EXERCISES ABOUT PROPERTIES OF REGULAR LANGUAGES

- 1 Pumping Lemma. [SELECTED]
- a) Show using the pumping lemma that the language $L=\{0^n1^{2n} \mid n\geq 1\}$ is not a regular language.
- b) Show using the pumping lemma that the language of the strings v1^m, in which v is an arbitrary string over the alphabet {0,1} with length m, is not regular.
- c) Try to show using the pumping lemma that the language of the strings given by (00+11)* is not regular.
- d) Idem for the language given by 01*0*1.
- e) Idem for the language $\{0^n \mid n \text{ is a perfect square}\}$.
- 2 Being L a language and a symbol, we define: [SELECTED]

L/a (quotient of L and a) – the set of strings w in which wa belongs to L;

a\L (derivate of L in order to a) – the set of strings w in which aw belongs to L.

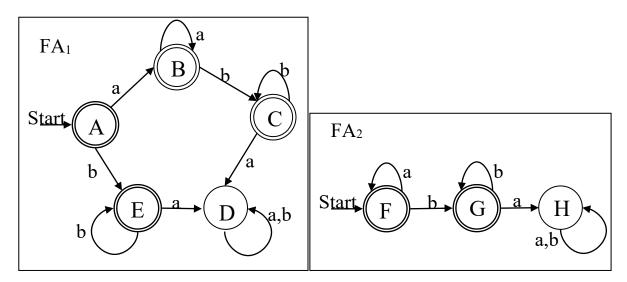
For example, given L= $\{a, aab, baa\}$; then L/ $a=\{\varepsilon, ba\}$ and $a\L=\{\varepsilon, ab\}$.

- a) Prove that if L is regular then L/a is also regular. Suggestion: use the DFA of L and analyze the final states.
- b) Prove that if a language L is regular, then $a \setminus L$ is also regular. Suggestion: the regular languages are closed for the reverse and quotient operations.
- c) Which of the following equalities are true?
 - (L/a)a = L
 - $a(a \setminus L) = L$
 - (La)/a = L
 - $a \setminus (aL) = L$
- The closure properties can be also used to show that certain languages are not regular. Beginning with the knowledge that $L_0^{n_1^n} = \{0^n1^n \mid n \ge 0\}$ is not regular, show that $\{0^i1^j \mid i \ne j\}$ is not regular, using the operations closed to regular languages. **[SELECTED]**
- **4** Suppose a language L defined over the alphabet Σ. [SELECTED]
- a) Show an algorithm to determine if the language is infinite. Suggestion: use the pumping lemma and the length of the strings.
- b) Show an algorithm to identify if $L=\Sigma^*$, i.e., if the language accepts all the strings over the alphabet.

5 Consider the following DFA. [SELECTED]

	0	1
\rightarrow A	В	Е
В	С	F
*C	D	Н
D	Е	Н
Е	F	I
*F	G	В
G	Н	В
Н	I	С
*I	A	Е

- a) Build the table of distinguishable states.
- b) Obtain the minimum DFA equivalent to the one given above.
- 6 Consider the following DFAs: [SELECTED]



- a) Obtain the minimum DFA equivalent to FA₁.
- b) The automata FA₁ and FA₂ are equivalent? Justify.