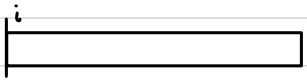
W10 PCRS

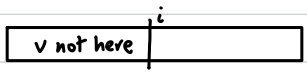
Linear Search

```
def linear_search(L: list, v: object) -> int:
    i = 0
    while i != len(L) and v != L[i]:
        i = i + 1
    if i == len(L):
        return -1
    else:
        return i
```

Initial state:

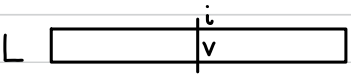


General case:



After the loop terminates, if v isn't in the list:

After the loop terminates, if v is in the list:



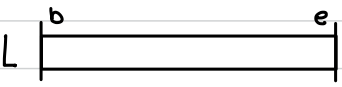
Invariant: something that doesn't change.

Loop invariant: something that is true before and after each iteration of the loop.

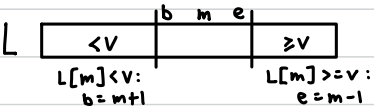
Binary Search

```
def binary_search(L: list, v: object) -> int:
    b = 0
    e = len(L) - 1
    while b <= e:
        m = (b + e) // 2
        if L[m] < v:
            b = m + 1
        else:
            e = m - 1
    if b == len(L) or L[b] != v:
        return -1
    else:
        return b
```

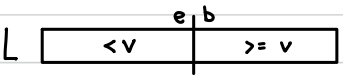
Initial State:



General State:

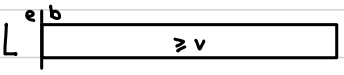


After loop terminates, v is in L:

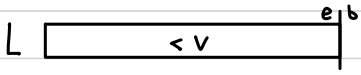


CASE 1

After loop terminates, v is not in L:



CASE 2

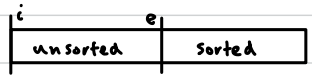


↳ Requires list to be sorted first.

Bubble Sort

Initial State:

General State:



End State:

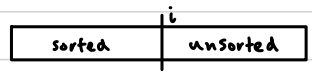
first item is technically unsorted, but it is smaller than the rest.

```
def bubble_sort (L: List) -> NoneType:
    end = len(L) - 1
    while end != 0:
        for i in range(end):
            if L[i] > L[i+1]:
                L[i], L[i+1] = L[i+1], L[i]
        end = end - 1
```

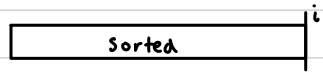
Selection Sort

Initial State:

General State:



End State:



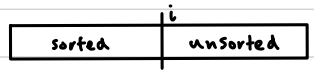

```
def get_index_of_smallest (L: list, i: int) -> int:
    index_of_smallest = i
    for j in range (i+1, len(L)):
        if L[j] < L[index_of_smallest]:
            index_of_smallest = j
    return index_of_smallest

def selection_sort (L: list) -> None:
    for i in range (len(L)):
        index_of_smallest = get_index_of_smallest (L, i)
        L[index_of_smallest], L[i] = L[i], L[index_of_smallest]
```

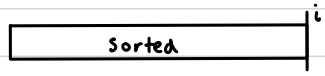
Insertion Sort

Initial State:

General State:



End State:




```
def insert(L: list, i: int) -> None:
    value = L[i]
    j = i
    while j != 0 and L[j-1] > value:
        L[j] = L[j-1]
        j = j-1
    L[j] = value

def insertion_sort(L: list) -> None:
    for i in range(len(L)):
        insert(L, i)
```