

Exercise Question (Inventory & Aggregate Planning)

1(a) What is the economic order quantity (EOQ)?

$$Q^* = \sqrt{\frac{2DS}{H}}$$

$$Q^* = \sqrt{\frac{2(5000)(30)}{50}} = \sqrt{6000} = 77 \text{ units} \quad \#$$

b) What is the average inventory?

$$\frac{\text{Order quantity}}{2}$$

$$= \frac{77}{2} = 39 \text{ units} \quad \#$$

c) What is the optimal number of orders per year (N)?

$$\text{Expected number of orders} = N = \frac{\text{Demand}}{\text{Order quantity}} = \frac{D}{Q^*}$$

$$N = \frac{5000}{77} = 65 \text{ orders per year} \quad \#$$

d) What is the optimal number of working days between orders (T)?

$$\text{Expected time between orders} = T = \frac{\text{Number of working days per year}}{N}$$

$$T = \frac{250}{65} = 4 \text{ days between orders}$$

1 e) What is the total annual Inventory cost?

Total Annual cost = Setup (order) cost + Holding cost

$$TC = \frac{D}{Q} S + \frac{Q}{2} H$$

$$= \frac{5000}{77} (30) + \frac{77}{2} (50)$$

$$= 1.95 + 1.93$$

$$= RM 3.88 \quad \#$$

f) What is the reorder point (ROP)?

ROP = Demand per day \times Lead time for a new order
in days

$$ROP = d \times L$$

$$d = \frac{D}{\text{Number of working days in a year}}$$

$$= \frac{5000}{250} = 20 \text{ units}$$

$$ROP = d \times L$$

$$= 20 \text{ unit per day} \times 10 \text{ day} = 200 \text{ units} \quad \#$$

2) Inventory Management: Quantity Discount

$D = 4900$

$s = \text{RM } 50$

$H = 40\% \text{ of } \text{pur}$

$0 - 999$

$\text{RM } 5$

$1000 - 3999$

$\text{RM } 4.95$

$4000 - 5999$

$\text{RM } 4.90$

6000 or more

$\text{RM } 4.85$

Calculation of EOQ:

$H = 0.40(5)$

$= 2$

$Q_5 = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2(4900)(50)}{2}} = 495 \text{ units}$

$H = 0.40(4.95)$

$= 1.98$

$Q_{4.95} = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2(4900)(50)}{1.98}} = 498 \text{ units}$

$H = 0.40(4.90)$

$= 1.96$

$Q_{4.90} = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2(4900)(50)}{1.96}} = 500 \text{ units}$

$H = 0.40(4.85)$

$= 1.94$

$Q_{4.85} = \sqrt{\frac{2DS}{H}} = \sqrt{\frac{2(4900)(50)}{1.94}} = 503 \text{ units}$

Calculation of Total Cost:

TC = Setup cost + Holding cost + Product cost

$$TC = \frac{D}{Q} s + \frac{Q}{2} H + PD$$

$$TC_{495} = \frac{4900(50)}{495} + \frac{495}{2}(2) + (5)(4900) = \text{RM } 25490$$

$$TC_{1000} = \frac{4900(50)}{1000} + \frac{1000}{2}(1.98) + (4.95)(4900) = \text{RM } 25490$$

$$TC_{4000} = \frac{4900(50)}{4000} + \frac{4000}{2}(1.96) + (4.90)(4900) = \text{RM } 27991$$

$$TC_{6000} = \frac{4900(50)}{6000} + \frac{6000}{2}(1.94) + (4.85)(4900) = \text{RM } 29626$$

Order quantity that will minimize the total cost is 495 and 1000 *

(3) Aggregate Planning

Month	Demand	Production	Inventory	Hiring	Layoffs	Total Cost
January	1100	1300	0	0	²⁰⁰ (2 × 6000)	Rm 12 000
February	1200	1300	0	0	¹⁰⁰ (1 × 6000)	Rm 6 000
March	1400	1300	0	¹⁰⁰ (1 × 3000)	0	Rm 3 000
April	1800	1300	0	⁵⁰⁰ (5 × 3000)	0	Rm 15 000
May	1800	1300	0	⁵⁰⁰ (5 × 3000)	0	Rm 15 000
June	1600	1300	0	³⁰⁰ (3 × 3000)	0	Rm 9 000
					Total	Rm 60 000