

Bragg Scattering with ultracold Erbium atoms

Pedro Castro Perez

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Acknowledgements

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CHAPTER 1

Introduction

Erbium Bose-Einstein condensate

This chapter has the objective of briefly review some relevant properties of Erbium, which will clarify what makes it relevant in the study of ultra cold atoms. After this, the basic theory of Bose-Einstein condensation will be discussed, along with a brief description of the experimental phases required to create and observe an erbium Bose-Einstein condensate (BEC). This experimental realization will be the foundation on which the following chapters will be grounded when discussing further experimental achievements.

2.1 Properties of erbium

Erbium is a chemical element with an atomic number of 68, which belongs to the series of the Lanthanides. It is also part of the group called Rare-earth elements and it was first discovered by G. Monsander in 1843 [1]. The name of “Erbium” comes from the name of the Swedish village of Ytterby, the place where it was extracted. At that time, the similarity of rare-earth metals’ chemical properties made their distinction extremely difficult. For this reason, what G. Monsander thought to be pure Erbium oxide was in fact a mixture of different rare-earth metal oxides. The element is not obtained in a reasonably pure form until 1937 by W. Klemm and H. Bommer [2].

Considering some basic properties of this element, under standard conditions erbium is in a solid state. It has a silver shining surface, which oxidizes with air contact. This rare-earth metal has a melting point of 1 802 K and boiling point of 3 136 K. As a result, to be able to work with a free atomic gas of erbium requires to heat up the solid erbium metal to high temperatures [3].

The number of stable isotopes of Erbium is 6 and they can be seen in Table 2.1. All of them are bosons with nuclear spin of zero, in exception of ^{167}Er , which is a fermion with spin of $7/2$. The chosen isotope for this experiment is ^{168}Er because of its bosonic nature (see Section 2.2), high abundance and favorable scattering properties.

In addition to these properties, erbium atoms have a rather complex energetic level scheme due to its open 4f shell. This one lacks 2 electrons to be completely filled, which makes erbium to have an electronic ground state with an orbital angular momentum value of $L = 5$ and a high magnetic moment of seven Bohr magneton $7\mu_B$ [5]. This high value for the orbital angular momentum in the ground state of erbium provides several advantages for Raman-coupling processes. Leading to longer coherence times and stronger synthetic magnetic fields when comparing with other alkali metals like rubidium or cesium, commonly used in ultracold atoms experiments [6].

Isotope	Abundance [%]	Atomic Mass [u]	Nuclear Spin [\hbar]
Er ¹⁶²	0.14	161.928775	0
Er ¹⁶⁴	1.61	163.929198	0
Er ¹⁶⁶	33.60	165.930290	0
Er ¹⁶⁷	22.95	166.932046	7/2
Er ¹⁶⁸	26.80	167.932368	0
Er ¹⁷⁰	14.90	169.935461	0

Table 2.1: Table with the stable isotopes of Erbium that can be found on Nature with their respective Abundance ratio, Atomic mass and Nuclear Spin. Spectroscopy data taken from [4].

A scheme of erbium energy levels together with the atomic transitions used in this experiment can be seen in figure 2.1. The scheme shows that the electronic ground state of erbium is $[\text{Xe}] 4f^{12}6s^2$, where $[\text{Xe}]$ represents the complete electronic configuration of Xenon¹. Moreover, the used optical transitions are represented by colored arrows in the figure and its spectroscopic data is shown in table 2.2. From now on, these three transitions will respectively be referred to as the 401nm, 583nm, and 841nm transitions.

Finally, it must be noted that aside from the discussed application in ultracold atoms, erbium is used in multiple commercial applications. One prominent example is the use of erbium as a fiber amplifier in doped silicon fibers [7]. Furthermore, in nuclear physics it is used as neutron absorbing control rods [8].

Parameters			Transitions		
Name	Symbol	Unit	401nm	583nm	841nm
Wavelength in vacuum	λ	nm	400.91	582.84	841.22
Lifetime	τ	μs	0.045	0.857	20
Natural linewidth	$\Delta\nu_0$	kHz	33 370	185.71	7.96
Decay rate	γ	s^{-1}	2.22×10^8	1.17×10^6	5.00×10^4
Saturation intensity	I_S	mW cm^{-1}	71.80	0.12	1.74
Doppler temperature	T_D	μK	848.69	4.46	0.19
Doppler velocity	v_D	cm s^{-1}	21.5	1.49	0.31
Recoil temperature	T_R	nK	354.95	167.94	80.43
Recoil velocity	v_R	mm s^{-1}	5.93	4.08	2.82

Table 2.2: Spectroscopic data for the optical transitions of Erbium used in this experiment. These transitions are called the 401nm, 583nm, and 841nm transitions and can be seen in figure 2.1. Shown spectroscopic data taken from [5, 9–12]

¹ $[\text{Xe}] = 1s^2 2s^2 2p^6 3s^2 3p^6 3d^{10} 4s^2 4p^6 4d^{10} 5s^2 5p^6$



Figure 2.1: Energy level scheme of Erbium represented as a function of the total angular momentum J . This scheme shows only a range of energies relevant for the experiment of up to 25000 cm^{-1} . The different arrows show us the used transitions and for which phase of the experiment they are used for. The red lines represent energy states with even parity and the black lines those with odd parity. Data taken from [13].

2.2 Bose-Einstein Condensation

A BEC is generally defined as a state of matter formed when a gas of bosons with a low density is cooled to near-zero temperatures (typically a few hundreds nanokelvins). To understand this definition and the next theoretical principles is necessary to define what is a Boson. In quantum mechanics, bosons are particles with an integer value in their spin. Because of this, also have a symmetric wave function under the interchange of two particles, which allows bosons to have the same quantum state. Unlike its counterpart fermions, which have a half odd integer spin and an anti-symmetric wave function. Leading to Pauli's exclusion principle that avoids more than one fermion to occupy the same quantum state [14].

It was the Indian physicist S. N. Bose in 1924, the first one who described in a successful way an ideal gas of non interacting free photons, behaving like mass-less bosons. His idea was initially rejected for publication in scientific journals. However, Bose sent the manuscript to A. Einstein, who recognized its importance, translated the paper to german and saw to it that was published [15]. After this, Einstein extended Bose's treatment to massive particles and predicted the occurrence of a phase transition in a gas of non-interacting atoms, what is today known as a BEC [16, 17].

These publications led to Bose-Einstein statistics, a model that explains the energetic behavior of a non-interacting gas of indistinguishable N bosons, each one with mass M . The average number of particles at a given non-degenerate state with wave vector \mathbf{k} and energy $E_{\mathbf{k}} = \hbar^2 \mathbf{k}^2 / 2M$ is given by

$$\bar{N}_{\mathbf{k}} = \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \quad (2.1)$$

For an ideal gas of bosons in thermal equilibrium at a temperature T , Boltzmann constant k_B and chemical potential μ , which depends of N and T [18]. This relation can be expressed as

$$N = \sum_{\mathbf{k}} \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \quad (2.2)$$

So the chemical potential μ is determined such that Eq. (2.2) is satisfied for any given N remaining constant. Now, expanding into the thermodynamic limit where N and the occupied volume V are increased to infinite values keeping the particle density $n = V/N$ constant. The sum over \mathbf{k} appearing in Eq. (2.2) can be replaced by an integral such as

$$n = \frac{N}{V} = \frac{1}{(2\pi)^3} \int d^3 k \frac{1}{e^{(E_{\mathbf{k}} - \mu)/k_B T} - 1} \quad (2.3)$$

For decreasing values of T and constant n , the chemical potential increases becoming zero at a critical temperature T_C . By making $\mu = 0$, $T = T_C$ and $E_{\mathbf{k}} = \hbar^2 \mathbf{k}^2 / 2M$ in Eq. (2.3) results

$$n = \zeta(3/2) \left(\frac{M k_B T_C}{2\pi \hbar^2} \right)^{3/2} \quad (2.4)$$

Where $\zeta(3/2) \simeq 2.612$ denotes the Riemann zeta function evaluated at $3/2$. So the critical temperature of the BEC is given by

$$T_C = 3.31 \frac{\hbar^2 n^{2/3}}{k_B M} \quad (2.5)$$

A relevant case of study is when $T < T_C$ because a fraction of the N bosons remains in the ground state with an energy $E = 0$. So the ideal gas of bosons can be divided in two energetic groups $N = N_{E=0} + N_{E>0}$. It must be noted that, the replacement of a sum by an integral in Eq. (2.3) can only be take place in group of particles with an energy greater than zero $E > 0$. As a result of this, the integral of Eq. (2.3) for the case $T < T_C$ results

$$\frac{N_{E>0}}{V} = \zeta(3/2) \left(\frac{M k_B T}{2\pi \hbar^2} \right)^{3/2} \quad (2.6)$$

Using now equations (2.5), (2.4) and the fact that $N_{E>0} = N - N_{E=0}$ results in an expression of the

relative population of a BEC in an ideal bosons gas as a function of temperature:

$$\frac{N_{E=0}}{N} = 1 - \left(\frac{T}{T_C} \right)^{3/2} \quad (2.7)$$

An intuitive way to think about this is to imagine the bosons as wave packets with a size of the thermal de Broglie length λ_{th} . This parameter is conventionally defined [19].

$$\lambda_{th} = \frac{h}{\sqrt{2\pi M k_B T}} \quad (2.8)$$

For falling temperatures, the thermal de Broglie length begins to increase and the wave packets representing the bosons become greater in size. At $T \lesssim T_C$ the particles begin to occupy macroscopically the ground state and its wave packets start to overlap forming a macroscopic wave function, capable of describing the whole particle system. This is one of the most relevant properties of a BEC.

Now, we combine equations 2.4 and 2.8 obtaining

$$n\lambda_{th}^3 = \zeta(3/2) \simeq 2.612 \quad \text{for } T = T_C \quad (2.9)$$

The product of density with cubic de Broglie length is defined in literature as the phase-space density $\rho_{psd} \equiv n\lambda_{th}^3$. This parameter is normally used as a way of quantifying a given bosonic system. From Eq. (2.9), one can deduce that to form a BEC with an atomic (bosonic) cloud in three dimensions the phase space density must fulfill $\rho_{psd} \geq 2.612$. As a result, the required conditions to form a BEC can only be fulfilled when the atomic cloud is sufficiently cold and dense. For the case of a three dimensional gas of atoms trapped in an harmonic potential the condition over the phase space density is decreased to $\rho_{psd} \geq 1.2$ [20].

A further description about the theory of Bose-Einstein Condensation can be found in [18, 20].

2.3 Experimental realization of an erbium BEC

To create experimentally a BEC of an atomic element such as erbium requires a multiple set of phases. Each one being based on different physical principles. The main purpose of this section is to discuss briefly every one of those together with its underlying foundation. For a more detailed description of the experimental set refer to [21].

Figure 2.2 shows a scheme of the experimental setup. It must be noted that all the devices used for the experiment lay on top of three optical tables represented in the figure by gray areas. Moreover, the laser beams produced by different laser systems are represented by colored lines. The erbium atoms are at all times kept inside an ultra-high vacuum (UHV) system formed by an oven, zeeman slower (ZS) and main chamber. This UHV is maintained by an ion getter pump reaching a pressure of 10^{-8} mbar. Additionally, for the main chamber there is a titanium sublimation pump, which reduces the vacuum even further to 10^{-10} mbar. The need of an UHV comes from the fact that to reach an atomic BEC, the cooling process must be so extreme that any interaction with room temperature atoms would lead to heating and destructiveness of the cold erbium cloud.

Most of the laser systems in this experiment produce resonant light for the ^{168}Er atomic transitions. For this reason, these light sources are kept on different optical tables separated from the UHV system. Thus, unwanted atom-light interaction that could damage the cooling capabilities of the experiment is



Figure 2.2: Scheme of the experimental setup. It is divided in three optical tables represented by gray areas. The 401nm laser system is used for the transversal cooling (TC), zeeman slower (ZS) and absorption imaging (AI). It is generated by a frequency doubled diode laser locked to a spectroscopic signal of the 401nm transition of ^{168}Er . The 583nm laser system is used for the magneto optical trap (MOT) and is frequency looked to an ultra low expansion cavity (ULE cavity). This trap uses 401nm laser beam in three spacial dimensions x , y and z . The CO_2 laser is used as main source of an optical dipole trap (ODT). The 841nm laser system is used to form the two lattice beams used for the Bragg scattering process which will be described in next Chapter.

reduced. This laser light is guided into the main table by using optical fibers that can be blocked and unblocked through the use of acousto-optical modulators (AOMs) before the fiber coupler. Allowing for a fast response time (typically a few microseconds) and better control of the experimental phases.

The different phases required to obtain an erbium BEC are chronologically very organized. There is almost no temporal overlay between phases. This allows for a very accurate description of the experiment by just explaining every procedure in a chronological order. In every cycle, the atoms start in the oven and pass through the transversal cooling (TC) and zeeman slower (ZS) to reach the main chamber, where the magneto optical trap (MOT), optical dipole trap (ODT) and evaporative cooling take place to generate the erbium Bose-Einstein condensate.

2.3.1 Oven

The required first step to form an erbium BEC consist in transforming a solid state metal, with a high purity of erbium atoms (typically over 99%), into an atomic beam. There are multiple reasons to why this is necessary. The main one being that it reduces the interaction between atoms and allows for laser cooling and trapping techniques. This will become more clear in the next experimental phases.

In order to produce an erbium beam, an oven of the type known as Dual filament effusion cell (DFC)² is used, operating inside an UHV chamber. The left side of Figure 2.3 shows a basic scheme of this device, which is divided into two tantalum wired cavities. The first one is called Effusion cell (EC) and contains the bulk metal of erbium, which is heated up to 1 200 °C and sublimated into gas. After this, the erbium gas is transferred through a 3 cm pinhole into the second cavity of the DFC known as Hot lip (HL). This last part of the oven is heated a 100 °C higher than the EC temperature to avoid condensation of material at the pinholes. Lastly, the erbium gas leaves the oven forming an atomic beam through a second pinhole that connects the HL cavity with all the following experimental stages. In order to avoid the atomic beam from altering some of these sensitive experimental phases, the second pinhole is closed by a mechanical shutter at these moments.

The speed at which the atoms are leaving the oven can be estimated in average with a parameter called root mean squared (RMS) velocity \bar{v}_{RMS} . For the case of an ideal gas it has been obtained as [22]

$$\bar{v}_{RMS} = \sqrt{\frac{3k_B T}{M}} \quad (2.10)$$

This means that for a HL temperature of 1 400 K the resulting RMS velocity of the erbium beam leaving the oven is approximately 457 m s⁻¹.



Figure 2.3: Scheme of the oven, transversal cooling and zeeman slower. The atomic beam of erbium and the 401 nm laser beam are represented by gray and blue arrows respectively. A cross section of the transversal cooling can be seen inside a box. And the different coils used for the zeeman slower are also represented.

² Model DFC-40-10-WK-2B by CreaTec Fischer & Co. GmbH

2.3.2 Transversal and Optical cooling

An atomic beam produced by the DFC oven presents two main problems. They are a poor collimation of the beam and a high speed of the erbium atoms forming the beam. These obstacles must be fixed before being able to trap the atoms into an atomic ensemble and form an erbium BEC. The main purpose of this Transversal cooling (TC) phase is to solve the problem due to poor beam collimation. While the high atomic speed problem will be dealt with in the following Zeeman slower section. However, these two phases are based in the same underlying physical principle, commonly known as Optical or Laser cooling.

Optical cooling

This technique relies on the force applied on particles by red detuned near resonant photons. From Eq. (2.10), it can be seen that the temperature of an ideal gas is proportional to its velocity. So this light-produced force, known as radiation pressure, can be used as a way to lower the temperature of an atomic gas simply by reducing its overall speed. To gain an insight into the physical model of this force, it is necessary to analyse a two-level atomic system [23].

Due to this, an two level atom must be considered, which has a ground state $|g\rangle$, an excited state $|e\rangle$ and an energy difference between both states of $\Delta E = \hbar\omega_0$, here ω_0 represents the atomic resonance frequency. The atom at rest can absorb a photon with resonant frequency ω_0 . Thus, transferring its energy $\hbar\omega_0$ and momentum $\vec{p} = \hbar\vec{k}$ to the atom. Where \vec{k} represents the photon wave vector, such as for light with wavelength λ , the wave number results $|\vec{k}| = 2\pi/\lambda$. According to which was the initial state of the atom before receiving the photon, it can relax into the ground state by spontaneous or by stimulated emission. The first case is produced when the atom was initially at the state $|e\rangle$, which makes the incoming photon trigger an relaxation into $|g\rangle$ of the atom. Resulting in the production of a second identical photon with the same frequency and direction than the triggering one. Because of this, the momentum transfer of the initial photon gets cancelled by the second one and therefore the effective momentum transferred to the atom adds up to zero. However, the second case of spontaneous emission results in a non-zero momentum transfer. Because in this case, the atom is initially in the ground state, allowing it to absorb the initial photon to get in the excited state. After a decay time τ the atom decays back to $|g\rangle$ and re-emits a second photon in a random direction. Due to the fact, that this photon is at average emitted isotropically in all directions, the momentum transfer produced by the second photon adds up to zero. Resulting in an effective momentum transfer of the atom equal to the initial momentum of the first photon.

In order to obtain an analytical analysis, the Bloch equations must be solved for a two level system. Resulting in the stationary solution for an occupation probability of the excited given by

$$\rho_{ee} = \frac{s_0/2}{1 + s_0 + \left(\frac{2\delta}{\gamma}\right)^2} \quad (2.11)$$

Where $\gamma = 1/\tau$ is the decay rate, $\delta = \omega - \omega_0$ the detuning between laser light and atomic resonance frequency and $s_0 = I/I_s$ the saturation parameter defined as the ratio of laser light intensity I and saturation intensity $I_s = 2\pi^2\hbar c/3\lambda^2\tau$, with λ the wavelength and c the speed of light.

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APPENDIX **A**

Useful information

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Acronyms

AOM	acousto-optical modulator
BEC	Bose-Einstein condensate
DFC	dual filament effusion cell
EC	effusion cell
HL	hot lip
MOT	magneto optical trap
ODT	optical dipole trap
RMS	root mean squared
TC	transversal cooling
UHV	ultra-high vacuum
ZS	zeeman slower