

Multilinear Galois Mode

ALBANESE Research Lab

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S. Smyshlyaev, Ed.
CryptoPro
V. Nozdrunov
V. Shishkin
TC 26
E. Griboedova
CryptoPro
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Multilinear Galois Mode (MGM)

Abstract

Multilinear Galois Mode (MGM) is an Authenticated Encryption with Associated Data (AEAD) block cipher mode based on the Encrypt-then-MAC (EtM) principle. MGM is defined for use with 64-bit and 128-bit block ciphers.

MGM has been standardized in Russia. It is used as an AEAD mode for the GOST block cipher algorithms in many protocols, e.g., TLS 1.3 and IPsec. This document provides a reference for MGM to enable review of the mechanisms in use and to make MGM available for use with any block cipher.

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Table of Contents

1. Introduction
2. Conventions Used in This Document
3. Basic Terms and Definitions
4. Specification
 - 4.1. MGM Encryption and Tag Generation Procedure
 - 4.2. MGM Decryption and Tag Verification Check Procedure
5. Rationale
6. Security Considerations
7. IANA Considerations
8. References
 - 8.1. Normative References
 - 8.2. Informative References

Appendix A. Test Vectors

- A.1. Test Vectors for the Kuznyechik Block Cipher
 - A.1.1. Example 1
 - A.1.2. Example 2
- A.2. Test Vectors for the Magma Block Cipher
 - A.2.1. Example 1
 - A.2.2. Example 2

Contributors

Authors' Addresses

1. Introduction

Multilinear Galois Mode (MGM) is an Authenticated Encryption with Associated Data (AEAD) block cipher mode based on EtM principle. MGM is defined for use with 64-bit and 128-bit block ciphers. The MGM design principles can easily be applied to other block sizes.

MGM has been standardized in Russia [AUTH-ENC-BLOCK-CIPHER]. It is used as an AEAD mode for the GOST block cipher algorithms in many protocols, e.g., TLS 1.3 and IPsec. This document provides a reference for MGM to enable review of the mechanisms in use and to make MGM available for use with any block cipher.

This document does not have IETF consensus and does not imply IETF support for MGM.

2. Conventions Used in This Document

The key words "MUST", "MUST NOT", "REQUIRED", "SHALL", "SHALL NOT", "SHOULD", "SHOULD NOT", "RECOMMENDED", "NOT RECOMMENDED", "MAY", and "OPTIONAL" in this document are to be interpreted as described in BCP 14 [RFC2119] [RFC8174] when, and only when, they appear in all capitals, as shown here.

3. Basic Terms and Definitions

This document uses the following terms and definitions for the sets and operations on the elements of these sets:

- V^* The set of all bit strings of a finite length (hereinafter referred to as strings), including the empty string; substrings and string components are enumerated from right to left starting from zero.
- V_s The set of all bit strings of length s , where s is a non-negative integer. For $s = 0$, the V_0 consists of a single empty string.
- $|X|$ The bit length of the bit string X (if X is an empty string, then $|X| = 0$).
- $X || Y$ Concatenation of strings X and Y both belonging to V^* , i.e., a string from $V_{\{|X|+|Y|\}}$, where the left substring from $V_{\{|X|\}}$ is equal to X , and the right substring from $V_{\{|Y|\}}$ is equal to Y .
- a^s The string in V_s that consists of s 'a' bits.
- (xor) Exclusive-or of two bit strings of the same length.
- $Z_{\{2^s\}}$ Ring of residues modulo 2^s .
- MSB_i $V_s \rightarrow V_i$
- The transformation that maps the string $X = (x_{\{s-1\}}, \dots, x_0)$ in V_s into the string $MSB_i(X) = (x_{\{s-1\}}, \dots, x_{\{s-i\}})$ in V_i , $i \leq s$ (most significant bits).
- Int_s $V_s \rightarrow Z_{\{2^s\}}$
- The transformation that maps the string $X = (x_{\{s-1\}}, \dots, x_0)$ in V_s , $s > 0$, into the integer $Int_s(X) = 2^{\{s-1\}} * x_{\{s-1\}} + \dots + 2 * x_1 + x_0$ (the interpretation of the bit string as an integer).
- Vec_s $Z_{\{2^s\}} \rightarrow V_s$
- The transformation inverse to the mapping Int_s (the interpretation of an integer as a bit string).
- E_K $V_n \rightarrow V_n$
- The block cipher permutation under the key K in V_k .
- k The bit length of the block cipher key.
- n The block size of the block cipher (in bits).

len $V_s \rightarrow V_{\{n/2\}}$

The transformation that maps a string X in V_s , $0 \leq s \leq 2^{\{n/2\}} - 1$, into the string $\text{len}(X) = \text{Vec}_{\{n/2\}}(|X|)$ in $V_{\{n/2\}}$, where n is the block size of the used block cipher.

[+] The addition operation in $Z_{\{2^{\{n/2\}}\}}$, where n is the block size of the used block cipher.

(x) The transformation that maps two strings, $X = (x_{\{n-1\}}, \dots, x_0)$ in V_n and $Y = (y_{\{n-1\}}, \dots, y_0)$, in V_n into the string $Z = X(x) Y = (z_{\{n-1\}}, \dots, z_0)$ in V_n ; the string Z corresponds to the polynomial $Z(w) = z_{\{n-1\}} * w^{\{n-1\}} + \dots + z_1 * w + z_0$, which is the result of multiplying the polynomials $X(w) = x_{\{n-1\}} * w^{\{n-1\}} + \dots + x_1 * w + x_0$ and $Y(w) = y_{\{n-1\}} * w^{\{n-1\}} + \dots + y_1 * w + y_0$ in the field $\text{GF}(2^n)$, where n is the block size of the used block cipher; if $n = 64$, then the field polynomial is equal to $f(w) = w^{64} + w^4 + w^3 + w + 1$; if $n = 128$, then the field polynomial is equal to $f(w) = w^{128} + w^7 + w^2 + w + 1$.

incr_l $V_n \rightarrow V_n$

The transformation that maps an n -byte string $A = L || R$ into the n -byte string $\text{incr}_l(A) = \text{Vec}_{\{n/2\}}(\text{Int}_{\{n/2\}}(L) [+] 1) || R$, where L and R are $n/2$ -byte strings.

incr_r $V_n \rightarrow V_n$

The transformation that maps an n -byte string $A = L || R$ into the n -byte string $\text{incr}_r(A) = L || \text{Vec}_{\{n/2\}}(\text{Int}_{\{n/2\}}(R) [+] 1)$, where L and R are $n/2$ -byte strings.

4. Specification

An additional parameter that defines the functioning of MGM is the bit length S of the authentication tag, $32 \leq S \leq n$. The value of S MUST be fixed for a particular protocol. The choice of the value S involves a trade-off between message expansion and the forgery probability.

4.1. MGM Encryption and Tag Generation Procedure

The MGM encryption and tag generation procedure takes the following parameters as inputs:

1. Encryption key K in V_k .
2. Initial counter nonce ICN in $V_{\{n-1\}}$.

3. Associated authenticated data A , $0 \leq |A| < 2^{\{n/2\}}$. If $|A| > 0$, then $A = A_1 || \dots || A*_h$, A_j in V_n , for $j = 1, \dots, h - 1$, $A*_h$ in V_t , $1 \leq t \leq n$. If $|A| = 0$, then by definition $A*_h$ is empty, and the h and t parameters are set as follows: $h = 0$, $t = n$. The associated data is authenticated but is not encrypted.
4. Plaintext P , $0 \leq |P| < 2^{\{n/2\}}$. If $|P| > 0$, then $P = P_1 || \dots || P*_q$, P_i in V_n , for $i = 1, \dots, q - 1$, $P*_q$ in V_u , $1 \leq u \leq n$. If $|P| = 0$, then by definition $P*_q$ is empty, and the q and u parameters are set as follows: $q = 0$, $u = n$.

The MGM encryption and tag generation procedure outputs the following parameters:

1. Initial counter nonce ICN.
2. Associated authenticated data A .
3. Ciphertext C in $V_{\{|P|\}}$.
4. Authentication tag T in V_S .

The MGM encryption and tag generation procedure consists of the following steps:

```

+-----+
| MGM-Encrypt(K, ICN, A, P)                                     |
+-----+
| 1. Encryption step:                                           |
|   - if  $|P| = 0$  then                                           |
|     -  $C*_q = P*_q$                                              |
|     -  $C = P$                                                   |
|   - else                                                       |
|     -  $Y_1 = E_K(0^1 || ICN)$ ,                                |
|     - For  $i = 2, 3, \dots, q$  do                               |
|        $Y_i = \text{incr}_r(Y_{\{i-1\}})$ ,                            |
|     - For  $i = 1, 2, \dots, q - 1$  do                           |
|        $C_i = P_i \text{ (xor) } E_K(Y_i)$ ,                          |
|     -  $C*_q = P*_q \text{ (xor) } \text{MSB}_u(E_K(Y_q))$ ,                |
|     -  $C = C_1 || \dots || C*_q$ .                               |
|                                                                 |
| 2. Padding step:                                              |
|   -  $A_h = A*_h || 0^{\{n-t\}}$ ,                                |
|   -  $C_q = C*_q || 0^{\{n-u\}}$ .                                |
|                                                                 |
| 3. Authentication tag T generation step:                       |
|   -  $Z_1 = E_K(1^1 || ICN)$ ,                                    |
|   -  $\text{sum} = 0^n$ ,                                              |
|   - For  $i = 1, 2, \dots, h$  do                                  |
|      $H_i = E_K(Z_i)$ ,                                          |
|      $\text{sum} = \text{sum} \text{ (xor) } (H_i \text{ (x) } A_i)$ ,                  |
|      $Z_{\{i+1\}} = \text{incr}_l(Z_i)$ ,                              |
|   - For  $j = 1, 2, \dots, q$  do                                |

```

```

|         H_{h+j} = E_K(Z_{h+j}),
|         sum = sum (xor) ( H_{h+j} (x) C_j ),
|         Z_{h+j+1} = incr_l(Z_{h+j}),
|     - H_{h+q+1} = E_K(Z_{h+q+1}),
|     - T = MSB_S(E_K(sum (xor) ( H_{h+q+1} (x)
|               ( len(A) || len(C) ) ))).
|
| 4. Return (ICN, A, C, T).
+-----+

```

The ICN value for each message that is encrypted under the given key K must be chosen in a unique manner.

Users who do not wish to encrypt plaintext can provide a string P of zero length. Users who do not wish to authenticate associated data can provide a string A of zero length. The length of the associated data A and of the plaintext P MUST be such that $0 < |A| + |P| < 2^{n/2}$.

4.2. MGM Decryption and Tag Verification Check Procedure

The MGM decryption and tag verification procedure takes the following parameters as inputs:

1. Encryption key K in V_k .
2. Initial counter nonce ICN in $V_{\{n-1\}}$.
3. Associated authenticated data A, $0 \leq |A| < 2^{n/2}$. If $|A| > 0$, then $A = A_1 || \dots || A_h$, A_j in V_n , for $j = 1, \dots, h - 1$, A_h in V_t , $1 \leq t \leq n$. If $|A| = 0$, then by definition A_h is empty, and the h and t parameters are set as follows: $h = 0$, $t = n$. The associated data is authenticated but is not encrypted.
4. Ciphertext C, $0 \leq |C| < 2^{n/2}$. If $|C| > 0$, then $C = C_1 || \dots || C_q$, C_i in V_n , for $i = 1, \dots, q - 1$, C_q in V_u , $1 \leq u \leq n$. If $|C| = 0$, then by definition C_q is empty, and the q and u parameters are set as follows: $q = 0$, $u = n$.
5. Authentication tag T in V_S .

The MGM decryption and tag verification procedure outputs FAIL or the following parameters:

1. Associated authenticated data A.
2. Plaintext P in $V_{\{|C|\}}$.

The MGM decryption and tag verification procedure consists of the following steps:

```

+-----+
|  MGM-Decrypt(K, ICN, A, C, T)
|

```

```

1. Padding step:
  -  $A_h = A*_h \parallel 0^{\{n-t\}}$ ,
  -  $C_q = C*_q \parallel 0^{\{n-u\}}$ .

2. Authentication tag T verification step:
  -  $Z_1 = E_K(1^1 \parallel ICN)$ ,
  -  $sum = 0^n$ ,
  - For  $i = 1, 2, \dots, h$  do
     $H_i = E_K(Z_i)$ ,
     $sum = sum \text{ (xor) } (H_i \text{ (x) } A_i)$ ,
     $Z_{i+1} = incr_l(Z_i)$ ,
  - For  $j = 1, 2, \dots, q$  do
     $H_{h+j} = E_K(Z_{h+j})$ ,
     $sum = sum \text{ (xor) } (H_{h+j} \text{ (x) } C_j)$ ,
     $Z_{h+j+1} = incr_l(Z_{h+j})$ ,
  -  $H_{h+q+1} = E_K(Z_{h+q+1})$ ,
  -  $T' = MSB_S(E_K(sum \text{ (xor) } (H_{h+q+1} \text{ (x) } (len(A) \parallel len(C))))$ ,
  - If  $T' \neq T$  then return FAIL.

3. Decryption step:
  - if  $|C| = 0$  then
    -  $P = C$ 
  - else
    -  $Y_1 = E_K(0^1 \parallel ICN)$ ,
    - For  $i = 2, 3, \dots, q$  do
       $Y_i = incr_r(Y_{i-1})$ ,
    - For  $i = 1, 2, \dots, q - 1$  do
       $P_i = C_i \text{ (xor) } E_K(Y_i)$ ,
    -  $P*_q = C*_q \text{ (xor) } MSB_u(E_K(Y_q))$ ,
    -  $P = P_1 \parallel \dots \parallel P*_q$ .

4. Return  $(A, P)$ .

```

The length of the associated data A and of the ciphertext C MUST be such that $0 < |A| + |C| < 2^{\{n/2\}}$.

5. Rationale

MGM was originally proposed in [PDMODE].

From the operational point of view, MGM is designed to be parallelizable, inverse free, and online and is also designed to provide availability of precomputations.

Parallelizability of MGM is achieved due to its counter-type structure and the usage of the multilinear function for authentication. Indeed, both encryption blocks $E_K(Y_i)$ and authentication blocks H_i are produced in the counter mode manner, and the multilinear function determined by H_i is parallelizable in itself. Additionally, the counter-type structure of the mode

provides the inverse-free property.

The online property means the possibility of processing messages even if it is not completely received (so its length is unknown). To provide this property, MGM uses blocks $E_K(Y_i)$ and H_i , which are produced based on two independent source blocks Y_i and Z_i .

Availability of precomputations for MGM means the possibility of calculating H_i and $E_K(Y_i)$ even before data is retrieved. It holds again due to the usage of counters for calculating them.

6. Security Considerations

The security properties of MGM are based on the following:

Different functions generating the counter values:

The functions incr_r and incr_l are chosen to minimize intersection (if it happens) of counter values Y_i and Z_i .

Encryption of the multilinear function output:

It allows attacks based on padding and linear properties to be resisted (see [FERG05] for details).

Multilinear function for authentication:

It allows the small subgroup attacks to be resisted [SAAR12].

Encryption of the nonces ($0^1 || \text{ICN}$) and ($1^1 || \text{ICN}$):

The use of this encryption minimizes the number of plaintext/ciphertext pairs of blocks known to an adversary. It prevents attacks that need a substantial amount of such material (e.g., linear and differential cryptanalysis and side-channel attacks).

It is crucial to the security of MGM to use unique ICN values. Using the same ICN values for two different messages encrypted with the same key eliminates the security properties of this mode.

It is crucial for the security of MGM not to process empty plaintext and empty associated data at the same time. Otherwise, a tag becomes independent from a nonce value, leading to vulnerability to forgery attacks.

Security analysis for MGM with E_K being a random permutation was performed in [SEC-MGM]. More precisely, the bounds for confidentiality advantage (CA) and integrity advantage (IA) (for details, see [AEAD-LIMITS]) were obtained. According to these results, for an adversary making at most q encryption queries with the total length of plaintexts and associated data of at most s blocks, and allowed to output a forgery with the summary length of ciphertext and associated data of at most l blocks:

$$\text{CA} \leq (3(s + 4q)^2) / 2^n,$$

$$\text{IA} \leq (3(s + 4q + l + 3)^2) / 2^n + 2/2^s,$$

where n is the block size and S is the authentication tag size.

These bounds can be used as guidelines on how to calculate confidentiality and integrity limits (for details, also see [AEAD-LIMITS]).

7. IANA Considerations

This document has no IANA actions.

8. References

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Appendix A. Test Vectors

A.1. Test Vectors for the Kuznyechik Block Cipher

Test vectors for the Kuznyechik block cipher ($n = 128$, $k = 256$) are defined in [GOST3412-2015] (the English version can be found in [RFC7801]).

A.1.1. Example 1

Encryption key K:

00000: 88 99 AA BB CC DD EE FF 00 11 22 33 44 55 66 77
00010: FE DC BA 98 76 54 32 10 01 23 45 67 89 AB CD EF

ICN:

00000: 11 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88

Associated authenticated data A:

00000: 02 02 02 02 02 02 02 02 01 01 01 01 01 01 01 01
00010: 04 04 04 04 04 04 04 04 03 03 03 03 03 03 03 03
00020: EA 05 05 05 05 05 05 05 05 05

Plaintext P:

00000: 11 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88
00010: 00 11 22 33 44 55 66 77 88 99 AA BB CC EE FF 0A
00020: 11 22 33 44 55 66 77 88 99 AA BB CC EE FF 0A 00
00030: 22 33 44 55 66 77 88 99 AA BB CC EE FF 0A 00 11
00040: AA BB CC

1. Encryption step:

0^1 || ICN:

00000: 11 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88

Y_1 :

00000: 7F 67 9D 90 BE BC 24 30 5A 46 8D 42 B9 D4 ED CD

$E_K(Y_1)$:

00000: B8 57 48 C5 12 F3 19 90 AA 56 7E F1 53 35 DB 74

```

Y_2:
00000:  7F 67 9D 90 BE BC 24 30 5A 46 8D 42 B9 D4 ED CE
E_K(Y_2):
00000:  80 64 F0 12 6F AC 9B 2C 5B 6E AC 21 61 2F 94 33

Y_3:
00000:  7F 67 9D 90 BE BC 24 30 5A 46 8D 42 B9 D4 ED CF
E_K(Y_3):
00000:  58 58 82 1D 40 C0 CD 0D 0A C1 E6 C2 47 09 8F 1C

Y_4:
00000:  7F 67 9D 90 BE BC 24 30 5A 46 8D 42 B9 D4 ED D0
E_K(Y_4):
00000:  E4 3F 50 81 B5 8F 0B 49 01 2F 8E E8 6A CD 6D FA

Y_5:
00000:  7F 67 9D 90 BE BC 24 30 5A 46 8D 42 B9 D4 ED D1
E_K(Y_5):
00000:  86 CE 9E 2A 0A 12 25 E3 33 56 91 B2 0D 5A 33 48

C:
00000:  A9 75 7B 81 47 95 6E 90 55 B8 A3 3D E8 9F 42 FC
00010:  80 75 D2 21 2B F9 FD 5B D3 F7 06 9A AD C1 6B 39
00020:  49 7A B1 59 15 A6 BA 85 93 6B 5D 0E A9 F6 85 1C
00030:  C6 0C 14 D4 D3 F8 83 D0 AB 94 42 06 95 C7 6D EB
00040:  2C 75 52

```

2. Padding step:

```

A_1 || ... || A_h:
00000:  02 02 02 02 02 02 02 02 01 01 01 01 01 01 01 01
00010:  04 04 04 04 04 04 04 04 03 03 03 03 03 03 03 03
00020:  EA 05 05 05 05 05 05 05 05 00 00 00 00 00 00 00

C_1 || ... || C_q:
00000:  A9 75 7B 81 47 95 6E 90 55 B8 A3 3D E8 9F 42 FC
00010:  80 75 D2 21 2B F9 FD 5B D3 F7 06 9A AD C1 6B 39
00020:  49 7A B1 59 15 A6 BA 85 93 6B 5D 0E A9 F6 85 1C
00030:  C6 0C 14 D4 D3 F8 83 D0 AB 94 42 06 95 C7 6D EB
00040:  2C 75 52 00 00 00 00 00 00 00 00 00 00 00 00 00

```

3. Authentication tag T generation step:

```

1^1 || ICN:
00000:  91 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88

Z_1:
00000:  7F C2 45 A8 58 6E 66 02 A7 BB DB 27 86 BD C6 6F

H_1:
00000:  8D B1 87 D6 53 83 0E A4 BC 44 64 76 95 2C 30 0B
current sum:
00000:  4C F4 27 F4 AD B7 5C F4 C0 DA 39 D5 AB 48 CF 38

```

Z_2:
 00000: 7F C2 45 A8 58 6E 66 03 A7 BB DB 27 86 BD C6 6F
 H_2:
 00000: 7A 24 F7 26 30 E3 76 37 21 C8 F3 CD B1 DA 0E 31
 current sum:
 00000: 94 95 44 0E F6 24 A1 DD C6 F5 D9 77 28 50 C5 73

 Z_3:
 00000: 7F C2 45 A8 58 6E 66 04 A7 BB DB 27 86 BD C6 6F
 H_3:
 00000: 44 11 96 21 17 D2 06 35 C5 25 E0 A2 4D B4 B9 0A
 current sum:
 00000: A4 9A 8C D8 A6 F2 74 23 DB 79 E4 4A B3 06 D9 42

 Z_4:
 00000: 7F C2 45 A8 58 6E 66 05 A7 BB DB 27 86 BD C6 6F
 H_4:
 00000: D8 C9 62 3C 4D BF E8 14 CE 7C 1C 0C EA A9 59 DB
 current sum:
 00000: 09 FE 3F 6A 83 3C 21 B3 90 27 D0 20 6A 84 E1 5A

 Z_5:
 00000: 7F C2 45 A8 58 6E 66 06 A7 BB DB 27 86 BD C6 6F
 H_5:
 00000: A5 E1 F1 95 33 3E 14 82 96 99 31 BF BE 6D FD 43
 current sum:
 00000: B5 DA 26 BB 00 EB A8 04 35 D7 97 6B C6 B5 46 4D

 Z_6:
 00000: 7F C2 45 A8 58 6E 66 07 A7 BB DB 27 86 BD C6 6F
 H_6:
 00000: B4 CA 80 8C AC CF B3 F9 17 24 E4 8A 2C 7E E9 D2
 current sum:
 00000: DD 1C 0E EE F7 83 C8 EB 2A 33 F3 58 D7 23 0E E5

 Z_7:
 00000: 7F C2 45 A8 58 6E 66 08 A7 BB DB 27 86 BD C6 6F
 H_7:
 00000: 72 90 8F C0 74 E4 69 E8 90 1B D1 88 EA 91 C3 31
 current sum:
 00000: 89 6C E1 08 32 EB EA F9 06 9F 3F 73 76 59 4D 40

 Z_8:
 00000: 7F C2 45 A8 58 6E 66 09 A7 BB DB 27 86 BD C6 6F
 H_8:
 00000: 23 CA 27 15 B0 2C 68 31 3B FD AC B3 9E 4D 0F B8
 current sum:
 00000: 99 1A F5 C9 D0 80 F7 63 87 FE 64 9E 7C 93 C6 42

 Z_9:
 00000: 7F C2 45 A8 58 6E 66 0A A7 BB DB 27 86 BD C6 6F
 H_9:

```

00000:  BC BC E6 C4 1A A3 55 A4 14 88 62 BF 64 BD 83 0D
len(A) || len(C):
00000:  00 00 00 00 00 00 01 48 00 00 00 00 00 00 02 18
sum (xor) ( H_9 (x) ( len(A) || len(C) ) ):
00000:  C0 C7 22 DB 5E 0B D6 DB 25 76 73 83 3D 56 71 28

Tag T:
00000:  CF 5D 65 6F 40 C3 4F 5C 46 E8 BB 0E 29 FC DB 4C

```

A.1.2. Example 2

Encryption key K:

```

00000:  99 AA BB CC DD EE FF 00 11 22 33 44 55 66 77 FE
00010:  DC BA 98 76 54 32 10 01 23 45 67 89 AB CD EF 88

```

ICN:

```

00000:  11 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88

```

Associated authenticated data A:

```

00000:  01 01 01 01 01 01 01 01 01 01 01 01 01 01 01 01

```

Plaintext P:

```

00000:

```

1. Encryption step:

```

C:
00000:

```

2. Padding step:

```

A_1 || ... || A_h:
00000:  01 01 01 01 01 01 01 01 01 01 01 01 01 01 01 01

C_1 || ... || C_q:
00000:

```

3. Authentication tag T generation step:

```

1^1 || ICN:
00000:  91 22 33 44 55 66 77 00 FF EE DD CC BB AA 99 88

Z_1:
00000:  79 32 72 68 96 C4 3E 3F BF D6 50 89 EB F1 E5 B6
H_1:
00000:  99 3A 80 66 CC C0 A4 0F AC 4A 14 F7 A2 F6 6D 9B
current sum:
00000:  0A C1 1E 2C 1C D6 07 D8 2F E3 55 54 B4 01 02 81

Z_2:
00000:  79 32 72 68 96 C4 3E 40 BF D6 50 89 EB F1 E5 B6
H_2:
00000:  0C 38 A7 1E E7 93 BF 76 89 81 BF CD 7C DA 78 C8

```

```

len(A) || len(C):
00000: 00 00 00 00 00 00 00 00 80 00 00 00 00 00 00 00
sum (xor) ( H_2 (x) ( len(A) || len(C) ) ):
00000: CA 1E F8 92 71 EA 60 C4 53 9E 40 EB 26 C2 80 5D

Tag T:
00000: 79 01 E9 EA 20 85 CD 24 7E D2 49 69 5F 9F 8A 85

```

A.2. Test Vectors for the Magma Block Cipher

Test vectors for the Magma block cipher ($n = 64$, $k = 256$) are defined in [GOST3412-2015] (the English version can be found in [RFC8891]).

A.2.1. Example 1

```

Encryption key K:
00000: FF EE DD CC BB AA 99 88 77 66 55 44 33 22 11 00
00010: F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA FB FC FD FE FF

ICN:
00000: 12 DE F0 6B 3C 13 0A 59

Associated authenticated data A:
00000: 01 01 01 01 01 01 01 01 02 02 02 02 02 02 02 02
00010: 03 03 03 03 03 03 03 03 04 04 04 04 04 04 04 04
00020: 05 05 05 05 05 05 05 05 05 EA

Plaintext P:
00000: FF EE DD CC BB AA 99 88 11 22 33 44 55 66 77 00
00010: 88 99 AA BB CC EE FF 0A 00 11 22 33 44 55 66 77
00020: 99 AA BB CC EE FF 0A 00 11 22 33 44 55 66 77 88
00030: AA BB CC EE FF 0A 00 11 22 33 44 55 66 77 88 99
00040: AA BB CC

```

1. Encryption step:

```

0^1 || ICN:
00000: 12 DE F0 6B 3C 13 0A 59

Y_1:
00000: 56 23 89 01 62 DE 31 BF
E_K(Y_1):
00000: 38 7B DB A0 E4 34 39 B3

Y_2:
00000: 56 23 89 01 62 DE 31 C0
E_K(Y_2):
00000: 94 33 00 06 10 F7 F2 AE

Y_3:
00000: 56 23 89 01 62 DE 31 C1
E_K(Y_3):
00000: 97 B7 AA 6D 73 C5 87 57

```

Y_4:
 00000: 56 23 89 01 62 DE 31 C2
 E_K(Y_4):
 00000: 94 15 52 8B FF C9 E8 0A

Y_5:
 00000: 56 23 89 01 62 DE 31 C3
 E_K(Y_5):
 00000: 03 F7 68 BF F1 82 D6 70

Y_6:
 00000: 56 23 89 01 62 DE 31 C4
 E_K(Y_6):
 00000: FD 05 F8 4E 9B 09 D2 FE

Y_7:
 00000: 56 23 89 01 62 DE 31 C5
 E_K(Y_7):
 00000: DA 4D 90 8A 95 B1 75 C4

Y_8:
 00000: 56 23 89 01 62 DE 31 C6
 E_K(Y_8):
 00000: 65 99 73 96 DA C2 4B D7

Y_9:
 00000: 56 23 89 01 62 DE 31 C7
 E_K(Y_9):
 00000: A9 00 50 4A 14 8D EE 26

C:
 00000: C7 95 06 6C 5F 9E A0 3B 85 11 33 42 45 91 85 AE
 00010: 1F 2E 00 D6 BF 2B 78 5D 94 04 70 B8 BB 9C 8E 7D
 00020: 9A 5D D3 73 1F 7D DC 70 EC 27 CB 0A CE 6F A5 76
 00030: 70 F6 5C 64 6A BB 75 D5 47 AA 37 C3 BC B5 C3 4E
 00040: 03 BB 9C

2. Padding step:

A_1 || ... || A_h:
 00000: 01 01 01 01 01 01 01 01 01 02 02 02 02 02 02 02
 00010: 03 03 03 03 03 03 03 03 03 04 04 04 04 04 04 04
 00020: 05 05 05 05 05 05 05 05 05 EA 00 00 00 00 00 00

C_1 || ... || C_q:
 00000: C7 95 06 6C 5F 9E A0 3B 85 11 33 42 45 91 85 AE
 00010: 1F 2E 00 D6 BF 2B 78 5D 94 04 70 B8 BB 9C 8E 7D
 00020: 9A 5D D3 73 1F 7D DC 70 EC 27 CB 0A CE 6F A5 76
 00030: 70 F6 5C 64 6A BB 75 D5 47 AA 37 C3 BC B5 C3 4E
 00040: 03 BB 9C 00 00 00 00 00

3. Authentication tag T generation step:

```

1^1 || ICN:
00000:  92 DE F0 6B 3C 13 0A 59

Z_1:
00000:  2B 07 3F 04 94 F3 72 A0
H_1:
00000:  70 8A 78 19 1C DD 22 AA
current sum:
00000:  D6 BB 5B EA 81 93 12 62

Z_2:
00000:  2B 07 3F 05 94 F3 72 A0
H_2:
00000:  6F 02 CC 46 4B 2F A0 A3
current sum:
00000:  DD 1C 82 4E 91 78 49 A5

Z_3:
00000:  2B 07 3F 06 94 F3 72 A0
H_3:
00000:  9F 81 F2 26 FD 19 6F 05
current sum:
00000:  05 89 22 17 F6 5A DA C7

Z_4:
00000:  2B 07 3F 07 94 F3 72 A0
H_4:
00000:  B9 C2 AC 9B E5 B5 DF F9
current sum:
00000:  D1 DB 9B 7F C4 9E 7C 97

Z_5:
00000:  2B 07 3F 08 94 F3 72 A0
H_5:
00000:  74 B5 EC 96 55 1B F8 88
current sum:
00000:  56 45 F6 B5 18 5C B7 1A

Z_6:
00000:  2B 07 3F 09 94 F3 72 A0
H_6:
00000:  7E B0 21 A4 03 5B 04 C3
current sum:
00000:  3F C2 C2 E6 FB EE D0 4D

Z_7:
00000:  2B 07 3F 0A 94 F3 72 A0
H_7:
00000:  C2 A9 C3 A8 70 4D 9B B0
current sum:
00000:  15 47 1F B5 CD 8E 6C 02

```


Z_8:
00000: 2B 07 3F 0B 94 F3 72 A0
H_8:
00000: F5 D5 05 A8 7B 83 83 B5
current sum:
00000: 12 56 78 96 1D 40 E0 93

Z_9:
00000: 2B 07 3F 0C 94 F3 72 A0
H_9:
00000: F7 95 E7 5F DE B8 93 3C
current sum:
00000: 6E F4 0A B0 C1 5F 20 48

Z_10:
00000: 2B 07 3F 0D 94 F3 72 A0
H_10:
00000: 65 A1 A3 E6 80 F0 81 45
current sum:
00000: A4 64 A7 08 FF 45 14 22

Z_11:
00000: 2B 07 3F 0E 94 F3 72 A0
H_11:
00000: 1C 74 A5 76 4C B0 D5 95
current sum:
00000: 60 94 4E 05 D0 85 75 14

Z_12:
00000: 2B 07 3F 0F 94 F3 72 A0
H_12:
00000: DC 84 47 A5 14 E7 83 E7
current sum:
00000: EE 98 B9 B5 0F F7 83 E8

Z_13:
00000: 2B 07 3F 10 94 F3 72 A0
H_13:
00000: A7 E3 AF E0 04 EE 16 E3
current sum:
00000: C0 39 0F A2 28 AF 6D CB

Z_14:
00000: 2B 07 3F 11 94 F3 72 A0
H_14:
00000: A5 AA BB 0B 79 80 D0 71
current sum:
00000: 73 E0 6E 07 EF 37 CD CC

Z_15:
00000: 2B 07 3F 12 94 F3 72 A0
H_15:
00000: 6E 10 4C C9 33 52 5C 5D

```

current sum:
00000:  2F 40 69 0A EB 53 F5 39

Z_16:
00000:  2B 07 3F 13 94 F3 72 A0
H_16:
00000:  83 11 B6 02 4A A9 66 C1
len(A) || len(C):
00000:  00 00 01 48 00 00 02 18
sum (xor) ( H_16 (x) ( len(A) || len(C) ) ):
00000:  73 CE F4 4B AE 6B DB 61

Tag T:
00000:  A7 92 80 69 AA 10 FD 10

```

A.2.2. Example 2

```

Encryption key K:
00000:  99 AA BB CC DD EE FF 00 11 22 33 44 55 66 77 FE
00010:  DC BA 98 76 54 32 10 01 23 45 67 89 AB CD EF 88

ICN:
00000:  00 77 66 55 44 33 22 11

Associated authenticated data A:
00000:

Plaintext P:
00000:  22 33 44 55 66 77 00 FF

```

1. Encryption step:

```

0^1 || ICN:
00000:  00 77 66 55 44 33 22 11

Y_1:
00000:  5B 2A 7E 60 4F 9F BB 95
E_K(Y_1):
00000:  48 A6 A5 17 0D 52 9D B1

C:
00000:  6A 95 E1 42 6B 25 9D 4E

```

2. Padding step:

```

A_1 || ... || A_h:
00000:

C_1 || ... || C_q:
00000:  6A 95 E1 42 6B 25 9D 4E

```

3. Authentication tag T generation step:

```

1^1 || ICN:
00000: 80 77 66 55 44 33 22 11

Z_1:
00000: 59 73 54 78 7E 52 E6 EB
H_1:
00000: EC E3 F9 DA 11 8C 7D 95
current sum:
00000: 25 D0 E4 20 7B 6B F6 3D

Z_2:
00000: 59 73 54 79 7E 52 E6 EB
H_2:
00000: 31 0C 0D AC C9 D0 4D 93
len(A) || len(C):
00000: 00 00 00 00 00 00 00 40
sum (xor) ( H_2 (x) ( len(A) || len(C) ) ):
00000: 66 D3 8F 12 0F 78 92 49

Tag T:
00000: 33 4E E2 70 45 0B EC 9E

```

Contributors

Evgeny Alekseev
CryptoPro

Email: alekseev@cryptopro.ru

Alexandra Babueva
CryptoPro

Email: babueva@cryptopro.ru

Lilia Akhmetzyanova
CryptoPro

Email: lah@cryptopro.ru

Grigory Marshalko
TC 26

Email: marshalko_gb@tc26.ru

Vladimir Rudskoy
TC 26

Email: rudskoy_vi@tc26.ru

Alexey Nesterenko
National Research University Higher School of Economics

Email: anesterenko@hse.ru

Lidia Nikiforova
CryptoPro

Email: nikiforova@cryptopro.ru

Authors' Addresses

Stanislav Smyshlyaev (editor)
CryptoPro

Phone: +7 (495) 995-48-20
Email: svb@cryptopro.ru

Vladislav Nozdrunov
TC 26

Email: nozdrunov_vi@tc26.ru

Vasily Shishkin
TC 26

Email: shishkin_va@tc26.ru

Ekaterina Griboedova
CryptoPro

Email: griboedovaekaterina@gmail.com