American Computer Science League

Contest #1

JUNIOR DIVISION SOLUTIONS

1. Com	outer	Number	Systems
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$$2018 = 3 * 8^3 + 7 * 8^2 + 4 * 8^1 + 2 * 8^0 = 3742_8$$

1. 3742₈ or 3742

2. Computer Number Systems

$$1_{10} = 1_2$$
 and $32_{10} = 100000_2$
Number of digits in the binary number: 1 2 3 4 5
Number with same number of 1's as 0's: 0 1 0 3 0
Total is 4.

3. 4

2. 4

3. Recursive Functions

$$f(18) = f(18-5)+1 = f(13)+1 = 3+1 = 4$$

$$f(13) = f(13-5)+1 = f(8)+1 = 2+1 = 3$$

$$f(8) = f(8-5)+1 = f(3)+1 = 1+1 = 2$$

$$f(3) = f(3+3)-2 = f(6)-2 = 3-2 = 1$$

$$f(6) = f(6-5)+1 = f(1)+1 = 2+1 = 3$$

$$f(1) = f(1+3)-2 = f(4)-2 = 4-2 = 2$$

$$f(4) = f(4+3)-2 = f(7)-2 = 6-2 = 4$$

$$f(7) = f(7-5)+1 = f(2)+1 = 5+1 = 6$$

$$f(2) = f(2+3)-2 = f(5)-2 = 7-2 = 5$$

$$f(5) = 7$$

4. Recursive Functions

$$f(24) = [24/2] + 1 = [12] + 1 = 12 + 1 = 13$$

$$f(13) = [13/3] - 2 = [4.333...] - 2 = 4 - 2 = 2$$

$$f(2) = [2/2] + 1 = [1] + 1 = 2$$

$$So f(f(f(f(24)))) = f(f(f(13)))$$

$$= f(f(2))$$

$$= f(2) = 2$$

4. 2

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5. What Does This Program Do? - Branching

a	В	С	D	E	f
2	1	0	3	4	
2	1	0	3	4	10
2	1	0	3	4	2
2	3	0	3	4	2
2	3	0	4	4	2
2	4	0	4	4	2
2	4	0	0	4	2

$$2*a+b*(c-d)+e/2*f = 2*2+4*(0-0)+4/2*2$$

= $2*2+4*0+4/2*2$
= $4+0+4$
= 8

5. 8