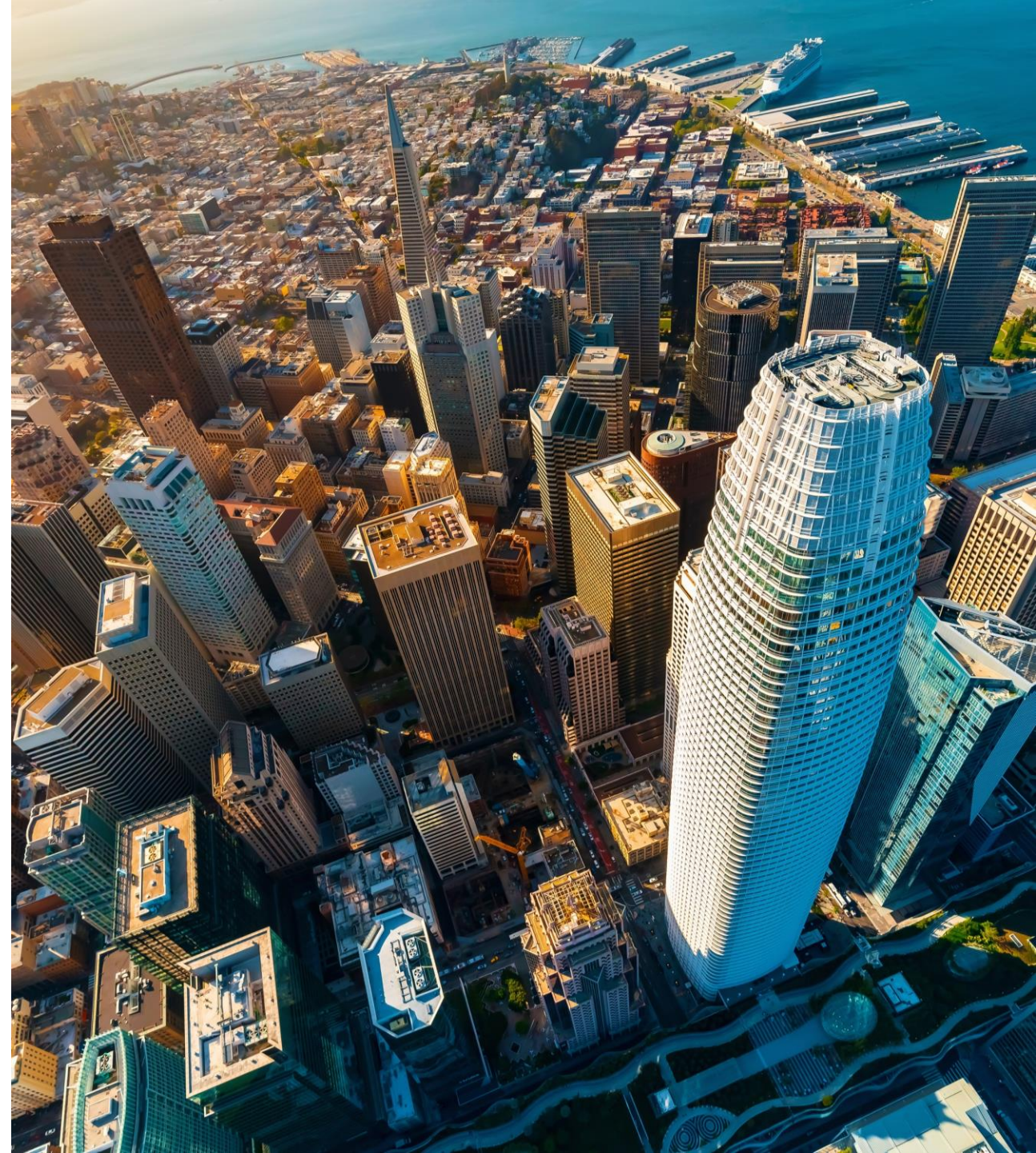




# Continual Learning: Overcoming catastrophic forgetting in neural networks

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# **Agenda**

## **Overview & Introduction to Continual Learning via E.W.C.**

Overview of the paper – “Overcoming catastrophic forgetting in neural networks”

Core Idea and some math

## **Toy Example**

Toy Example / Implementing the paper

## **Relevance in Mapmaking**

Discussion on projects

Fisher Information – intuitions (if time permits)



# Motivation, Overview of the paper

...

- Have over 4000 citations
- Written by 14 people, mostly DeepMind
- Tutorial in 2022 NeurIPS on “[Lifelong Learning Machines](#)”
- One of the authors - Dharshan Kumaran – is a grand master
- One of the authors - Razvan Pascanu – wrote about [exploding gradients](#), with Yoshua Bengio

... in all, the paper has all ingredients for an awesome paper

## Overcoming catastrophic forgetting in neural networks

James Kirkpatrick<sup>a</sup>, Razvan Pascanu<sup>a</sup>, Neil Rabinowitz<sup>a</sup>, Joel Veness<sup>a</sup>, Guillaume Desjardins<sup>a</sup>, Andrei A. Rusu<sup>a</sup>, Kieran Milan<sup>a</sup>, John Quan<sup>a</sup>, Tiago Ramalho<sup>a</sup>, Agnieszka Grabska-Barwinska<sup>a</sup>, Demis Hassabis<sup>a</sup>, Claudia Clopath<sup>b</sup>, Dharshan Kumaran<sup>a</sup>, and Raia Hadsell<sup>a</sup>

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### Abstract

The ability to learn tasks in a sequential fashion is crucial to the development of artificial intelligence. Neural networks are not, in general, capable of this and it has been widely thought that *catastrophic forgetting* is an inevitable feature of connectionist models. We show that it is possible to overcome this limitation and train networks that can maintain expertise on tasks which they have not experienced for a long time. Our approach remembers old tasks by selectively slowing down learning on the weights important for those tasks. We demonstrate our approach is scalable and effective by solving a set of classification tasks based on the MNIST hand written digit dataset and by learning several Atari 2600 games sequentially.

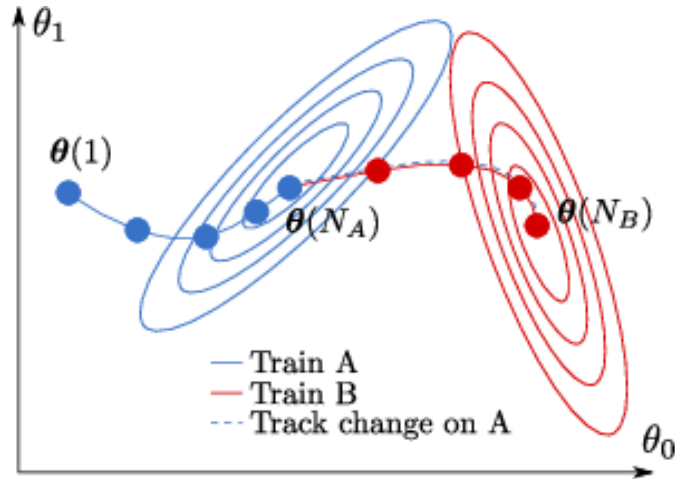
### 1 Introduction

Achieving artificial general intelligence requires that agents are able to learn and remember many different tasks [Legg and Hutter [2007]]. This is particularly difficult in real-world settings: the sequence of tasks may not be explicitly labelled, tasks may switch unpredictably, and any individual task may not recur for long time intervals. Critically, therefore, intelligent agents must demonstrate a capacity for *continual learning*: that is, the ability to learn consecutive tasks without forgetting how to perform previously trained tasks.

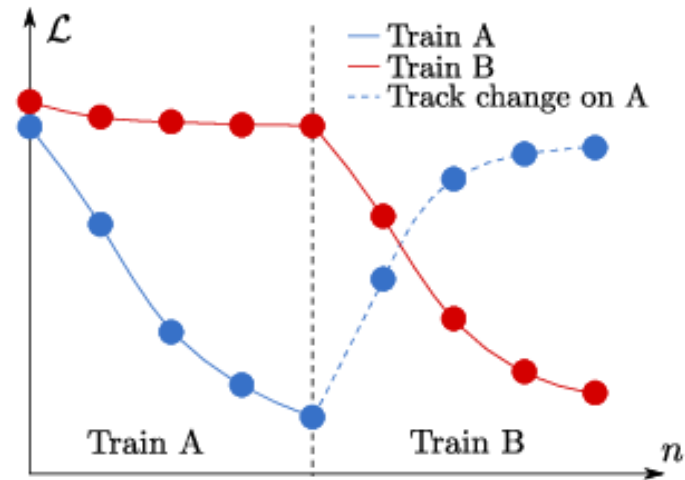
Continual learning poses particular challenges for artificial neural networks due to the tendency for

# Catastrophic Forgetting

a.k.a. Catastrophic Interference



- We see that standard backpropagation network can generalize to unseen inputs, but they are very sensitive to new information.
- The main cause of catastrophic interference seems to be **overlap in the representations** at the hidden layer of distributed neural networks.



How humans / animals deal with Catastrophic Forgetting:

- The mammalian brain may avoid catastrophic forgetting by protecting the previously-acquired knowledge in neocortical circuits [Cichon and Gan, 2015]. **The dendrites (spine) persists swollen / enlarged despite the subsequent learning of other tasks**, accounting for retention of performance [Yang et al., 2009]

# Continual Learning v Catastrophic forgetting

$D_1 \rightarrow D_2 \rightarrow \dots \rightarrow D_n$  : Sequence of data shown to the model

- **Continual Learning:**

$$p(y_n | x, D_1 \rightarrow \dots \rightarrow D_n)$$

- **Catastrophic Forgetting:**

$$p(y_1 | x, D_1 \rightarrow \dots \rightarrow D_n), \text{ or mostly}$$

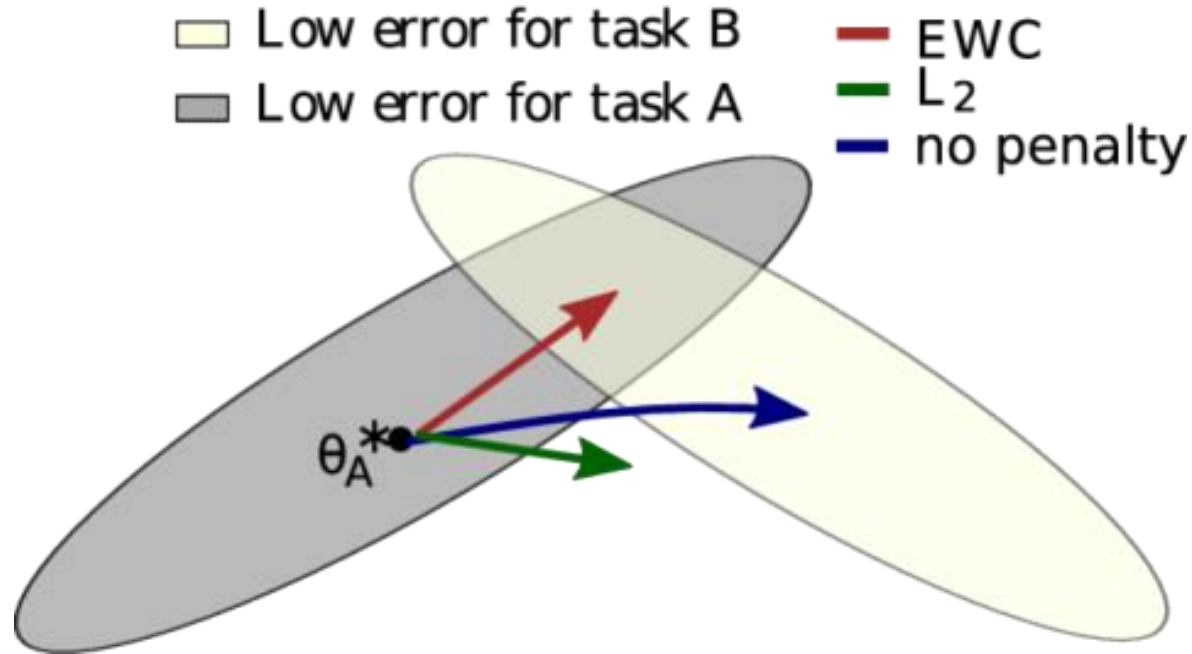
$$p(y_1 | x, D_1 \rightarrow D_2)$$

- Concerned about Model's ability to learn  $n^{th}$  task given  $n - 1$  task

- Concerned about Model's ability to remember  $n - 1$  tasks given training on new  $n^{th}$  task.
- Interference due to new task, the old task is forgotten

# Core Idea in a picture

Penalize, but softly and choose whom to penalize



$\theta_A^*$  are the optimum parameters (solution) for  $Task_A$

- For 'no penalty', we don't do bad, at least we are good for  $Task_B$

- For  $L_2$  penalty, we neither do good on  $Task_A$  nor on  $Task_B$
- This is worse than 'no penalty'. Too restrictive.

- For EWC penalty, we do good both on  $Task_A$  and on  $Task_B$ . A softer way to penalize.
- The new optimum lies in the low error planes for both  $Task_A$  and  $Task_B$

- We typically look for low error (plane / zone..) for the parameters.
- When I'm learning new task, I would like my parameters to be close to original task's parameters  $\theta_A^*$
- There are a lot of parameters to play with, so we can choose whom to modify / penalize modification

# Core Idea in math

If  $\theta$  is weights of model and  $D$  is data distribution, then we are concerned about what is the best  $\theta$  that would fit the data  $D$

$$p(\theta|D) = \frac{p(D|\theta) \cdot p(\theta)}{p(D)}$$

or,  $\log p(\theta|D) = \log p(D|\theta) + \log p(\theta) - \log p(D)$

$\log p(D|\theta)$  : best data distribution for  $\theta$ , loss term ( $-\mathcal{L}(\theta)$ )

$\log p(\theta)$ ,  $\log p(D)$  : priors of  $\theta$  (initialization) and Data

Extending this to scenarios where we have one Data after another

$$\log p(\theta|D) = \log p(D_B|\theta) + \log p(\theta|D_A) - \log p(D_B)$$

$D$  : Entire Data  $= D_A + D_B$

$\log p(\theta|D)$  : represents the overall loss,  $\mathcal{L}(\theta)$ ,

$\log p(D_B|\theta)$  : represents the loss for the task B,  $\mathcal{L}_B(\theta)$ , Likelihood

$\log p(\theta|D_A)$  : This should capture essence of first task

$\log p(\theta|D_A)$  : an assumption is made to find this

$$\log p(\theta|D_A) \approx \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2$$

$\lambda$  : Weightage of old task

$F_i$  : Fisher Information Matrix (diagonal entry)

This can be thought of a matrix which gives importance to each weight

$$F_i = \mathbb{E}_x (\partial_{\theta_i} \log p_{\theta}(x))^2$$

We can now say that

$$\mathcal{L}(\theta) = \mathcal{L}_B(\theta) + \sum_i \frac{\lambda}{2} F_i (\theta_i - \theta_{A,i}^*)^2$$

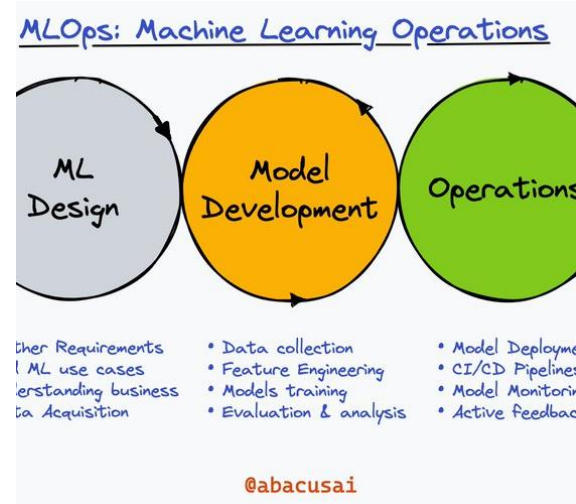
# Toy Example

[https://github.com/peeyushsinghal/ContinualLearning/blob/main/EWC\\_experiment.ipynb](https://github.com/peeyushsinghal/ContinualLearning/blob/main/EWC_experiment.ipynb)



# Relevance in Mapmaking

Where all we can use continual learning



- Cerebro – One model for MoMa and Mapillary images
- Same model for APTs and POIs

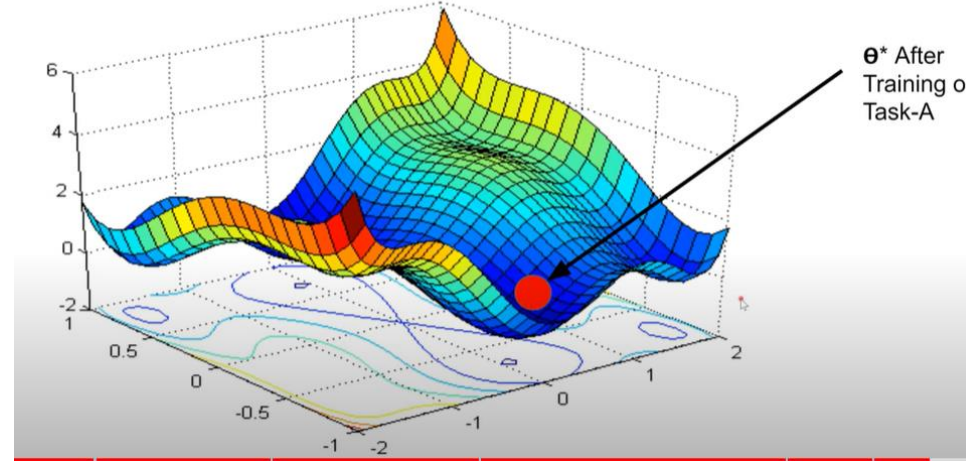
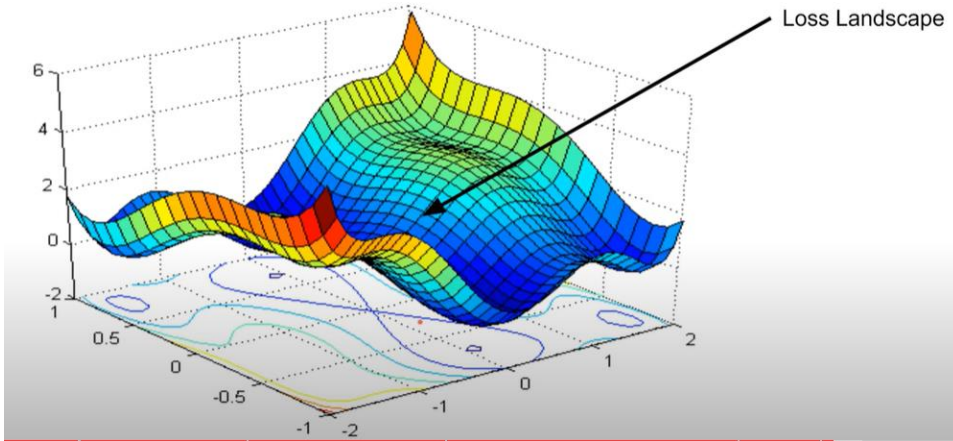
- Extending Models to similar datasets, BFP creation models

- Reduction in number of models, less burden for MLOPs

- ... many more

# Fisher Information Matrix – view 1

Intuition and match



Perturbing the weight in different direction helps us understand where the impact of movement is high

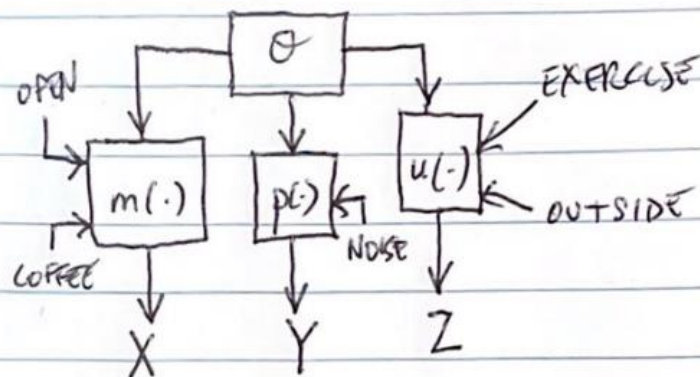
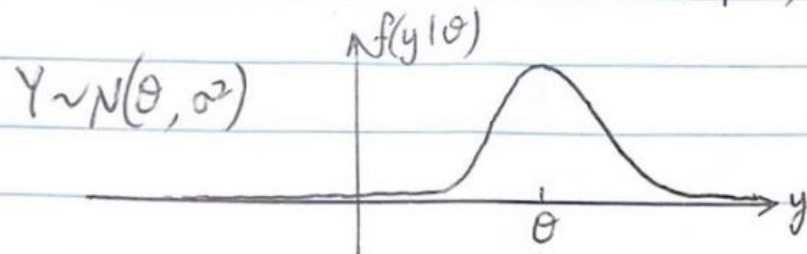
- Ideally, we would like to understand the curvature of  $\mathcal{L}(\theta)$ , using the Hessian (second derivative), but that is intractable due to a large number of parameters. Please note that already first derivative is 0 at  $\theta^*$
- Instead, we approximate Hessian with the diagonal of the empirical Fisher Matrix. It provides a view of the loss landscape using double derivative
- Loss takes form of multivariate Gaussian with diagonal covariance

# Fisher Information Matrix – view 2

Intuition and math

$$I_Y(\theta) = E \left[ \left( \frac{\partial}{\partial \theta} \ln f(Y; \theta) \right)^2 \right]$$

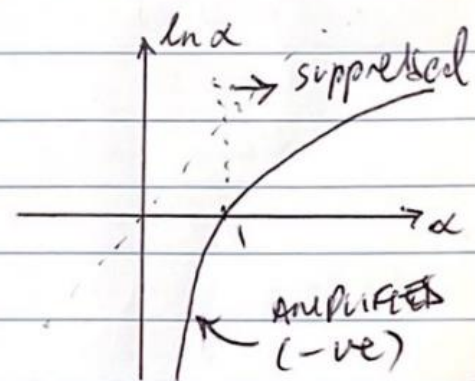
Ex.  $Y = \theta + W$      $W \sim N(0, \sigma^2)$



$$f(y; \theta) = \frac{1}{\sqrt{2\pi}\sigma} \exp \left( -\frac{(y-\theta)^2}{2\sigma^2} \right)$$

$$I_Y(\theta) = E \left[ \left( \frac{y-\theta}{\sigma^2} \right)^2 \right] = \frac{1}{\sigma^2}$$

$$= \frac{1}{\sigma^4} \int (y-\theta)^2 f(y; \theta) dy$$



# Fisher Information Matrix – view 3

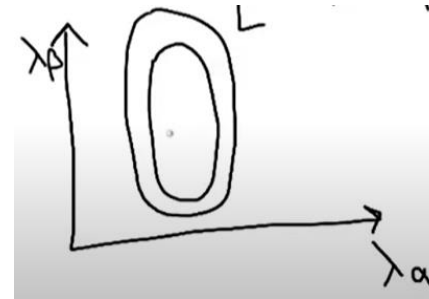
Intuition and math

$$F_{\alpha\beta}^{-1} = C_{\alpha\beta}$$

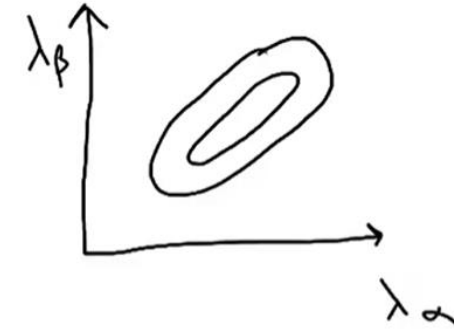
$\alpha, \beta$  are two weights of  $\theta$

$C$  is covariance matrix

$$C_{\alpha\beta} = \begin{bmatrix} \sigma_{\alpha}^2 & \sigma_{\beta\alpha} \\ \sigma_{\alpha\beta} & \sigma_{\beta}^2 \end{bmatrix}$$



$$\sigma_{\alpha\beta} = 0 \text{ and } \sigma_{\beta\alpha} = 0$$



$$\sigma_{\alpha\beta} \neq 0 \text{ and } \sigma_{\beta\alpha} \neq 0$$

Fisher Information Matrix looks to be curvature matrix : Bigger the Fisher Information Matrix, smaller the covariance matrix (therefore the variances), the smaller the contours, the peakier / curved our loss landscape is.

For simplified perspective, we take  $\sigma_{\alpha\beta} = 0$  and  $\sigma_{\beta\alpha} = 0$  , therefore we look at the diagonal of Fisher Information Matrix



Thank You