```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
    [] => []
    | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

What Your Interpreter Can and Cannot Assume

What we know

- Define (abstract) syntax of language B with Racket structs
 - B called MUPL in homework
- Write B programs directly in Racket via constructors
- Implement interpreter for B as a (recursive) Racket function

Now, a subtle-but-important distinction:

- Interpreter can assume input is a "legal AST for B"
 - Okay to give wrong answer or inscrutable error otherwise
- Interpreter must check that recursive results are the right kind of value
 - Give a good error message otherwise

Legal ASTs

"Trees the interpreter must handle" are a subset of all the trees
 Racket allows as a dynamically typed language

```
(struct const (int) #:transparent)
(struct negate (e) #:transparent)
(struct add (e1 e2) #:transparent)
(struct multiply (e1 e2) #:transparent)
```

- Can assume "right types" for struct fields
 - const holds a number
 - negate holds a legal AST
 - add and multiply hold 2 legal ASTs
- Illegal ASTs can "crash the interpreter" this is fine

```
(multiply (add (const 3) "uh-oh") (const 4))
(negate -7)
```

Interpreter results

- Our interpreters return expressions, but not any expressions
 - Result should always be a *value*, a kind of expression that evaluates to itself
 - If not, the interpreter has a bug
- So far, only values are from const, e.g., (const 17)
- But a larger language has more values than just numbers
 - Booleans, strings, etc.
 - Pairs of values (definition of value recursive)
 - Closures
 - **–** ...

Example

See code for language that adds booleans, number-comparison, and conditionals:

```
(struct bool (b) #:transparent)
(struct eq-num (e1 e2) #:transparent)
(struct if-then-else (e1 e2 e3) #:transparent)
```

What if the program is a legal AST, but evaluation of it tries to use the wrong kind of value?

- For example, "add a boolean"
- You should detect this and give an error message not in terms of the interpreter implementation
- Means checking a recursive result whenever a particular kind of value is needed
 - No need to check if any kind of value is okay