Carculo I - Agrupamento 4

Exame Final - J- Parte

Resolução

1)
$$A = \{(x, y) \in \mathbb{R}^2 : 2x \le y \le -x^2 + 5x \}$$

(a)
$$\begin{cases} y = 2x \\ y = -x^2 + 5x \end{cases} \iff \begin{cases} 2x = -x^2 + 5x \\ & = 0 \end{cases}$$

$$\Leftrightarrow \begin{cases} x^2 - 3x = 0 \Leftrightarrow \begin{cases} x(x-3) = 0 \Leftrightarrow \begin{cases} x = 0 & \forall x - 3 = 0 \end{cases} \end{cases}$$

Os pontos de interseção pedidos são: (0,0) e (3,6)

(b) y = 2xA é a região sombreada. $y = -x^2 + 5x$

(c) Area de
$$A = \int_{0}^{3} -x^{2} + 5x - 2x \, dx = \int_{0}^{3} -x^{2} + 3x \, dx$$

$$= \left[-\frac{x^{3}}{3} + \frac{3x^{2}}{2} \right] \Big|_{0}^{3} = -9 + \frac{27}{2} = \frac{9}{2}$$

Calcul I -agr. 4 Resolução do exame final

$$\frac{2^{2} \text{ poste}}{2^{2} \text{ poste}} = \frac{18/e^{2/2021}}{2^{2}}$$
1. (a) $\int_{-1}^{1} \left(\frac{1}{\sqrt{2-2n^{2}}}\right)^{2} = \frac{1}{\sqrt{2-2n^{2}}} \left(\frac{1}{\sqrt{2-2n^{2}}}\right)^{2} = \frac{1}{\sqrt{2-2n^{2}}} \left(\frac{1}{\sqrt{2-2n^{2}}}\right)^{2}$

$$\left(\frac{1}{\sqrt{2-2n^{2}}}\right)^{2} = \frac{1}{\sqrt{2-2n^{2}}} \left(\frac{1}{\sqrt{2-2n^{2}}}\right)^{2} = \frac{1}{\sqrt{2-2n^{2}}} = \frac{1}{\sqrt{2-2n^{2}}}$$

2.(a)
$$\frac{2n^2+7n+4}{\pi(n^2+2n+2)} = \frac{A}{n} + \frac{Bn+C}{n^2+2n+2}$$

$$\frac{2n^2 + 7n + 4}{n(n^2 + 2n + 2)} = \frac{A(n^2 + 2n + 2) + n(Bn + C)}{n(n^2 + 2n + 2)}$$

$$2\pi^{2} + 7\pi + 4 = A\pi^{2} + 2A\pi + 2A + B\pi^{2} + C\pi$$

$$\begin{cases}
 2 = A + B \\
 7 = 2A + C \\
 4 = 2A
 \end{cases}
 \begin{cases}
 2 = 2 + B \\
 7 = 4 + C \\
 4 = 2A
 \end{cases}
 \begin{cases}
 2 = 2 + B \\
 7 = 4 + C \\
 4 = 2
 \end{cases}
 \Rightarrow \frac{2\pi^{2} + 7\pi + 4}{\pi(\pi^{2} + 2\pi + 2)} = \frac{2}{\pi} + \frac{3}{\pi^{2} + 2\pi + 2}
 \end{cases}$$

$$\int \frac{2\pi^2 + 7x + 4}{x(x^2 + 2x + 2)} dx = \int \frac{2}{\pi} + \frac{3}{x^2 + 2x + 2} dx = 2\ln|x| + 3\int \frac{1}{(x+1)^2 + 1} dx$$

(b)
$$x = \frac{1}{3} t g t$$
, $t \in J - \frac{\pi}{2}$, $\frac{\pi}{2} [= > \frac{dn}{dt} = \frac{1}{3} \frac{1}{\cos^2 t}$, $t = \operatorname{arctg}(3n)$

$$\int \frac{1}{(9\pi^2+1)^{3/2}} d\pi = \int \frac{1}{(tg^2+1)^{3/2}} \frac{1}{3} \frac{1}{\cos^2 t} dt = \frac{1}{3} \int \frac{1}{(\cos^2 t)^{3/2}} \frac{1}{\cos^2 t} dt$$

$$=\frac{1}{3}\operatorname{S[cost]}^{3}\frac{1}{\operatorname{cos}^{2}t}dt=\frac{1}{3}\operatorname{Scostdt} \quad C,A:\ t\in]-\overline{[1]},\overline{[1]}C,\log p$$

$$=\frac{1}{3}\sinh t + c = \frac{1}{3}\sinh(\operatorname{arctg}(3x)) + c \left| \frac{1}{\cosh(3x)} \right| = \cosh(3x)$$

$$= \pm \frac{1}{3} \sqrt{\frac{(3\pi)^2}{1 + (3\pi)^2}} + c$$

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$$=\frac{\chi}{\sqrt{1+9\chi^2}}+C, \quad C\in\mathbb{R}.$$

$$C,A: t\in]-\overline{1},\overline{1}[,logs]$$
 $|cost>0 =)|cost|=cost$

$$(A)$$
: $n = \frac{1}{3} \frac{\sin t}{\cos t}$, $t \in]-\frac{11}{2}$, $\frac{11}{2}$