

**Student Version — Questions only (NO answers). All multiple regression questions are multiple choice.**  
students should compute  $(X'X)$  inverse.

## Simple Regression — Q1: Study Hours and Exam Grade

DATA:

Study Hours	Exam Grade
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2	55
---	----

4	60
---	----

6	72
---	----

8	80
---	----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q2: Advertising and Sales

DATA:

Advertising (000)Sales(000)

2 25

4 35

6 45

8 55

TASK: Compute beta0 and beta1 using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q3: Experience and Wage

DATA:

Experience (years)	Wage (\$/hr)
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1	8
---	---

3	10
---	----

5	13
---	----

7	15
---	----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q4: Price and Quantity Demanded

DATA:

Price	Quantity
-------	----------

10	100
----	-----

12	90
----	----

14	80
----	----

16	70
----	----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q5: Age and Medical Expenses

DATA:

Age	Expenses (\$)
-----	---------------

30	200
----	-----

40	300
----	-----

50	400
----	-----

60	500
----	-----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q6: Hours Worked and Weekly Income

DATA:

Hours	Income (\$)
-------	-------------

20	250
----	-----

30	300
----	-----

40	350
----	-----

50	400
----	-----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q7: Years of Schooling and Income

DATA:

Years of Schooling	Monthly Income (\$)
--------------------	---------------------

8	1200
---	------

10	1500
----	------

12	1800
----	------

14	2100
----	------

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.



## Simple Regression — Q8: Coffee Price and Cups Sold

DATA:

	Price (\$)	Cups Sold
--	------------	-----------

1		90
---	--	----

2		80
---	--	----

3		70
---	--	----

4		60
---	--	----

TASK: Compute  $\beta_0$  and  $\beta_1$  using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q9: Temperature and Ice Cream Sales

DATA:

Temperature (°C)	Sales (\$)
------------------	------------

20	150
----	-----

25	200
----	-----

30	250
----	-----

35	300
----	-----

TASK: Compute beta0 and beta1 using  $S_{xx}/S_{xy}$  formulas and interpret.

## Simple Regression — Q10: Years in Business and Profit

DATA:

Years	Profit (000\$)
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1	10
---	----

3	20
---	----

5	30
---	----

7	40
---	----

TASK: Compute beta0 and beta1 using  $S_{xx}/S_{xy}$  formulas and interpret.

## Multiple Regression — Q1: Wage, Education, and Experience

DATA:

Education	Experience	Wage
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8.0	1.001680	9.0
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9.0	1.999067	10.0
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11.0	3.995834	13.0
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13.0	5.999333	16.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q2: Sales, Advertising, and Price

DATA:

Advertising (000)PriceSales(000)

2.0 10.0 42.0

3.0 9.0 51.0

4.0 8.0 63.0

6.0 7.0 80.0

TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q3: House Price, Size, and Distance

DATA:

Size (m2)	Distance (km)	Price (000\$)
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80.0	15.0	200.0
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95.0	10.0	250.0
------	------	-------

120.0	5.0	300.0
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150.0	2.0	360.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q4: Profit, Employees, and Capital

DATA:

Employees	Capital (000)	Profit(000)
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5.0	10.0	40.0
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12.0	15.0	70.0
------	------	------

18.0	25.0	110.0
------	------	-------

25.0	40.0	160.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q5: Crop Yield, Fertilizer, and Rainfall

DATA:

Fertilizer (kg)	Rainfall (mm)	Yield (tons)
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20.0	50.0	12.0
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45.0	65.0	18.0
------	------	------

70.0	75.0	24.0
------	------	------

95.0	90.0	30.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.



## Multiple Regression — Q6: Car Price, Age, and Mileage

DATA:

Age (yrs)	Mileage (000 km)	Price (000\$)
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1.0	10.0	50.0
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2.0	22.0	46.0
-----	------	------

3.0	35.0	42.0
-----	------	------

5.0	55.0	30.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q7: Productivity, Training, and Experience

DATA:

Training Hours	Experience	Output (units/hr)
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5.0	1.0	11.0
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12.0	4.0	18.0
------	-----	------

18.0	6.0	24.0
------	-----	------

25.0	10.0	36.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q8: Demand, Income, and Price

DATA:

Income (000\$)	Price	Quantity
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20.0	5.0	100.0
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30.0	4.0	140.0
------	-----	-------

40.0	3.0	180.0
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60.0	2.0	260.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q9: Energy Use, Temperature, and House Si

DATA:

Temperature (°C)	Size (m2)	Energy Use (kWh)
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15.0	80.0	210.0
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22.0	105.0	270.0
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28.0	125.0	330.0
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35.0	160.0	420.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.

## Multiple Regression — Q10: Life Satisfaction, Income, and Leisure

DATA:

Income (000\$)	Leisure Hours	Life Satisfaction
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20.0	10.0	5.0
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35.0	15.0	6.0
------	------	-----

50.0	25.0	8.0
------	------	-----

70.0	30.0	10.0
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TASK: Compute  $\beta_0$ ,  $\beta_1$ ,  $\beta_2$  using  $(X'X)^{-1} X'y$ . Show  $X'X$  and check invertibility.

Then compute SSE,  $\sigma^2$  and Var-Cov matrix.