



Detection of Li in Technological Materials through Nuclear Reactions

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Abstract

The following paper describes a scientific research on the ability to detect the presence of lithium (${}^7\text{Li}$) through the byproducts of nuclear reactions. The research was conducted in three different samples: lithium fluoride (LiF), lithium aluminate (LiAlO_2) and an implanted sample. Energy spectra were obtained for each sample with a tandem accelerator and 1.3 MeV protons. Considering the theoretical values for the nuclear reaction of ${}^7\text{Li}$, we were able to identify the presence of lithium in all samples. Also, some other phenomena were observed, such as back-scattering, pile-up and energy profiling. Finally, using the information on each spectrum, we computed the quantity of lithium in each sample.

1 Main Goal

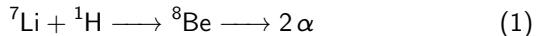
Our main goal is to develop a scientific research project alongside three senior investigators from CTN (Centro Tecnológico e Nuclear), Rodrigo Mateus, Rui Silva and Norberto Catarino. Our project will be focused on the detection of Li in technological materials through nuclear reactions. The main motivation for this project is to study and develop a detection technique for elements such as Li with high sensitivity.

2 Scientific Background

The development of this scientific procedure is based on a physics phenomenon: nuclear reactions. We have an accelerator in order to allow protons with specific energy to collide with the sample whose composition we are interested in studying. The protons will undergo a nuclear reaction with the ones in the samples and byproducts of these reaction will be released. These byproducts are charged particles and we can detect their energy spectrum. Through the analysis of it, we want to infer what were the elements with whom they reacted on the sample and what is their composition percentage.

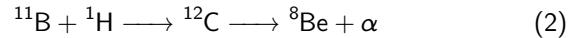
2.1 Nuclear Reaction

The main nuclear reaction in which we are interested is the one between ${}^7\text{Li}$ and an incoming proton on the beam:



Before the emission of the reaction products, the reaction leads to the formation of a ${}^8\text{Be}$ compound nucleus (intermediate state), which then rapidly decays into two alpha particles. These are the particles we detect. An alpha particle is a helium nucleus, composed of two protons and two neutrons.

Some of the samples we are going to work with also include boron and according to the beam energy we use it is possible that the protons lead to a nuclear reaction with the boron atoms in the samples. Therefore, the ${}^{11}\text{B}$ reaction with a proton is as follows:



The reaction first leads to the formation of a ${}^{12}\text{C}$ compound nucleus which decays into one alpha particle and a ${}^8\text{Be}$ nucleus. The α particle can be detected with more or less energy according to the energy level on which the ${}^8\text{Be}$ nucleus is emitted. If the latter is on the fundamental state, the α particle will have more energy and if it is on a higher state, the α particle will have less energy.

2.2 Energy Peaks and Energy Profile

Regarding the phenomena expected in the collected energy spectrum, the primary aspect involves the energy values. Both the alpha particles and other byproducts are emitted with distinct energies immediately following the nuclear reaction. These energies can be calculated based on the reaction and the beam's energy. The computation process will be detailed in section 3.4.

Firstly, we expect to see intensity peaks on the spectrum on these specific energies. However, we must take into account the fact that before arriving at the detector, the emitted particles have to go through the other atoms on the sample. As an incident proton comes in, it might react with another proton from the material that sits on its surface but it can also react with one inside it. The byproducts produced inside the sample initially have the energy we compute but do lose part of it as they collide with other particles before reaching the detector. Basically, we must consider the sample's thickness. The bigger the depth at which the reaction takes place, the smaller the energy with whom they are detected because more of it gets dissipated. Therefore, this will result in an energy profile - the energy peak will be gradually preceded by less intense peaks due to particles that lost energy on their way to the detector. It is less likely for the particles that are emitted inside the sample to reach the detector than for those who were emitted on its surface since on each collision there is a chance that its direction might change. This is why the intensity on the energy profile as a steady increase before hitting a maximum value at the energy with whom the particle comes out of the reaction.

We expect this phenomena to be particularly significant in samples where the atom that takes part in the reaction can be found not only at the surface of the sample but also in its depth. Therefore, in implanted samples where the substrate is only a layer, the energy profile will be less evident.

2.3 Back-scattering

Another possible occurrence is back-scattering, where the incoming proton from the accelerator is elastically reflected back by the sample and subsequently detected. During this reflection, the energy of the proton and the target is conserved and distributed according to the kinematics of the collision. This will result in a range of energy values for the back-scattered proton.

2.4 Pile-up

Pile-up is a phenomenon that is a consequence of the finite time resolution of the detector. It occurs when two particles are detected at the same time and the detector only detects one with the energy doubled. This is a problem because it can lead to the misinterpretation of the data. Therefore, we expect that, for very intense energy ranges in the spectrum, the pile-up might be significant. If we have particles emitted with an $[a, b]$ keV energy range, the pile-up will occur in the $[2a, 2b]$ keV.

3 Experimental Procedure

3.1 Work Plan

Obtaining the energy spectrum of the particles resulting from the nuclear reactions between the protons and the samples will take the following steps:

1. Accelerator Startup - beam energy increase;
2. Sample Preparation;
3. Channel-energy calibration of the detection system with a well-known triple α source;
4. Lenses and electromagnets set up and adjustment;
5. Obtaining the energy spectrum of all samples;

3.2 Experimental Set-Up

The experimental set-up consists of a Tandem accelerator, a beam line with electromagnets and a chamber with both the samples and the detectors.

Theoretically, the accelerator produces a beam of protons with a kinetic energy of up to 5 MeV, which is deviated by the steering electromagnet before hitting the sample. The electromagnet deflect particles with different angles according to their charge-to-mass ratio and, with that, allows us to remove any unwanted particles from the beam and only let the protons pass through.

The detectors used, which are silicon-based, detect charged particles through the ionisation they produce in the silicon.

In addition, the detectors are connected to a electronic system that amplifies the signal and sends it to a computer where the spectra can be seen.

The beam line is under a vacuum of around 10^{-7} mbar in order to avoid the protons colliding with other particles and losing energy.

They reach the sample with the specified kinetic energy and cause a nuclear reaction whose products are the charged particles detected. We aim to analyse the energy spectrum of these particles.

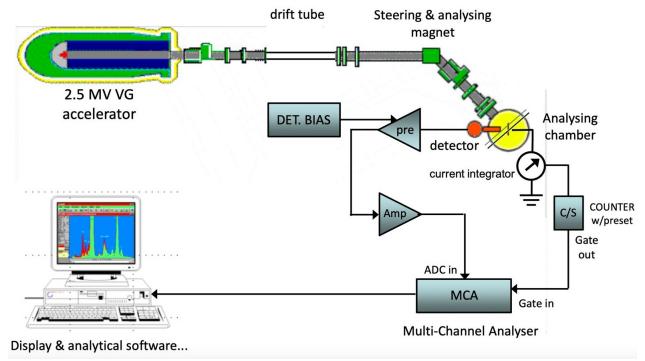


Figure 1: Experimental Set-up

3.3 Beam Energy Selection

In order to choose the energy of the beam we need to take into account the cross section of the reaction between the protons and the Li-7. We collected data from the IBANDL database for this reaction in a range of [0.5, 7] MeV and plotted it in the following graph:

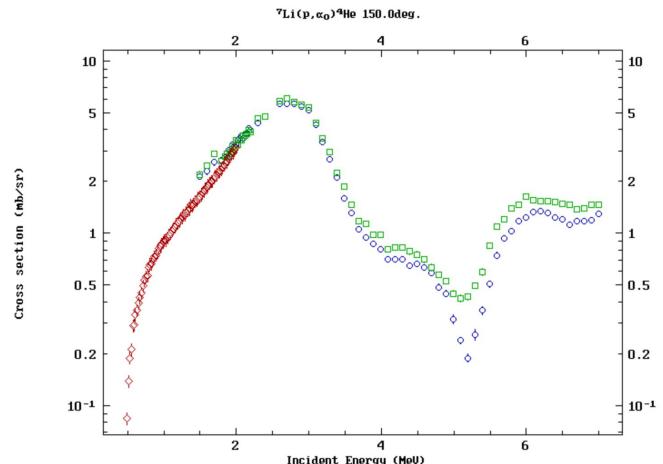


Figure 2: Cross section of the reaction between protons and Li-7 as a function of the beam energy

We are only interested in the energy range of [0.5, 5] MeV because the energy of the beam is limited by the accelerators range. As we can see in the above figure, the cross section of the reaction is maximum in the [2.5, 3] MeV range. Therefore, since we want to detect the Li-7 in the samples, we should choose the energy of the beam to be in this range.

However, practically, the accelerator cannot reach a beam within the [2.5, 3] MeV energy range. Increasing beam energies take exponentially more time to be set up. Also, we are interested in the possible boron identification in some of the used samples. Boron does not react with such high energies but a lower energy beam is effective in doing that. Having this into consideration, we choose a beam energy of 1.3 MeV for our experimental procedure.

3.4 NRA Calculations - Theoretical Values

After concluding that the best beam energy to work within the previously described conditions is 1.3 MeV, we now need to obtain theoretical values for their energy. In order to do this, we will use the NRA calculator [6]. This is an online calculator developed by investigators at CTN that allows researchers to compute the Q value of a reaction as well as the energy values and scattering angles of the particles these reactions emit. Considering an incident beam whose protons have $E_p = 1.3$ MeV and a scattering angle of $\theta = 165^\circ$ of our detector we computed the following values:

Lithium Firstly, for the reaction 1:

$$\begin{aligned} E_{\alpha_0} &= 7.6298 \text{ MeV} \\ E_{\alpha_0} &= 11.0314 \text{ MeV} \\ \theta_{\alpha_0} &= 165^\circ \\ \theta_{\alpha_0} &= 12^\circ \\ Q(^7\text{Li}) &= 17.346 \text{ MeV} \end{aligned} \quad (3)$$

E_{α_0} and E_{α_0} are the energies of both alpha particles considering that they are in the fundamental state. In this case, the only other option would be for the ^8Be to be formed in an excited state and therefore give origin to alpha particles also in an excited state. There is not enough energy for this to happen since the difference between the ground state and the first state in an helium nuclei is very big, around *INSERT* MeV.

Also, we can see that the scattering angle of the second alpha particle is around 12° meaning that it is different from the detector's angle and will not be detected. To sum up, if there is lithium in any sample that reacts with the incoming protons according to 1, we expect to detect alpha particles that were emitted with 7.6298 MeV.

Boron Secondly, for the reaction 2:

$$\begin{aligned} E_{\alpha_0} &= 3.7372 \text{ MeV} \\ E_{^8\text{Be}} &= 3.1086 \text{ MeV} \\ \theta_{\alpha_0} &= 165^\circ \\ \theta_{^8\text{Be}} &= 11^\circ \\ Q(^{11}\text{Br}) &= 8.591 \text{ MeV} \end{aligned} \quad (4)$$

We need to comment these energies.

3.5 Procedure

We started by displaying the samples in a vertical sample holder with the given order: in the lowest position the implanted sample, followed by lithium aluminate (LiAlO_2) and finally lithium fluoride (LiF). In order to do a calibration from the number of counts per channel to energy, we added an additional source on the holder just above the lithium fluoride one. Using a pachymeter, we measured the distance between the samples so that afterwards we could control the height in order to change the sample on the beam's target.

We placed the sample holder on a support and afterwards both of them inside the chamber. A vacuum machine was connected to the accelerator to reduce the pressure inside both the chamber and the beam.

Afterwards, we started the procedure to turn on the TANDEM accelerator, according to the provided instruction manual. Firstly,

we turned on the H^+ duoplasmatron source of the accelerator as well as the magnets and lenses. Then, we opened the valves to propagate the vacuum throughout the entirety of the tubes.

In the control panel, we adjusted the angles of the lenses and the magnets current according to the manual, so that the beam would reach the samples. Finally, we used a collimator with a 2mm radius to collimate the beam.

Finally, we used a computer program to obtain the spectra of the different sources. The multichannel analyzer (MCA) used to acquire data was gradually set to 70 V and the angle between the top two detectors was 165° .

Analysis

4 Calibration

For the calibration, we used a triple α source. In order to do this procedure, for each of spectrum relevant peaks, we need to find the channel with the maximum number of counts. Then, we find the theoretical values for these peaks and, using both the experimental values for the peaks in channel units and the theoretical ones in MeV, we want to obtain a mathematical relation that allows us to convert channel values into energy values. To accomplish this, we will make a linear regression with the energy-channel data.

The spectrum obtained for the triple source was the following:

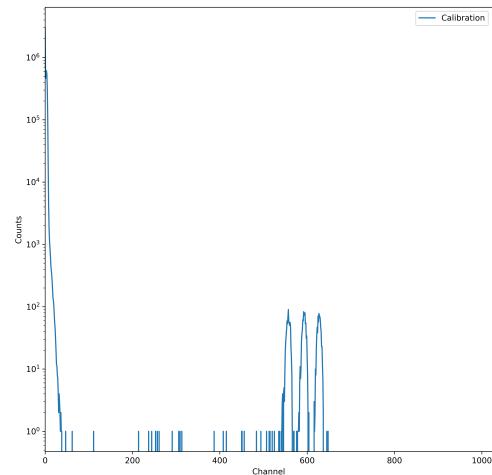
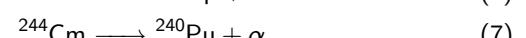
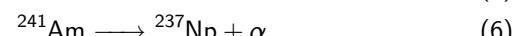


Figure 3: Spectrum of the Calibration source

We separated the spectra of channel/detectors 0, 1 and 2 (2 corresponding to the bottom one) and used a triple gaussian sum function to fit on the three energy peaks. According to theory, the first peak corresponds to the decay of plutonium into uranium, the second of americium into neptunium and the third of curium into plutonium. The decay equations are:



We decided to do the analysis only with detector/channel 0. This analysis could be further corroborated using the "detector 1" data. Using the triple gaussian, we obtained the following fit for channel 0:

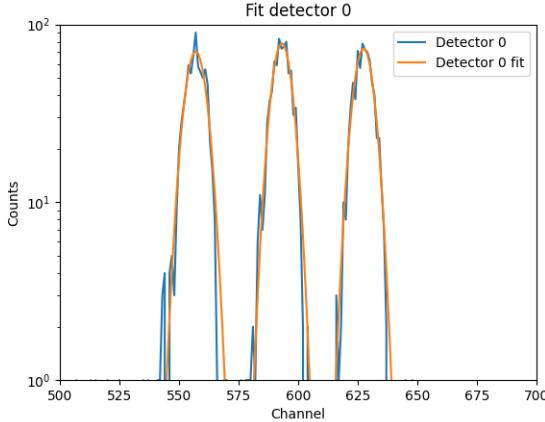


Figure 4: Detector 0 spectrum fit with triple gaussian

The fit parameters for the means, μ_0 , μ_1 and μ_2 obtained from the triple gaussian fit represent the energy value of each peak in channels. The computed values for these parameters, as well as the theoretical values of the energy, in MeV, for the peaks, are organised in the following tables:

Peak	Detector 0 [Chn]	Theoretical Energy [keV]
1 st	$\mu_0 = 557.00 \pm 0.11$	5156.59
2 nd	$\mu_1 = 593.14 \pm 0.10$	5485.56
3 rd	$\mu_2 = 627.44 \pm 0.10$	5804.82

Table 1: Calibration Values for detector 0

Using the values in the table we now have to compute a calibration equation for channel/detector 0. We plotted the theoretical values of the energy of the three peaks as a function of fit parameters:

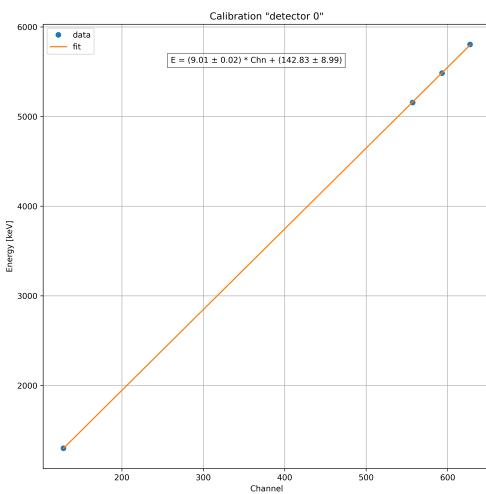


Figure 5: Calibration "detector 0"

The calibration equation for channel 0 is:

$$E[\text{keV}] = m_0 \times E[\text{Chn}] + b_0 \quad (8)$$

$$m_0 = 9.01 \pm 0.02$$

$$b_0 = 142.83 \pm 8.99$$

5 Alpha Peaks

For the analysis, we began by calculating the theoretical energy values of the two alphas.

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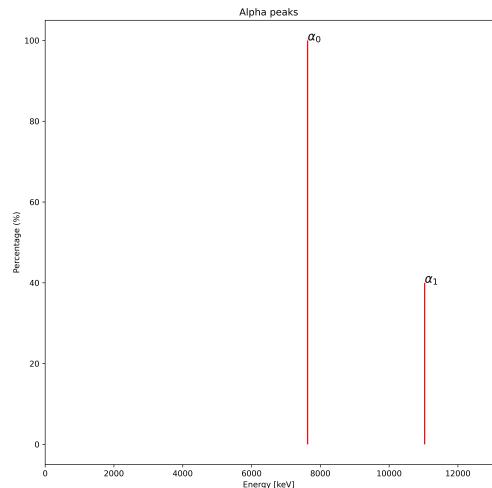


Figure 6: Theoretical energy values of the two alphas

The energies obtained were 7629.80 keV and 11031.44 keV. (FALTA EXPLICAR PERCENTAGENS) For the identification of lithium in our samples, we need to compare the theoretical energy values with the experimental ones. Since we know the emitted alpha in our samples is more energetic than the theoretical values, it is expected that the experimental peaks are slightly higher than the theoretical ones. If the samples contains a peak in the proximity of the alpha peaks it shows that the sample contains lithium.

6 Lithium Fluoride Sample

For the LiF sample, we used the calibration [4] to convert the channel values into energy values. we overlapped the expected α energy with the spectrum, and obtained the following:

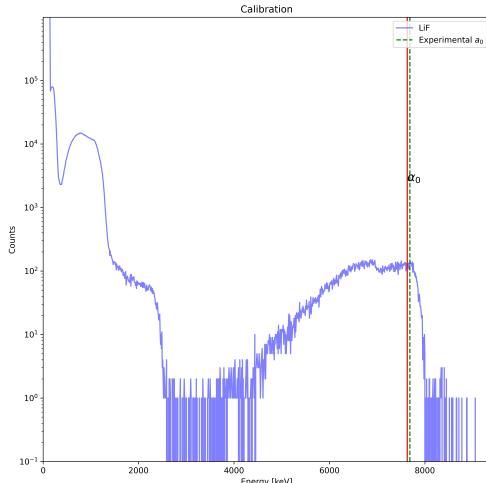


Figure 7: Spectrum of the LiF sample

The experimental α_0 is extremely close to the theoretical value, therefore we can confirm the presence of lithium in this sample. Moreover, it is according to the expected hypothesis that the observed lithium energy is slightly higher than the theoretical value. Analysing this spectrum further:

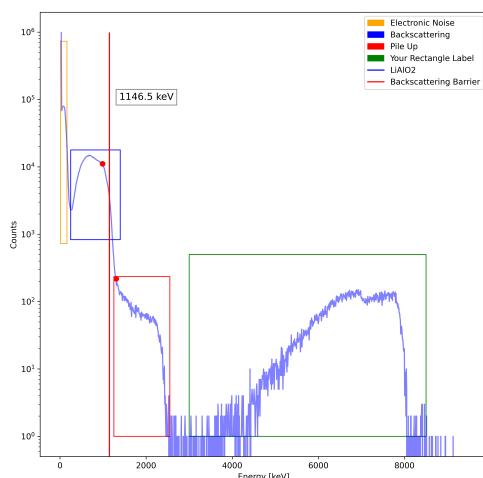


Figure 8: Full Analysis of LiF Spectrum

There are three noticeable structures in this spectrum. The first one is a peak around 0 keV, which is just electronic noise. The following structure is back scattering [2.3], identified by the barrier of 1146.5 keV. The back scattering is followed by event pile-up [2.4]. The last structure is the lithium peak. The depth of the sample creates the visible energy profile and this procedure is explained in section [2.2].

7 Lithium Aluminate Sample

We used the calibration again to obtain the Lithium Aluminate energy spectrum overlapped with the expected α energy:

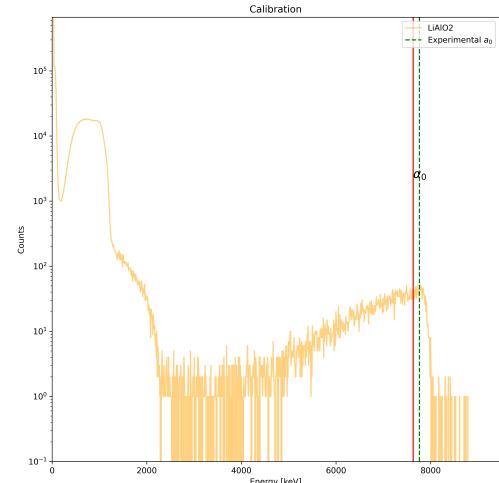


Figure 9: Spectrum of the LiAlO₂ sample

The experimental α_0 is very similar to the theoretical value, hence we can confirm the presence of lithium in this sample. If we analyze this spectrum further, we can see the following:

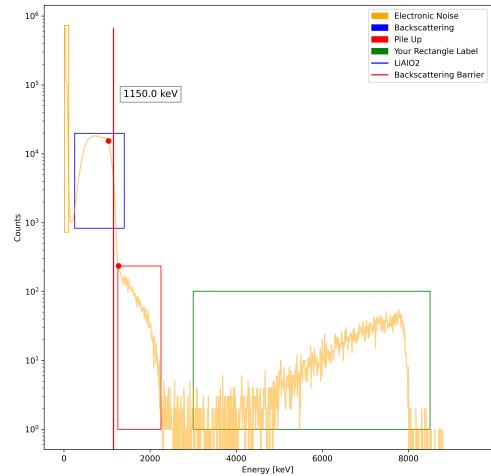


Figure 10: Full Analysis of LiAlO₂ Spectrum

It is evident that the structure of the spectrum follows a similar pattern to the one in the previous sample. First, there is electrical noise, followed by back scattering [2.3] and event pile-up [2.4]. The back scattering is identified by the barrier of 1150.0 keV. Finally, there is the lithium peak, which has an energy profile [2.2] as well due to the depth of the sample.

8 Implanted Sample

Finally, we used the calibration to obtain the implanted sample energy spectrum overlapped with the expected α energy:

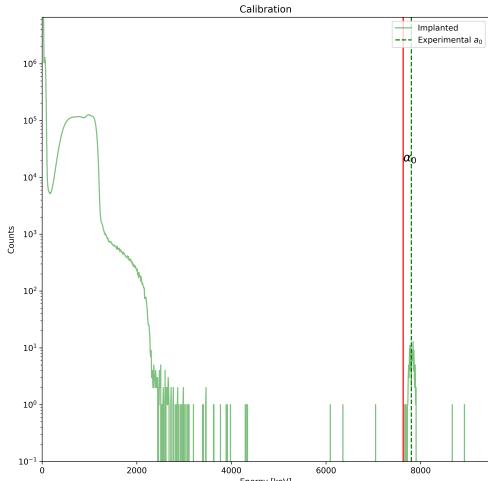


Figure 11: Spectrum of the implanted sample

There is a peak in the proximity of the α_0 peak, which is the expected lithium peak. One more time we can confirm the presence of lithium in this sample.

If we analyze the spectrum further:

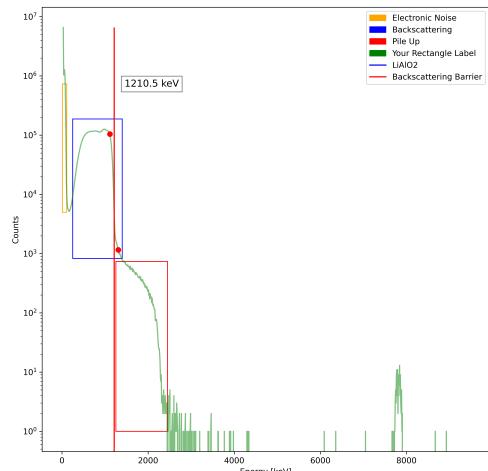


Figure 12: Full Analysis of the Implanted Sample Spectrum

Just like before, there is electrical noise, followed by back scattering [2.3] and event pile-up [2.4]. However, this sample is implanted only on the surface, therefore there is no energy profile as expected, since the lithium isn't being detected at different depths.

9 Quantitative Analysis

According to [2] it is possible to calculate the concentration of the element in the samples using with the following equations:

$$N\tau_i = \frac{H_i}{\sigma(E_i)\Omega Q} \quad (9) \quad N\Delta x = \frac{A}{\sigma(E_i)\Omega Q} \quad (10)$$

Where $N\tau_i$ are $N\Delta x$ different values for the superficial concentration of the element. For comparison, we can approximate $N\Delta x \approx N\tau_i \times \# \text{ channels}$.

H_i is the height, in counts, on a spectrum with accumulation (used in the LiAlO₂ and LiF samples), A is the area of a singular peak (used in the implanted sample), $\sigma(E_i)$ is the cross section of the reaction, Ω is the solid angle of the detector and Q is the max charge acquisition divided by e .

With this we get:

Implanted Sample: $N\Delta x = 9.25 \times 10^{16}$ atoms per cm²

LiAlO₂: $N\tau_i = 4.31 \times 10^{17}$ atoms per cm²

LiF: $N\tau_i = 1.15 \times 10^{18}$ atoms per cm²

For comparison: LiAlO₂: $N\Delta x = 2.15 \times 10^{19}$ atoms per cm²

LiF: $N\Delta x = 5.71 \times 10^{19}$ atoms per cm²

From this, it is noticeable that the implanted sample has around 200x less Lithium than the LiAlO₂ and 600x less Lithium than the LiF, as expected.

10 Conclusion

To conclude, we ended up with a successful experiment. We were able to detect the presence of lithium in all the analysed samples through nuclear reactions. Furthermore, we managed to go beyond our proposal and estimate the amount of lithium in each sample. The results obtained were in accordance with the values obtained from the Danish Institute that provided the samples. MEIO INVENTADO

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