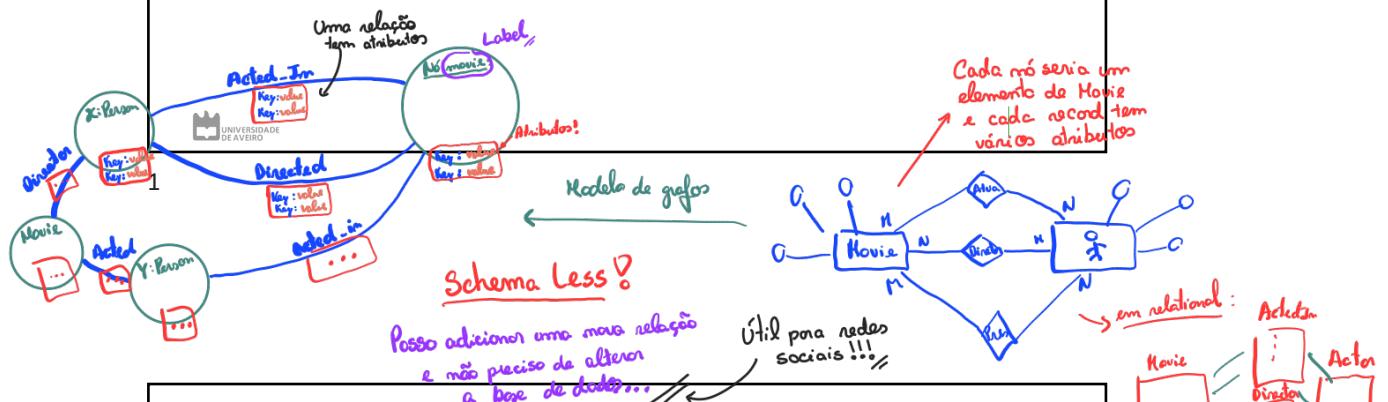


Graph Databases

UA.DETI.CBD

José Luis Oliveira / Carlos Costa

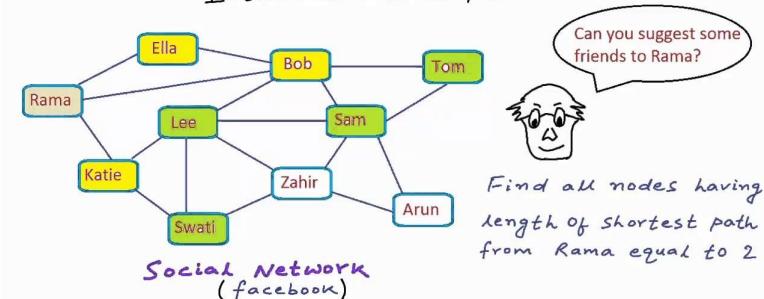


Some theory about graph theory

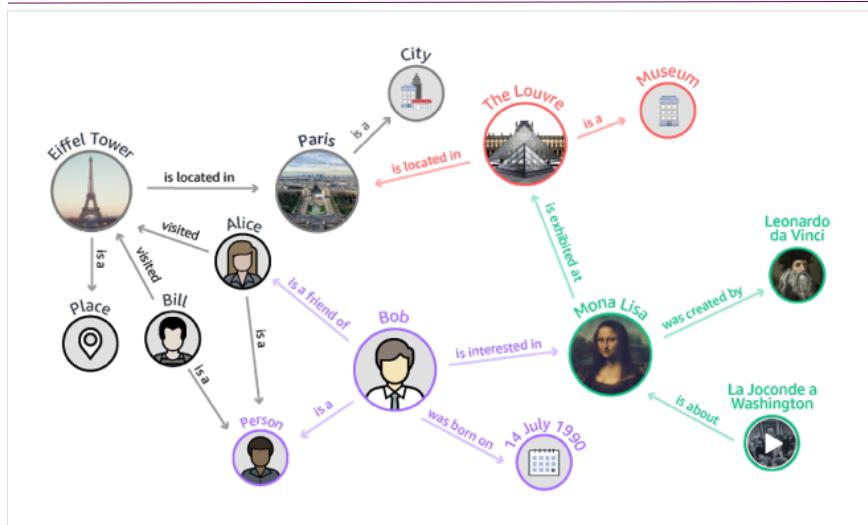
"Graphs are one of the unifying themes of computer science - an abstract representation that describes the organization of transportation systems, human interactions, and telecommunication networks. That so many different structures can be modeled using a single formalism is a source of great power to the educated programmer."

The Algorithm Design Manual, by Steven S. Skiena (Springer)

Introduction to Graphs



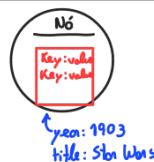
Graphs



<https://www.allthingsdistributed.com/2019/12/power-of-relationships.html>

3

3



Graphs

❖ Data: a set of entities and their relationships

- e.g., social networks, travelling routes, ...
- We need to efficiently represent graphs

❖ Operations: finding the neighbours of a node, checking if two nodes are connected by an edge, updating the graph structure, ...

- We need efficient graph operations

↳ ShortestPath!,,

❖ $G = (V, E)$ is commonly modelled as

- set of nodes (vertices) V
- set of edges E
- $n = |V|, m = |E|$

Um grafo é definido
por um set de vertices
e arestas



4

4

Types of Graphs

Os que queremos

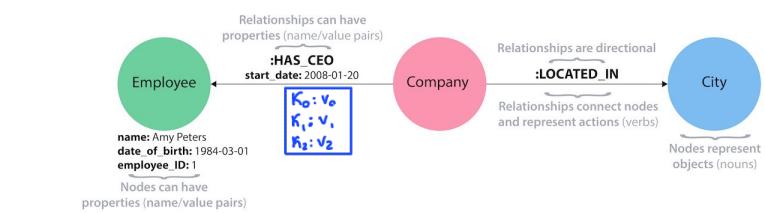
❖ Single-relational

- Edges are homogeneous in meaning
 - e.g., all edges represent friendship

Simplesmente
sem propriedades,,

❖ Multi-relational (property) graphs

- Edges are typed or labelled
 - e.g., friendship, business, communication
- Vertices and edges maintain a set of key/value pairs
 - Representation of non-graphical data (properties)
 - e.g., name of a vertex, the weight of an edge



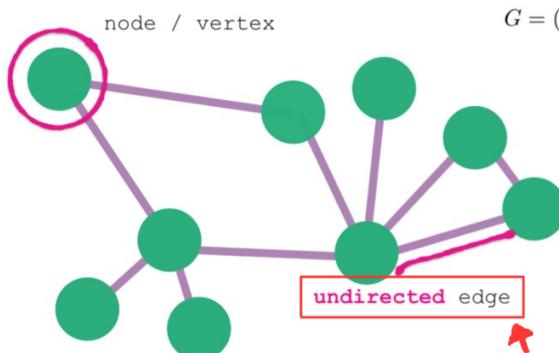
5

5

Graphs

❖ Which data structure should be used?

undirected graph / network
 $G = (V, E)$



6

6

Adjacency Matrix

$N \times N$

- Bi-dimensional array A of $n \times n$ Boolean values

- Indexes = node identifiers
- A_{ij} indicates whether the two nodes i, j are connected

- Pros:

- Checking if two nodes are connected
- Adding/removing edges

- Cons:

- Quadratic space with respect to n
 - We usually have sparse graphs (lots of 0)
 - Addition of nodes is expensive
 - Retrieval of all the neighbouring - $O(n)$

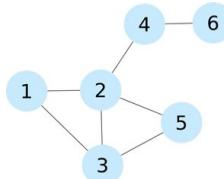
- Other variants:

- Directed graphs, Weighted graphs, ...



Já não seria espelhado!

Poderia meter peso por aresta! //



→ Não existem ligações a eles próprios!
⇒ Diagonal = 0,,

Matriz de adjacência

0	1	1	0	0	0
1	0	1	1	1	0
1	1	0	0	1	0
0	1	0	0	0	1
0	1	1	0	0	0
0	0	0	1	0	0

bidimensional

Informação duplicada

sem ligação interna

7

7

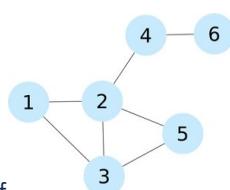
Adjacency List

- A set of lists where each accounts for the neighbours of one node

- A vector of n pointers to adjacency lists

- Undirected graph:

- An edge connects nodes i and j => the list of neighbours of i contains the node j and vice versa



Apenas guardamos os que estão ligados

$$N1 \rightarrow \{N2, N3\}$$

$$N2 \rightarrow \{N1, N3, N5\}$$

$$N3 \rightarrow \{N1, N2, N5\}$$

$$N4 \rightarrow \{N2, N6\}$$

$$N5 \rightarrow \{N2, N3\}$$

$$N6 \rightarrow \{N4\}$$

- Pros:
- Obtaining the neighbours of a node
- Cheap addition of nodes to the structure
- Compact representation of sparse matrices

- Cons:

- Checking an edge between two nodes

↳ em Directed Graphs tento de van mos 2 listas



8

8

Incidence Matrix

- Bi-dimensional Boolean matrix of n rows and m columns

- A **column** represents an **edge**
 - Nodes that are connected by a certain edge
- A **row** represents a **node**
 - All edges that are connected to the node

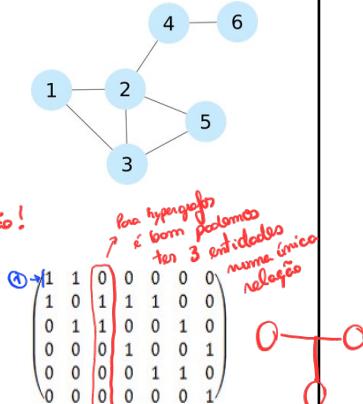
Pros:

- For representing hypergraphs, where one edge connects an arbitrary number of nodes

Cons:

- Requires $n \times m$ bits

\uparrow Tem maior dimensão !



9

9

Laplacian Matrix

\downarrow Matriz de Adjacência !

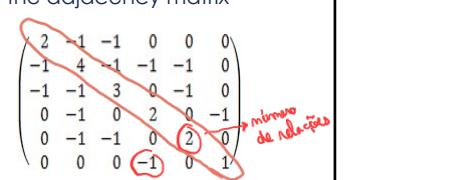
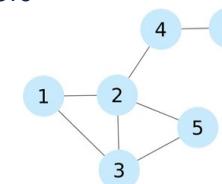
- Bi-dimensional array of $n \times n$ integers

- Diagonal of the Laplacian matrix indicates the **degree** of the node
- The rest of positions are set to -1 if the two vertices are connected, 0 otherwise
- $L = D - A$

• where D is degree matrix of graph G and A is the adjacency matrix

Pros & Cons:

- = Adjacency Matrix
 - But, it retains more information
 - Allows analyzing the graph structure by means of spectral analysis



grafo
máximo
de relações
de um determinado
no !!

\Rightarrow Na Matriz do Adj. era
só zeros ... //

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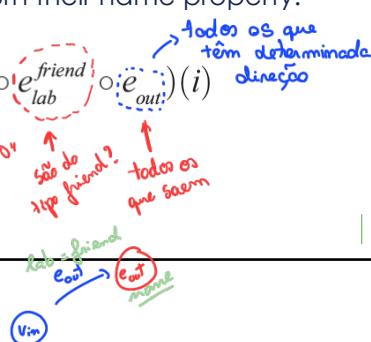
10

Graph Traversals

- ❖ Single step **traversal** from element i to element j ,
where $i, j \in (V \cup E)$
- ❖ Expose explicit **adjacencies** in the graph
 - e_{out} : traverse to the outgoing edges of the vertices
 - e_{in} : traverse to the incoming edges of the vertices
 - v_{out} : traverse to the outgoing vertices of the edges
 - v_{in} : traverse to the incoming vertices of the edges
 - e_{lab} : allow (or filter) all edges with the label
 - ϵ : get element property values for key r
 - e_p : allow (or filter) all elements with the property s for key r
 - $\epsilon=$: allow (or filter) all elements that are the provided element

Graph Traversals

- ❖ Single step traversals can **compose complex traversals** of arbitrary length
- ❖ e.g., find all friends of Alberto
 - Traverse to the outgoing edges of vertex i (representing Alberto),
 - then only allow those edges with the label friend,
 - then traverse to the incoming (i.e. head) vertices on those friend-labelled edges.
 - Finally, of those vertices, return their name property.



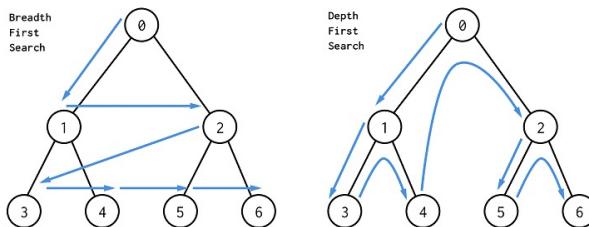
Graph Traversals

❖ Breadth First Search (BFS)

- one node is selected and then all of the adjacent nodes are visited one by one.
- it moves further to check another node.

❖ Depth First Search (DFS)

- one starting vertex is given, and when an adjacent vertex is found, it moves to that adjacent vertex first and try to traverse in the same manner.



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13

13

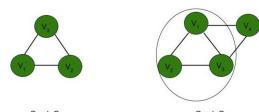
Transactional Graph Databases

Encontrar subgrafos

Types of Queries

❖ Sub-graph queries

- More general type: sub-graph isomorphism
- Searches for a specific pattern in the graph database
- A small graph or a graph, where some parts are uncertain
 - e.g., vertices with wildcard labels



❖ Super-graph queries → *Se dentro da base de dados tem algum subgrafo neste supergrafo*

- Searches for the graph database members of which their whole structures are contained in the input query

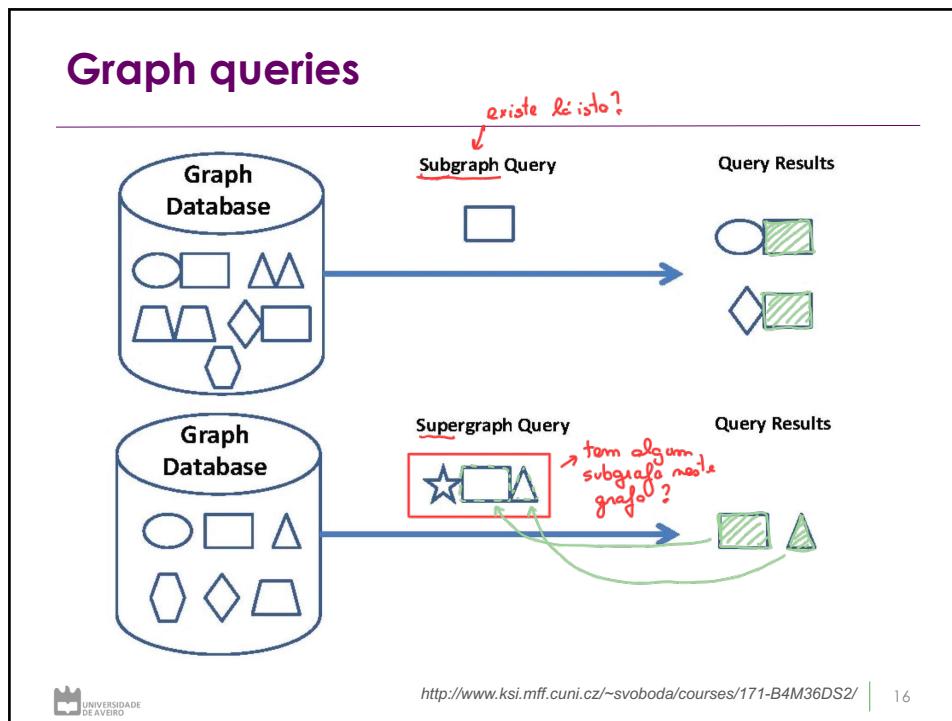
❖ Similarity (approximate matching) queries

- Finds graphs which are similar, but not necessarily isomorphic to the input query

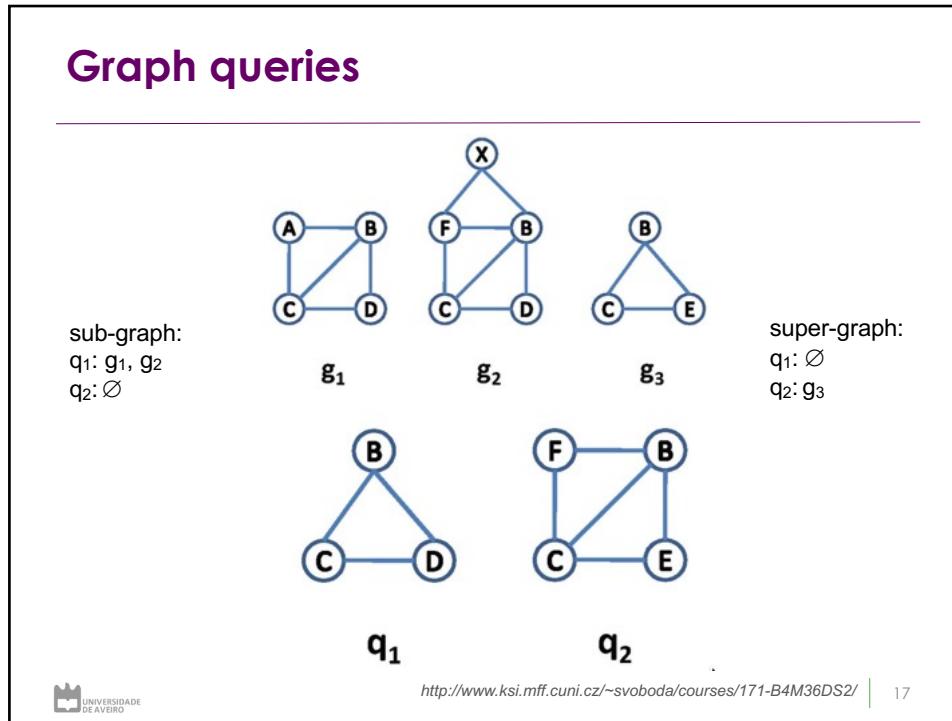
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15

15



16



17

Graph-oriented Database



21

Graph-like Data Models

- ❖ Many-to-many relationships are an important distinguishing feature between different data models.
- | | | | | |
|-------------------|---------------------|----------------|------------------------------|--------------------|
| key-value model | column-family model | document model | <u>relational model</u> | <u>graph model</u> |
| | | | Neo4j
ACID
graph model | |
| unrelated records | | | highly connected data | |
- ❖ The relational model can handle simple cases of many-to-many relationships, but
 - as the connections become more complex, it becomes more natural to start modelling as a graph.

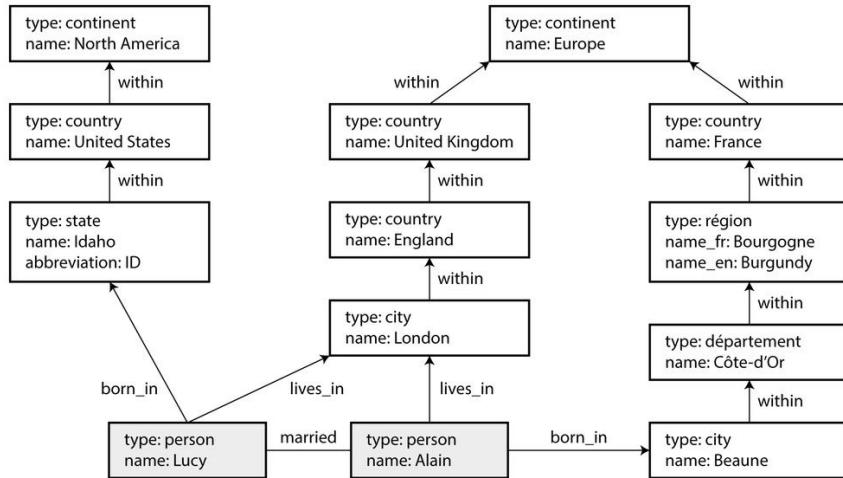


22

Sai no teste

22

Graph-like Data Models



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23

Graph-like Data Models

- ❖ A graph consists of two kinds of object:
 - **vertices** (also known as nodes or entities)
 - **edges** (also known as relationships).
- ❖ Many kinds of data can be modelled as a graph:
 - **Social graphs** – vertices are people, edges indicate which people know each other.
 - The **web graph** – vertices are web pages, edges indicate HTML links to other pages.
 - **Road or rail networks** – vertices are junctions, and edges represent the roads or railway lines between them.

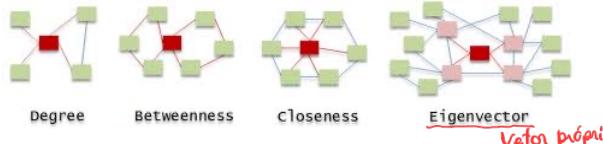
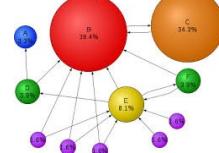
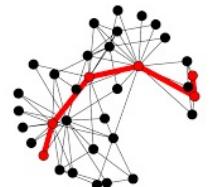
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24

24

Graph-like Data Models

- ❖ Well-known **algorithms** can operate on these graphs: for example,
 - the **shortest path** in a road network is useful for routing.
 - **PageRank** on the web graph to determine the popularity of a web page.
 - Degree, Betweenness, Closeness, etc.



25

25

Graph-like Data Models

- ❖ There are several different, but related, ways of **structuring** and querying data in graphs. Two examples:
 - **property graph** model
 - implemented by Neo4j, Titan, InfiniteGraph
 - **the triple-store** model
 - implemented by Datomic, AllegroGraph and others.
- ❖ Some declarative **query languages** for graphs
 - Cypher
 - SPARQL
 - Datalog

Para web
semântica ! //



26

26

Property graphs

- ❖ Each **vertex** consists of:

- a unique identifier,
- a set of outgoing edges,
- a set of incoming edges, and
- a collection of properties (key-value pairs).

O vértice tem propriedades

- ❖ Each **edge** consists of:

- a unique identifier,
- the vertex at which the edge starts (the tail vertex),
- the vertex at which the edge ends (the head vertex),
- a label to describe the type of relationship between the two vertices, and
- a collection of properties (key-value pairs).

As relações têm propriedades!



27

27

Property graphs

- ❖ Any vertex can have an edge connecting it with any other vertex. ↗

- There is no schema that restricts which kinds of things can or cannot be associated.

- ❖ Given any vertex,

- We can efficiently find both incoming and outgoing edges.
- Traverse the graph.

- ❖ Different labels for different kinds of relationship

- Allow storing several different kinds of information in a single graph, while still maintaining a clean data model.



28

28

Triple-stores *que é igual*

- The **triple-store model** is mostly equivalent to the property graph model
 - using different words to describe the same ideas.
- Information is stored in the form of very simple three-part statements:
 - subject, predicate, object.**



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29

29

Triple-stores

Não do gráfico

- The **subject** of a triple is equivalent to a **vertex** in a graph.
- The **object** is one of two things:
 - a **value** in a primitive datatype, such as a string or a number.
 - In that case, the **predicate** and **object** of the triple are equivalent to the **key** and **value** of a property on the subject vertex.
 - For example, (lucy, age, 33) is like a vertex lucy with properties {"age":33}.
 - another vertex** in the graph.
 - In that case, the **predicate** is an **edge** in the graph, the subject is the tail vertex and the object is the head vertex.
 - For example, in (lucy, marriedTo, alain).

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30

30

Graph Databases



TITAN



ArangoDB

A P A C H E
G I R A P H

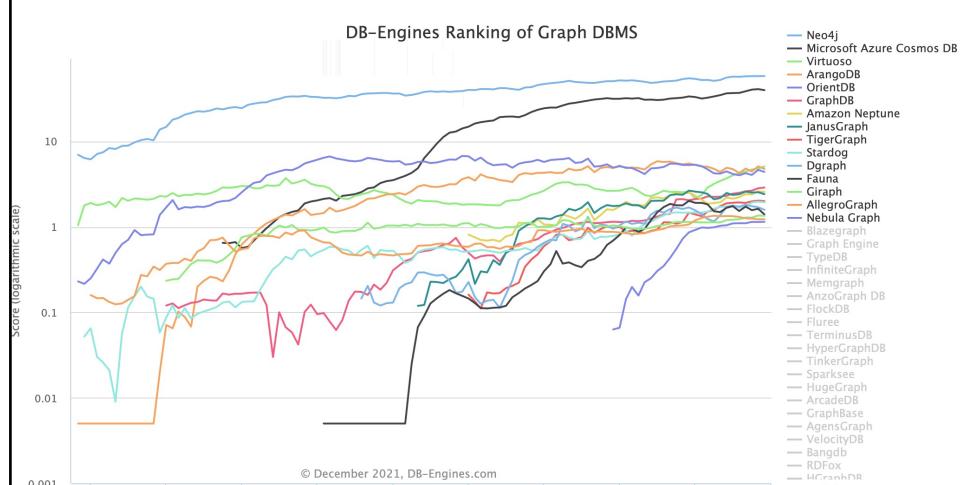
INFINITEGRAPH®



32

32

Graph Databases Popularity



33

33

Graph Databases

❖ Suitable use cases

- Social networks, routing, dispatch, and location-based services,
- recommendation engines, chemical compounds, biological pathways, linguistic trees, ...
- i.e. simply for graph structures

Muitas relações!

❖ When not to use

- Extensive batch operations are required
 - Multiple nodes / relationships are to be affected
- Only too large graphs to be stored
 - Graph distribution is difficult or impossible at all



35

35

Neo4j Graph Database



36

36

Neo4j

- ❖ Graph database
 - <https://neo4j.com/>
- ❖ Features
 - Open source, massively scalable (billions of nodes), high availability, fault-tolerant, master-slave replication, ACID transactions, embeddable, ...
 - Expressive graph query language (Cypher), traversal framework
- ❖ Developed by Neo Technology
- ❖ Implemented in Java
- ❖ Operating systems: cross-platform
- ❖ Initial release in 2007

Term indexes também!



37

37

Features of Neo4j

- ❖ Data model (flexible schema)
 - Neo4j follows a data model named native **property graph model**.
 - The graph contains **nodes** (entities) and these nodes are connected with each other (depicted by **relationships**).
Nodes and relationships store data in key-value pairs known as **properties**.
 - In Neo4j, there is no need to follow a fixed schema.
- ❖ ACID properties !
 - Neo4j supports full ACID (Atomicity, Consistency, Isolation, and Durability) rules.



38

38

Features of Neo4j

❖ Scalability and reliability

- You can scale the database by increasing the volume without affecting the query processing speed and data integrity.
- Neo4j also provides support for replication for data safety and reliability. ☺

❖ Cypher Query Language

- Neo4j provides a powerful declarative query language known as Cypher.
- It uses ASCII-art for depicting graphs.
- Cypher is easy to learn and can be used to create and retrieve relations between data without using the complex queries like Joins.



39

39

Features of Neo4j

❖ Built-in web application

- Neo4j provides a built-in **Neo4j Browser** web application. Using this, we can create and query any graph data.

❖ Drivers – Neo4j can work with

- It supports two kinds of Java API: Cypher API and Native Java API to develop Java applications.
- REST API to work with programming languages such as Java, Spring, Scala etc.
- Java Script to work with UI MVC frameworks such as Node JS.

❖ Indexing – Neo4j supports Indexes by using Apache Lucene. ☺



40

40

Data Model

- ❖ Database system structure
 - Instance → single graph
- ❖ Property graph = directed labelled multigraph
 - Collection of vertices (nodes) and edges (relationships)

❖ Graph node

- Has a unique (internal) identifier
- Can be associated with a set of labels
 - Allow us to categorize nodes
- Can also be associated with a set of properties
 - Allow us to store additional data together with nodes

Data Model

- ❖ Graph relationship
 - Has a unique (internal) identifier
 - Has a direction
 - Relationships are equally well traversed in either direction!
 - Directions can be ignored when querying
 - Always has a start and end node
 - Can be recursive (i.e. loops are allowed)
 - Is associated with exactly one type
 - Can also be associated with a set of properties

Relacionamento: apenas a um tipo
Nó: pode estar associado a vários tipos

X: Movie, serial

Data Model

- ❖ Node and relationship **properties**
- ❖ Key-value pairs
 - Key is a string
 - Value is an atomic value of any primitive data type, or an array of atomic values of one primitive data type
V₀ ou [V₀, V₁, V₂]
- ❖ Primitive **data types**
 - **boolean** – boolean values **true** and **false**
 - **byte, short, int, long** – integers (1B, 2B, 4B, 8B)
 - **float, double** – floating-point numbers (4B, 8B)
 - **char** – one Unicode character
 - **String** – sequence of Unicode characters



43

43

Cypher

- ❖ Declarative graph query language
 - Allows for expressive and efficient querying and updates
 - Inspired by SQL (query clauses) and SPARQL (pattern matching)
- ❖ Clauses
 - E.g. MATCH, RETURN, CREATE, ...
 - Clauses are (almost arbitrarily) chained together
 - Intermediate result of one clause is passed to a subsequent one



44

44

Cypher – Nodes

- ❖ Cypher uses a pair of parentheses to represent Nodes
 - Like a circle or a rectangle with rounded corners.

○

- Represents an anonymous, uncharacterized node.

`(matrix)`

- If we want to refer to the node elsewhere, we can add an variable

`(:Movie)`

- The Movie **label** declares the node's type or role

`(matrix:Movie)`

label podia usar where!

`(matrix:Movie {title: "The Matrix"})`

`(matrix:Movie {title: "The Matrix", released: 1999})`

- The node's **properties** (title, released, et cetera) are represented as a list of key/value pairs, enclosed within a pair of braces

`(matrix:Movie:Promoted)`

Uma só pode ter múltiplos labels! //



| 45

45

Cypher – Relationships

- ❖ Cypher uses a pair of square brackets and arrows to represent relationships

`[RELATION]`

`-, >, <-`

direção obliqua!

- ❖ Relationships are arrows pointing from one node to another

`(node1)-[:REL_TYPE]->(node2)`

- General relation, from node1 to node2

`(actor:Person)-[:ACTED_IN]->(movie:Movie)`

- matches all nodes Person that had a relationship type ACTED_IN with other nodes Movie.



| 46

46

Creating Nodes

❖ CREATE

```
CREATE (node:label { key1: value, key2: value, ... })
```

```
CREATE (Aveiro)
```

```
CREATE (Porto),(Coimbra),(Espinho)
```

```
CREATE (ric:person:player)  
z labels  
CREATE (leo:person:player)
```

```
CREATE (aveiro:cidade{name:"Aveiro"})
```

```
CREATE (ricg:player{name: "Ricardo Gomes",  
YOB: 1985, POB: "Porto"})
```



47

47

Creating Relationships

Representação Visual

```
CREATE (RuiPatrício:player {name: "Rui Patrício", YOB: 1988, POB:  
"Leiria"})
```

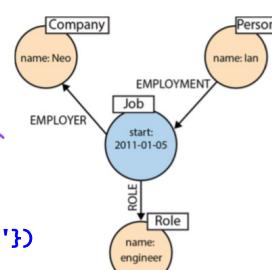
```
CREATE (PT:Country {name: "Portugal"})
```

```
CREATE (RuiPatrício)-[:Guarda_Redes]->(PT)
```

```
CREATE (RuiPatrício)-[:JogadorDeFutebol]->(PT)
```

Opção de Ler

```
CREATE (:Person {name:'Ian'})  
-[:EMPLOYMENT]->  
(:employment:Job {start_date:'2011-01-05'})  
-[:EMPLOYER]->  
(:Company {name:'Neo'}),  
(employment) -[:ROLE]-> (:Role {name:'engineer'})
```



48

48

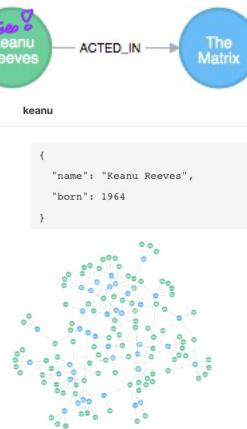
Cypher – Patterns

- Combining the syntax for nodes and relationships, we can express patterns.

```
MATCH (matrix:Movie {title:"The Matrix"} )
  <-[role:ACTED_IN {roles:["Neo"]}]-
    (keanu:Person {name:"Keanu Reeves"})
RETURN matrix, role, keanu
```

matrix	role	keanu
<pre>{ "title": "The Matrix", "tagline": "Welcome to the Real World", "released": 1999 }</pre>	<pre>{ "roles": ["Neo"] }</pre>	<pre>{ "name": "Keanu Reeves", "born": 1964 }</pre>

```
MATCH (cast)= (:Person)-[:ACTED_IN]->(:Movie)
RETURN cast
```



49

49

Cypher – Selection

❖ MATCH

```
MATCH (node1)-[rel:TYPE]->(node2)
RETURN rel.property
• Generic format, from node1 to node2.
```

```
MATCH (n) RETURN n
• all nodes
```

```
MATCH (me:Person) WHERE me.name="My Name" RETURN me.name
MATCH (me:Person){name:"My Name"}) RETURN me.name
```

UPDATE →

```
MATCH (movie:Movie)
WHERE movie.title = "Mystic River"
SET movie.released = 2003
RETURN movie.title AS title, movie.released AS released
```



title	released
Mystic River	2003

50

50

Cypher – Filtering

❖ WHERE

```

MATCH (tom:Person)-[:ACTED_IN]->()-[:ACTED_IN]-(actor:Person)
WHERE tom.name="Tom Hanks" AND actor.born < tom.born
RETURN DISTINCT actor.name AS Name
    • ?? Atores que fizeram
        atuado num filme com Tom Hanks mesmo nô que...
MATCH (gene:Person)-[:ACTED_IN]->()-[:ACTED_IN]-(other:Person)
WHERE gene.name="Gene Hackman" AND exists( (other)-[:DIRECTED]->() )
    que fez direção de outro filme
RETURN DISTINCT other
    • ???
MATCH (gene:Person {name:"Gene Hackman"})-[:ACTED_IN]->(movie:Movie),
    (other:Person)-[:ACTED_IN]->(movie),
    (robin:Person {name:"Robin Williams"})
WHERE NOT exists( (robin)-[:ACTED_IN]->(movie) )
RETURN DISTINCT other
    • ???

```



51

51

Cypher – Ordering

❖ ORDER BY, LIMIT, SKIP, DISTINCT

❖ Return the five oldest people in the database

```

MATCH (person:Person)
RETURN person
ORDER BY person.born crecente!
LIMIT 5;
1902  

1901  

1900

```

❖ List all actors, ordered by age

```

MATCH (actor:Person)-[:ACTED_IN]->()
RETURN DISTINCT actor
ORDER BY actor.born
Pora  

nô  

temos  

2 vezes o M

```



52

52

Variable Length Paths

MATCH (node1)-[*]-(node2)

- ❖ Relationships that traverse any depth are:
 $(a)-[*]-(b)$
- ❖ Specific depth of relationships
 $(a)-[*\text{depth}]-(b)$
- ❖ Relationships from one to four levels deep
 $(a)-[*1..4]-(b)$
- ❖ Relationships of type KNOWS at 3 levels distance:
 $(a)-[:KNOWS*3]-(b)$
- ❖ Relationships of type KNOWS or LIKES from 2 levels distance:
 $(a)-[:KNOWS|:LIKES*2..]-(b)$
 - ↑ 2 ou mais!
 - e.g.: amigos de 2º grau



53

53

Indexes

- ❖ Neo4j use indexes to speed up the finding of starting points by value, textual prefix or range
- ❖ To search efficiently people by name:
 $\rightarrow \text{CREATE INDEX ON :Person(name);}$
- ❖ Now, the lookup of "Gene Hackman" will be faster

```
MATCH (gene:Person)-[:ACTED_IN]->(movie),
      (other:Person)-[:ACTED_IN]->(movie)
      WHERE gene.name="Gene Hackman"
      RETURN DISTINCT other;
```
- ❖ To remove the index:
 $\text{DROP INDEX ON :Person(name);}$



54

54

Aggregation

- ❖ Cypher provides support for a number of aggregate functions

- **count(x)** Count the number of occurrences
- **min(x)** Get the lowest value
- **max(x)** Get the highest value
- **avg(x)** Get the average of a numeric value
- **sum(x)** Sum up values

Coleção em lista → **collect(x)** Collect all the values into an collection

↳ Filme [A₀, A₁, A₂, ...]

```
MATCH (person:Person)-[:ACTED_IN]->(movie:Movie)
RETURN person.name, count(movie)
ORDER BY count(movie) DESC
LIMIT 10;
```

- Top ten actors who acted in more movies



55

55

Removing nodes/relationships

❖ DELETE

- Removes nodes, relationships or paths from the data graph
- Relationships must be removed before the nodes
 - Unless the DETACH modifier is specified

```
MATCH (p:Person {name:"Trump"})
DELETE p
• Remove node "Trump". Error if it has relations
```



```
MATCH (p:Person {name:"Trump"})
OPTIONAL MATCH (p)-[r]-o
DELETE p,r
• Remove node "p" with name= "Trump" and all nodes with any
relationship with "p".
```

quebra as ligações!

```
MATCH (n) DETACH DELETE n
• delete all nodes and relationships
```



56

56

Importing Data

❖ LOAD CSV

❖ Content of "movies.csv"

```
id,title,country,year
1,Wall Street,USA,1987
2,The American President,USA,1995
3,The Shawshank Redemption,USA,1994
```

❖ In Cypher:

```
LOAD CSV WITH HEADERS
FROM "http://neo4j.com/docs/stable/csv/intro/movies.csv"
AS line
CREATE (movie:Movie
{ id:line.id, title:line.title, released:Int(line.year) });
```



57

57

Other Write Clauses

❖ SET clause

- allows to...
 - set a value for a property, or remove a property when NULL is assigned
 - replace all the current properties with new ones
 - add new properties to the existing ones
 - add labels to nodes
- Cannot be used to set relationship types

❖ REMOVE clause

- Allows to...
 - remove a particular property
 - remove labels from nodes
- Cannot be used to remove relationship types



58

58

Summary

- ❖ Graph theory
 - brief concepts
- ❖ Graph-oriented databases
 - Property graphs
- ❖ Neo4j graph database
- ❖ Cypher (graph query language)
 - Read (sub-)clauses: MATCH, WHERE, ...
 - Write (sub-)clauses: CREATE, DELETE, SET, REMOVE, ...
 - General (sub-)clauses: RETURN, WITH, ORDER BY, LIMIT, ...



59

59

Resources

- ❖ Pramod J Sadalage and Martin Fowler,
NoSQL Distilled. Addison-Wesley, 2012
- ❖ Ian Robinson, Jim Webber and Emil Eifrem,
Graph Databases, O'Reilly's, 2013
 - <https://neo4j.com/graph-databases-book/>
- ❖ Neo4j
 - <https://neo4j.com/developer/>
- ❖ Martin Sloboda, "B4M36DS2: Database Systems"
 - <http://www.ksi.mff.cuni.cz/~sloboda/courses/171-B4M36DS2/>



60

60

