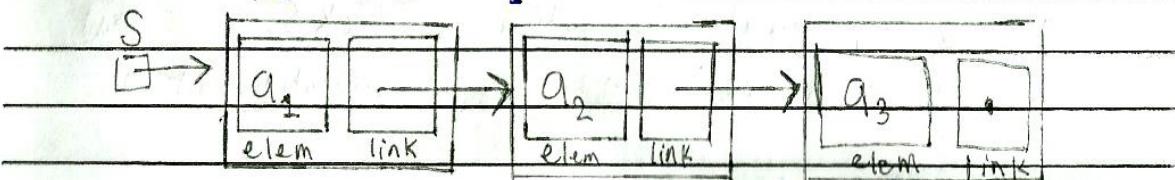
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Illustration

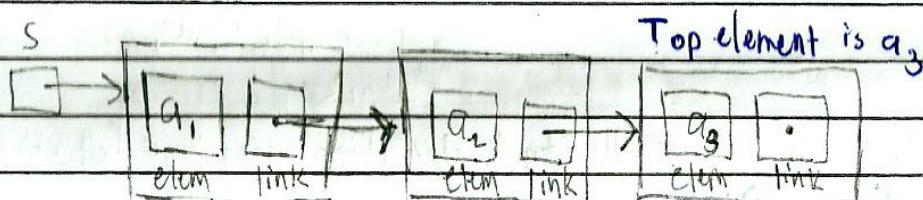
→ Two orientations of top element:

1.) Top element is stored in the cell pointed to by stack pointer S.

Top element is a_1



2.) Top element is stored in the cell whose next field is NULL



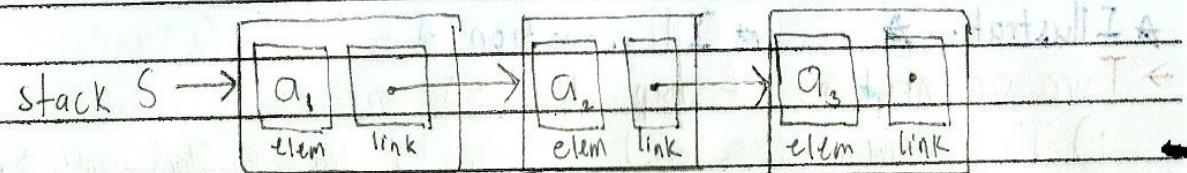
• Which Orientation is better? •

→ Orientation 1 is better than 2 since we would only need to access the top element. Orientation 2 requires traversal and is considered to have a running time of $O(n)$, which is not the best.

Orientation 1 requires NO traversal & has a running time of $O(1)$

Exercise 2 - singly Linked List Implementation of Stack

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- 1.) Write an appropriate definition of Stack S. NOTE that "top" in this implementation is only an orientation, not a variable.

* Data Struct Def.:

```
typedef struct node {  
    char elem;  
    struct node *link;  
}*stack;
```

- 2.) Write the code of all Stack Operations using your definition.

a.) Initialize(S);

```
void initStack(stack *S){  
    *S = NULL;  
}
```

b.) push(x, S);

```
void push(char x, stack *S){  
    stack temp = (stack) malloc(sizeof(struct node));  
    if(temp != NULL){  
        temp->data = elem;  
        temp->link = *S;  
        *S = temp;  
    }  
}
```

NOTE: This is equivalent to insertFirst()

Strdmore

Exercise 2

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3) POP(s);

```
void pop(stack *S){  
    stack temp;  
    if (*S != NULL){  
        temp = *S;  
        *S = temp->link;  
        free(temp);  
    }  
}
```

4) TOP (s);

```
char top (stack S){  
    return S != NULL ? S->data : '0';  
}
```

5) EMPTY (s);

```
int isEmpty (stack S){  
    return (S == NULL);  
}
```

6) FULL (s);

```
int isFull (stack S){  
    return 0;  
}
```

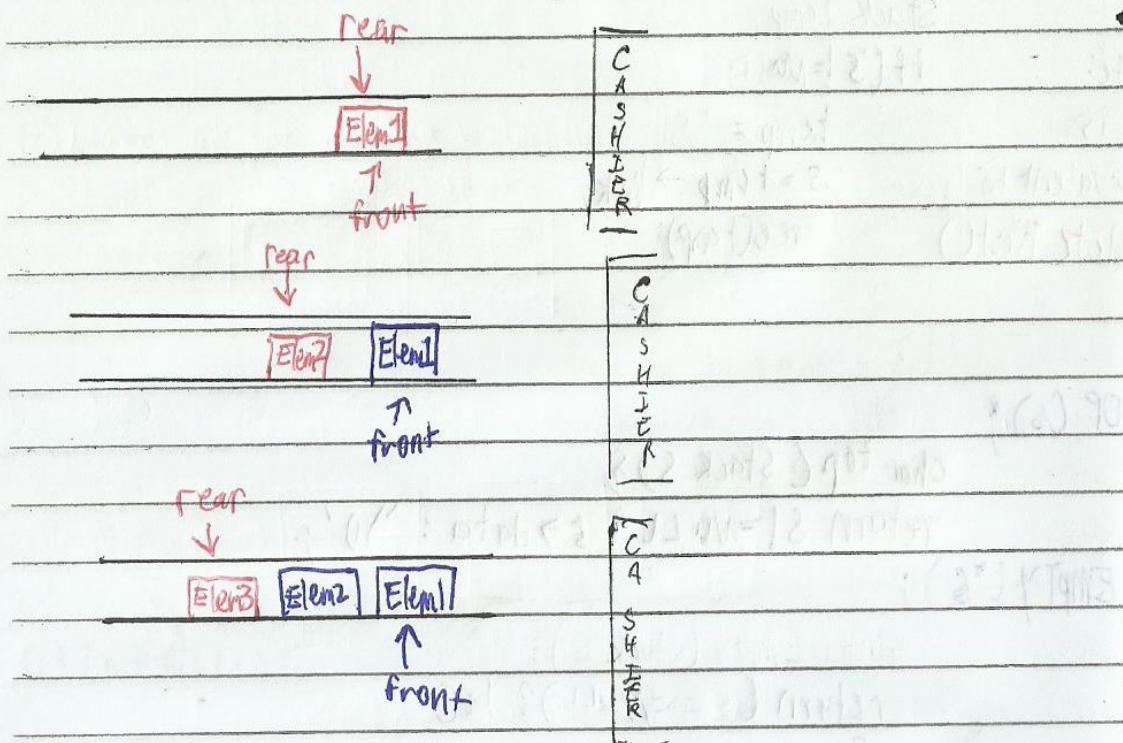
(NOTE: This function is only applicable
in Array & Cursor based implementation,
NOT LL implementation)

QUEUES

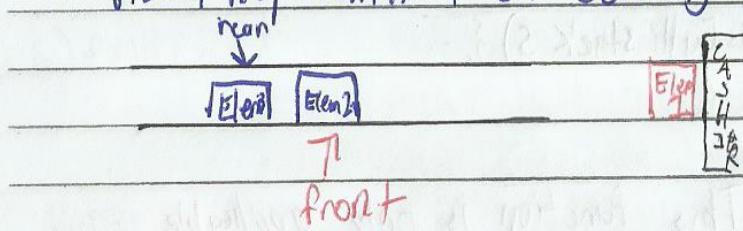
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"First is First" or "Last is Last"

* Visual Representation of inserting elements in the Queue



* Visual Representation of deleting elements in the Queue



* What is a queue?

→ It is a special kind of list in which insertion is done on one side called rear, while deletion is done on the other side called front.

→ is called FIFO (First In First Out) List.

QUEUES

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• ADT Queue Operations •

1.) ENQUEUE (x, Q) - insert element x at the rear of the Queue Q .

2.) DEQUEUE (Q) - deletes the front ^{element} of the Queue Q .

3.) FRONT (Q) - returns the element at the front of the Queue Q .

4.) EMPTY (Q) - returns true (nonzero value) if the Queue Q is empty; otherwise returns false (zero)

5.) FULL (Q) - returns true (nonzero value) if the Queue Q is full; otherwise return false (zero).

- NOTE: applicable for both Array & C.B. implementations only

* Some Queue Applications *

1.) Scheduling Algorithms

→ process scheduling in a time-shared computing system.

→ resource scheduling as printers, disks, etc.

2.) Searching Algorithms

→ Non-linear search such as Depth First search (?)

* Implementations of ADT Queue *

1.) Linked List (using pointers) - Singly-Linked, Doubly-Linked

2.) Array Implementation - Static Array, Dynamic array

3.) Cursor-based Implementation.

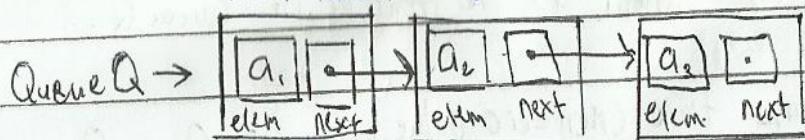
Queue Linked-List Implementation

Date 2/20/2023

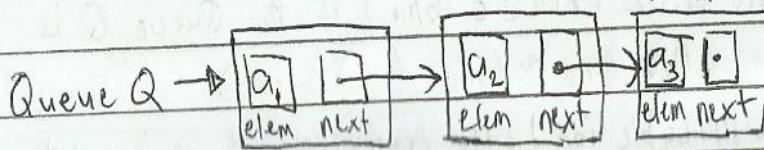
- Singly-Linked Version 1 - Queue is a pointer to a self-reference structure

- Two Orientations of FRONT element

- Front element is stored in the cell pointed to by Queue Q.
Front element is a_1 ,



- Front element is stored in the cell whose next field is NULL.
Front element is a_3



Which Orientation is better?

For Orientation #1, ENQUEUE is $O(N)$ &

DEQUEUE is $O(1)$, constant time.

For Orientation #2, ENQUEUE is $O(1)$ &

DEQUEUE is $O(N)$.

They are BOTH the SAME

Queue & Linked List (Pointer) Implementation

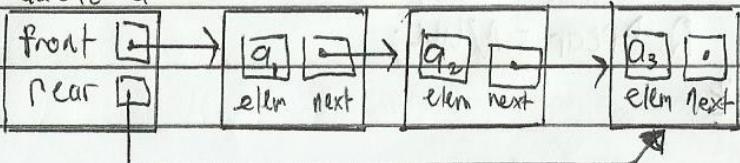
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- Singly-Linked Version 2 - Queue is a structure containing FRONT & REAR pointers.

- Two versions of Queue Q

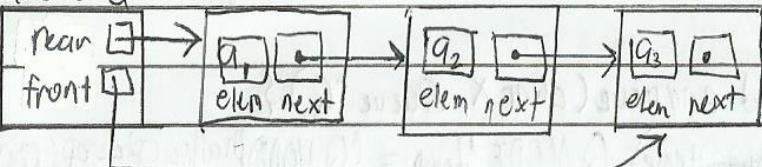
Version A:

Queue Q



Version B:

Queue Q



Which version is better? - A is the better version

Exercise - Write an appropriate declaration of Queue Q

Code:

```
typedef struct node {
```

```
    char elem;
```

```
    struct node *next;
```

```
} QNODE;
```

```
typedef struct { // Queue is a structure in this version
```

```
    QNODE *front, *rear;
```

```
} Queue;
```

Queues - LL implementation practice

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- Write the code of the ff. functions:

a.) initQueue() - the function will initialize it to be empty.

- Code:

```
void initQueue(Queue *Q) {
```

set
to empty
to initialize

```
    Q->front = NULL;  
    Q->rear = NULL;
```

b.) enqueue() - Given the queue and an element, the function will insert the element at the rear of the queue

InsertLast

in LL

- Code:

```
void enqueue(char X, Queue *Q) {
```

Pointer to
pointer
concept

```
    QNODE *temp = (QNODE*)malloc(sizeof(QNODE));
```

```
    if (temp != NULL) { // checking
```

```
        temp->elem = X;
```

```
        temp->next = NULL;
```

to check if

```
if (Q->front == NULL && Q->rear == NULL) {
```

Queue is empty

```
    Q->front = temp; // set the front to new node (temp)
```

& if it is the

```
} else {
```

first node to

```
    Q->rear->next = temp; // add the new node
```

be inserted

```
}
```

in rear->next

```
    Q->rear = temp; // make the new node as the  
                    // new rear
```

NOTE: This

```
}
```

can still be improved,

it's just too sleepy A.A.



Queues - LL Implementation

Date _____

c.) dequeue() - Given the queue, the function will delete the front element if it exists.

deleteFirst
inLL (?) • Code:

```
Void dequeue (Queue *Q) {
```

```
    QNODE *temp;
```

```
    if (Q->front != NULL) {
```

```
        temp = Q->front; // let temp hold the current front
```

```
        Q->front = Q->front->next; // set front to the next
```

```
        free (temp); // free temp value
```

}

```
    if (Q->front == NULL) {
```

```
        Q->rear = NULL; } // if front is NULL, set rear to NULL
```

}

d.) front() - Given the queue, the function will return the front element if it exists.

```
char front (Queue Q) {
```

```
    return Q.front != NULL ? Q.front->elem : '0';
```

e.) EMPTY()

```
int isEmpty (Queue Q) {
```

```
    return (Q.front == NULL && Q.rear == NULL) ? 1 : 0;
```

}

Queues Array Implementation

Date 2/20/2023

• Variation 1

• ENQUEUE •

Queue Q

ELEM
H
D
P
E
V
0
■

Enqueue Element 'Y':

Steps:

- Check if there is available space
- increment rear
- insert the element.

• DEQUEUE •

Queue Q

ELEM
X
O
P
E
F
Y
V
■

Dequeue an element:

Steps:

- Check if queue is not empty
- Shift elements
- decrement rear

NOTE: physically element V at index 4
is still there but logically it is
not part of the queue anymore.

Queues Array Implementation

Variation 2 date 2/20/2023

Queue Q

DEQUEUE

	Elem
0	H
1	O
2	P
3	E
4	front
5	3
6	Rear
7	

Dequeue an element

steps:

- check if queue is not empty
- Increment front

NOTE: Physically H element is still there but logically it is not part of the queue anymore.

ENQUEUE

Queue Q

	Elem
0	H
1	O
2	P
3	E
4	Y
5	3
6	4
7	rear

Steps:

- Check if there is available space
- increment rear
- insert the element

What if Queue was like this

Queue Q

	Elem
0	H
1	O
2	P
3	E
4	Y
5	D
6	O
7	O
#	Rear

• How many elements are there in the Queue Q? - 3

• Is Enqueue possible & How

↳ Yes, shift existing elements to make room for new elements

Queues Array Implementation

Date 2/20/2023

• ENQUEUE Revisited.

Queue Q	
	Elem
0	H 0
1	S 0
2	P 0
3	E 0
4	Y front
5	D
6	O
7	0 rear

Enqueue element D:

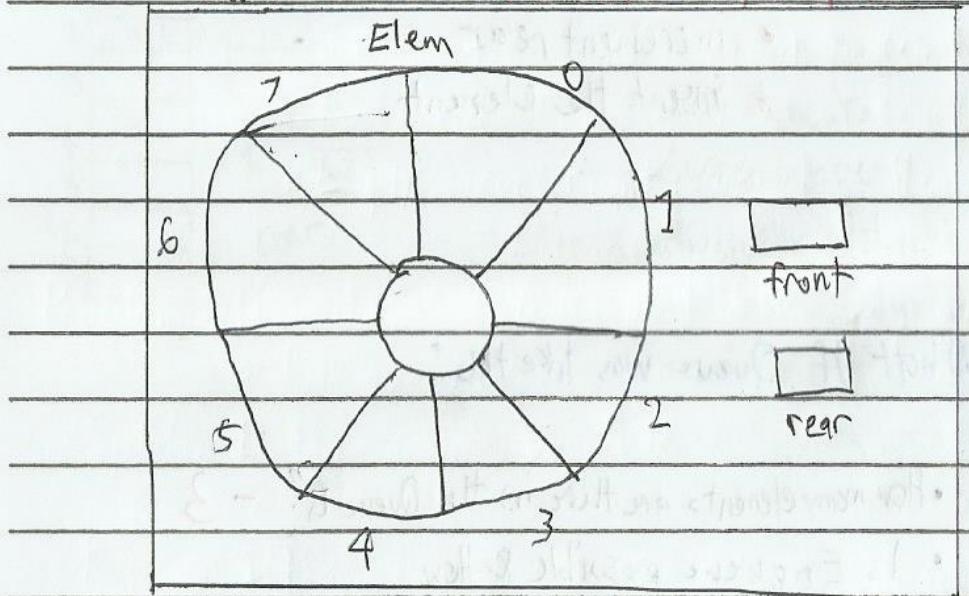
Steps:

- Check if there is available space
- if rear is max-1 & front not 0, SHIFT elements
- Adjust front & rear
- increment rear
- insert the element.

is there a solution where shifting of elements can be avoided? Yes:

Queue Q

* Circular Array Implementation



Queue - Circular Array Implementation

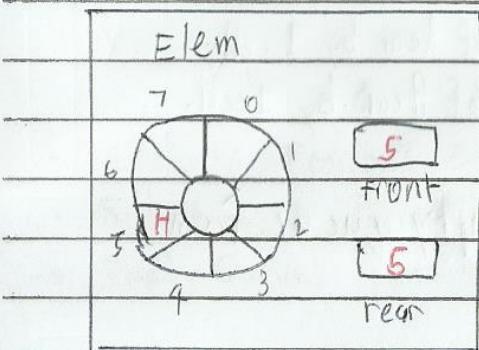
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⇒ Characteristics of Circular Array

- Declared in the same manner as any array in C.
- Being circular is just an orientation, or a manner in which the array is manipulated.
- Like a circle, the array has no beginning and no end; hence the first element can be stored anywhere.
- Succeeding elements are inserted in CLOCKWISE or COUNTERCLOCKWISE direction; hence front & rear will also move clockwise or counter-clockwise
- Note: CLOCKWISE MOVEMENT will be used in the ff. operations.

⇒ ENQUEUE 1 ELEMENT

Queue Q



Enqueue 7st element = H:

- How many different options are there?

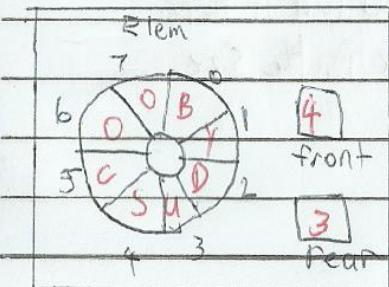
→ 8

- Relative position of front & rear?

→ Front is equal to rear

⇒ FULL QUEUE ⇒

Queue Q



Enqueue the elements = SCOOBYDOO

- What is the relative position of front & rear? - front is ahead by 1 cell

Stradmore

Queues - Circular Array Implementation

EMPTY QUEUE

date

2/20/2023

Queue Q

Elem		Dequeue	Remove	Front
7		1st	H	7
0		2nd	O	0
P		3rd	P	1
E		4th	E	2
2				
front				
1				
rear				

Diagram of a circular queue with 8 slots. Slots 0, 1, 2, and 3 contain values H, O, P, and E respectively. Slot 4 is empty. The front pointer is at index 2 (value 0) and the rear pointer is at index 1 (value 1). The label 'EMPTY QUEUE!!' is written to the right of the table.

- What is the relative position of front and rear?

- front is ahead of rear
by 1 cell

* Summary: Circular Queue

- 1 Element : Front is equal to rear
- Full Queue: Front is ahead of Rear by 1 cell.
- Empty Queue: Front is ahead of Rear by 1 cell.

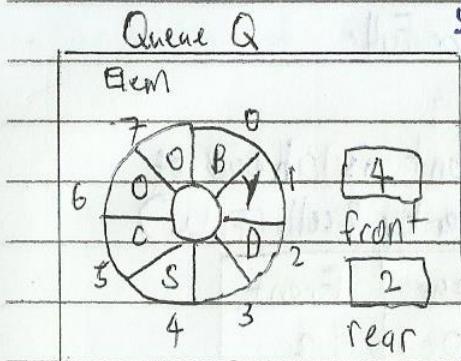
Problem: How do we distinguish an empty queue from a full queue?

• Solution 1: Add a counter variable

• Solution 2: Sacrifice 1 cell (Queue is considered full if there are $(\text{Max} - 1)$ elements, where max is the size of the array.)

Queues - Circular Array Implementation

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Sol.2: FULL QUEUE

- Enqueue elements:

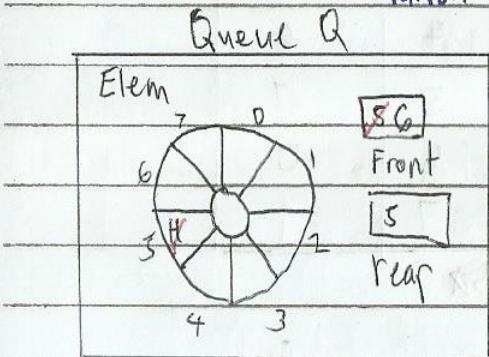
SCOOBYDOO

→ 'U' is sacrificed

• What is the relative position of front & rear?

→ front is ahead of rear by 2 cells.

Solution 2: Empty Queue



- Dequeue an element.

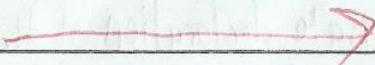
• Relative position of front & rear?

→ Front is ahead of rear by 1 cell

★ SUMMARY: Solution 2 ★

- 1 Element: Front is equal to Rear
- Full Queue: Front is ahead of Rear by 2 cells.
- Empty Queue: Front is ahead of Rear by 1 cell.

More illustration:



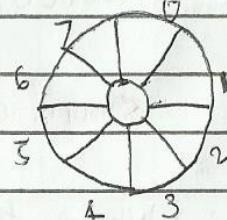
Queues! Circular Array Implementation

Date 2/20/2023

- Checking if Empty or Full.

Front is ahead of
Rear by 1 cell (Empty)

Rear	Front
0	1
1	2
2	3
3	4
4	5
5	6
6	7
7	0



Front is ahead of
Rear by 2 cells (Full)

Rear	Front
0	2
1	3
2	4
3	5
4	6
5	7
6	0
7	1

★ ADDITIONAL NOTES ★

- To move Front:

$$\text{front} = (\text{front} + 1) \% \text{MAX}$$

- To move Rear

$$\text{rear} = (\text{rear} + 1) \% \text{MAX}$$

- Empty: $(\text{rear} + 1) \% \text{MAX} == \text{front}$.

- Full: $(\text{rear} + 2) \% \text{MAX} == \text{front}$

Practice Exercise:

- 1.) Write an appropriate declaration of the circular array implementation of Queue Q using Solution 2.

- 2.) Using the declaration in #1, write the code of the Queue operations:

Queue Circular Array Imp. Exercise

date

- ## • Declaration of Quor Q:

Writers note: not sure if correct; >

```
#define MAX 8  
typedef struct {  
    char ELEM [MAX];  
    int front;  
    int rear;  
} Queue;
```

- #### • Queue Operations in Solution 2 circular Array

```

1) initialize: void initQueue(Queue *Q) {
    Q->front = 1; } front is
    Q->rear = 0; } ahead by
    { 1 cell if
      empty
  }
```

```

2.) int isEmpty() :-----|  

| int isEmpty(Queue Q) {  

|   return((Q.rear + 1) % MAX == Q.front)? 1 : 0;  

| }

```

3) int isFull(): int isFull (Queue Q) {
return ((Q.rear + 1) % MAX == Q.front)? 1 : 0;

4) enqueue(): void enqueue(Queue *Q, char x) {
 if (isFull(*Q) != 1) {
 Q->rear = (Q->rear + 1) % MAX; // set rear to the
 Q->elem[Q->rear] = data; // place the
 next node (?)
 }
 }


Queue Circular Array Simple
Exercise

Date _____

5.) dequeue () : void dequeue (Queue *Q) {
 if (isEmpty != 1) {
 Q->front = (Q->front + 1) % MAX;
 }

6.) front () : char front (Queue Q) {
 return (isEmpty(Q) != 1) ? Q.Elem [Q.front] : '0';

7.) display Queue : void display Queue (Queue Q) {
 int index;
 if ((Q.rear + 1) % MAX != Q.front) {
 for (index = Q.front; index != (Q.rear + 1) % MAX; index = (index + 1) % MAX) {
 printf ("%c ", Q.Elem [index]);
 }
 } else {
 printf ("Queue is empty");
 }