# Caderno

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# 1 Geometry

#### 1.1 Point Struct

```
typedef long long type;
double EPS = 1e-12;
struct point {
    type x, y;
   point (type xp = 0.0, type yp = 0.0) {
       x = xp;
        y = yp;
   point(const fpoint &p) {
       x = p.x;
       y = p.y;
    point operator+ (const point &p) const {return point(x+p.x, y+p.y);}
    point operator - (const point &p) const {return point(x-p.x, y-p.y);}
    point operator* (type c) {return point(c*x, c*y);}
    point operator/ (type c) {return point(x/c, y/c);}
   bool operator < (const point &p) {return x < p.x \mid | x = p.x && y < p.y;}
};
```

```
type dot(point p, point q) {return p.x*q.x+p.y*q.y;}
type dist(point p, point q) {return sqrt(dot(p-q,p-q));}
type cross(point p, point q) {return p.x*q.y-p.y*q.x;}
point projectInLine(point c, point a, point b) {
    return a + (b-a)*dot(c-a, b-a)/dot(b-a, b-a);
point projectInSegment(point c, point a, point b) {
    point lineP = projectInLine(c, a, b);
    type maxDist = max(dist(a, lineP), dist(b, lineP));
    if (maxDist > dist(a, b)) {
        if (dist(a, c) > dist(b, c)) return b;
        else return a;
    else return lineP;
}
1.2
     Convex Hull
double side (point a, point b, point c) {
    return cross(a, b) + cross(b, c) + cross(c, a);
}
vector<point> convex_hull(vector<point> p) {
    int n = p.size(), k = 0;
    if (n == 1) return p;
    vector < point > hull(2*n);
    sort(p.begin(), p.end());
    for (int i=0; i < n; i++) {
        while (k \ge 2 \&\& (side(hull[k-2], hull[k-1], p[i]) \le 0)) k--;
        hull[k++] = p[i];
    }
    for (int i=n-2, t=k+1; i>=0; i--)
        while (k)=t \&\& (side(hull[k-2], hull[k-1], p[i]) <= 0)) k--;
        hull[k++] = p[i];
    }
    hull.resize(k-1);
    return hull;
}
```

## 2 Data Structures

#### 2.1 BIT

```
int b[N];
int update(int p, int val, int n) {
    for (; p < n; p += p \& -p) b[p] += val;
int getsum(int p) {
    int sum = 0;
    for (; p != 0; p -= p & -p) {
        sum += b[p];
    return sum;
}
2.2
     Recursive Segment Tree
int t [N < <1];
void build(int n) {
    for (int i = n-1; i > 0; i--) t[i] = min(t[i <<1], t[i <<1|1]);
}
void modify(int pos, int val, int n) {
    for (t [pos += n] = val; pos != 1; pos >>=1)
        t [pos >> 1] = min(t [pos], t [pos^1]);
int query(int 1, int r, int n) \{ // [1, r) \}
    int resp = 1000000007;
    for (1 += n, r += n; 1 < r; 1 >>= 1, r >>= 1)
        if (1\&1) \text{ resp} = \min(\text{resp}, t[1++]);
        if (r\&1) resp = min(resp, t[--r]);
    return resp;
}
2.3
    Lazy Segment Tree
int seg[4*N];
int lazy[4*N];
void do_lazy(int root, int ll, int rl) {
```

```
seg \left[ \hspace{1mm} \mathtt{root} \hspace{1mm} \right] \hspace{1mm} + \hspace{-1mm} = \hspace{1mm} \mathtt{lazy} \hspace{1mm} \left[ \hspace{1mm} \mathtt{root} \hspace{1mm} \right];
     if (11 != rl) {
          lazy[2*root+1] += lazy[root];
          lazy [2*root+2] += lazy [root];
     lazy[root] = 0;
}
int update(int root, int ll, int rl, int l, int r, int val) {
     do_lazy(root, ll, rl);
     if (r < 11 \mid | 1 > r1) return seg[root];
     if (ll >= l && rl <= r) {
          lazy[root] += val;
          do_lazy(root, ll, rl);
          return seg[root];
     int update_left = update(2*root+1, ll, (ll+rl)/2, l, r, val);
     int update_right = update(2*root+2, (1l+r1)/2+1, rl, l, r, val);
     return seg[root] = min(update_left, update_right);
}
int query(int root, int ll, int rl, int l, int r) {
     do_lazy(root, ll, rl);
      if \ (r < ll \ || \ l > rl) \ return \ inf; \\
     if (11 >= 1 \&\& rl <= r) return seg[root];
     int query_left = query (2*root+1, ll, (ll+rl)/2, l, r);
     int query_right = query (2*root+2, (1l+rl)/2+1, rl, l, r);
     return min(query_left , query_right);
}
```