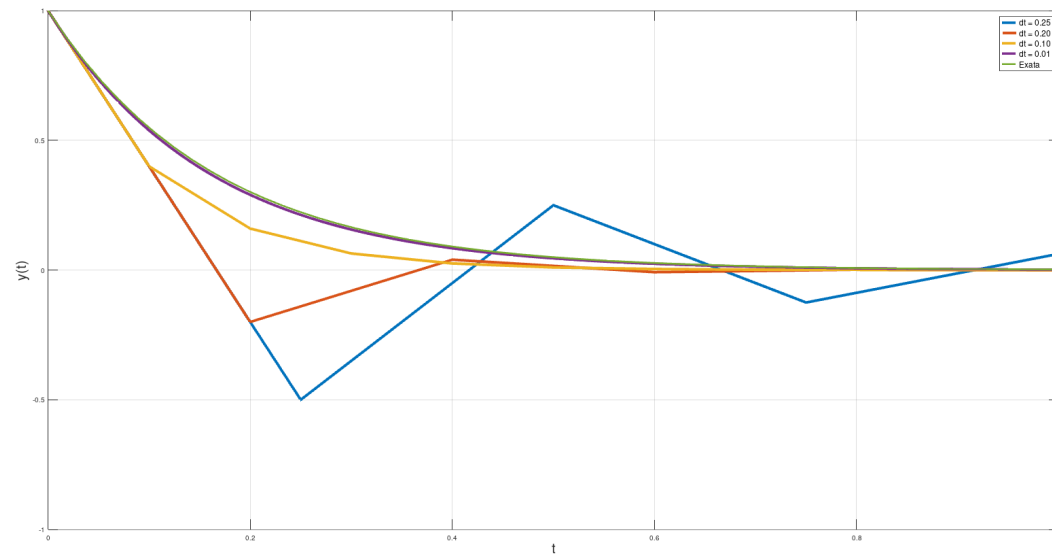


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## Exercício 1



## Exercício 2

Considera o seguinte sistema, em malha fechada, com realimentação unitária,

1

A equação característica  $f$  é

$f = (\text{sym})$

$$2 \cdot l^2 - 4 \cdot l + 5$$

$X = (\text{sym})$

$$\left( A \cdot \cos\left(\frac{\sqrt{6} \cdot t}{2}\right) + B \cdot \sin\left(\frac{\sqrt{6} \cdot t}{2}\right) \right) \cdot e^t$$

A solução acima descreve um sistema instável

2

A equação característica  $f$  é

$f = (\text{sym})$

$$-l^2 + 2 \cdot l - 2$$

$X = (\text{sym})$

$$(A \cdot \cos(t) + B \cdot \sin(t)) \cdot e^t$$

A solução acima descreve um sistema instável

## Exercício 3

a)

Symbolic pkg v3.0.1: Python communication link active, SymPy v1.9.

$m d^2x/dt^2 + c dx/dt + kx = A$

$m = 2$

$c = -4$

$k = 5$

$A = 3 \cdot \exp(-2 \cdot t)$

$Y = (\text{sym})$

$$\frac{2 \cdot (s + 2) \cdot (a \cdot s - 2 \cdot a + b) + 3}{(s + 2) \cdot (2 \cdot s^2 - 4 \cdot s + 5)}$$

Waiting.....

$y = (\text{sym})$

$$\frac{\left( \sqrt{6} \cdot \left( -14 \cdot a \cdot \sin\left(\frac{\sqrt{6} \cdot t}{2}\right) + 7 \cdot \sqrt{6} \cdot a \cdot \cos\left(\frac{\sqrt{6} \cdot t}{2}\right) + 14 \cdot b \cdot \sin\left(\frac{\sqrt{6} \cdot t}{2}\right) + 6 \cdot \sin\left(\frac{\sqrt{6} \cdot t}{2}\right) - \sqrt{6} \cdot \cos\left(\frac{\sqrt{6} \cdot t}{2}\right) \right) \cdot e^{3 \cdot t} + 6 \right) \cdot e^{-2 \cdot t}}{42}$$

>> |

b)

```
Symbolic pkg v3.0.1: Python communication link active, SymPy v1.9.
m d2x/dt2 + c dx/dt + kx = A
m = 1
```

```
c = 2
```

```
k = -2
```

```
A = 5*sin(2*t)
```

```
Y = (sym)
```

$$\frac{\left(s^2 + 4\right) \cdot (a \cdot s + 2 \cdot a + b) + 10}{\left(s^2 + 4\right) \cdot \left(s^2 + 2 \cdot s - 2\right)}$$

```
y = (sym)
```

$$\frac{\left(-15 \cdot (3 \cdot \sin(2 \cdot t) + 2 \cdot \cos(2 \cdot t)) \cdot e^{t \cdot (1 + \sqrt{3})} + \sqrt{3} \cdot \left(-13 \cdot a + 13 \cdot \sqrt{3} \cdot a - 13 \cdot b + (13 \cdot a + 13 \cdot \sqrt{3} \cdot a + 13 \cdot b + 5 \cdot \sqrt{3} + 20) \cdot e^{2 \cdot \sqrt{3} \cdot t} - 20 + 5 \cdot \sqrt{3}\right)\right) \cdot e^{-t \cdot (1 + \sqrt{3})}}$$

78

```
>> |
```

c)

```
Symbolic pkg v3.0.1: Python communication link active, SymPy v1.9.  
md2x/dt2 + cdx/dt +kx = A  
m = 5
```

```
c = vpa(0.5)
```

```
k = -1
```

```
A = 8
```

```
Y = (sym)
```

$$\frac{s \cdot (5 \cdot a \cdot s + 0.5 \cdot a + 5 \cdot b) + 8}{s \cdot \left( 5 \cdot s^2 + 0.5 \cdot s - 1 \right)}$$

```
y = (sym)
```

$$\left( 0.44444444444444441977282167499652 \cdot a - 1.111111111111111160454356650007 \cdot b + \left( 0.55555555555555558022717832500348 \cdot a + 1.111111111111111160454356650007 \cdot b + 4.444444444444444446418174266000278 \right) \cdot e^{0.4 \cdot t} - 8.0 \right) \cdot e^{0.5 \cdot t} + 3.5555555555555553581825733999722 \cdot e^{-0.5 \cdot t}$$

```
>>
```