PrimeOmega gives how many multipled primes there are in total in a prime factorization.

```
In[*]:= FactorInteger@12
```

$$\textit{Out[\circ]} = \{\{2,2\},\{3,1\}\}$$

The primes are 2, 3, the quantities are 2, 1.

In[\*]:= PrimeOmega@12

Out[ • ]= 3

PrimeOmega is the sum of the quantities.

```
In[*]:= FactorInteger@327
```

```
Out[\circ]= { {3, 1}, {109, 1}}
```

In[\*]:= PrimeOmega@327

Out[ • ]= 2

How many primes there are in the factorization itself can be inferred from the size of the resulting list.

```
In[*]:= FactorInteger@330
```

```
Out[\circ]= { {2, 1}, {3, 1}, {5, 1}, {11, 1}}
```

In[\*]:= Length@FactorInteger@330

Out[ • ]= 4

Let's create an index from the quantity of primes in a factorization together with the multiplicity of primes in the factorization, to create a rough "size" for each factorization.

```
In[@]:= Clear[FacSize];
```

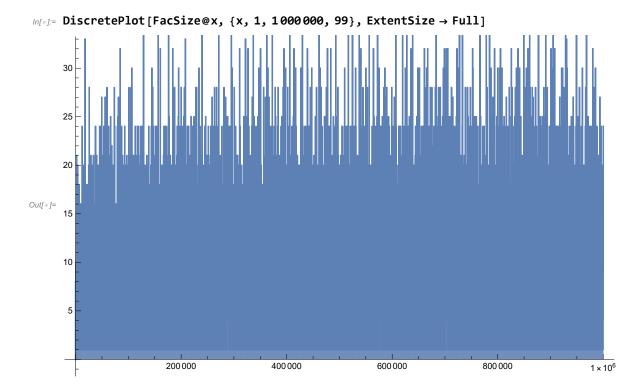
FacSize=Function[{n},Length@FactorInteger@n\*PrimeOmega@n];

```
In[*]:= {FacSize@12, FacSize@327, FacSize@330}
```

Out[ $\bullet$ ]= {6, 4, 16}

Which agrees with the prior observations.

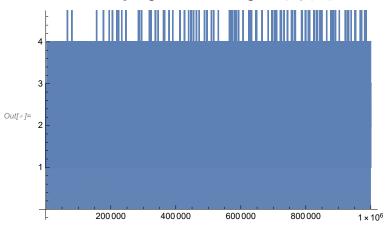
Let's plot the "factorization size" as a function of each integer:



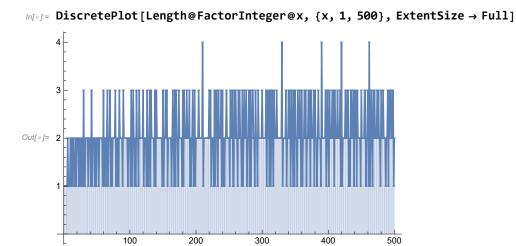
This tells there is a ceiling of approximately  $35.\,$ 

If only the number of primes is plotted,

ln[\*]:= DiscretePlot[Length@FactorInteger@x, {x, 1, 1000000, 99}, ExtentSize  $\rightarrow$  Full]



Let's zoom in to the graph.



This seems to indicate no matter the size of the integer, there seems to be a clear upper bound on the size, by count of primes, of its prime factorization.

Note: this seems to be what's proved in the Hardy-Ramanujam theorem [1].

TODO: check the *composition* of the factors i.e. the regularity of which primes are in them.

## References

1. Hardy-Ramanujam theorem, Wikipedia. https://en.wikipedia.org/wiki/Hardy%E2%80%93Ramanujan\_theorem