

Seminar 4: Activity

Question:

Run `equivalence.py` in your chosen Jupyter Notebook workspace - Testing with Python - which is an implementation of equivalence partitioning. This test partitions integers $[-3, 5]$ into equivalence classes based on $\lambda x, y: (x-y)\%4 == 0$.

In the output, you should be able to see how a set of objects to be partitioned are considered, and a function evaluates if the two objects are equivalent before printing the result.

`test_equivalence_partition()` produces the following output:

```
set([1, -3]) set([2, -2]) set([3, -1]) set([0, 4]) 0 : set([0, 4]) 1 : set([1, -3]) 2 : set([2, -2]) 3 : set([3, -1]) 4 : set([0, 4]) -2 : set([2, -2]) -3 : set([1, -3]) -1 : set([3, -1])
```

You should carry out further investigations on the code and experiment with it.

Remember to record your results, ideas and team discussions in your e-portfolio.

`equivalence.py` code:

```
# CODE SOURCE: https://stackoverflow.com/questions/38924421/is-there-a-standard-way-to-partition-an-interable-into-equivalence-classes-given/38924631#38924631
```

```
def equivalence_partition(iterable, relation):
```

```
    """Partitions a set of objects into equivalence classes
```

Args:

iterable: collection of objects to be partitioned

relation: equivalence relation. I.e. `relation(o1,o2)` evaluates to True

if and only if `o1` and `o2` are equivalent

Returns: classes, partitions

classes: A sequence of sets. Each one is an equivalence class

partitions: A dictionary mapping objects to equivalence classes

"""

classes = []

partitions = {}

for o in iterable: # for each object

find the class it is in

found = False

for c in classes:

if relation(next(iter(c)), o): # is it equivalent to this class?

c.add(o)

```
partitions[o] = c
```

```
found = True
```

```
break
```

```
if not found: # it is in a new class
```

```
classes.append(set([o]))
```

```
partitions[o] = classes[-1]
```

```
return classes, partitions
```

```
def equivalence_enumeration(iterable, relation):
```

```
    """Partitions a set of objects into equivalence classes
```

Same as equivalence_partition() but also numbers the classes.

Args:

iterable: collection of objects to be partitioned

relation: equivalence relation. I.e. relation(o1,o2) evaluates to True

if and only if o1 and o2 are equivalent

Returns: classes, partitions, ids

classes: A sequence of sets. Each one is an equivalence class

partitions: A dictionary mapping objects to equivalence classes

ids: A dictionary mapping objects to the indices of their equivalence classes

```
"""
```

```
classes, partitions = equivalence_partition(iterable, relation)
```

```
ids = {}
```

```
for i, c in enumerate(classes):
```

```
    for o in c:
```

```
        ids[o] = i
```

```
return classes, partitions, ids
```

```
def check_equivalence_partition(classes, partitions, relation):
```

```
    """Checks that a partition is consistent under the relationship"""
```

```
    for o, c in partitions.items():
```

```
        for _c in classes:
```

```
assert (o in _c) ^ (not _c is c)
```

```
for c1 in classes:
```

```
    for o1 in c1:
```

```
        for c2 in classes:
```

```
            for o2 in c2:
```

```
                assert (c1 is c2) ^ (not relation(o1, o2))
```

```
def test_equivalence_partition():
```

```
    relation = lambda x, y: (x - y) % 4 == 0
```

```
    classes, partitions = equivalence_partition(
```

```
        range(-3, 5),
```

```
        relation
```

```
    )
```

```
    check_equivalence_partition(classes, partitions, relation)
```

```
    for c in classes: print(c)
```

```
    for o, c in partitions.items(): print(o, ': ', c)
```

```
if __name__ == '__main__':
```

```
    test_equivalence_partition()
```

Answer Response:

The equivalence partitioning test ran successfully and produced the following results:

1. Equivalence Classes:

- Set 1: $\{-3, 1\}$
- Set 2: $\{-2, 2\}$
- Set 3: $\{-1, 3\}$
- Set 4: $\{0, 4\}$

2. Partitions:

- -3 belongs to the set $\{-3, 1\}$
- -2 belongs to the set $\{-2, 2\}$
- -1 belongs to the set $\{-1, 3\}$
- 0 belongs to the set $\{0, 4\}$
- 1 belongs to the set $\{-3, 1\}$
- 2 belongs to the set $\{-2, 2\}$
- 3 belongs to the set $\{-1, 3\}$
- 4 belongs to the set $\{0, 4\}$

The partitioning is done based on the equivalence relation $(x - y) \% 4 == 0$, which groups numbers with the same remainder when divided by 4.