

PPRL Bloom Filter attack exercise

| | Bloom Filter | Frequency |
|---|--------------|-----------|
| 1 | 110100 | 111 |
| 2 | 000101 | 78 |
| 3 | 111001 | 49 |
| 4 | 111000 | 43 |
| 5 | 000111 | 19 |

| Name | Frequency |
|--------|-----------|
| Daniel | 242 |
| Carlos | 184 |
| Danilo | 115 |
| David | 95 |
| Carla | 41 |

- Suppose that the filters were built using 2-grams.

| Name | 2-grams |
|--------|----------------------|
| Daniel | {da, an, ni, ie, el} |
| Carlos | {ca, ar, rl, lo, os} |
| Danilo | {da, an, ni, il, lo} |
| David | {da, av, vi, id} |
| Carla | {ca, ar, rl, la} |

- Now build the possible candidate set of 2-grams for each position of the filter.

| Position | Type | 2-gram set | Candidate 2-grams |
|----------|------|--|--|
| P_0 | + | {da, an, ni, ie, el, il, lo, av, vi, id} | {da, an, ni, ie, el, il, lo, av, vi, id} |
| | - | {ca, ar, rl, lo, os, la} | |
| P_1 | + | {da, an, ni, ie, el, il, lo, av, vi, id} | {da, an, ni, ie, el, il, lo, av, vi, id} |
| | - | {ca, ar, rl, lo, os, la} | |
| P_2 | + | {da, an, ni, il, lo, av, vi, id} | {il, lo, av, vi, id} |
| | - | {da, an, ni, ie, el, ca, ar, rl, lo, os, la} | |
| P_3 | + | {da, an, ni, ie, el, ca, ar, rl, lo, os, la} | {ie, el, ca, ar, rl, lo, os, la} |
| | - | {da, an, ni, il, lo, av, vi, id} | |
| P_4 | + | {ca, ar, rl, la} | {la} |
| | - | {da, an, ni, ie, el, ca, ar, rl, lo, os, il, lo, av, vi, id, la} | |
| P_5 | + | {ca, ar, rl, lo, os, da, an, ni, il, lo, la} | {ca, ar, rl, lo, os, il, lo, la} |
| | - | {da, an, ni, ie, el, av, vi, id} | |

3. Analyze Bloom Filters to try to re-identify the names encoded in each one.

| Filter | Positions to analyze (1) | Discarded matches (2) | Result (3) |
|--------|--------------------------|-----------------------|-----------------|
| 1 | 0, 1, 3 | Carlos -> 0 | {Daniel} |
| | | Danilo -> 3 | |
| | | David -> 3 | |
| | | Carla -> 0 | |
| 2 | 3, 5 | Daniel -> 5 | {Carlos, Carla} |
| | | Danilo -> 3 | |
| | | David -> 3 | |
| 3 | 0, 1, 2, 5 | Daniel -> 2 | {Danilo} |
| | | Carlos -> 0 | |
| | | David -> 5 | |
| | | Carla -> 0 | |
| 4 | 0, 1, 2 | Daniel -> 2 | {Danilo, David} |
| | | Carlos -> 0 | |
| | | Carla -> 0 | |
| 5 | 3, 5 | Daniel -> 0 | {Carla} |
| | | Danilo -> 3 | |
| | | David -> 3 | |
| | | Carlos -> 4 | |

- (1) -> We just analyze those positions that are set to 1 in the given filter
- (2) -> We discard those names whose q-grams are not in any of the activated positions. The position that caused the exclusion is indicated along with the name.
- (3) -> Those names that are not discarded are the candidate ones. In some cases, more than a name can be paired with a single filter. It could also happen that no candidates are found for a given filter.