
Redes de Computadores

The Data Link Layer

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-
- » *What are the main services and functions of the Data Link layer?*
 - » *What is a frame? How to frame data? Why is stuffing important?*
 - » *What is the relationship between Bit Error Ratio and Frame Error Ratio?*
 - » *How to detect errors in a frame?*
 - » *How does Cyclic Redundancy Check operate?*
 - » *What are the CRC error detection capabilities?*
 - » *What is the purpose of Automatic Repeat ReQuest (ARQ)?*
 - » *What are the common ARQ mechanisms?*
 - » *How does Stop & Wait ARQ work?*
 - » *How does Go Back N ARQ ARQ work?*
 - » *How does the Selective Reject ARQ work?*
 - » *Why are sequence numbers important in ARQ mechanisms?*
 - » *What is the efficiency of the ARQ mechanisms?*
 - » *What mechanisms are employed in Ethernet, PPP and WLAN?*
 - » *What are the differences between End-to-End ARQ and Link-by-Link ARQ?*
 - » *Where are the ARQ mechanisms used in the TCP/IP reference model ?*

Data Link layer functions and services



Data Link Layer – Functions and Services

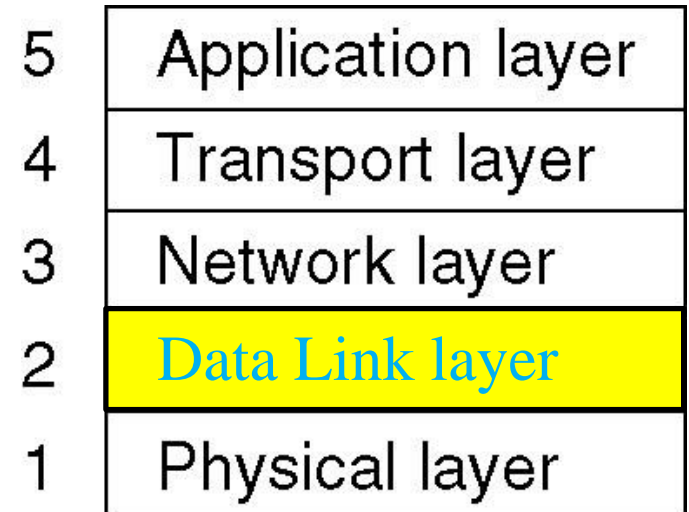
♦ Main functions

- » Provide service to the network layer
- » Eliminate/reduce transmission errors
- » Regulate data flow

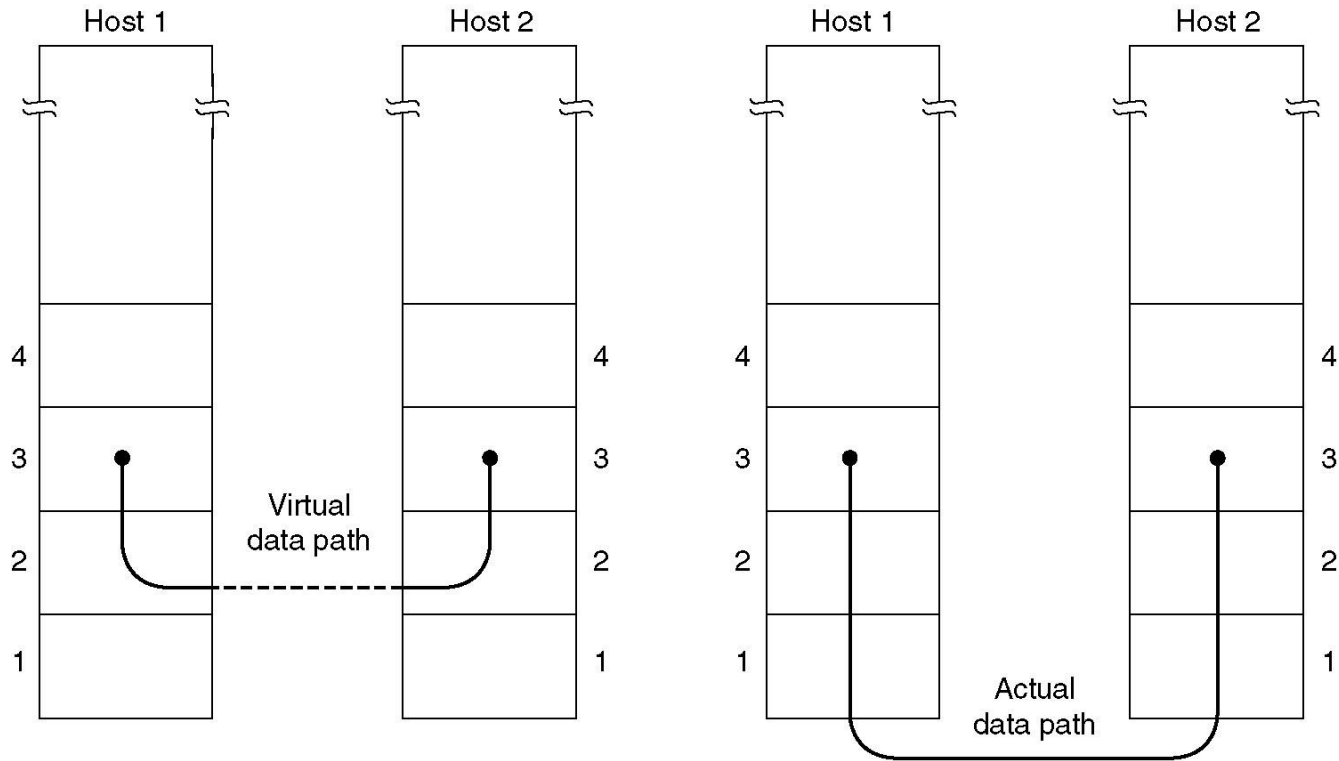
Slow receivers not swamped by fast senders

♦ Services provided

- » Unacknowledged connectionless service 
- » Acknowledged connectionless service 
- » Acknowledged connection-oriented service



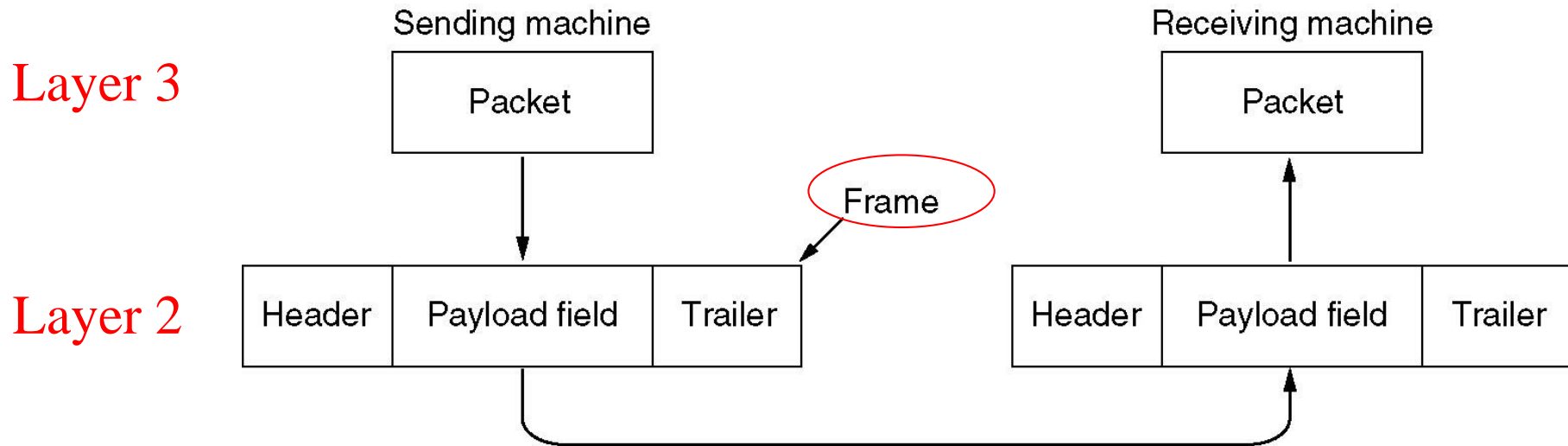
Services Provided to Network Layer



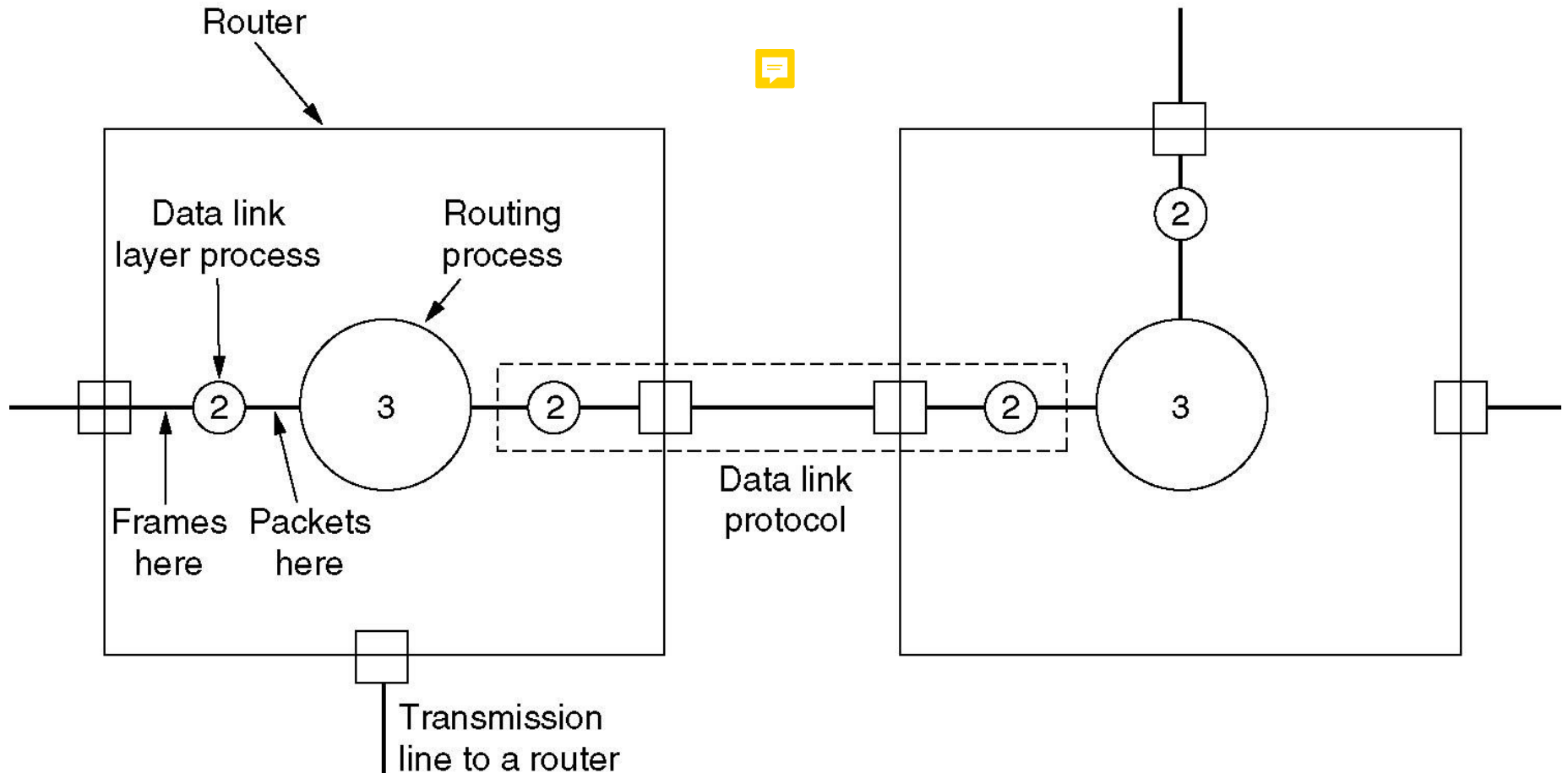
(a) Virtual communication

(b) Actual communication

Layer 3 Packets and Layer 2 Frames



Placement of the Data Link Protocol



Framing

To Think

[Sender] → ..1001101101101101101101110101.. → [Receiver]

Where is the data? Where does the frame start and stop?

How to split this bit stream into frames (sets of bits)?

Framing

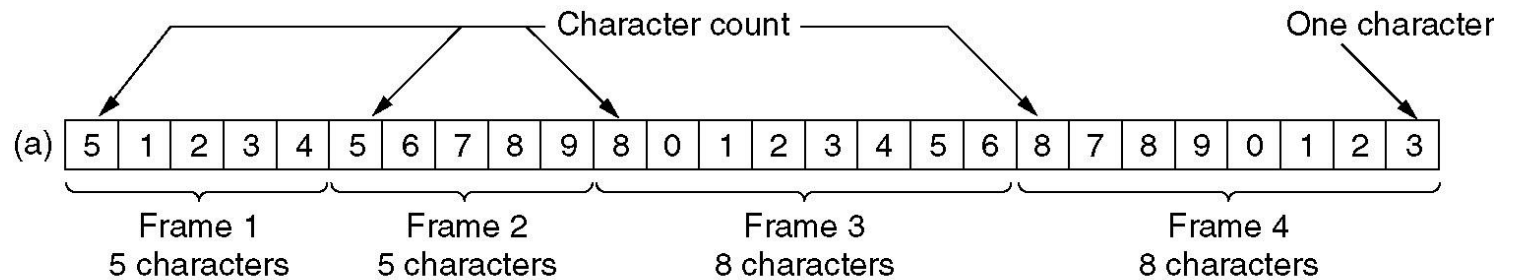
- ♦ [Sender] → ..1001101101101101101101101110101.. → [Receiver]
 - » Where is the data?
 - » Where does the frame start and stop?

- ♦ Three methods
 - » **Character count**
 - » **Flag bytes with byte stuffing**
 - » **Start and ending flags, with bit stuffing**

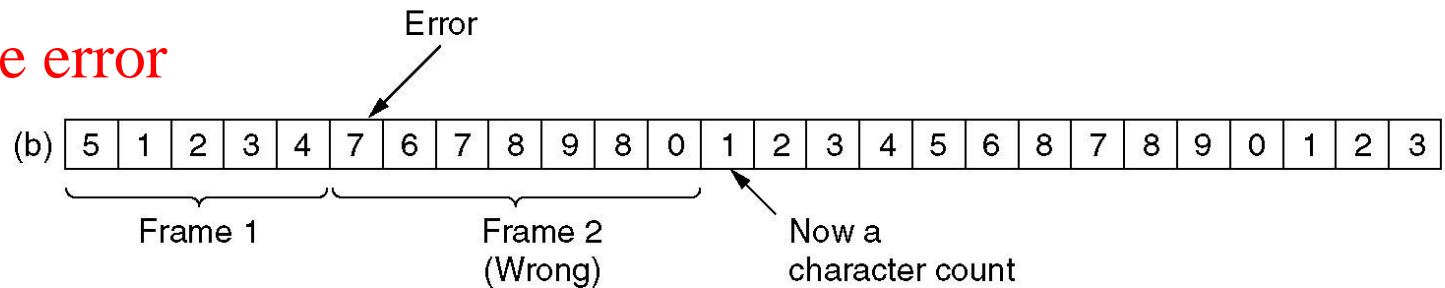
Framing – Character count

A stream of characters

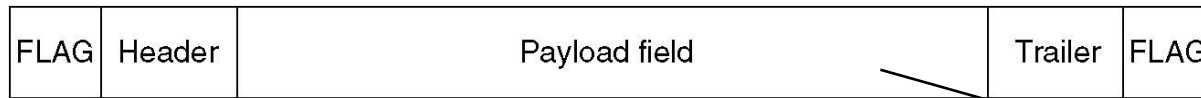
(a) **Without errors**



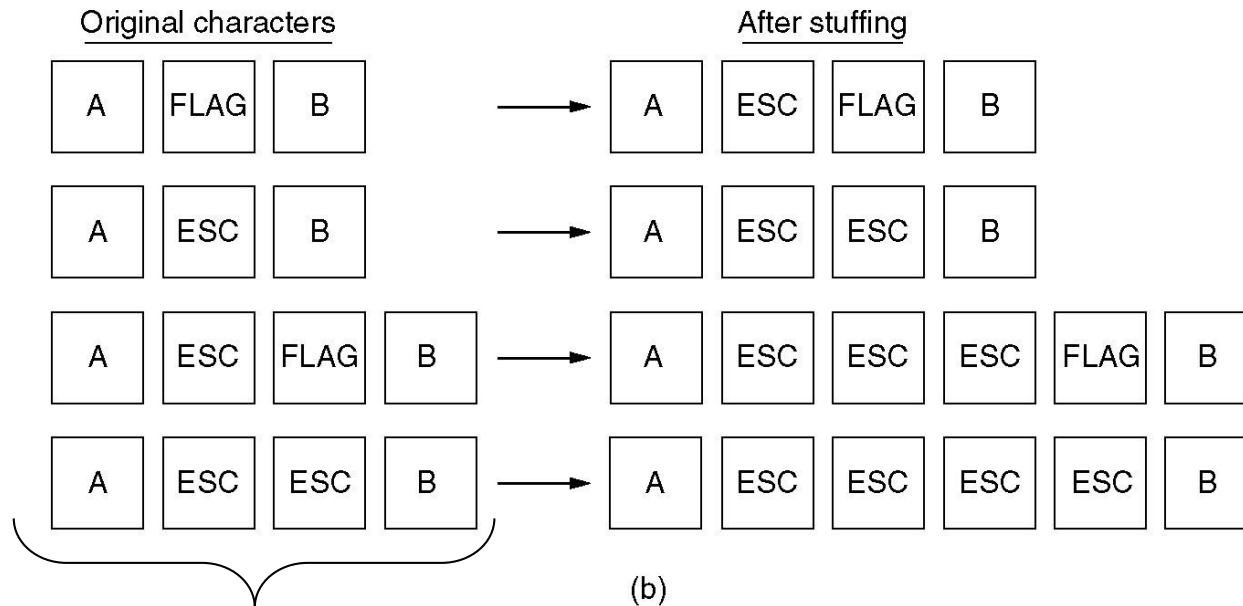
(b) **With one error**



Framing - Flag bytes with *byte stuffing*



(a)



(b)

Problem if frame
has internal
character equal to
FLAG!

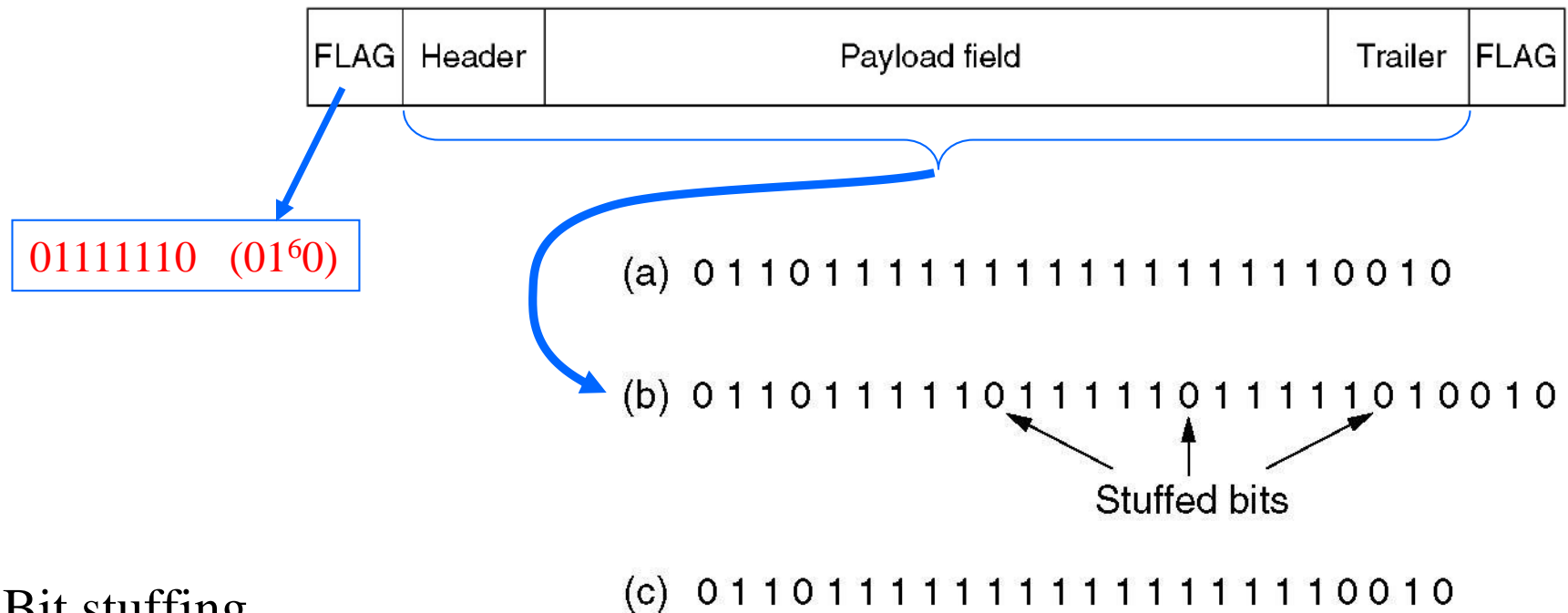
Problem solved
by stuffing
mechanism!

Data to be transported in the payload field

(a) A frame delimited by flag bytes

(b) Four examples of byte sequences before and after stuffing

*Framing - Start and ending flags, with **bit stuffing***



Bit stuffing

(a) The original data

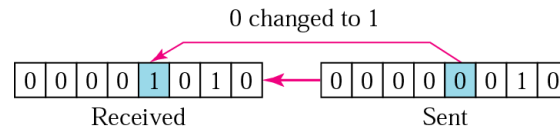
(b) The data as it appears on the line: $1^5 \rightarrow 1^5\underline{0}$

(c) The data as stored in receiver's memory **after destuffing**: $01^5\underline{0} \rightarrow 01^5$

Error detection

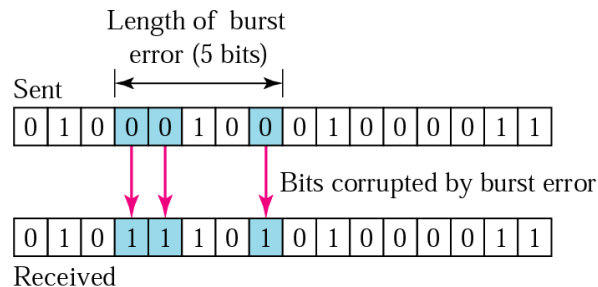
◆ Simple Error

- » Random and independent from previous error



◆ Errors in burst

- » Not independent; affect neighbour bits
- » Burst length defined by the first and last bits in error



To Think

◆ Assume

- p – bit error probability (or **Bit Error Ratio – BER**)
- n – frame length
- Independent errors
- FER: Frame Error Ratio



◆ Student A explains to Student B

why $P[\text{frame has no errors}] = (1 - p)^n$

◆ Student B explains to Student A

why $P[\text{frame has errors}] = 1 - (1 - p)^n \Leftrightarrow FER = 1 - (1 - BER)^n$

Counting Errors

◆ Assume


- p – bit error probability (or **Bit Error Ratio – BER**)
- n – frame length
- Independent errors

◆ $P[\text{frame has no errors}] = (1 - p)^n$

the n bits are good!

◆ $P[\text{frame has errors}] = 1 - (1 - p)^n$

$P[\text{frame has errors}] = \text{Frame Error Ratio (FER)}$


$$FER = 1 - (1 - BER)^n$$

$p = 10^{-7}$ (**good wired channel**)

$n = 10^4$ (~ Ethernet frame length)

$$FER = 1 - (1 - 10^{-7})^{10^4} \approx 10^{-3}$$

◆ $P[1 \text{ bit received in error}] = \binom{n}{1} p(1 - p)^{n-1}$

◆ $P[i \text{ bits received in error}] = \binom{n}{i} p^i (1 - p)^{n-i}$

$p = 10^{-3}$ (**wireless channel**) 

$n = 10^4$ (~ Ethernet frame length)

$$FER = 1 - (1 - 10^{-3})^{10^4} \approx 1$$

Error Techniques

- ◆ Error techniques required!
 - » Detection (and correction)
- ◆ Effectiveness of **error detection** technique (code) characterized by
 - » Minimum distance of code: **d**
 - min number of bit errors **undetected** in a block of n bits
 - if fewer than d errors occur, errors are detected
 - » Burst detecting ability: **B**
 - max burst length of errors **detected**

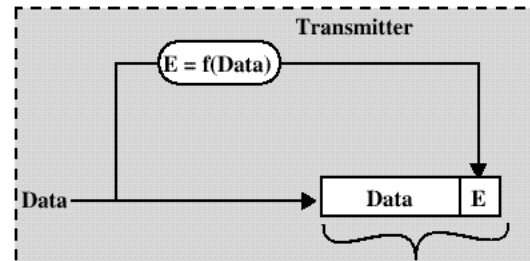
Error Detection Techniques

- ◆ Used by the receiver to determine if a packet contains errors
 - » If a packet is found to contain errors, the receiver may request the transmitter to re-send the packet

- ◆ Introducing redundancy →

» $k \rightarrow k+r$

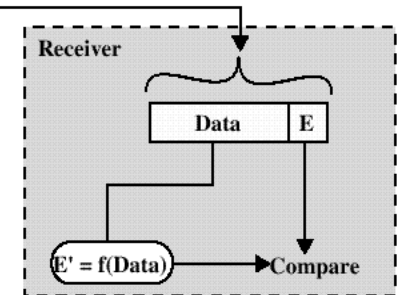
k: data bits; r: redundancy bits



E, E' = error detecting codes
 f = error detecting code function

- ◆ Error detection techniques

- » Parity check
- » Cyclic Redundancy Check (CRC)
- » ...



Simple Parity Check

- ♦ One parity bit added to every k information bits so that

- » The total number of bits 1 even → even parity

1110111	1101110	1010110	1101100	1100100
11101110	11011101	10101100	11011000	11001001

- » The total number of bit 1 is odd → odd parity

- ♦ Detection of

- » simple errors

- » any number of odd errors in a block of $k+1$ bits

- ♦ Undetected

- » Even number of errors in a block

$n=k+1$, block size

p : bit error probability

$$P(\text{undetected}) = \sum_{i \text{ even}} \binom{n}{i} p^i (1-p)^{n-i}$$

- ♦ Used in Character Oriented protocols

Bi-dimensional Parity

- ◆ Blocks represented in rows
 - » Parity bit per row; parity bit per column

1	0	0	1	0	1	0	1
0	1	1	1	0	1	0	0
1	1	1	0	0	0	1	0
1	0	0	0	1	1	1	0
0	0	1	1	0	0	1	1
<hr/>							0
1	0	1	1	1	1	1	0

Vertical checks

1	0	0	1	0	1	0	1
0	1	1	1	0	1	0	0
1	1	1	0	0	0	1	0
1	0	0	0	1	1	1	0
0	0	1	1	0	0	1	1
<hr/>							0
1	0	1	1	1	1	1	0

Horizontal checks

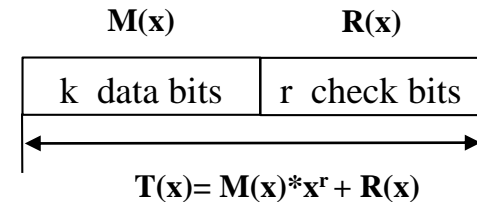
- ◆ Minimum code distance $d=4$
 - Any four errors in a rectangular configuration becomes undetectable

Cyclic Redundancy Check (CRC)

- ♦ Bit string represented as a polynomial
 - » $110011 \rightarrow x^5 + x^4 + x + 1$
- ♦ Module 2 operations
 - » Additions and subtractions identical to **exclusive OR**
 - » **no carry, no borrow**
- ♦ $M(x)$; $R(x)$; $T(x) = M(x) * x^r + R(x)$
- ♦ How to compute the check bits: $R(x)$?
 - » Choose a generator string $G(x)$ of length $r+1$ bits
 - » Choose $R(x)$ such that **$T(x)$ is a multiple of $G(x)$** : $T(x) = A * G(x)$
- ♦ $T(x) = M(x)x^r + R(x) = A * G(x) \iff$

$$M(x)x^r = A * G(x) + R(x) \quad (\text{mod } 2 \text{ arithmetic})$$

$$\Rightarrow R(x) = \text{remainder of } M(x)x^r / G(x)$$
- ♦ Choice of $G(x)$ is very important! (**$G(x) = x^r + \dots + 1$**)



CRC - Generating $R(x)$

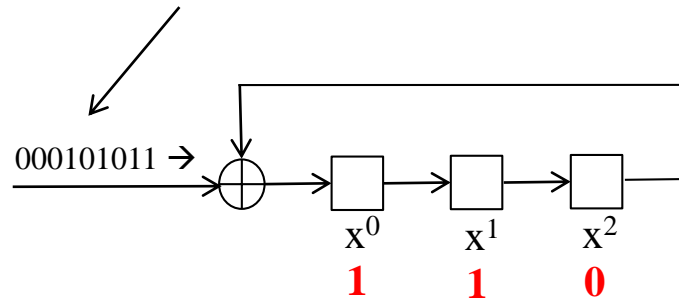
- ♦ $r=3, x^r=x^3$; $G(x)=x^3+1$ (1001)
- ♦ $M(x)=x^5+x^4+x^2+1$ (110101)
- ♦ $M(x) * x^3 = x^8+x^7+x^5+x^3$ (110101000)
- ♦ $R(x)$ = remainder of $M(x)x^r / G(x)$
- ♦ $R(x)=x+1$ (011)
- ♦ Sent word
 » $T(x)=M(x) * x^r + R(x) = x^8+x^7+x^5+x^3+x+1 = 110101011$

$M(x) * x^3$								$G(x)$			
1	1	0	1	0	1	0	0	1	0	0	1
1	0	0	1	↓	↓	↓	↓	1	1	0	0
0	1	0	0	0	↓	↓	↓				
	1	0	0	1	↓	↓	↓				
	0	0	0	1	1	↓	↓				
		0	0	0	0	↓	↓				
		0	0	1	1	0	↓				
			0	0	0	0	↓				
			0	1	1	0	0	↓			
				1	0	0	1	↓			
				0	1	0	1	0			
					1	0	0	1			
					0	0	1	1			

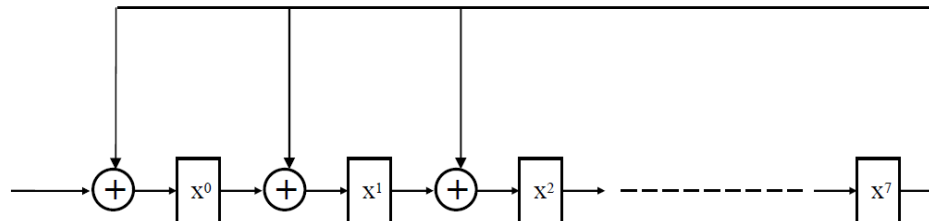
R(x)

CRC - Generating $R(x)$ with a Shift Register

- ♦ $R(x)$ easily generated in hardware
- ♦ $G(x)=x^3+1$
 - » $M(x) * x^3 = x^8 + x^7 + x^5 + x^3$ (110101000)
 - » $R(x)=x+1$ (011)



- ♦ $G(x)=x^8+x^2+x+1$



CRC – Checking at the Receiver

- ◆ Let $T'(x)$ be the received word
 - » $T'(x) = x^8 + x^7 + x^5 + x^3 + x + 1$ (110101 011)
- ◆ Divide $T'(x)$ by $G(x)$
 - » If remainder $R(x) = 0 \rightarrow$ no errors
 - » If remainder $R(x) \neq 0 \rightarrow$ errors have occurred

$T'(x)$										$G(x)$				
1	1	0	1	0	1	0	1	1		1	0	0	1	
1	0	0	1							1	1	0	0	1
0	1	0	0	0										
	1	0	0	1										
	0	0	0	1	1									
		0	0	0	0									
		0	0	1	1	0								
			0	0	0	0								
			0	1	1	0	1							
				1	0	0	1							
				0	1	0	0	1						
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CRC - Performance

- ◆ For r check bits per frame the following can be detected
 - » All patterns of 1, 2, or 3 errors ($d > 3$)
 - » All bursts of errors of r or fewer bits
 - » All errors consisting of an odd number of inverted bits

- ◆ Common polynomials
 - » ITU-16: $r=16$, $G(x) = x^{16} + x^{12} + x^5 + 1$ (1000100000100001)
 - » ITU-32: $r=32$,
 $G(x) = x^{32} + x^{26} + x^{23} + x^{22} + x^{16} + x^{12} + x^{11} + x^{10} + x^8 + x^7 + x^5 + x^4 + x^2 + x + 1$

Automatic Repeat reQuest (ARQ)

Automatic Repeat ReQuest (ARQ)

- ♦ When the receiver detects errors in a frame
how to ask the sender to retransmit the frame?
- ♦ ARQ mechanisms
Mechanisms that automatically request the retransmission of
 - missing packets
 - packets with errors
- ♦ Three common ARQ schemes
 - » **Stop and Wait**
 - » **Go Back N**
 - » **Selective Repeat**

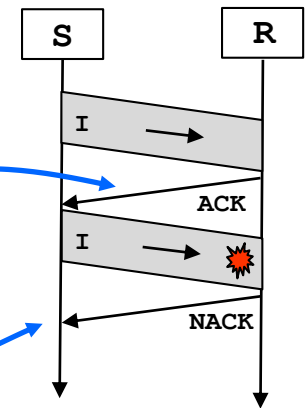
Stop and Wait ARQ

◆ Sender

- » transmits Information frame **I**
- waits for positive confirmation **ACK** from receiver

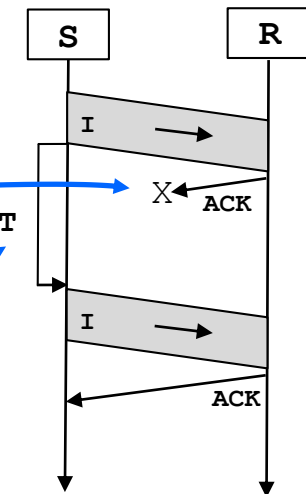
◆ Receiver: receives **I** frame

- » If **I** frame has no error → confirms with **ACK**
- » If **I** frame has error → sends **NACK**



◆ Sender

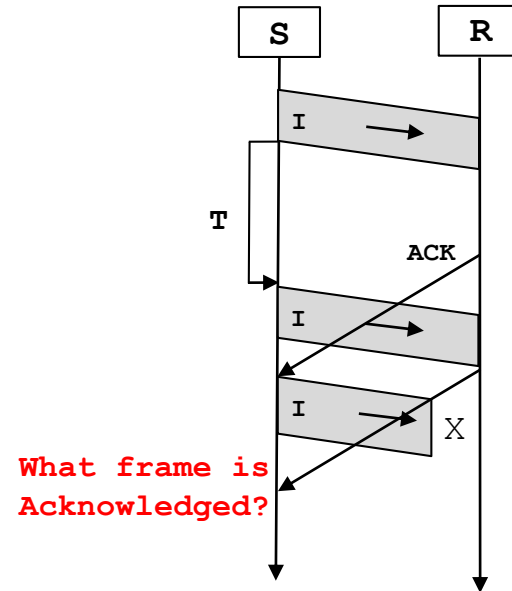
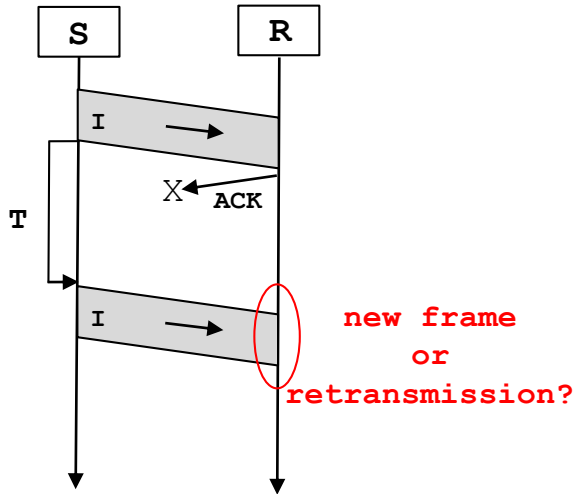
- » Receives **ACK** → proceeds and transmits **new** frame
- » Receives **NACK** → **retransmits** frame **I**



◆ Problem

- » What happens if **I**, **ACK** or **NACK** is lost?
- Timeout required!

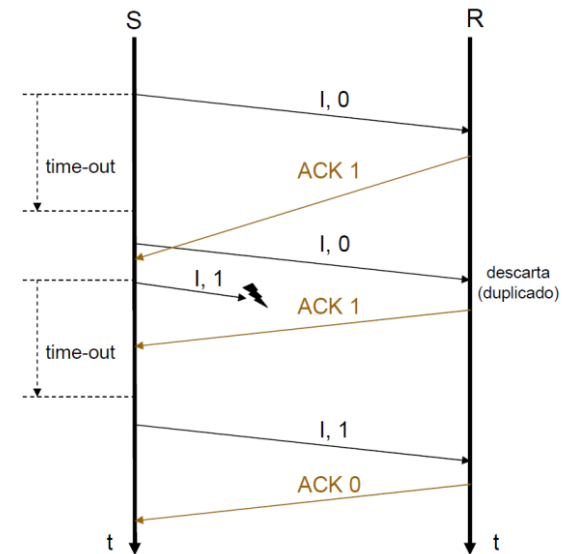
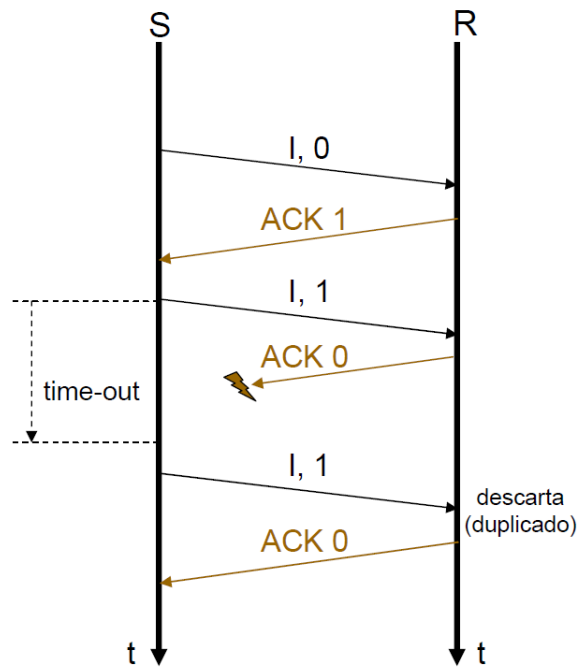
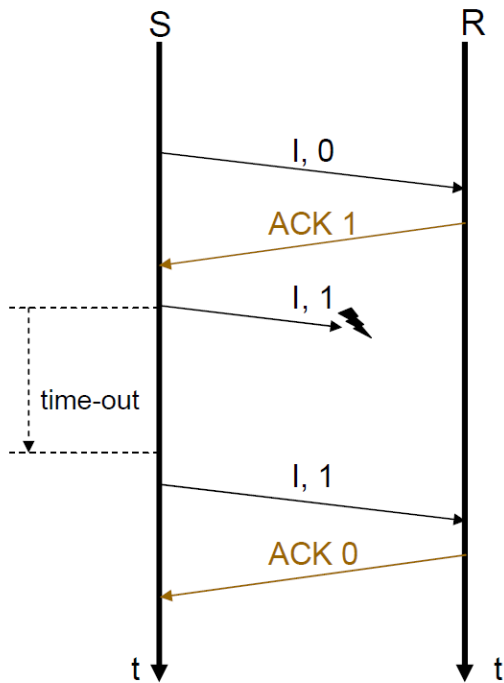
Stop and Wait ARQ – Sequence Numbers Required



◆ Solution

- » **I** frames numbered: **I(0)**, **I(1)**
- » **ACK** frames numbered: **ACK(0)**, **ACK(1)**
- » **ACK(i)** indicates that receiver is waiting for frame **I(i)**
- » No **NACK** required
- » Module 2 numbers

Stop and Wait ARQ – Examples



Stop and Wait – Efficiency Example



» WAN ATM

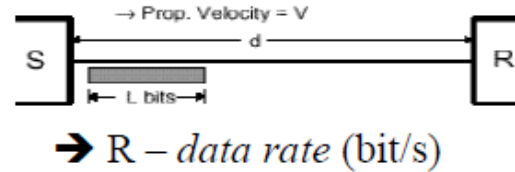
- $d = 1000 \text{ km}$
- $L = 424 \text{ bit}$, $R = 155.52 \text{ Mbit/s}$
- $T_t = 2.7 \mu\text{s}$
- Fibra óptica $\rightarrow 5 \mu\text{s/km} \rightarrow \tau = 5 \text{ ms}$
- $a = 1852$
- $S = 1 / 3705 = 0.0003$

» LAN

- $d = 0.1 \sim 10 \text{ km}$
- $L = 1000 \text{ bit}$, $R = 10 \text{ Mbit/s}$
- $T_t = 100 \mu\text{s}$
- Cabo coaxial $\rightarrow 4 \mu\text{s/km} \rightarrow \tau = 0.4 \sim 40 \mu\text{s}$
- $a = 0.004 \sim 0.4$
- $S = 0.55 \sim 0.99$ (e se $R = 100 \text{ Mbit/s?}$)

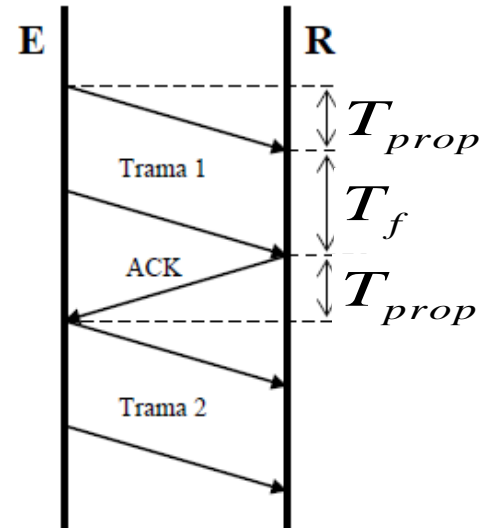
» Modem sobre linha telefónica

- $d = 1000 \text{ m}$
- $L = 1000 \text{ bit}$, $R = 28.8 \text{ kbit/s}$
- $T_t = 34.7 \text{ ms}$
- UTP $\rightarrow 5 \mu\text{s/km} \rightarrow \tau = 5 \mu\text{s}$
- $a = 1.44 \cdot 10^{-4}$
- $S \simeq 1.0$



$$T_f = \frac{L}{R} = T_t$$

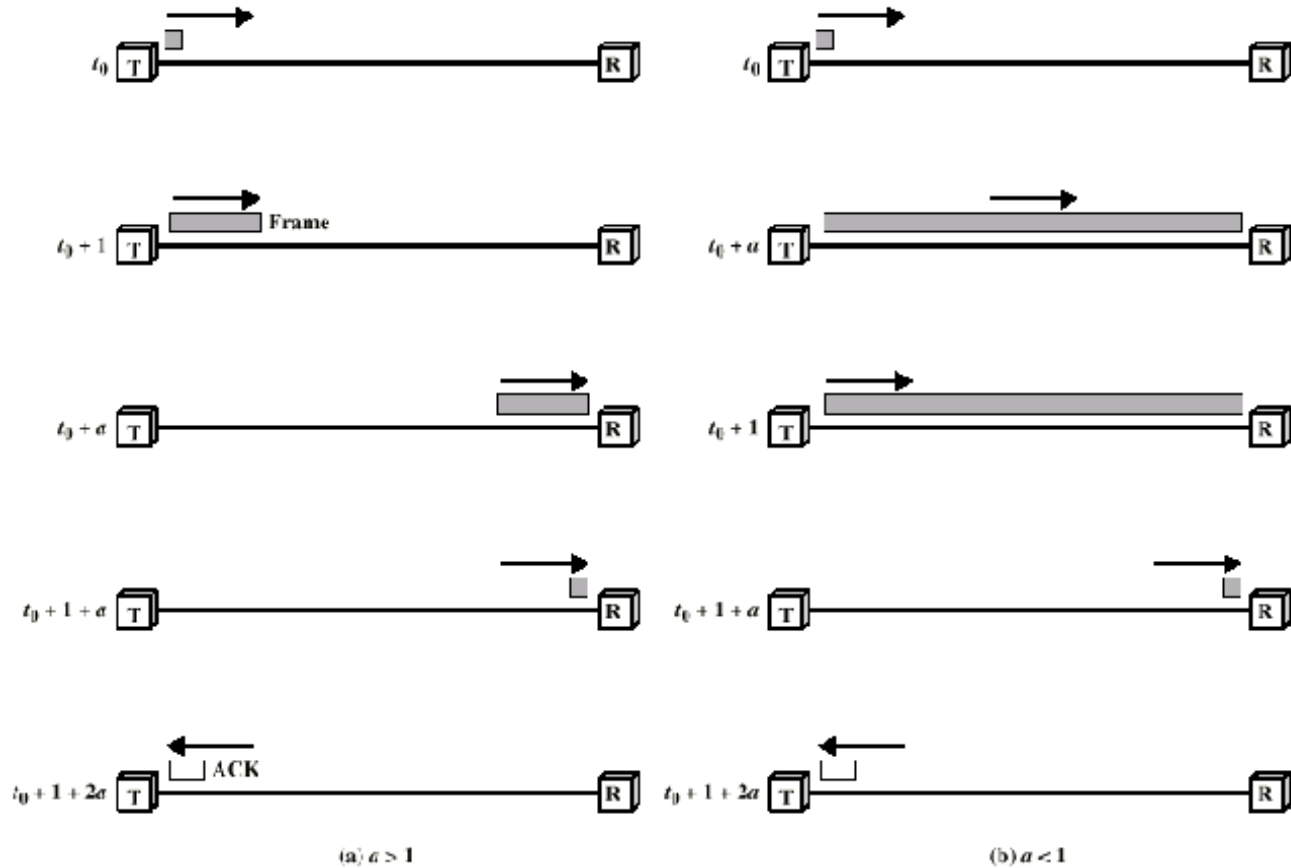
$$T_{prop} = \frac{d}{V} = \tau$$



$$a = \frac{T_{prop}}{T_f}$$

$$S = \frac{T_f}{T_{prop} + T_f + T_{prop}} = \frac{1}{1 + 2a}$$

Stop and Wait - Efficiency



Stop-and-Wait Link Utilization (transmission time = 1; propagation time = a)

Stop and Wait ARQ – Efficiency with Errors

- » p_e – frame error probability
- » $P[A=k]$
 - Probability of **k Attempts** required to transmit a frame with success

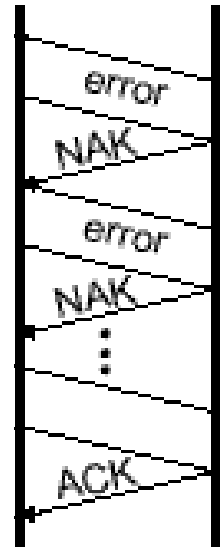
$$P[A = k] = p_e^{k-1} (1 - p_e)$$

- » $E[A]$
 - expected number of Attempts to transmit a frame with success

$$E[A] = \sum_{k=1}^{+\infty} k * P[A = k] = \frac{1}{1 - p_e}$$

- » Efficiency

$$S = \frac{T_f}{E[A](T_f + 2T_{prop})} = \frac{1}{E[A](1 + 2a)} = \frac{1 - p_e}{1 + 2a}$$



To Think

- ◆ Assume Sender and Receiver are separated by a large distance?
How to improve the Efficiency of the Stop & Wait ARQ?

Go Back N ARQ (Sliding Window)

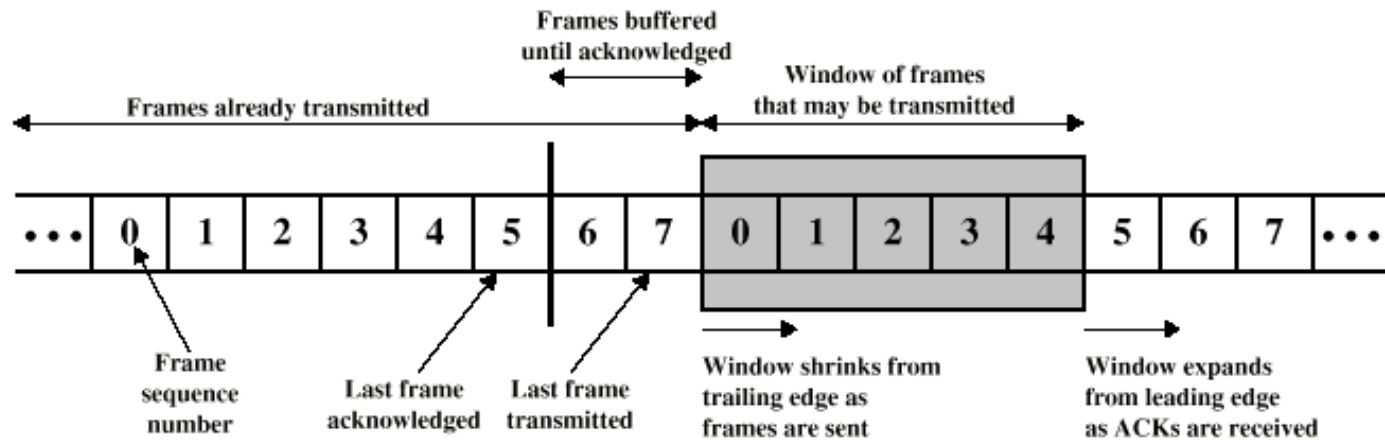
♦ Stop and Wait

- » inefficient when $T_{\text{prop}} > T_f$ ($a > 1$)
- » sends only one frame per Round-Trip Time ($\text{RTT} = 2 * T_{\text{prop}} + T_f$)

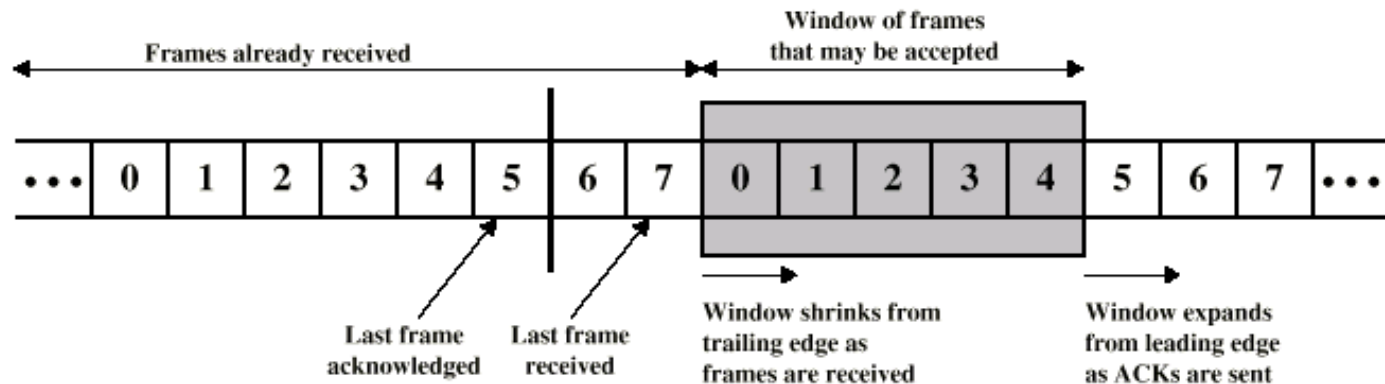
♦ Go Back N

- » allows transmission of new packets before earlier ones are acknowledged
- » uses a **Sliding Window** mechanism
 - sender can send packets that are within a “window” (range) of packets
 - window advances as acknowledgements for earlier packets are received

Sliding Window - Model

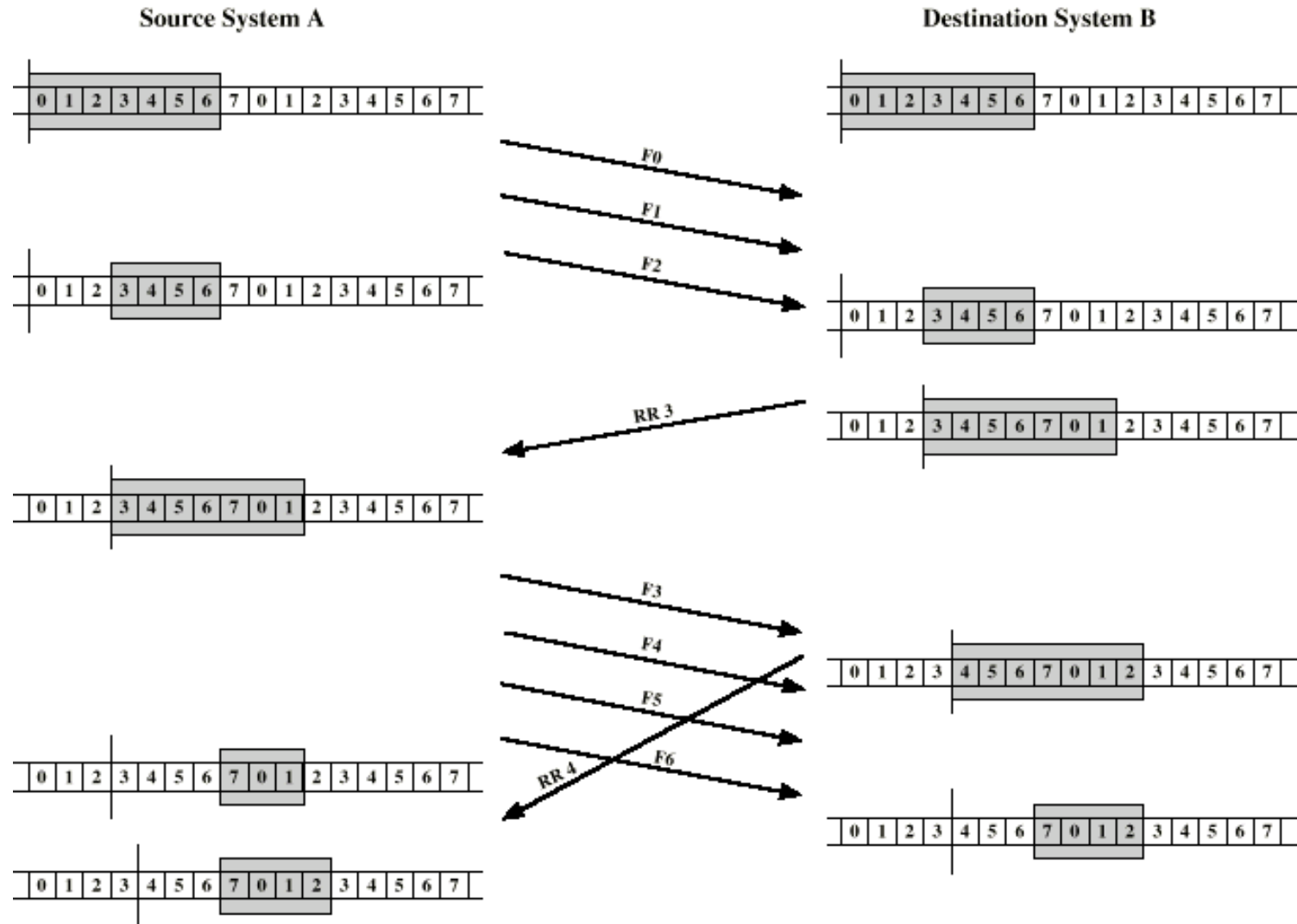


(a) Sender's perspective



(b) Receiver's perspective

Sliding Window - Example



Go Back N ARQ – Basic Behaviour

◆ Sender

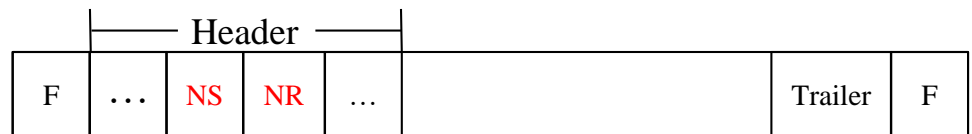
- » may transmit up to **W** frames without receiving RR
RR - Receiver Ready = ACK
- » I frames are numbered sequentially I(NS): I(0), I(1), I(2), ...
- » Cannot send I(NS=i+W) until it has received the RR(NR=i)

◆ Receiver

- » does not accept frames out of sequence
- » sends RR(NR) to sender indicating
 - that **all the packets up to NR-1 have been received in sequence**
 - the sequence number, NR, of the next expected frame

Go Back N ARQ – Maximum Window, Extensions

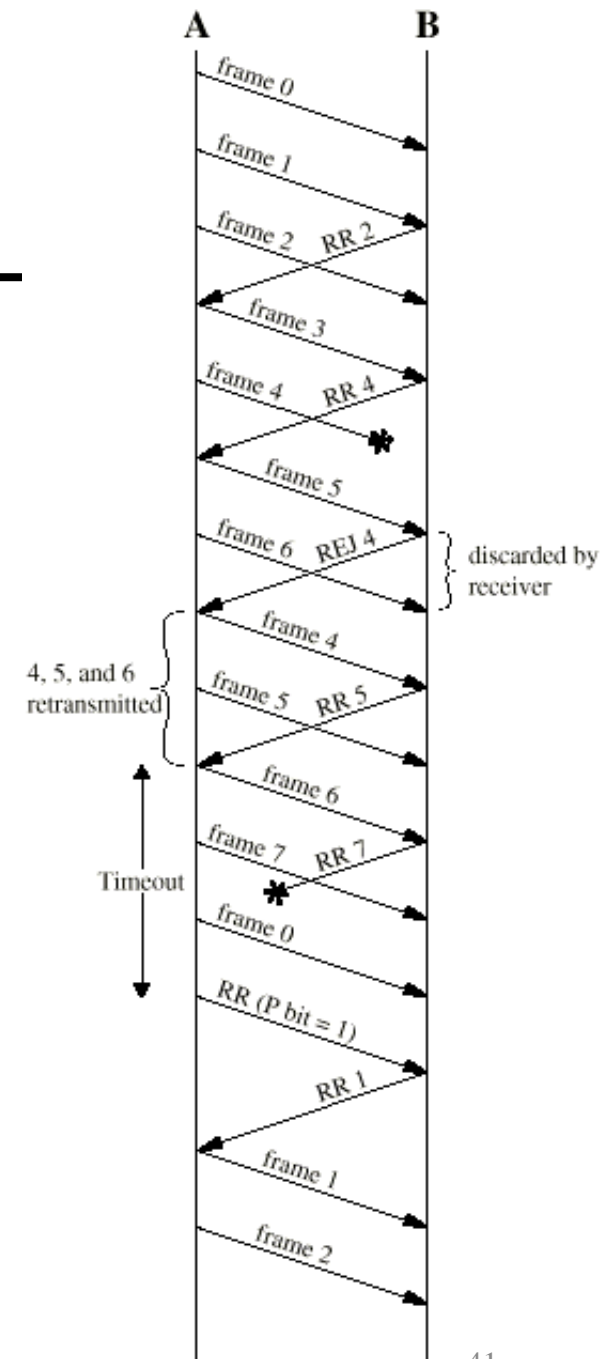
- ◆ Sequence numbers are represented module M
 - » NS, NR in $\{0, 1, \dots, M-1\}$
- ◆ Maximum Window
 - » $W = M-1 = 2^k - 1$
 - » k is number of bits used to code sequence numbers



- ◆ Extensions to basic behaviour
 - » Piggybacking can be used for bidirectional flows
 - » RR information can be sent in the data packets of opposite direction

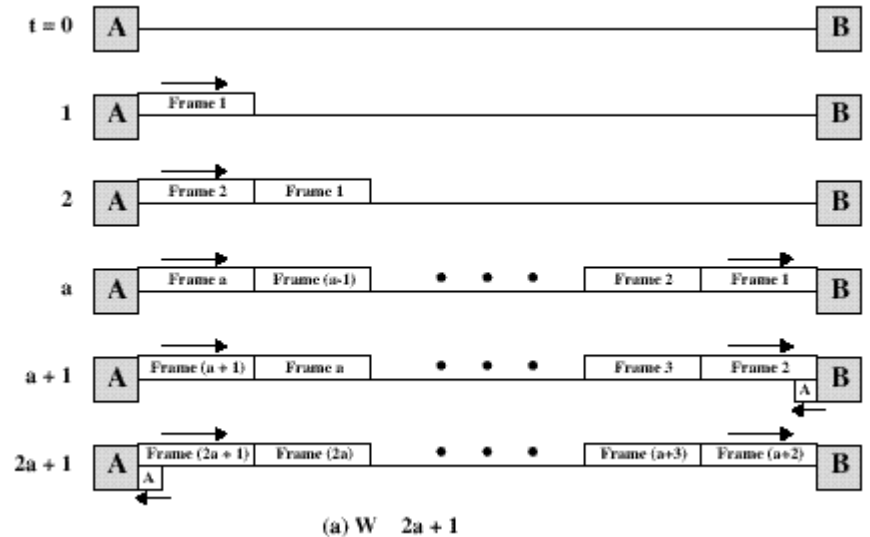
Go Back N ARQ – Behaviour under Errors

- ♦ Frame with errors
is silently discard by the Receiver
- ♦ If Receiver receives Data frame out of sequence
 - » First out-of-sequence-frame?
 - Receiver sends REJ(NR)
 - NR indicates the next in-sequence frame expected
 - » Following out-of sequence-frames
 - Receiver discards them; no REJ sent
- ♦ When Sender receives REJ(NR=x), the Sender
 - » **Goes-Back** and retransmits I(x), I(x+1), ...
 - » Continues using Sliding Window mechanism
- ♦ If timeout occurs, the Sender
 - » requests the Receiver to send a RR message
 - » by sending a special message (RR command message)

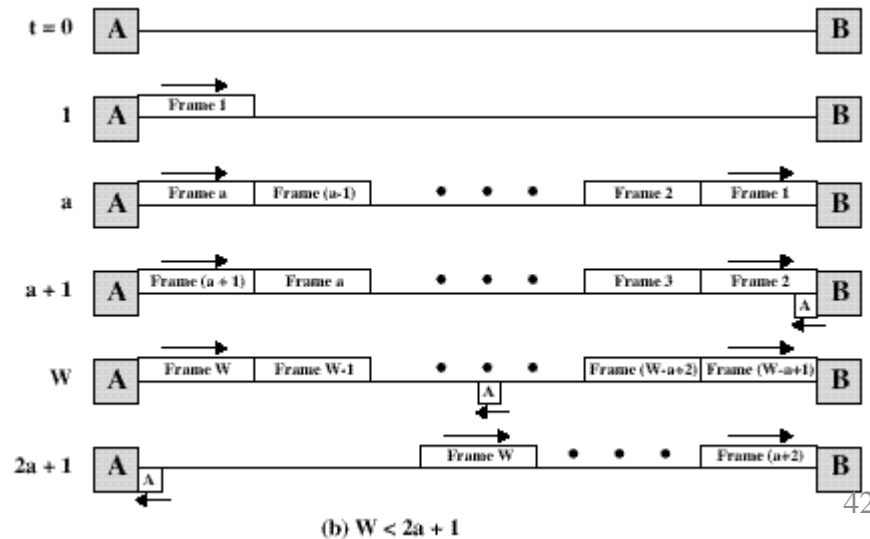


Go Back N – Efficiency

♦ If $W \geq 1+2a \rightarrow S = 1$

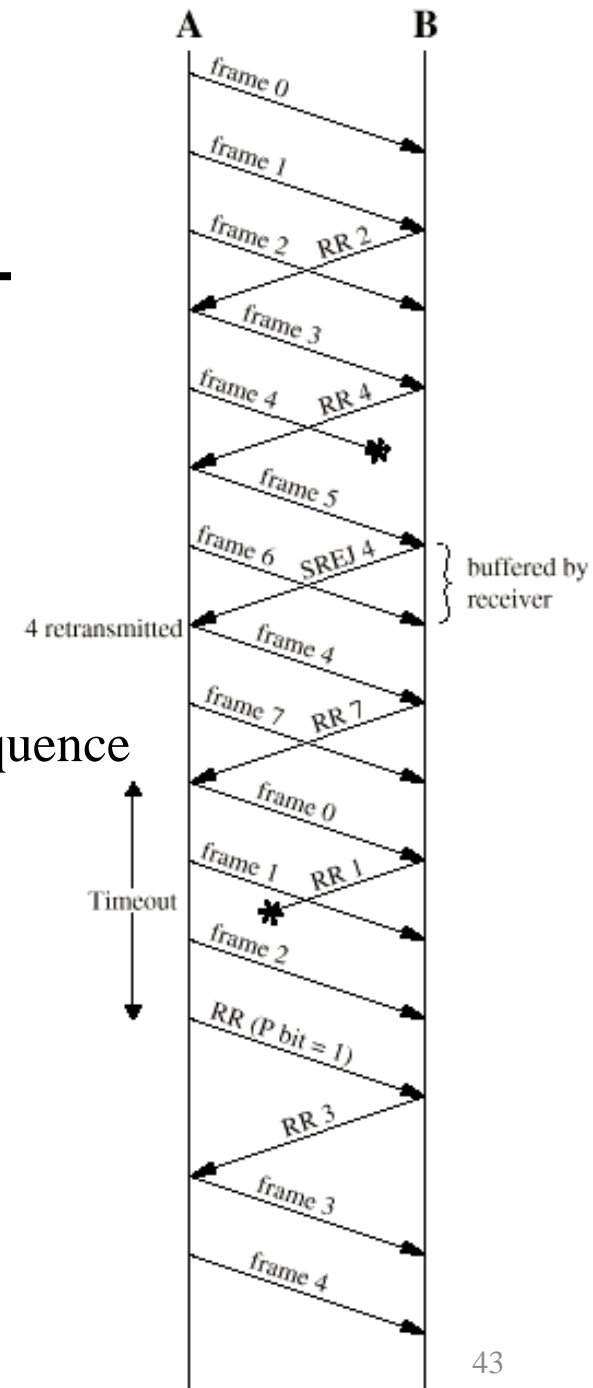


♦ If $W < 1+2a \rightarrow S = W/(1+2a)$



Selective Repeat ARQ

- ◆ Uses Sliding Window, but ...
- ◆ Receiver
 - » accepts out-of-sequence-frames
 - » confirms negatively, SREJ, a frame not arrived
 - » uses RR to confirm blocks of frames arrived in sequence
- ◆ Sender
 - » retransmits only the frames signaled by SREJ
- ◆ Adequate if W (a) is very large
- ◆ Maximum window size, $W = \frac{M}{2} = 2^{k-1}$



Go-Back-N and Selective Repeat ARQ – Efficiency under Errors

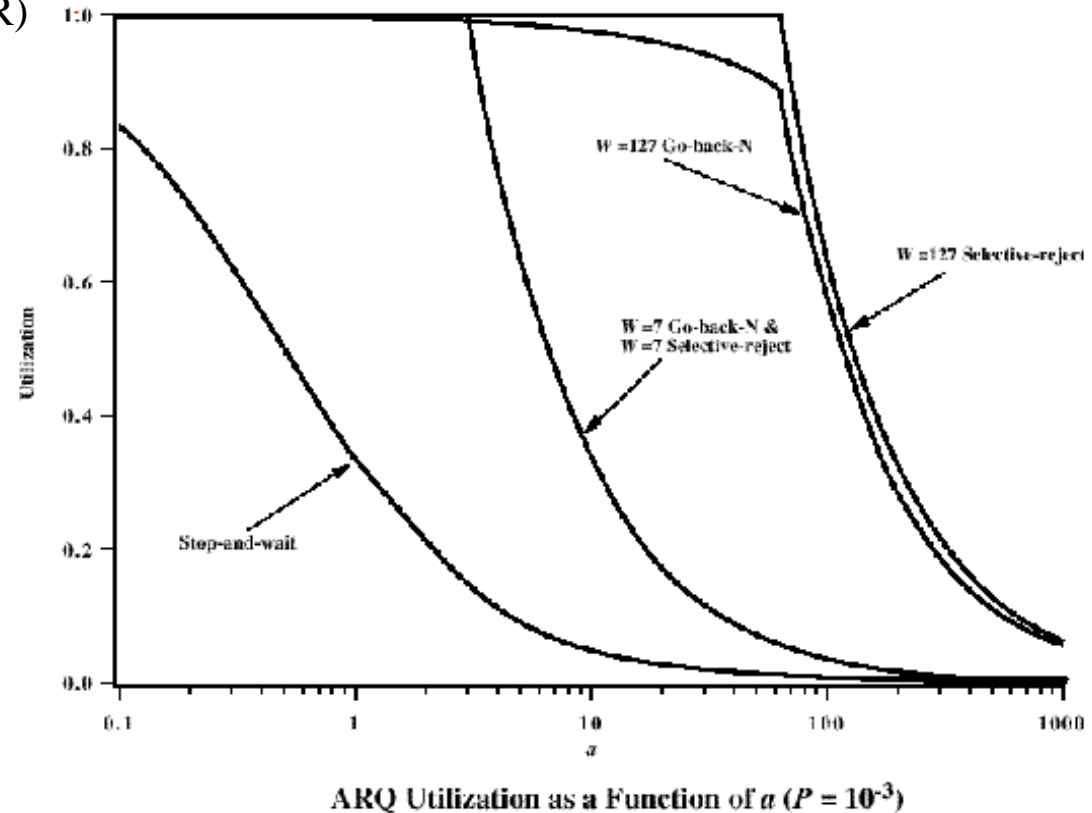
♦ Go-Back-N ARQ

p_e – frame error probability (ratio, FER)

$$S = \begin{cases} \frac{1 - p_e}{1 + 2ap_e} & , W \geq 1 + 2a \\ \frac{W(1 - p_e)}{(1 + 2a)(1 - p_e + Wp_e)} & , W < 1 + 2a \end{cases}$$

♦ Selective Repeat ARQ

$$S = \begin{cases} 1 - p_e & , W \geq 1 + 2a \\ \frac{W(1 - p_e)}{1 + 2a} & , W < 1 + 2a \end{cases}$$



Framing, Error detection and ARQ in common networks

Ethernet

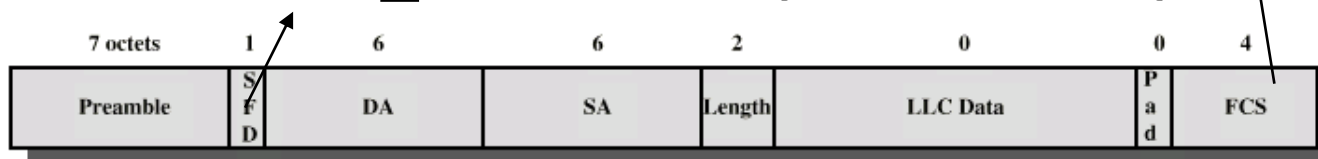
- ♦ Framing
 - » Start of frame: preamble + SFD
 - » End of frame: end of signal transitions (Manchester code), length
- ♦ Error detection: FCS → ITU-32, $G(x) = x^{32} + \dots + 1$
- ♦ No ARQ
 - » Bit Error ratio (BER) very low
→ Frame Error Ratio (FER) low
 - » CRC/FCS strong
 - Good detection of error frames
 - Frame detected with errors → discarded

$p=10^{-7}$ (good wired channel)

$n=10^4$ (~ Ethernet frame length)

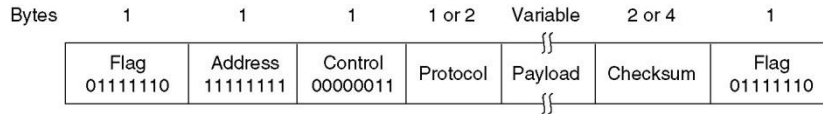
$P[\text{frame has errors}] = 1 - (1 - 10^{-7})^{10^4} \approx 10^{-3}$

7x 10101010 10101011



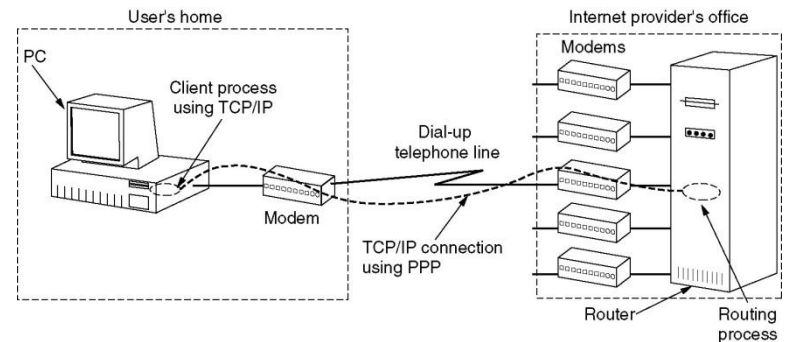
SFD = Start of frame delimiter
DA = Destination address
SA = Source address
FCS = Frame check sequence

Point to Point Protocol

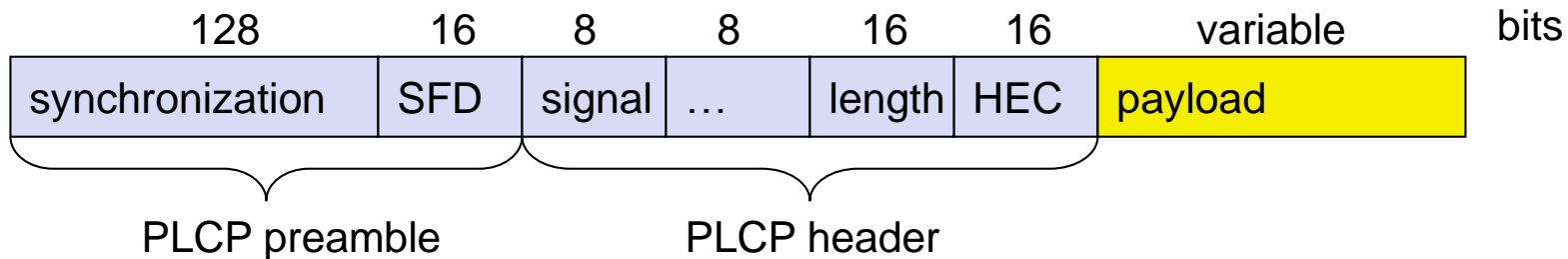


Byte stuffing

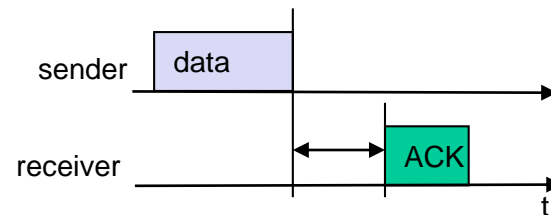
- ◆ Framing: Flags - 0x7E
- ◆ Byte stuffing: ESC – 0x7D
- ◆ Error detection – can be negotiated
- ◆ No ARQ



Wireless LAN

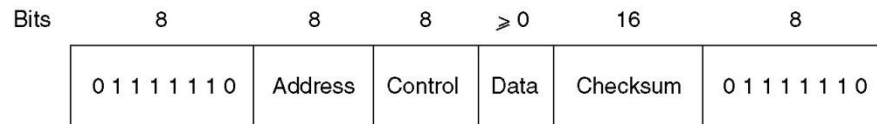


- ♦ Framing
 - » Synchronization: 0101010 ...
 - » SFD (Start Frame Delimiter) → 1111001110100000
 - » Length → Payload length **in us**
- ♦ HEC (Header Error Check)
 - » ITU-16, $G(x) = x^{16} + x^{12} + x^5 + 1$
- ♦ Payload (data)
 - » Protected by strong codes
- ♦ ARQ
 - » modified version of Stop and Wait
- ♦ Signal: Payload bitrate (0A: 1 Mbit/s DBPSK; 14: 2 Mbit/s DQPSK)



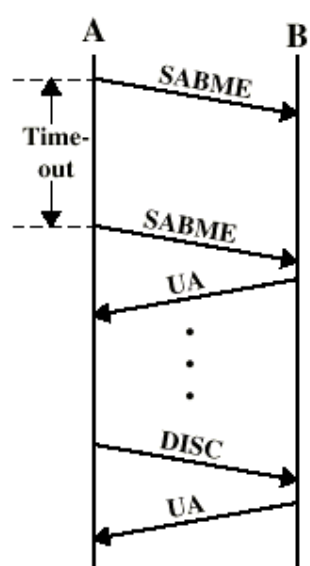
High-Level Data Link Control

- ◆ HDLC, Data Link Control, bit oriented

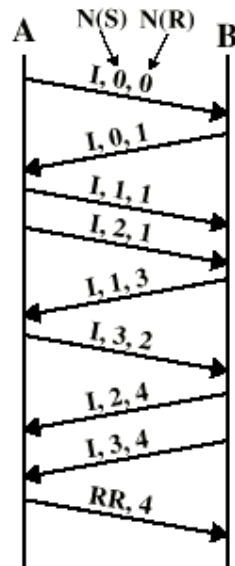


- ◆ Framing – FLAGS
- ◆ Bit stuffing
- ◆ Error detection – ITU-16
- ◆ ARQ – Selective Repeat ARQ
- ◆ Used as basis for many telecom networks
 - » GSM/GPRS/UMTS, Frame Relay
 - » LAP-x protocols

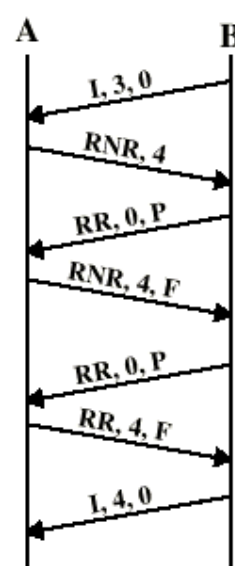
HDLC - Examples



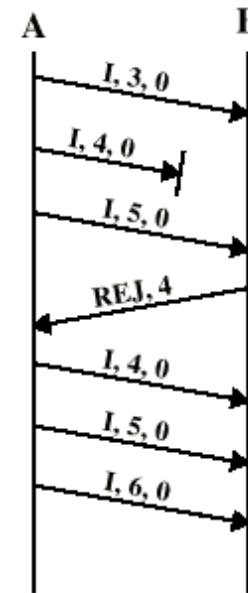
(a) Link setup and disconnect



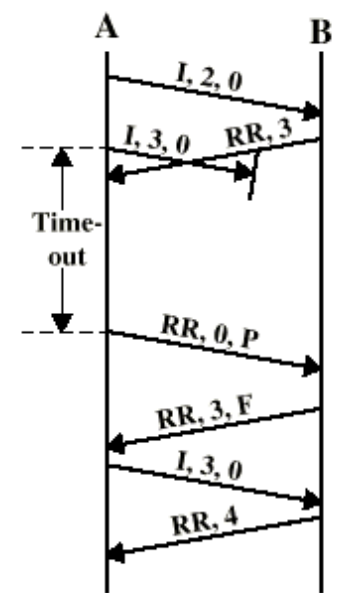
(b) Two-way data exchange



(c) Busy condition



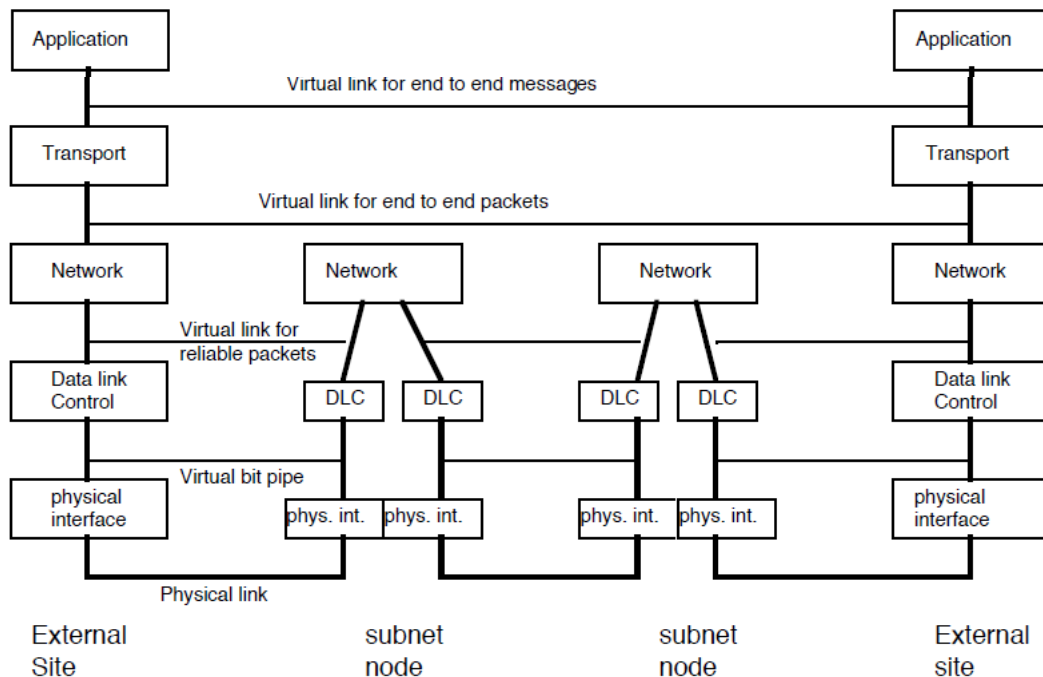
(d) Reject recovery




(e) Timeout recovery

Reliability in the Protocol Stack

Reliability in the Protocol Stack



FEC/ARQ


ARQ 

ARQ

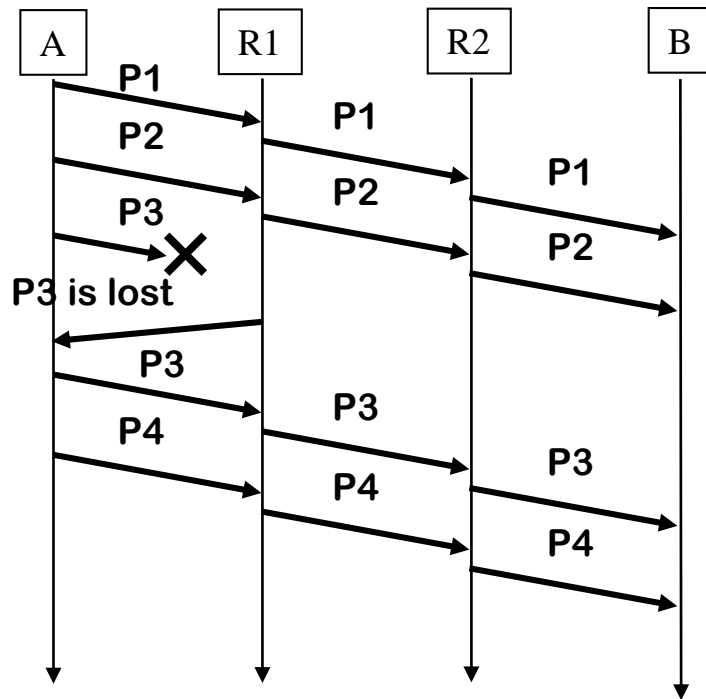
FEC coding

Reliability in the TCP/IP Reference Model

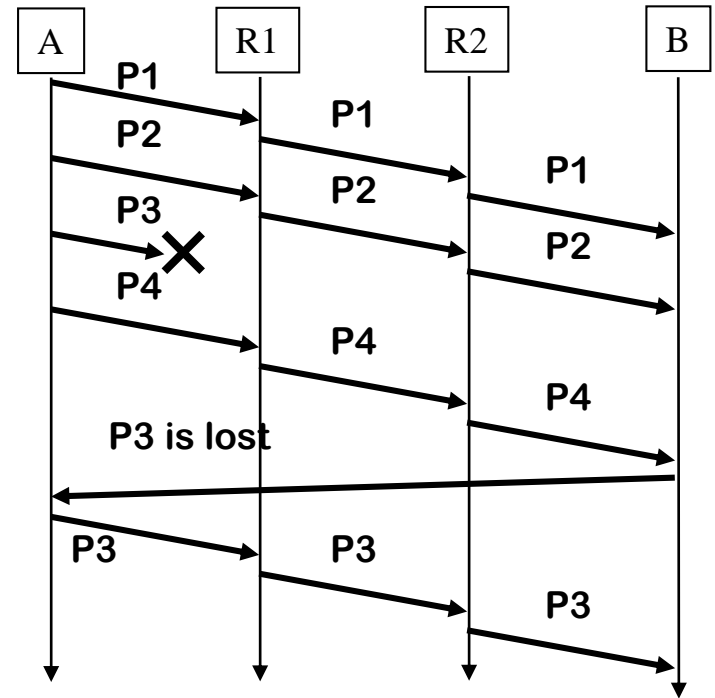
- ♦ The TCP/IP reference model assumes
 - » Every layer 2 offers an error free service to the upper layer
 - » Service Data Units are
 - delivered to upper layer without error,
 - or discarded
- ♦ The layered model **transforms bit error in packet losses**
Therefore, packet losses must be repaired ➔ ARQ solutions
- ♦ Two strategies can be used
 - » Link-by-Link ARQ
 - » End-to-end ARQ


$$FER = 1 - (1 - BER)^n$$

Link-by-Link ARQ versus End-to-End ARQ



Link-by-Link ARQ
(data link layer)



End-to-End ARQ
(transport or Application layers)

Link-by-Link ARQ versus End-to-End ARQ

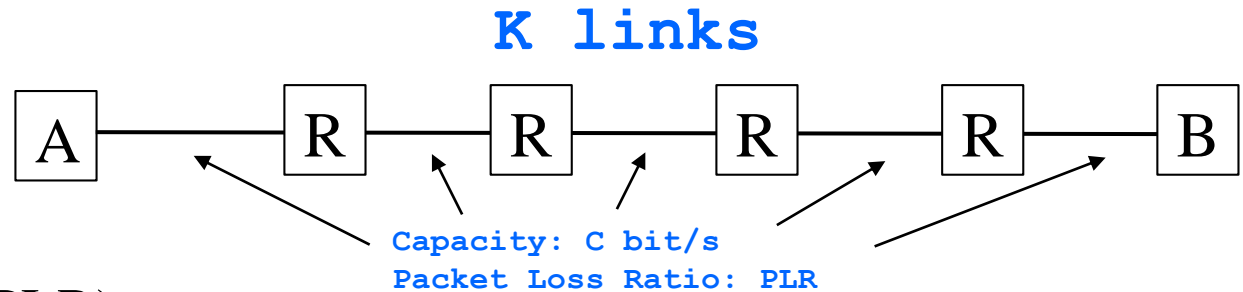
♦ Link-by-Link ARQ

- » Repairs losses link by link
- » Requires network elements to
 - remember information about packet flows → high processing per frame/packet
 - store packets in case they have to be retransmitted → memory required

♦ End-to-end ARQ

- » Low complexity in intermediate network elements
 - Switches/routers become simpler
- » Packets may follow different end-to-end paths
- » But, not acceptable when Packet Loss Ratio is high
- » Let's see why ...

End to End Capacity



- ◆ Packet Loss Ratio (PLR)
 - » Packet → layer 3; Frame → layer 2
 - » Let's assume PLR=FER
(not considering losses in queues)
- ◆ Capacity of one link $C_l = C * (1 - PLR)$
- ◆ End to End capacity
 - » using Link-by-Link ARQ: $C_{LL} = C_l = C * (1 - PLR)$
 - » Using End-to-End ARQ: $C_{EE} = C * (1 - PLR)^K$
- ◆ End-to-end ARQ → **Inefficient when PLR is High**

k	PLR	C_{EE}	C_{LL}
10	0.05	$0.6 * C$	$0.95 * C$
10	0.0001	$0.9990 * C$	$0.9999 * C$

ARQ in the TCP/IP Reference Model

- ◆ The TCP/IP architecture assumes that
 - » The Data Link layer **provides error-free packets** to the network layer
 - » Data link layer provides a service with very low FER
 - » End-to-End ARQ is used, implemented at
Transport or Application layers
- ◆ In the TCP/IP reference model, packet losses are repaired
 - » At the Data Link layer on lossy channels (e.g. wireless data links)
 - » At the end systems (transport layer or application layer)

Homework

1. Review slides
2. Read from Tanenbaum
 - » Chapter 3 (5th edition)
3. Read from Bertsekas&Gallager
 - » Sections 2.3, 2.4
4. Answer questions at moodle