

PrimeOmega gives how many multiplied primes there are in total in a prime factorization.

```
In[ ]:= FactorInteger@12
```

```
Out[ ]:= {{2, 2}, {3, 1}}
```

The primes are 2, 3, the quantities are 2, 1.

```
In[ ]:= PrimeOmega@12
```

```
Out[ ]:= 3
```

PrimeOmega is the sum of the quantities.

```
In[ ]:= FactorInteger@327
```

```
Out[ ]:= {{3, 1}, {109, 1}}
```

```
In[ ]:= PrimeOmega@327
```

```
Out[ ]:= 2
```

How many primes there are in the factorization itself can be inferred from the size of the resulting list.

```
In[ ]:= FactorInteger@330
```

```
Out[ ]:= {{2, 1}, {3, 1}, {5, 1}, {11, 1}}
```

```
In[ ]:= Length@FactorInteger@330
```

```
Out[ ]:= 4
```

Let's create an index from the quantity of primes in a factorization together with the multiplicity of primes in the factorization, to create a rough "size" for each factorization.

```
In[1]:= Clear[FacSize];  
FacSize=Function[{n},Length@FactorInteger@n*PrimeOmega@n];
```

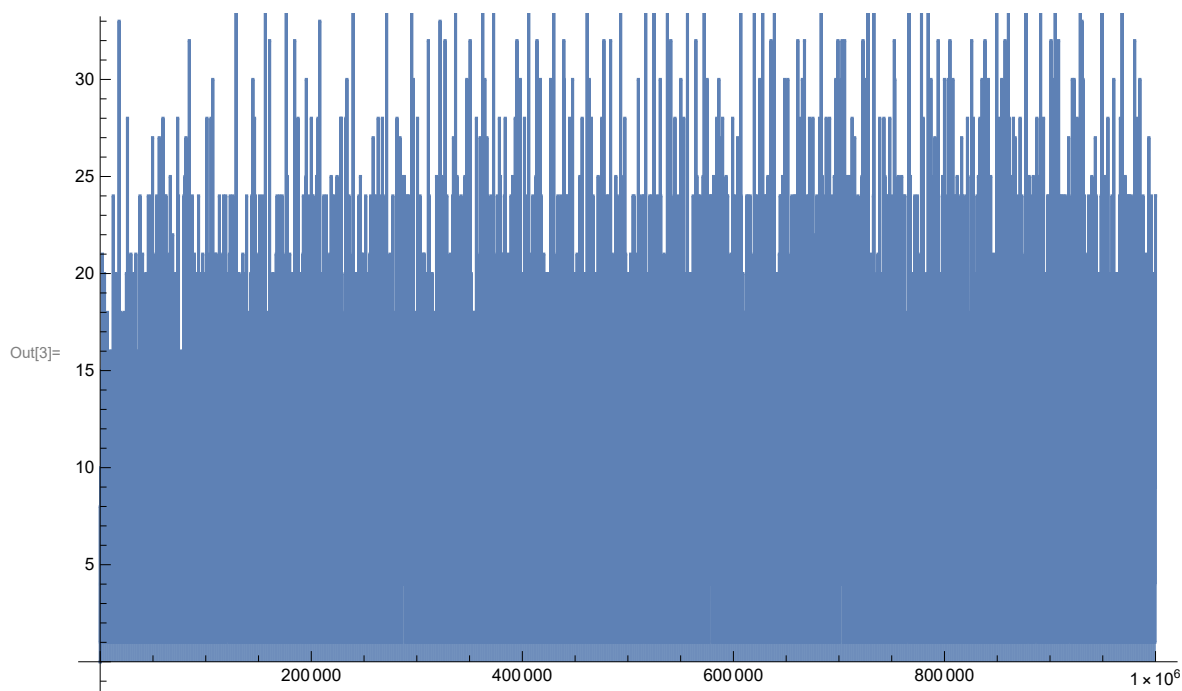
```
In[ ]:= {FacSize@12, FacSize@327, FacSize@330}
```

```
Out[ ]:= {6, 4, 16}
```

Which agrees with the prior observations.

Let's plot the "factorization size" as a function of each integer:

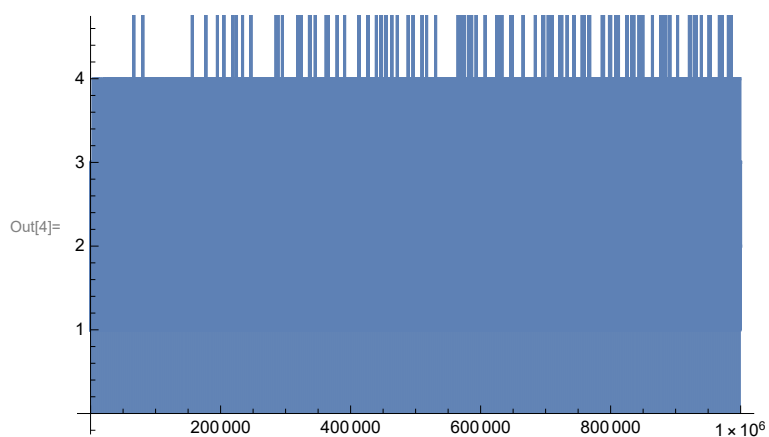
```
In[3]:= DiscretePlot[FacSize@x, {x, 1, 1000000, 99}, ExtentSize -> Full]
```



This tells there is a ceiling of approximately 35.

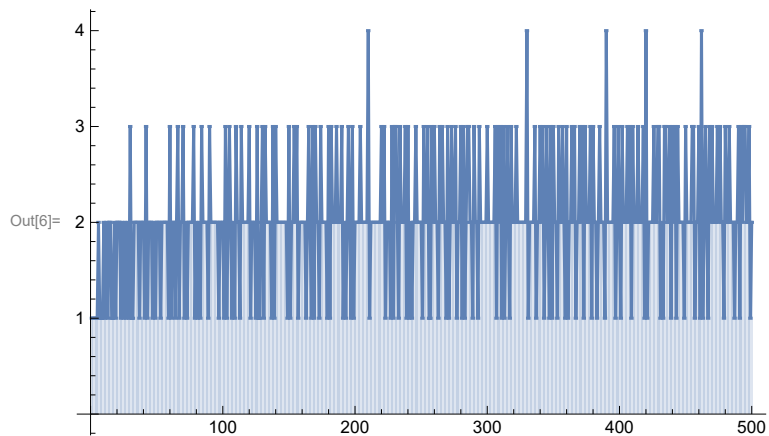
If only the number of primes is plotted,

```
In[4]:= DiscretePlot[Length@FactorInteger@x, {x, 1, 1000000, 99}, ExtentSize -> Full]
```



Let's zoom in to the graph.

```
In[6]:= DiscretePlot[Length@FactorInteger@x, {x, 1, 500}, ExtentSize -> Full]
```



This seems to indicate no matter the size of the integer, there seems to be a clear upper bound on the size, by whatever estimate, of its prime factorization.

It is interesting to note that seemingly primes larger than the fifth prime, **11**, are “useless”, in that they are not solicited by any factorization.

```
In[7]:= Prime@5
```

Out[7]= 11