

Presentations with L^AT_EX

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How to make an itemized list

- This is a beamer presentation template
- It is customised with ISEG colors



How to make an itemized list

You can also have text without bullets. And mix it with itemized lists in the same slide:

- random item 1
- random item 2



itemized lists inside itemized lists

- You can have itemized lists inside other itemized lists:
 - ▶ This is a sub item
 - ▶ This is another sub item
- You can even have sub sub items:
 - ▶ subitem
 - subsub item 1
 - subsub item 2
 - subsubitem 3



I built this template to

- Help ISEG students
- Improve my latex skills

Mathematical notation



- \LaTeX is very useful to typeset mathematical notation. For example, this is the formula for Benford's law of first digits:

$$P(D_1 = d_1) = \log \left(1 + \frac{1}{d_1} \right), d_1 \in \{1, \dots, 9\}$$

- You can also use inline mathematical formulas instead. For example, this is a regression model: $y = \beta_0 + \beta_1 x_1 + \epsilon$.

Mathematical notation



This is the equation environment:

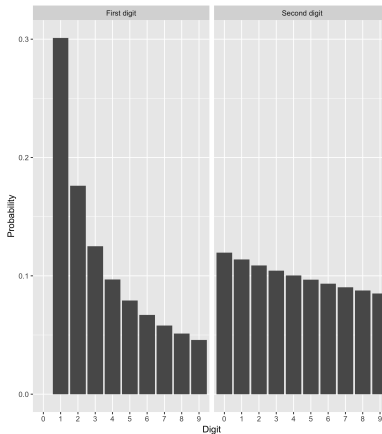
$$P(D_2 = d_2) = \sum_{d_1=1}^9 \log \left(1 + \frac{1}{10 d_1 + d_2} \right), d_2 \in \{0, \dots, 9\} \quad (1)$$

Note that with the equation environment equations are numbered.

including pictures



This picture is in the “figures” folder:





Multinomial \wedge Dirichlet Model

● Bayesian model selection:

- ▶ Likelihood: $\mathbf{x}|\boldsymbol{\theta} \sim \mathcal{M}_k(N, \boldsymbol{\theta})$
- ▶ Hypotheses: $H_0 : \boldsymbol{\theta} = \boldsymbol{\theta}_0$ vs $H_1 : \boldsymbol{\theta} \neq \boldsymbol{\theta}_0$
- ▶ Prior: $\pi(\boldsymbol{\theta}|H_0) = 1_{\boldsymbol{\theta}_0}(\boldsymbol{\theta}_0)$ and $\boldsymbol{\theta}|H_1, \boldsymbol{\alpha} \sim \text{Dir}_k(\boldsymbol{\alpha})$
- ▶ Marginal density: $m_i(\mathbf{x}) = \int_{\Theta_i} f(\mathbf{x}|\boldsymbol{\theta})\pi(\boldsymbol{\theta}|H_i) d\boldsymbol{\theta}, \quad i = 0, 1$

$$\blacksquare m_0(\mathbf{x}) = \frac{N!}{\prod_{i=1}^{k+1} x_i!} \prod_{i=1}^{k+1} \theta_{0i}^{x_i}$$

$$\blacksquare m_1(\mathbf{x}) = \frac{N!}{\prod_{i=1}^{k+1} x_i!} \frac{B(\boldsymbol{\alpha} + \mathbf{x})}{B(\boldsymbol{\alpha})}$$

- ▶ Bayes factor:

$$B_{01}(\mathbf{x}) = \frac{m_0(\mathbf{x})}{m_1(\mathbf{x})} = \frac{\prod_{i=1}^{k+1} (\theta_{0i}^{x_i}) \prod_{i=1}^{k+1} [\Gamma(\alpha_i)] \Gamma[\sum_{i=1}^{k+1} (\alpha_i + x_i)]}{\Gamma(\sum_{i=1}^{k+1} \alpha_i) \prod_{i=1}^{k+1} \Gamma(\alpha_i + x_i)}$$

● Bayesian parameter estimation:

- ▶ Prior: $\boldsymbol{\theta}|\boldsymbol{\alpha} \sim \text{Dir}_k(\boldsymbol{\alpha})$
- ▶ Posterior: $\boldsymbol{\theta}|\boldsymbol{\alpha}, \mathbf{x} \sim \text{Dir}_k(\boldsymbol{\alpha} + \mathbf{x}) \rightarrow$ Mean, mode, credible intervals.



Binomial \wedge Beta Model

● Bayesian model selection:

- ▶ Likelihood: $x \sim \text{Bin}(N, \theta)$
- ▶ Hypotheses: $H_0 : \theta = \theta_0$ vs $H_1 : \theta \neq \theta_0$
- ▶ Prior: $\pi(\theta|H_0) = \delta_{\theta_0}(\theta)$ and $\theta|H_1 \sim \text{Beta}(a, b)$
- ▶ Marginal density: $m_i(x) = \int_0^1 f(x|\theta)\pi(\theta|H_i)d\theta, i = 0, 1$
 - $m_0(x) = \binom{N}{x} \theta_0^x (1 - \theta_0)^{N-x}$
 - $m_1(x) = \binom{N}{x} \frac{B(x+a, n-x+b)}{B(a, b)}$
- ▶ Bayes factor: $B_{01}(x) = \frac{m_0(x)}{m_1(x)} = \frac{\theta_0(1-\theta_0)^{N-x} \Gamma(a) \Gamma(b) \Gamma(n+a+b)}{\Gamma(a+b) \Gamma(n+a-x) \Gamma(x+a)}$

● Bayesian parameter estimation:

- ▶ Prior: $\theta \sim \text{Beta}(a, b)$
- ▶ Posterior: $\theta|x \sim \text{Beta}(a+x, b+N-x) \rightarrow$ Mean, mode, credible intervals

References



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