Source: The Princeton Companion to Applied Mathematics, Nicholas J. Highham, Princeton University Press, 2015.

Second-order ODEs also arise in electrical networks. Consider the flow of electric current I(t) in a simple RLC circuit composed of an inductor with inductance L, a resistor with resistance R, a capacitor with capacitance C, and a source with voltage  $v_s$ , as illustrated in figure 8.

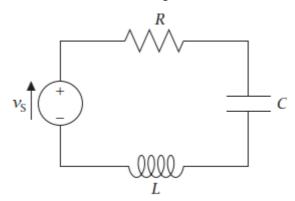


Figure 8 A simple RLC electric circuit.

The Kirchhoff voltage law states that the sum of the voltage drops around the circuit equals the input voltage,  $v_2$ . The voltage drops across the resistor, inductor, and capacitor are RI,  $L\frac{dI}{dt}$ , and  $\frac{Q}{C}$ , respectively, where Q(t) is the charge on the capacitor, so

$$Lrac{dI}{dt} + RI + rac{Q}{C} = v_s(t).$$

Since  $I=rac{dQ}{dt}$  , this equation can be rewritten as the second-order ODE

$$Lrac{d^2Q}{dt^2}+Rrac{dQ}{dt}+rac{1}{C}Q=v_s(t).$$