

Artificial intelligence in data science

Game models

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Learn to play games

- ▶ Rules
- ▶ Observables
- ▶ Possible moves
- ▶ Aim: choose best move from observables
- ▶ Two methods:
 - ▶ Genetic algorithm
 - ▶ Reinforcement learning

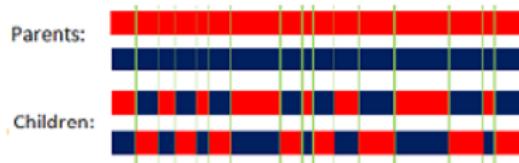
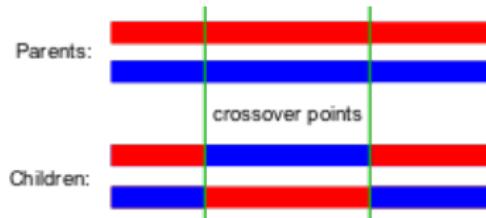
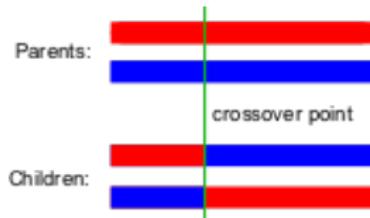
Genetic algorithm

- ▶ Learn from nature
- ▶ Let the fittest to survive
 - ▶ Fitness function, e.g. energy, length, etc.
- ▶ Combine different strategies
- ▶ State is represented by a vector (genetic code or genotype)
 - ▶ Phasespace, city order, neural network parameters, etc.
- ▶ Offsprings have two parents with shared genetic code
- ▶ Mutations
- ▶ Those who are not fit enough die out
 - ▶ Keep the number of agents fixed



Genetic algorithm: Reproduction

- ▶ Two parents and two children



With a probability of 0.5, children have 50% genes from first parent and 50% of genes from second parent even with randomly chosen crossover points.

Genetic algorithm terminology

- ▶ Chromosome: Carrier of the genetic representation
- ▶ Gene: Smallest units in the chromosome with individual meaning
- ▶ Parents: Pair of chromosomes, which produce offsprings
- ▶ Population: Set of chromosomes from which the parents are selected. Its size should be larger than the length of the chromosome
- ▶ Selection principle: The way parents are selected (random, elitistic)
- ▶ Crossover: Recombination of the genes of the parents by mixing
- ▶ Crossover rate: The rate by which crossover takes place (~90%)
- ▶ Mutation: Random change of genes
- ▶ Mutation rate: The rate by which mutation takes place (~1%)
- ▶ Generation: The pool after one sweep.

Genetic algorithm schema

1. Start with a randomly generated population
2. Calculate the fitnesses
3. Selection
 - ▶ Random
 - ▶ Best fitness (keep top 50% and generate new 50%)
 - ▶ Roulette (Monte-Carlo) selection
4. Crossover: offsprings must be viable (Sometimes difficult)

Parents

1	2	3	4	5	6	7	8	9
---	---	---	---	---	---	---	---	---

9	8	7	6	5	4	3	2	1
---	---	---	---	---	---	---	---	---

Offspring

				6	7	8	
--	--	--	--	---	---	---	--

9	5	4	3	2	6	7	8	1
---	---	---	---	---	---	---	---	---

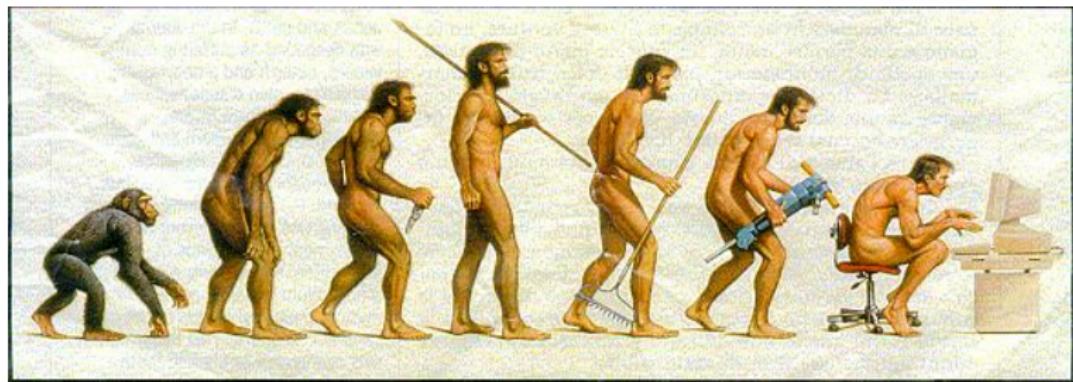
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4. Crossover: offsprings must be viable (Sometimes difficult)
 - ▶ One-point
 - ▶ Two-point
 - ▶ Uniform
 - ▶ Mutation: small rate

1	2	3	4	5	6	7	8	9	
---	---	---	---	---	---	---	---	---	--

1	2	8	4	5	6	7	3	9	
---	---	---	---	---	---	---	---	---	--

Genetic algorithm example



Reinforcement learning

- ▶ Agent gathers information about environment (explores its states): s_0, s_1, \dots
- ▶ Agent interacts with environment via actions t_0, t_1, \dots
- ▶ Agent gets reward depending on the actions r_0, r_1, \dots
- ▶ Modify agent's policy based on reward
- ▶ Agent moves to the next state

Ideas from: Fei-Fei Li, Justin Johnson, Serena Yeung

Q-value function

- ▶ Policy produces sample trajectories (or paths)
 $s_0, a_0, r_0, s_1, a_1, r_1 \dots$
- ▶ How good is a state? Value function (fitness) V , cumulative reward from a policy
- ▶ How good is a state-action pair? The Q-value function at state s and action a , is the expected cumulative reward from taking action a in state s and then following the policy. This is a conditional expected value

Bellman equation

- ▶ The optimal Q-value function Q^* is the maximum expected cumulative reward achievable from a given (state, action) pair:

$$Q^*(s, a) = \max_{\pi} \mathbb{E} \left(\sum_t \gamma^t r_t | s_0 = s, a_0 = a, \pi \right),$$

where π is the actual policy

- ▶ Q^* satisfies the following Bellman equation:

$$Q^*(s, a) = \mathbb{E}_{s' \sim \varepsilon} (r + \gamma \max_{a'} Q^*(s', a') | s, a)$$

- ▶ if the optimal state-action values for the next time-step $Q^*(s', a')$ are known, then the optimal strategy is to take the action that maximizes the expected value of $r + \gamma \max_{a'} Q^*(s', a')$
- ▶ iterative solution

Reinforcement learning algorithm

Algorithm 1 Deep Q-learning with Experience Replay

Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights
for episode = 1, M **do**
 Initialise sequence $s_1 = \{x_1\}$ and preprocessed sequenced $\phi_1 = \phi(s_1)$
 for $t = 1, T$ **do**
 With probability ϵ select a random action a_t
 otherwise select $a_t = \max_a Q^*(\phi(s_t), a; \theta)$
 Execute action a_t in emulator and observe reward r_t and image x_{t+1}
 Set $s_{t+1} = s_t, a_t, x_{t+1}$ and preprocess $\phi_{t+1} = \phi(s_{t+1})$
 Store transition $(\phi_t, a_t, r_t, \phi_{t+1})$ in \mathcal{D}
 Sample random minibatch of transitions $(\phi_j, a_j, r_j, \phi_{j+1})$ from \mathcal{D}
 Set $y_j = \begin{cases} r_j & \text{for terminal } \phi_{j+1} \\ r_j + \gamma \max_{a'} Q(\phi_{j+1}, a'; \theta) & \text{for non-terminal } \phi_{j+1} \end{cases}$
 Perform a gradient descent step on $(y_j - Q(\phi_j, a_j; \theta))^2$ according to equation 3
 end for
end for

Reinforcement learning algorithm

Algorithm 1 Deep Q-learning with Experience Replay

Initialize replay memory \mathcal{D} to capacity N
Initialize action-value function Q with random weights

Initialize replay memory, Q-network

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← Play M episodes (full games)

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Initialize state
(starting game
screen pixels) at the
beginning of each
episode

Reinforcement learning algorithm

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end for

end for



For each timestep t
of the game

Reinforcement learning algorithm

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end for

end for



With small probability
select a random
action (explore),
otherwise select
greedy action from
current policy

Reinforcement learning algorithm

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end for

end for

Take the action (a_t)
and observe the
reward r_t and next
state s_{t+1}

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 end for
end for

Store transition in
replay memory



Reinforcement learning algorithm

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end for

end for



Experience Replay:
Sample a random
minibatch of transitions
from replay memory
and perform a gradient
descent step

Reinforcement learning scoring

