

Project documentation

Container

Binary Search Tree (BST) SortedBag (SB)

A SortedBag is a container where the elements do not have to be unique and there are no positions for the elements and the elements are ordered using a relation. There are no operands that work with positions in a SortedBag.

Domain

$\mathbf{B} = \{b \mid b \text{ is a SortedBag with elements of type TComp}\}$

Representation

Node

info: TComp

leftChild: \uparrow Node

rightChild: \uparrow Node

parent: \uparrow Node

SortedBag

root: \uparrow Node

relation: \uparrow Relation

Interface

- ***create(relation)***
description: creates a new and empty SortedBag
pre: true
post: $b \in \mathbf{B}$, b is an empty SortedBag, rel will have the 'relation' property
- ***destroy(root)***
description: destroys a SortedBag
pre: root: $\uparrow\text{Node}$
post: b was destroyed (the allocated memory has been freed)
- ***add(parent, root, data)***
description: adds the element data to the SortedBag b
pre: parent: $\uparrow\text{Node}$, root: $\uparrow\text{Node}$, $data \in \text{TComp}$
post: $b' \in \mathbf{B}$, $b' = b \cup \{data\}$ (TComp data is added to the SortedBag)
- ***del(root, data)***
description: removes the element data from the SortedBag b if it exists
pre: root: $\uparrow\text{Node}$, $data \in \text{TComp}$
post: $b' \in \mathbf{B}$, $b' = b \setminus \{data\}$ (one occurrence of data was removed from the SortedBag). If data is not in b , b is not changed.
- ***find(root, data)***
description: returns a pointer to a node if the element data exists in the SortedBag, NIL otherwise
pre: root: $\uparrow\text{Node}$, $data \in \text{TComp}$
post: if $data \in \mathbf{B}$, $find \leftarrow \uparrow\text{Node}$, else $find \leftarrow \text{NIL}$
- ***findMin(root)***
description: returns a pointer to the left most node of the given root
pre: root: $\uparrow\text{Node}$, $data \in \text{TComp}$
post: if the root does not have a left node, it returns the $\uparrow\text{root}$

- ***count(root, counter)***
description: returns the number of elements from the SortedBag
pre: : root: \uparrow Node, counter: Integer
post: ***count*** \leftarrow the number of elements from b
- ***iterator(root, i)***
description: iterates through all the elements in the bag
pre: $b \in \mathbf{B}$
post: $i \in \mathbf{I}$, i is an iterator over b

Pseudocode implementation of the interface operation for the SortedBag

- subalgorithm ***create(relation)*** is:
 rel \leftarrow relation
 root \leftarrow NIL
end-subalgorithm – complexity **O(1)**
- subalgorithm ***destroy(root)*** is:
 if root \neq NIL then:
 destroy(root.left)
 destroy(root.right)
 free(root)
 endif
end-subalgorithm – complexity **O(n)**

- function *add(parent, root, data)* is:

if root != NIL then:

root<- new(Node)

root.data<- data

root.parent<- parent

root.left<- NIL

root.right<-NIL

else if rel(data,root.data)=1 then:

root.left<- add(root,root.left,data)

else

root.right<- add(root,root.right,data)

add<- root

end-function – complexity **$O(\log n)$**

- function *del(root, data)* is:

if root=NIL then:

del<- NIL

else if rel(data,root.data)=1 then:

root.left<-del(root.left,data)

else if rel(data,root.data)=-1 then:

root.right<-del(root.right,data)

else

if root.left=NIL and root.right=NIL then:

free(root)

root<-NIL

else if root.left=NIL then:

```
temp<-new(Node)
temp<- root.right
root.data<-root.right.data
root.left<-root.right.left
root.right<-root.right.right
free(temp)
```

else if root.right=NIL then:

```
temp<-new(Node)
temp<-root.left
root.data<-root.left.data
root.right<-root.left.right
root.left<-root.left.left
free(temp)
```

else:

```
temp<-new(Node)
temp<-findMin(root.right)
root.data<-temp.data
root.right<-del(root.right,temp.data)
```

endif

del<- root

end-function – complexity **$O(\log n)$**

- function *find*(*root*, *data*) is:

```
    if root!=NIL then:
        if data=root.data then:
            find<-root
        endif
        if rel(data,root.data)=1 then:
            find<- find(root.left,data)
        else:
            find<- find(root.right,data)
        endif
    else
        find<-NIL
```

end-function – complexity **$O(\log n)$**

- function *findMin*(*root*) is:

```
    while root.left != NIL execute:
        root<-root.left
    done
    findMin<-root
```

end-function – complexity **$O(\log n)$**

- function *count*(*root*, *counter*) is:

```
    if root=NIL then:
        count<-void
    endif
```

```
counter<- counter +1
if root.left !=NIL then:
    count(root.left,counter)
endif
if root.rigth !=NIL then:
    count(root.right,counter)
end-function – complexity O(n)
```

- function *iterator(root, i)* is:

```
iterator<- Iterator(root)
end-function – complexity O(1)
```

Iterator

Binary Search Tree (BST) SortedBag (SB) Iterator

An iterator is a structure that is used to iterate throughout the elements of a container, in this case, a SortedBag. An iterator usually contains: a reference to the container it iterates over and another reference to a current element from the container. Iterating through the elements of the container means actually moving said current element from one element to another until the iterator becomes invalid.

Domain

$\mathbf{I} = \{i \mid i \text{ is an iterator over } b \in \mathbf{B} \}$

Representation

Iterator

root: \uparrow Node

Interface

- ***init(i, root)***
description: creates a new iterator for a SortedBag
pre: $b \in \mathbf{B}$
post: $i \in \mathbf{I}$, i is an iterator over b
- ***isValid(i)***
description: returns true if the root is valid, false otherwise
pre: $i \in \mathbf{I}$
post: if the root from \mathbf{I} is a valid one, $\text{valid} \leftarrow \text{true}$,
else $\text{valid} \leftarrow \text{false}$
- ***next(i)***
description: performs the inorder traversal of the sorted bag;
jumps to the next element from the SortedBag or makes the
iterator invalid if no elements are left
pre: $i \in \mathbf{I}$, $\text{valid}(i)$
post: $i' \in \mathbf{I}$, the current element (the root which changes constantly) from i'
refers to the next element from the SortedBag b

- ***getValue(i)***
description: returns the data of the root from the iterator
pre: $i \in I$, valid(i)
post: $getValue \leftarrow$ the data from the root
- ***DeeperToLeft(root)***
description: root becomes the left most node from the sorted bag
pre: root: \uparrow Node
post: root is the left most node from the sorted bag

Pseudocode implementation of the interface operation for the Iterator

- subalgorithm ***init(i,root)*** is:

 root \leftarrow root

 DeeperToLeft(root.left)

end-subalgorithm - complexity **$O(n)$**

- function ***isValid(i)*** is:

 if root \neq NIL then:

 isValid \leftarrow true

 else

 isValid \leftarrow false

 end-if

end-function – complexity **$O(1)$**

- subalgorithm ***next(i)*** is:

if DeeperToLeft(root.right)=false then:

if root.parent!=NIL then:

while root.parent!=NIL and root=root.parent.right execute:

root<-root.parent

done

root<-root.parent

endif

endif

end-subalgorithm – complexity **O(1)**

- function ***getValue(i)*** is:

getValue<-root.data

end-function – complexity **O(1)**

- function ***DeeperToLeft(root)*** is:

if root=NIL then:

DeeperToLeft<-false

endif

if DeeperToLeft(root.left)=false then:

DeeperToLeft<-true

endif

end-function – complexity **O(log n)**

Tests for the functions written in C++

```
void Tests::testSearch() {
    SortedBag<int> BST{ ">" };

    BST.insert(5);
    BST.insert(10);
    BST.insert(3);
    BST.insert(4);
    BST.insert(1);
    BST.insert(11);
    assert(BST.search(5) == true);
    assert(BST.search(4) == true);
    assert(BST.search(2) == false);
    assert(BST.search(1) == true);
    assert(BST.search(12) == false);
}
```

```
void Tests::testRemove() {

    SortedBag<int> BST{ ">" };

    BST.insert(5);
    BST.insert(10);
    BST.insert(3);
    BST.insert(4);
    BST.insert(1);
    BST.insert(11);
    assert(BST.remove(5) == true);
    assert(BST.remove(123) == false);
    assert(BST.remove(12) == false);
    assert(BST.remove(1) == true);
    assert(BST.remove(11) == true);
}
```

```
void Tests::testSize() {

    SortedBag<int> BST{ ">" };

    BST.insert(5);
    BST.insert(10);
    BST.insert(3);
    BST.insert(4);
    BST.insert(1);
    BST.insert(11);
    assert(BST.size() == 6);
    assert(BST.remove(5) == true);
    assert(BST.size() == 5);
    assert(BST.remove(10) == true);
    assert(BST.remove(3) == true);
    assert(BST.remove(4) == true);
    assert(BST.size() == 2);
}
```

```
void Tests::testIterator()
{
    SortedBag<int> BST{ ">" };

    BST.insert(5);
    BST.insert(10);
    BST.insert(3);
    BST.insert(4);
    BST.insert(1);
    BST.insert(11);
    Iterator<int> it = BST.iterator();
    it.next();
    assert(it.getValue()==3);
    int k = 0;
    while (k < BST.size() - 1)
    {
        k++;
        it.next();
    }
    if (it.isValid() == NULL)
        k++;
}

void Tests::testAll() {
    testSearch();
    testRemove();
    testSize();
    testIterator();
}
```

Problem statement

Product sales tree

A company needs to store their daily product sales in a program and may chose to sort them in ascending order, add sales, remove sales. We will use a SortedBag ADT (implemented on a Binary Search Tree) to ensure the storing of similar elements.

Choice

The Sorted Bag is the best way of approaching this problem because, any element can be repeated and the position of the elements does not matter in the end, because the company wants to see how many sales they did. The elements can be sorted as the company wants, usually in ascending order.