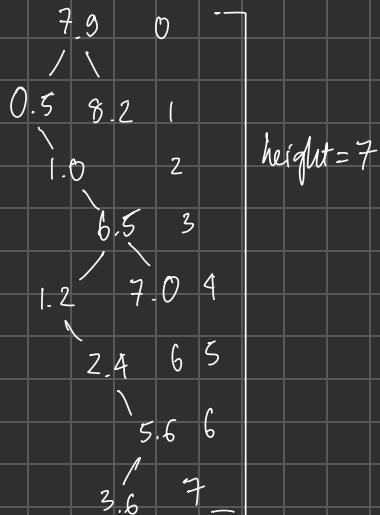


1.

- a)  $[7.9, 0.5, 1.0, 6.5, 8.2, 7.0, 6.6, 9.9, 1.2, 2.4, 5.6, 3.6]$

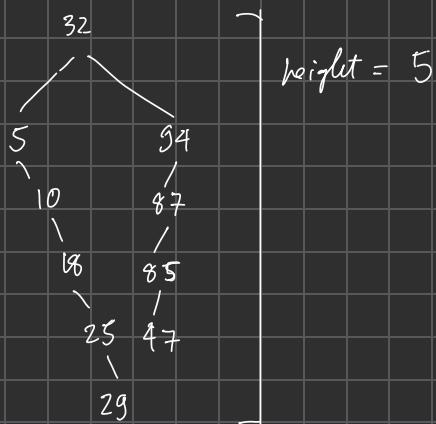
- b) "Petit Four", "Capake", "Donut", "Eclair", "Froyo",  
"Gingerbread", "HoneyComb"]



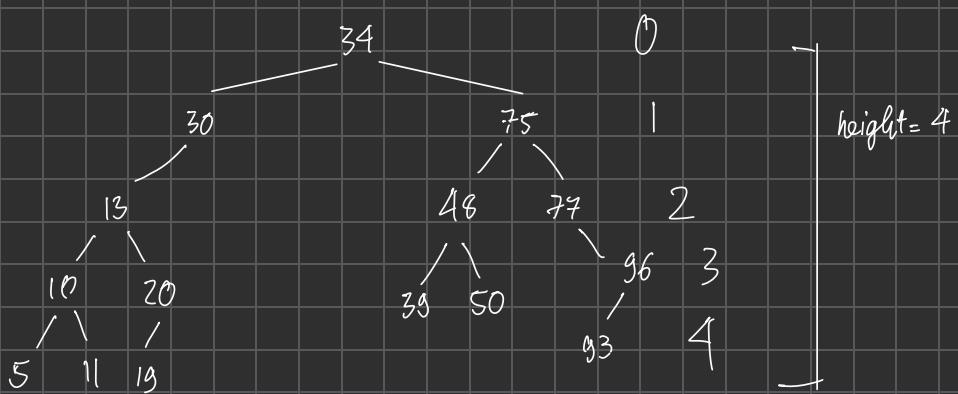
Height = 6



- c.  $[32, 5, 94, 87, 10, 18, 85, 47, 25, 29]$



- d.  $[34, 30, 75, 77, 96, 48, 39, 50, 93, 13, 3, 5, 11, 20, 19]$



2. First tree  $[68, 21, 15, 54, 46, 36, 37, 54, 46, 36, 37, 59, 65, 92, 80, 87, 97, 93]$

After node.data ± left.data + (right.data \* 2)

Preorder:  $[273, 144, 15, 218, 82, 110, 37, 189, 65, 366, 254, 87, 90, 93]$

a.  $68 + 21 + (92 \times 2) = 273$

$21 + 15 + (54 \times 2) = 144$

$15 + 0 + (0 \times 2) = 15$

$54 + 46 + (59 \times 2) = 218$

$46 + 36 + (0 \times 2) = 82$

$36 + 0 + 74 = 110$

$37 + 0 + (0 \times 2) = 37$

$59 + 0 + 130 = 189$

$65 + 0 + 0 = 65$

$72 + 80 + 194 = 366$

$80 + 0 + 174 = 254$

$87 + 0 + 0 = 87$

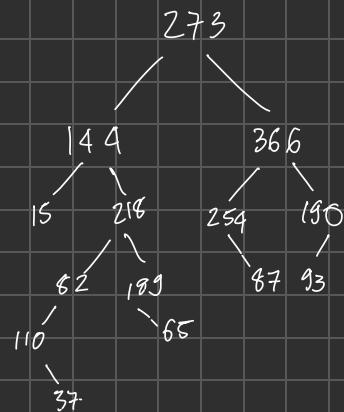
$97 + 93 + 0 = 190$

$93 + 0 + 0 = 93$

b. Not BST, because the node values are no longer in BST where  $\text{Left} < \text{Root} < \text{Right}$

E.g.: Node 273 has left child 144 and right 366 ✓  
But node 200 (left child of 218) has 189 as right child ✗  
 $189 < 218$

c. No because it's no longer a BST (AVL requires BST)  
and also the tree is unbalanced (Some subtrees are very deep)



5. For Election class, the time complexity is  $O(n \log n)$  where  $n$  is the # of candidates. This is because we call updateMaxHeap in every method which has time complexity of  $O(n \log n) \rightarrow$  this method rebuild the heap every time there is a new entries. All other methods run  $O(n)$  so it's like  $O(n + n + \dots + n \log n) \rightarrow O(n \log n)$

Space is  $O(n)$  because voteMap and maxHeap store  $n$  in space (all of the candidates)

For ElectionSystem class:

- Time :  $O(n \log n)$  where  $n$  is # candidates

- Space:  $O(n)$  because voteMap and MaxHeap store  $O(n)$