Bragg Scattering with ultracold Erbium atoms

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I hereby declare that this thesis was formulated by myself and that no sources or tools other than those cited were used.

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Introduction

Erbium Bose-Einstein Condensate

This chapter has the objective of briefly review some relevant properties of Erbium, which will clarify what makes it relevant in the study of ultra cold atoms. After this, the basic theory of Bose-Einstein condensation will be discussed, along with a brief description of the experimental phases and tools required to create and observe an Erbium Bose-Einstein Condensate (BEC). This experimental realization will be the foundation on which the following chapters will be grounded when discussing further experimental achievements.

2.1 Properties of atomic erbium

Erbium is a chemical element with an atomic number of 68, which belongs to the series of the Lanthanides. It is also part of the group called Rare-earth elements and it was first discovered by G. Monsander in 1843 [1]. The name of "Erbium" comes from the name of the Swedish village of Ytterby, the place where it was extracted. At that time, the similarity of rare-earth metals' chemical properties made their distinction extremely difficult. For this reason, what G. Monsander thought to be pure Erbium oxide was in fact a mixture of different rare-earth metal oxides. The element is not obtained in a reasonably pure form until 1937 by W. Klemm and H. Bommer [2].

Considering some basic properties of this element, under standard conditions erbium is in a solid state. It has a silver shining surface, which oxidizes with air contact. This rare-earth metal has a melting point of $1\,802\,\text{K}$ and boiling point of $3\,136\,\text{K}$. As a result, to be able to work with a free atomic gas of erbium requires to heap up the solid erbium metal to high temperatures [3].

The number of stables isotopes of Erbium is 6 and they can be seen in Table 2.1. All of them are bosons with nuclear spin of zero, in exception of ^{167}Er, which is a fermion with spin of 7/2. The chosen isotope for this experiment is ^{168}Er because of its bosonic nature, high abundance and favorable scattering properties.

In addition to these properties, erbium atoms have a rather complex energetic level scheme due to its open 4f shell. This one lacks 2 electrons to be completely filled, which makes erbium to have an electronic ground state with an orbital angular momentum value of $L = 5$ and a high magnetic moment of seven Bohr magneton $7\mu_B$ [5]. This high value for the orbital angular momentum in the ground state of erbium provides several advantages for Raman-coupling processes. Leading to longer coherence times and stronger synthetic magnetic fields when comparing with other alkali metals like rubidium or cesium, commonly used in ultracold atoms experiments [6].

Isotope	Abundance [%]	Atomic Mass [u]	Nuclear Spin [$\hbar$]
Er^{162}	0.14	161.928775	0
Er^{164}	1.61	163.929198	0
Er^{166}	33.60	165.930290	0
Er^{167}	22.95	166.932046	7/2
Er^{168}	26.80	167.932368	0
Er^{170}	14.90	169.935461	0

Table 2.1: Table with the stable isotopes of Erbium that can be found on Nature with their respective Abundance ratio, Atomic mass and Nuclear Spin. Spectroscopy data taken from [4].

A scheme of erbium energy levels together with the atomic transitions used in this experiment can be seen in figure 2.1. The scheme shows that the electronic ground state of erbium is [Xe] $4f^{12}6s^2$, where [Xe] represents the complete electronic configuration of Xenon[1]. Moreover, the used optical transitions are represented by colored arrows in the figure and its spectroscopic data is shown in table 2.2. From now on, these three transitions will respectively be referred to as the 401nm, 583nm, and 841nm transitions.

Finally, it must be noted that aside from the discussed application in ultracold atoms, erbium is used in multiple commercial applications. One prominent example is the use or erbium as a fiber amplifier in doped silicon fibers [7]. Furthermore, in nuclear physics it is used as neutron absorbing control rods [8].

Parameters			Transitions		
Name	Symbol	Unit	401nm	583nm	841nm
Wavelength in vacuum	λ	nm	400.91	582.84	841.22
Lifetime	τ	µs	0.045	0.857	20
Natural linewidth	$\Delta\nu_0$	kHz	33 370	185.71	7.96
Decay rate	γ	s^{-1}	2.22×10^8	1.17×10^6	5.00×10^4
Saturation intensity	I_S	mW cm^{-1}	71.80	0.12	1.74
Doppler temperature	T_D	µK	848.69	4.46	0.19
Doppler velocity	v_D	cm s^{-1}	21.5	1.49	0.31

Table 2.2: Spectroscopic data for the optical transitions of Erbium used in this experiment. These transitions are called the 401nm, 583nm, and 841nm transitions and can be seen in figure 2.1. Data taken from [5, 9–12]

2.2 Bose-Einstein Condensation

A BEC is generally defined as a state of matter formed when a gas of bosons with a low density is cooled to near-zero temperatures (typically a few hundreds nanokelvins). To understand this definition and the next theoretical principles is necessary to define what is a boson.

In quantum mechanics, bosons are particles with an integer value in their spin. Because of this,

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[1] [Xe] = $1s^2\ 2s^2\ 2p^6\ 3s^2\ 3p^6\ 3d^{10}\ 4s^2\ 4p^6\ 4d^{10}\ 5s^2\ 5p^6$

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Figure 2.1: Energy level scheme of Erbium represented as a function of the total angular momentum J. This scheme shows only a range of energies relevant for the experiment of up to 25000 cm^{-1}. The different arrows show us the used transitions and for which phase of the experiment they are used for. The red lines represent energy states with even parity and the black lines those with odd parity. Data taken from [13].

also have a symmetric wave function under the interchange of two particles, which allows bosons to have the same quantum state. Unlike its counterpart fermions, which have a half odd integer spin and an anti-symmetric wave function. Leading to Pauli's exclusion principle that avoids more than one fermion to occupy the same quantum state [14].

It was the Indian physicist S. N. Bose in 1924, the first one who described in a successful way an ideal gas of non interacting free photons, behaving like mass-less bosons. His idea was initially rejected for publication in scientific journals. However, Bose sent the manuscript to A. Einstein, who recognized its importance, translated the paper to german and saw to it that was published [15]. After this, Einstein extended Bose's treatment to massive particles and predicted the occurrence of a phase transition in a gas of non-interacting atoms, what is today known as a BEC [16, 17].

These publications led to Bose-Einstein statistics, a model that explains the energetic behavior of a non-interacting gas of indistinguishable N bosons, each one with mass M. The average number of particles at a given non-degenerate state with wave vector $\mathbf{k}$ and energy $E_{\mathbf{k}} = \hbar^2 \mathbf{k}^2/2M$ is given by

$$\bar{n}_{\mathbf{k}} = \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \tag{2.1}$$

For the ideal gas of bosons in thermal equilibrium at a temperature T, Boltzmann constant k_B and chemical potential μ, which depends of N and T [18]. This relation can be expressed as

$$N = \sum_{\mathbf{k}} \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \tag{2.2}$$

So the chemical potential μ is determined such that Eq. (2.2) is satisfied for any given N remaining constant. Now, expanding into the thermodynamic limit where N and the occupied volume V are increased to infinite values keeping the particle density $n = V/N$ constant. The sum over $\mathbf{k}$ appearing in Eq. (2.2) can be replaced by an integral such as

$$n = \frac{N}{V} = \frac{1}{(2\pi)^3} \int d^3k \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \tag{2.3}$$

For decreasing values of T and constant n, the chemical potential increases becoming zero at a critical temperature T_C. By making $\mu = 0$, $T = T_C$ and $E_{\mathbf{k}} = \hbar^2 \mathbf{k}^2/2M$ in Eq. (2.3) results

$$n = \zeta(3/2)\left(\frac{M k_B T_C}{2\pi\hbar^2}\right)^{3/2} \tag{2.4}$$

Where $\zeta(3/2) \simeq 2.612$ denotes the Riemann zeta function evaluated at 3/2. So the critical temperature of the BEC is given by

$$T_C = 3.31 \frac{\hbar^2 n^{2/3}}{k_B M} \tag{2.5}$$
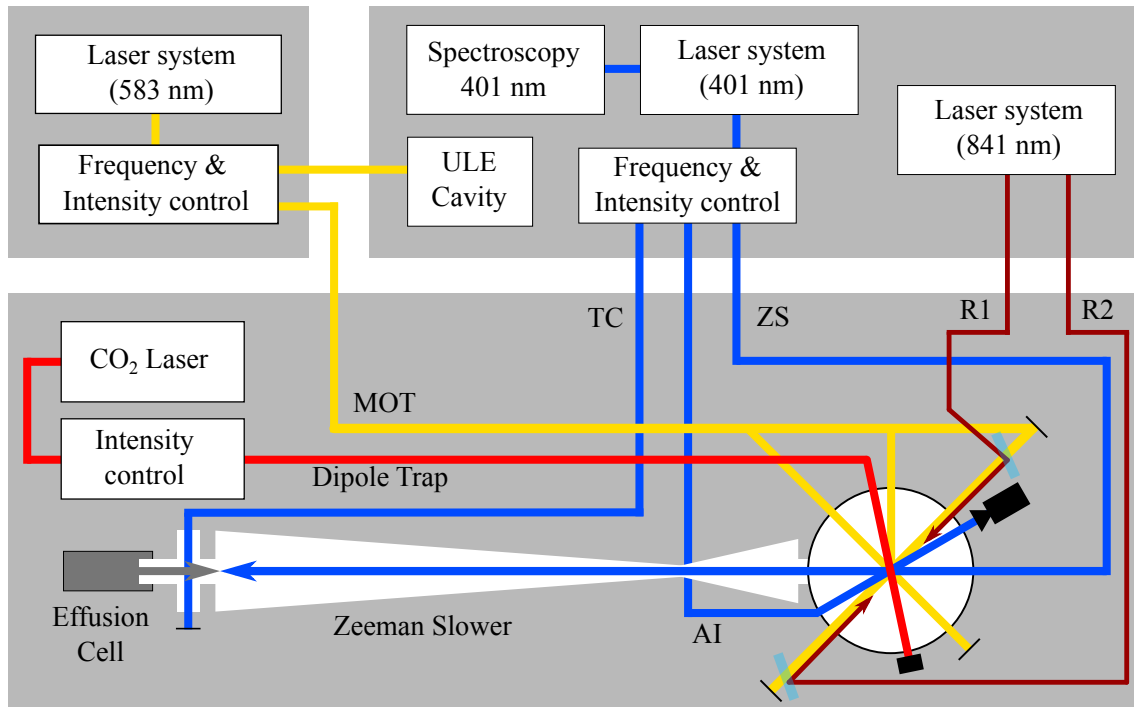
2.3 Experimental preparation

Figure 2.2: Scheme of the experimental set up

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Useful information

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Acronyms

BEC   Bose-Einstein Condensate