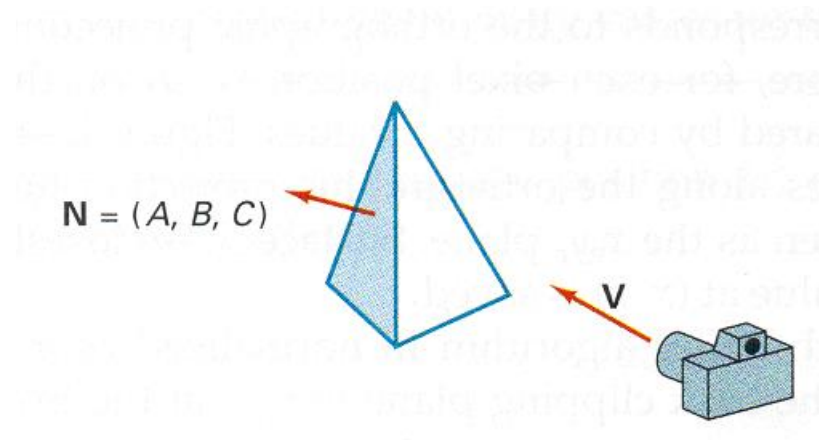




# Visible Surface Determination

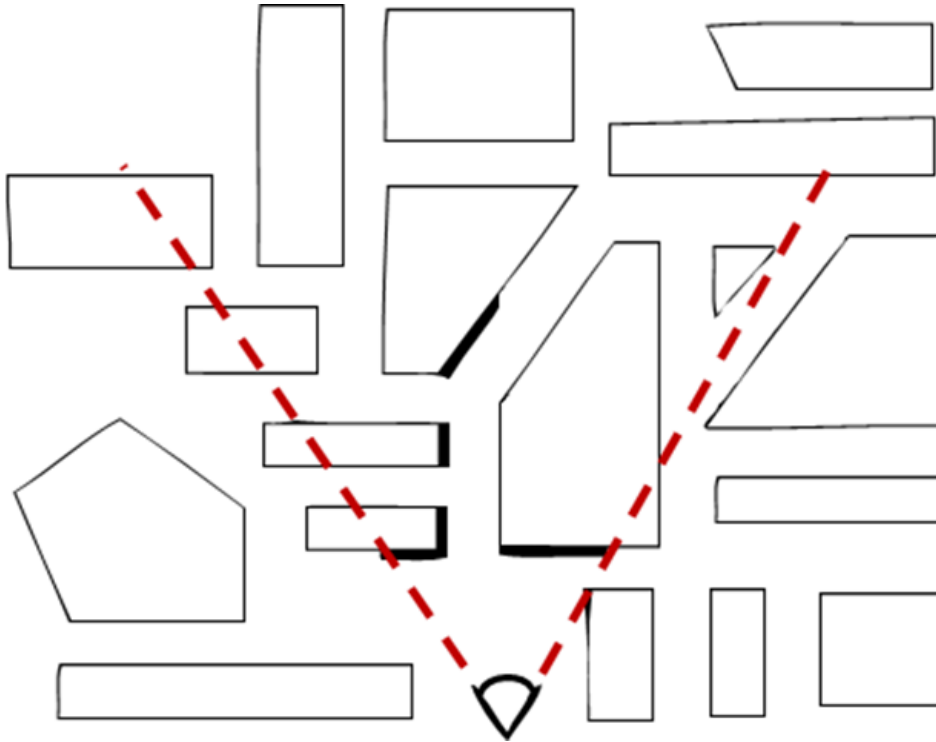


# Overview

- Visible Surface Determination
- Back-Face Culling
- Z-Buffer
- Application Example
- Projections in OpenGL / WebGL

# **VISIBLE SURFACE DETERMINATION**

# Visible Surface Determination



For each object compute:

- The visible edges and surfaces

Why might objects be hidden ?

- Clipping ?
- Occlusion ?

To render or not to render, that is the question...

[Andy Van Dam]

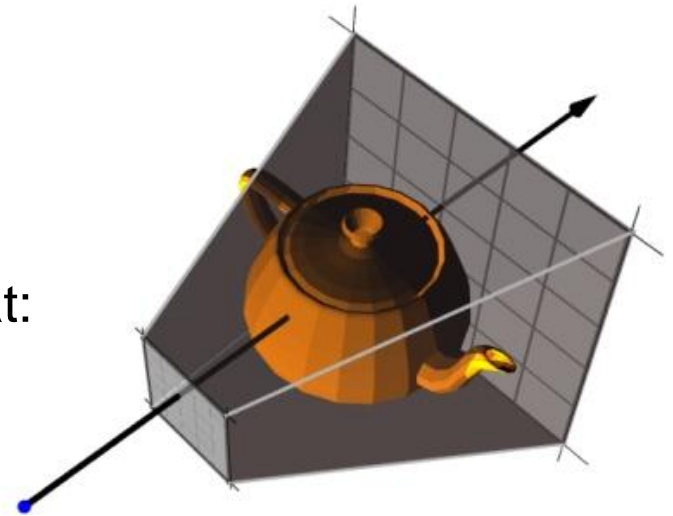
# Clipping vs Occlusion

- Clipping against the view volume
  - It is done at object-level !
- Occlusion / Hidden-Surface Removal
  - It is done at scene-level !
  - Compare depth of object / edges / pixels against other objects / edges / pixels

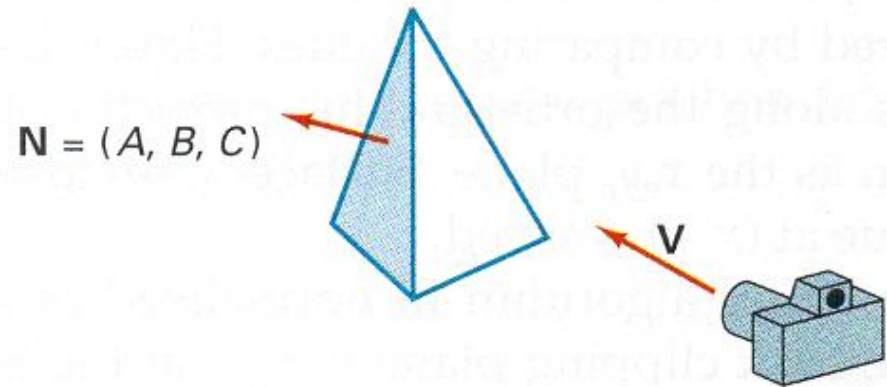
# Possible approaches

- Object-precision algorithms
  - Analyze / compare **objects** or parts of objects to determine which surfaces / faces / edges are **fully or partially visible**
  - Back-Face Culling
- Image-precision algorithms
  - Determine visibility for every **pixel** in the **viewing plane**
  - Work in **3D** to get / compare **depth** values (i.e., **z values**)
  - Z-buffer, A-buffer, Ray-Casting
- **Hybrid** – use both approaches
- Improve performance using
  - Coherence
  - Sorting

- The **visibility** problem
  - Which primitives – after **modeling** transformations, **projection** and **lighting** calculations – contribute for each image pixel
- In general, we solve the dual problem !!
- Which are the **hidden surfaces / faces** that:
  - are **outside of the view volume** ?
  - are **back-faces** in a closed and convex polyhedron ?
  - are **hidden by other faces** closer to the viewpoint / camera ?



- Determine which **models** or **parts of models** are **visible** from the chosen **viewpoint** and **projection type**
- There are various methods with different:
  - approaches
  - **running time**
  - **required memory**
  - ....
- More or less adequate given:
  - **scene complexity**
  - available hardware
  - ....





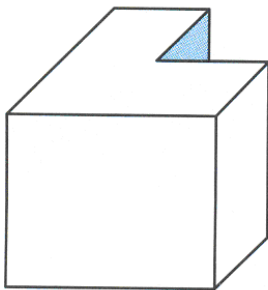
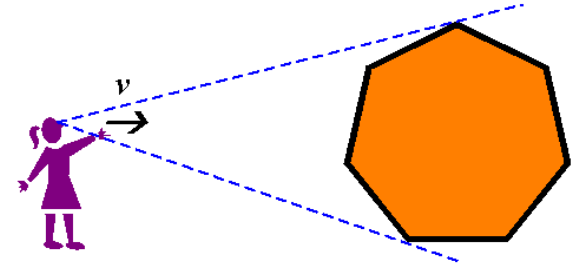
## Some methods

- Back-face **culling**
- Depth-buffer (**z-buffer**)
- A-buffer
- **Depth-sorting** (painter's algorithm)
- **Ray-casting**

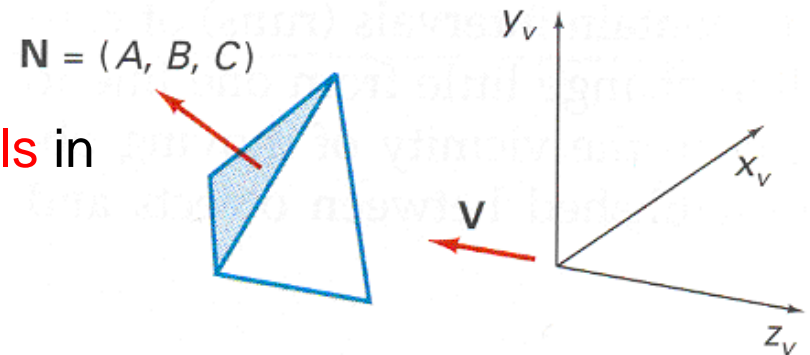
# **BACK-FACE CULLING**

# Back-Face Culling

- Sufficient for **a single convex polyhedron** which is not sectioned by clipping
- **Not sufficient** for
  - concave polyhedra
  - when there are **two or more models** in front of each other



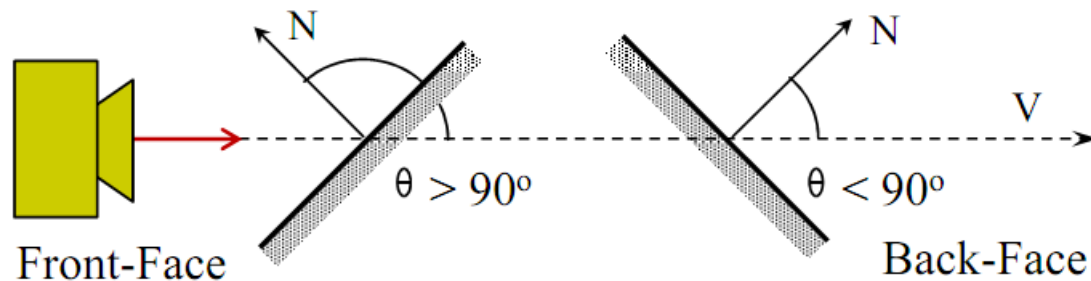
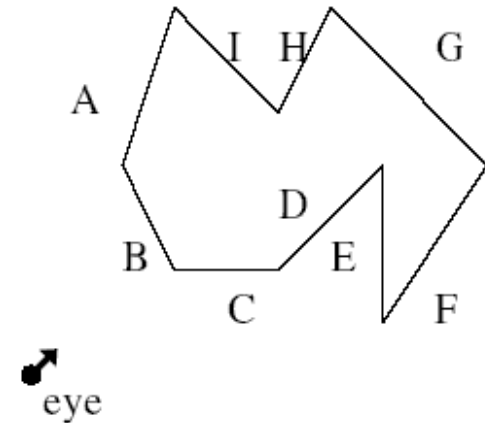
Concave model with a partially visible face



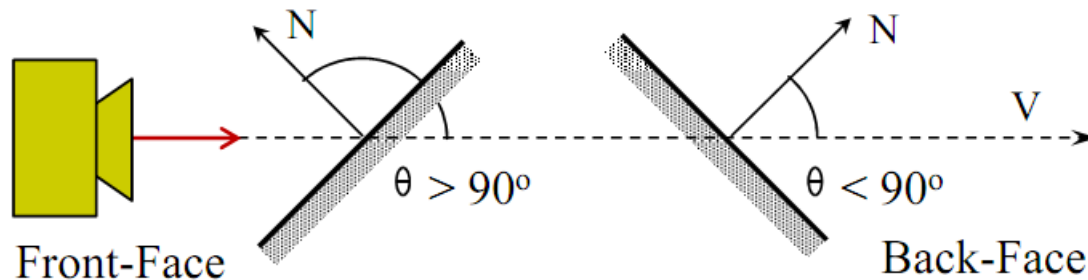
When looking at the negative  $z_z'$  semi-axis, a polygon is a **back-face** if  $C \leq 0$

# Back-Face Culling

- What to do in a general case ?
- For each face, compute the angle between
  - The normal vector to the face
  - The viewing direction, defined by the viewpoint



# Back-Face Culling



- Efficiency: just compute the **scalar product** !!
  - **Reject** a face if  $N \cdot V > 0$
  - What happens if  $N \cdot V = 0$  ?
- **Simplification** when  $V = (0, 0, -1)$  !!
- On average, approx. **half** of the faces are removed!

# OpenGL – Culling

- Back-Face Culling

```
glEnable( GL_CULL_FACE );
```

```
glCullFace( GL_BACK );
```

- Front-Face Culling

```
glEnable( GL_CULL_FACE );
```

```
glCullFace( GL_FRONT );
```

## WebGL – Culling

- Back-Face Culling

```
gl.enable( gl.CULL_FACE ); // Default: disabled!
```

```
gl.cullFace( gl.BACK ); // Default
```

- Front-Face Culling

```
gl.enable( gl.CULL_FACE );
```

```
gl.cullFace( gl.FRONT );
```

## WebGL – Culling

- Switching on / off

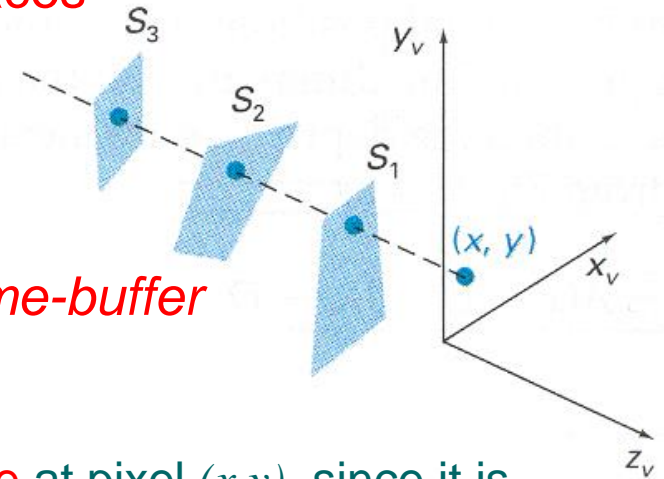
```
if( gl.isEnabled( gl.CULL_FACE ) )  
{  
    gl.disable( gl.CULL_FACE );  
}  
else  
{  
    gl.enable( gl.CULL_FACE );  
}
```



# Z-BUFFER

# Depth-Buffer (z-buffer)

- Works in *image-space*
- Compares the **depth** of each surface relative to each **pixel** in the **viewplane**
- Fast and easy to implement for **planar surfaces**
- Can be adapted for curved surfaces
- Needs a *depth-buffer* in addition to the *frame-buffer*



$S_1$  is **visible** at pixel  $(x, y)$ , since it is closer to the viewplane

# Z-Buffer Algorithm

- Draw **every polygon** that can't be rejected trivially
  - I.e., it is totally outside the view volume
- If **a piece** (one or more pixels) of a polygon that is **closer to the front** is found
- **Paint** over whatever was behind it
- Use plane equation for polygon,  $z = f(x, y)$
- Note: use **positive z** here  $[0, 1]$

# Z-Buffer Algorithm

```
void zBuffer() {  
    int x, y;  
    for (y = 0; y < YMAX; y++)  
        for (x = 0; x < XMAX; x++) {  
            WritePixel (x, y, BACKGROUND_VALUE);  
            WriteZ (x, y, 1);  
        }  
    for each polygon {  
        for each pixel in polygon's projection {  
            //plane equation  
            double pz = Z-value at pixel (x, y);  
            if (pz <= ReadZ (x, y)) {  
                // New point is closer to front of view  
                WritePixel (x, y, color at pixel (x, y))  
                WriteZ (x, y, pz);  
            }  
        }  
    }  
}
```

[Andy Van Dam]

# Example

Initial *z-buffer* values

0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

Depth-values for polygon

5	5	5	5	5	5	5	
5	5	5	5	5	5		
5	5	5	5	5			
5	5	5	5				
5	5	5					
5	5						
5							



Overwrite *z-buffer*

5	5	5	5	5	5	5	0
5	5	5	5	5	5	0	0
5	5	5	5	5	0	0	0
5	5	5	5	0	0	0	0
5	5	5	0	0	0	0	0
5	5	0	0	0	0	0	0
5	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

Another polygon

3							
4	3						
5	4	3					
6	5	4	3				
7	6	5	4	3			
8	7	6	5	4	3		



Final *z-buffer*

5	5	5	5	5	5	5	0
5	5	5	5	5	5	0	0
5	5	5	5	5	0	0	0
5	5	5	5	0	0	0	0
6	5	5	3	0	0	0	0
7	6	5	4	3	0	0	0
8	7	6	5	4	3	0	0
0	0	0	0	0	0	0	0

Note:

0 – background depth

Max – viewplane

# Another example

255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255

+

64	64	64	64	64	64	64	
64	64	64	64	64	64		
64	64	64	64	64			
64	64	64	64				
64	64	64					
64	64						
64							
64							

=

64	64	64	64	64	64	64	255
64	64	64	64	64	64	255	255
64	64	64	64	64	255	255	255
64	64	64	64	255	255	255	255
64	64	64	255	255	255	255	255
64	64	255	255	255	255	255	255
64	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255

64	64	64	64	64	64	64	255
64	64	64	64	64	64	255	255
64	64	64	64	64	255	255	255
64	64	64	64	255	255	255	255
64	64	64	255	255	255	255	255
64	64	255	255	255	255	255	255
64	255	255	255	255	255	255	255
255	255	255	255	255	255	255	255

+

127							
127	127						
127	127	127					
127	127	127	127				
127	127	127	127	127			

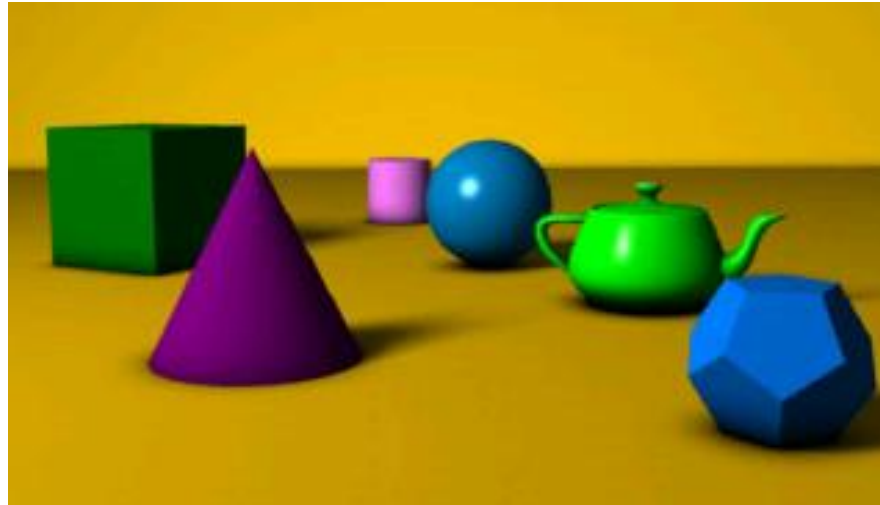
=

64	64	64	64	64	64	64	255
64	64	64	64	64	64	255	255
64	64	64	64	64	255	255	255
64	64	64	64	255	255	255	255
64	64	64	255	255	255	255	255
64	64	127	255	255	255	255	255
64	127	127	127	255	255	255	255
127	127	127	127	127	255	255	255

integer Z-buffer with  
near = 0, far = 255

[Andy Van Dam]

3D scene



Z-buffer



1. Initialize the depth buffer and refresh buffer so that for all buffer positions  $(x, y)$ ,

$$\text{depth}(x, y) = 0, \quad \text{refresh}(x, y) = I_{\text{backgnd}}$$

2. For each position on each polygon surface, compare depth values to previously stored values in the depth buffer to determine visibility.

- Calculate the depth  $z$  for each  $(x, y)$  position on the polygon.
- If  $z > \text{depth}(x, y)$ , then set

$$\text{depth}(x, y) = z, \quad \text{refresh}(x, y) = I_{\text{surf}}(x, y)$$

where  $I_{\text{backgnd}}$  is the value for the background intensity, and  $I_{\text{surf}}(x, y)$  is the projected intensity value for the surface at pixel position  $(x, y)$ . After all surfaces have been processed, the depth buffer contains depth values for the visible surfaces and the refresh buffer contains the corresponding intensity values for those surfaces.

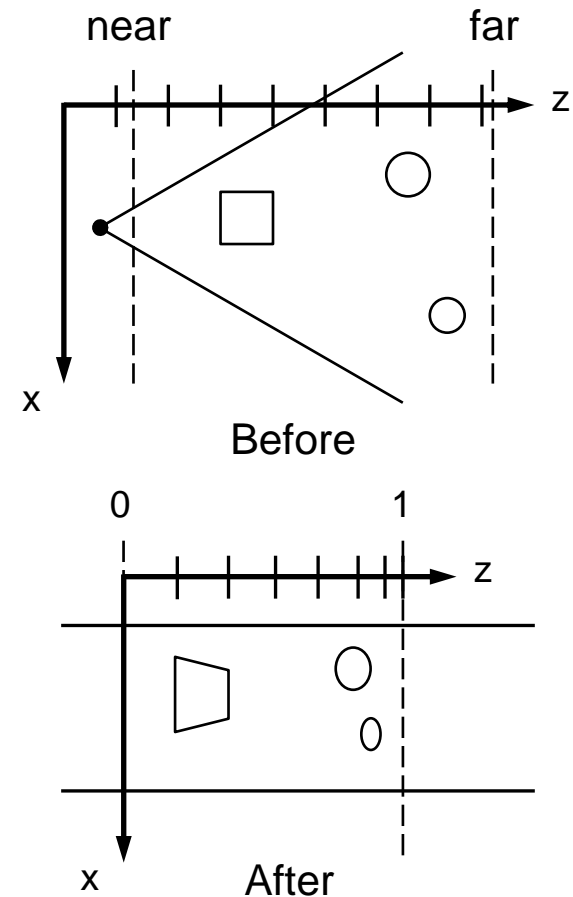
Some authors present different versions of the algorithm, using other depth values for the viewplane and the background and/or normalized coordinates



- Advantages:
  - Easy, **no** need to **previously sort** the various surfaces
  - Fast
- Disadvantages:
  - Need for **additional memory**
  - Depth **precision** problems / limitations
  - It finds **one visible surface** for each **pixel**
  - I.e. it can only handle **opaque surfaces**

# Depth precision loss

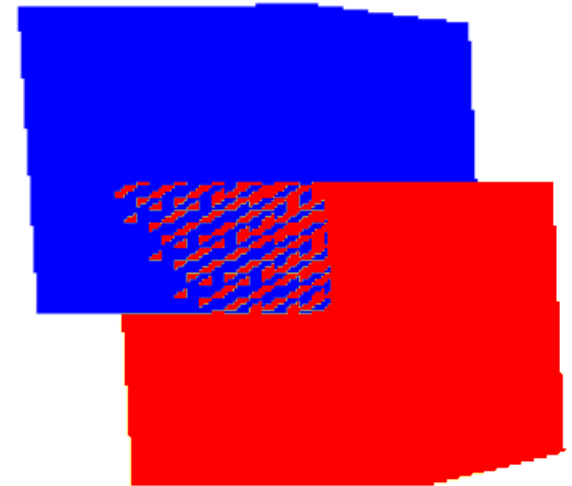
- Perspective foreshortening
  - Compression in z-axis in post-perspective space
  - Objects far away from camera have **z-values very close to each other**
- **Depth** information **loses precision** rapidly
  - Leads to z-ordering bugs called **z-fighting**



[Andy Van Dam]

# Z-Fighting

- Z-fighting occurs when two **primitives have similar values** in the z-buffer
  - Coplanar polygons (two polygons that occupy the same space)
  - One is arbitrarily chosen over the other, but z varies across the polygons and binning will cause artifacts
  - Behavior is deterministic: the same camera position gives the same z-fighting pattern



Two intersecting cubes

[Andy Van Dam]

Edwin Catmull, the z-buffer inventor,  
former president of Walt Disney and  
Pixar Animation Studios, received an  
Oscar in 2001

Pixar's RenderMan

<http://renderman.pixar.com/>



# OpenGL – Depth-Test

- Enabling

```
glEnable( GL_DEPTH_TEST );
```

- Buffers

```
glutInitDisplayMode( GLUT_RGB |  
                    GLUT_DOUBLE | GLUT_DEPTH );
```

- Clearing the buffers before rendering

```
glClear( GL_COLOR_BUFFER_BIT |  
        GL_DEPTH_BUFFER_BIT );
```

## WebGL – Depth-Test

- Enabling

```
gl.enable( gl.DEPTH_TEST ); // Default: disabled!
```

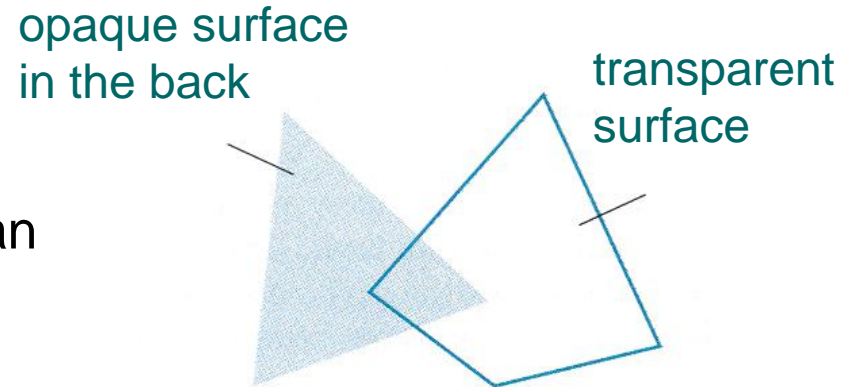
- Clearing the buffers before **each** rendering

```
gl.clear( gl.COLOR_BUFFER_BIT |  
          gl.DEPTH_BUFFER_BIT );
```

# A-BUFFER

# A-Buffer

- Anti-aliased area-average, **accumulation buffer**
- An **extension of the *depth-buffer***, allows to take into account more than one surface, i.e., handling **transparent surfaces**
- It also allows for ***lesser aliasing*** of model edges

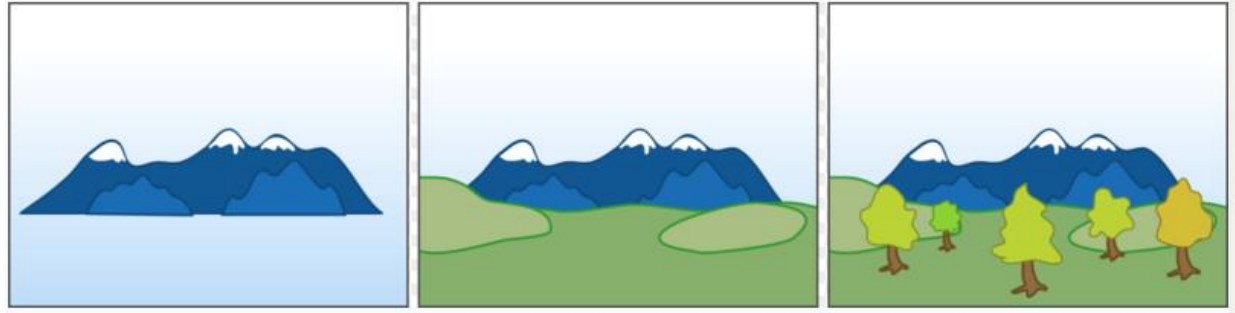


To see an **opaque surface** through a **transparent surface** requires the **accumulation** of the contributions from both surfaces

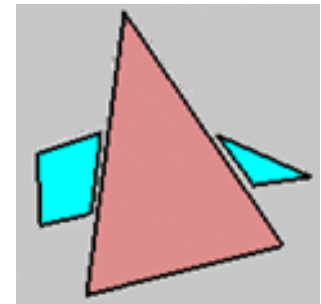
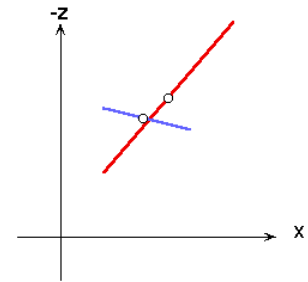


# **THE PAINTER'S ALGORITHM**

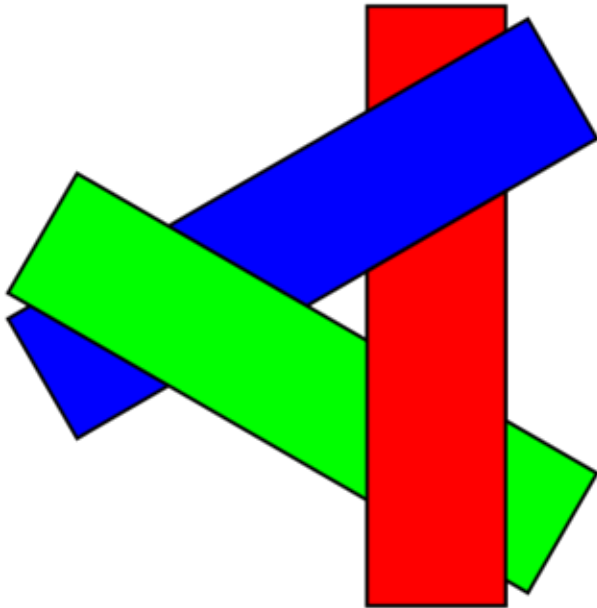
# Depth-Sorting (Painter's Algorithm)



- *Image-space* and *object-space* operations
- Main steps:
  - 1- **Sort** the surfaces by their **depth** relative to the viewplane
  - 2- **Back-to-front projection** of the sorted surfaces
- What if **superpositions** occur ?
  - **Subdivide** the surfaces or change their order
- **No** need for a **depth-buffer** !!
- BUT, it renders distant surface parts that, in the end, will **not be visible**



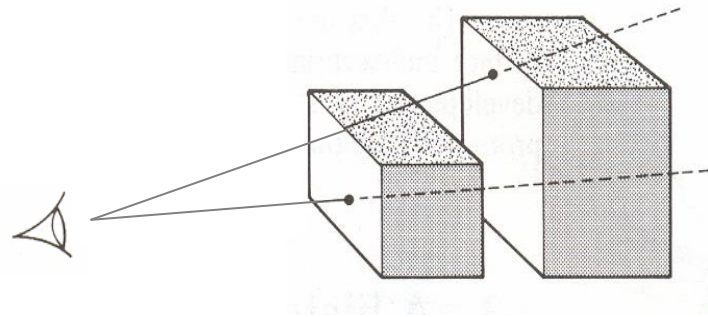
# Painter's algorithm – What happens ?



[Andy Van Dam]

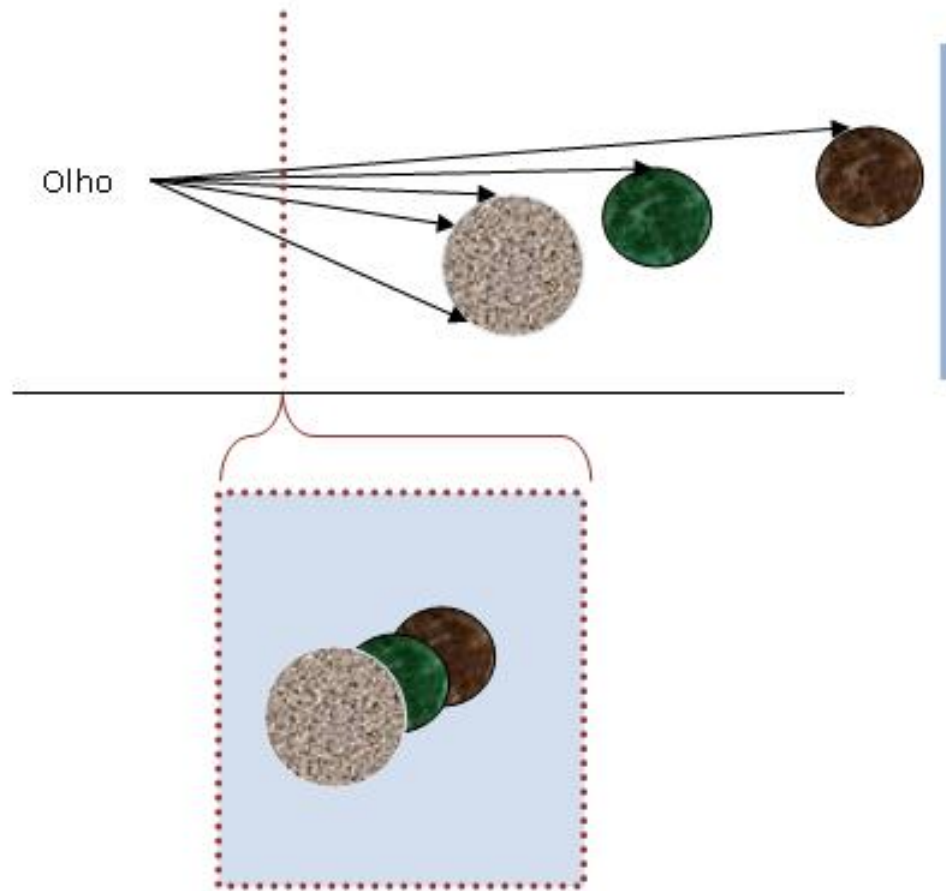
# RAY-CASTING

# Ray-Casting



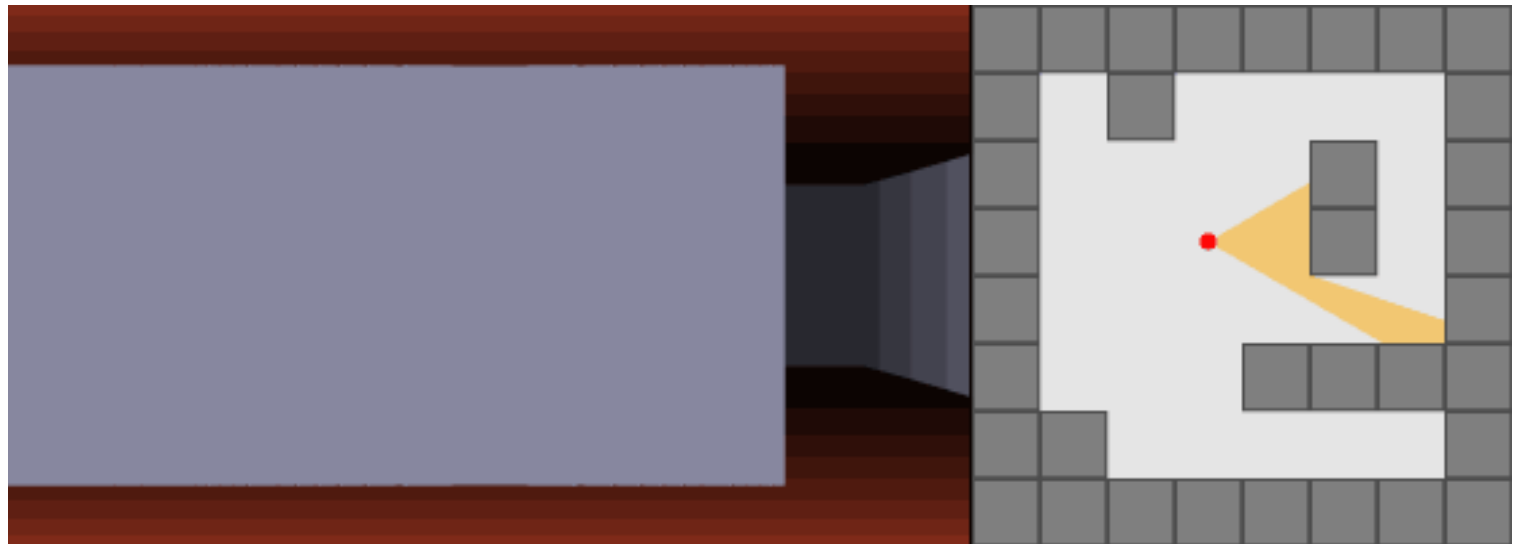
- **Image-space** method
- Which models are intersected by a **ray cast from the viewpoint** that passes through the **center of a pixel** ?
- If models are opaque, the **intersection point closer to the viewpoint** determines the color (i.e., visible surface) for the corresponding pixel

# Ray-Casting



[Wikipedia]

# Ray-Casting



[Wikipedia]

# REFERENCES



# References

- Hearn, D., P. Baker, *Computer Graphics with OpenGL*, Addison Wesley, 2004
- Hearn, D., P. Backer, *Computer Graphics*, 2nd. Ed., Prentice Hall, 1994
- Foley, J., S. Van Dam, S. Feiner, J. Hughes, *Computer Graphics, Principles and Applications*, 2nd. Ed., Addison Wesley, 1991
- Watt, A., F. Policarpo, *The Computer Image*, Addison Wesley, 1998