

Data Structure - Homework 2: Transpose

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三種轉置方式和運行時間：

```
5 6
0 0 1
0 2 1
1 1 2
2 0 4
2 2 3
^Z
Traditional 2-dimensional array:
1 0 4 0 0 0
0 2 0 0 0 0
1 0 3 0 0 0
0 0 0 0 0 0
0 0 0 0 0 0

1 0 1 0 0
0 2 0 0 0
4 0 3 0 0
0 0 0 0 0
0 0 0 0 0
0 0 0 0 0
traditional 2-dimensional array execution time: 10 milliseconds

Fast Transpose:
0 0 1
0 2 4
1 1 2
2 0 1
2 2 3
Transpose execution time: 5 milliseconds

Fast Transpose:
0 0 1
0 2 4
1 1 2
2 0 1
2 2 3
Fast Transpose execution time: 0 milliseconds
```

各種測資的時間(助教給的.in):

7_9:

```
traditional 2-dimensional array execution time: 12 milliseconds  
Transpose execution time: 5 milliseconds  
Fast Transpose execution time: 0 milliseconds
```

15_12:

```
traditional 2-dimensional array execution time: 19 milliseconds  
Transpose execution time: 12 milliseconds  
Fast Transpose execution time: 1 milliseconds
```

60_74:

```
traditional 2-dimensional array execution time: 115 milliseconds  
Transpose execution time: 610 milliseconds  
Fast Transpose execution time: 36 milliseconds
```

100_100:

```
traditional 2-dimensional array execution time: 398 milliseconds  
Transpose execution time: 2990 milliseconds  
Fast Transpose execution time: 104 milliseconds
```

256_512:

```
traditional 2-dimensional array execution time: 2706 milliseconds  
Transpose execution time: 85494 milliseconds  
Fast Transpose execution time: 1091 milliseconds
```

720_850:

```
traditional 2-dimensional array execution time: 12343 milliseconds  
Transpose execution time: 853105 milliseconds  
Fast Transpose execution time: 7716 milliseconds
```

第一種演算法的時間複雜度為: $O(\text{col} * \text{row})$

第二種演算法的時間複雜度為: $O(\text{col} * \text{輸入行數})$

第三種演算法的時間複雜度為: $O(\text{輸入行數})$

經過上面 testcase 的統計，雖然在陣列大小很小時的時間差距不大，但是到了 720_850 時，第一種演算法比第二種快了 71 倍，第三種比第二種快了 1218 倍，可見 $O(n^2)$ 和 $O(n)$ 的速度差距。