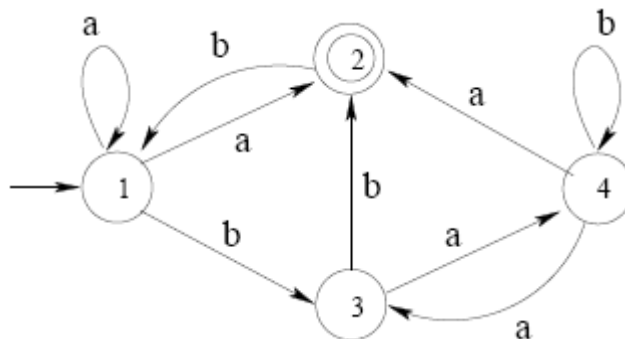


EXERCISES ABOUT REGULAR LANGUAGES

- 1 Consider the L language over the alphabet $\{0,1\}$ whose strings are defined by the regular expression $0^*1^*00^*$.
 - a) Draw a ϵ -NFA for the L language.
 - b) Draw an NFA for the L language with only 3 states.
 - c) Obtain an equivalent DFA.
 - d) Obtain a DFA for the complement of the language.
 - e) Obtain a regular expression for the complement of the language.
- 2 The following state diagram represents an NFA $N = (Q, \Sigma, \delta, q_0, F)$.



- a) Show for this automaton, the value of each element in the tuple.
 - b) Show the transition function using the transition table.
 - c) Obtain an equivalent DFA.
- 3 Write a regular expression for the strings over the alphabet $\{a,b\}$ with more than 2 a's.
 - 4 The following equality between languages is true or false? **[SELECTED]**

$$L(b^*a^*) \cap L(a^*b^*) = L(a^*) \cup L(b^*).$$
 - 5 For the DFA given by the transition function below and with q_1 as initial state and q_3 as final state, determine the regular expressions $R_{ij}^{(0)}$, $R_{ij}^{(1)}$, $R_{ij}^{(2)}$ and obtain from them the regular expression representing the language recognized by the automaton.

$$\begin{array}{lll} \delta(q_1, 0) = q_2 & \delta(q_1, 1) = q_3 & \delta(q_2, 0) = q_1 \quad \delta(q_2, 1) = q_3 \\ \delta(q_3, 0) = q_2 & \delta(q_3, 1) = q_1 & \end{array}$$
 - 6 For each of the following statements, identify if it is true or false and give a very short justification. **[SELECTED]**
 - a) Given a language defined by a non-deterministic finite automaton with k states, the equivalent deterministic finite automaton does not have more than 2^k states.
 - b) The closure language (L^*) of a regular language L is a language that includes the empty string.