```
fun append (xs,ys) =
    if xs=[]
    then ys
    else (hd xs)::append(tl xs,ys)

fun map (f,xs) =
    case xs of
      [] => []
      | x::xs' => (f x)::(map(f,xs'))

val a = map (increment, [4,8,12,16])
val b = map (hd, [[8,6],[7,5],[3,0,9]])
```

Programming Languages Dan Grossman

Optional: Abstract Methods

Connections

Answered in this segment:

- What does a statically typed OOP language need to support "required overriding"?
- How is this similar to higher-order functions?
- Why does a language with multiple inheritance (e.g., C++) not need Java/C#-style interfaces?

[Explaining Java's abstract methods / C++'s pure virtual methods]

Required overriding

Often a class expects all subclasses to override some method(s)

 The purpose of the superclass is to abstract common functionality, but some non-common parts have no default

A Ruby approach:

- Do not define must-override methods in superclass
- Subclasses can add it

Creating instance of superclass can cause method-missing

errors

```
# do not use A.new
# all subclasses should define m2
class A
  def m1 v
      ... self.m2 e ...
  end
end
```

Static typing

- In Java/C#/C++, prior approach fails type-checking
 - No method m2 defined in superclass
 - One solution: provide error-causing implementation

```
class A
  def m1 v
     ... self.m2 e ...
  end
  def m2 v
     raise "must be overridden"
  end
end
```

Better: Use static checking to prevent this error...

Abstract methods

- Java/C#/C++ let superclass give signature (type) of method subclasses should provide
 - Called abstract methods or pure virtual methods
 - Cannot creates instances of classes with such methods
 - Catches error at compile-time
 - Indicates intent to code-reader
 - Does not make language more powerful

```
abstract class A {
   T1 m1(T2 x) { ... m2(e); ... }
   abstract T3 m2(T4 x);
}
class B extends A {
   T3 m2(T4 x) { ... }
}
```

Passing code to other code

 Abstract methods and dynamic dispatch: An OOP way to have subclass "pass code" to other code in superclass

```
abstract class A {
   T1 m1(T2 x) { ... m2(e); ... }
   abstract T3 m2(T4 x);
}
class B extends A {
   T3 m2(T4 x) { ... }
}
```

 Higher-order functions: An FP way to have caller "pass code" to callee

```
fun f (g,x) = ... g e ...
fun h x = ... f((fn y => ...),...)
```

No interfaces in C++

- If you have multiple inheritance and abstract methods, you do not also need interfaces
- Replace each interface with a class with all abstract methods
- Replace each "implements interface" with another superclass

So: Expect to see interfaces only in statically typed OOP without multiple inheritance

- Not Ruby
- Not C++