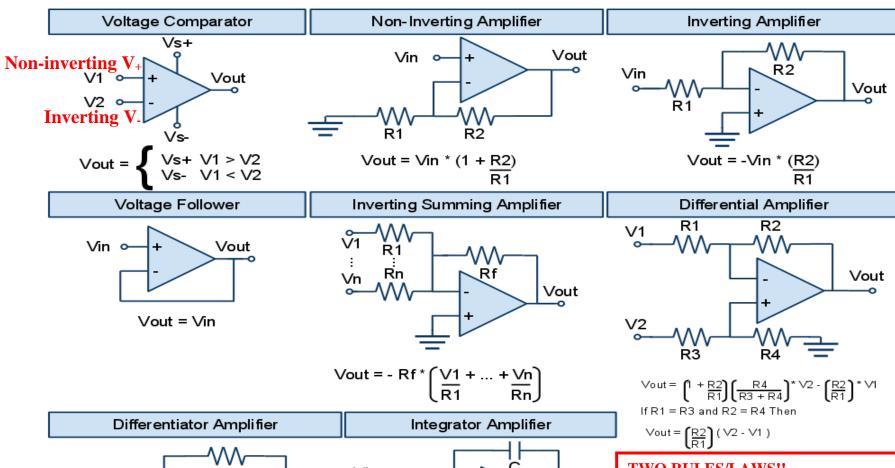
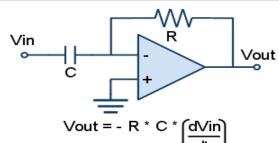
No Loop (no feedback)
$$\rightarrow$$
 V_{out} = A_{OL}(V₊ - V₋)

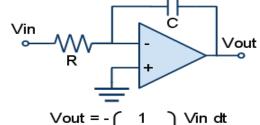
A_{OL} = Open Loop Gain = Usually >> 100k

With Loop (with feedback) \rightarrow Av = $\frac{V_{out}}{V_{in}}$ = A_{CL} Av = Voltage Gain = A_{CL} = Closed Loop Gain

Basic Operational Amplifier Configurations







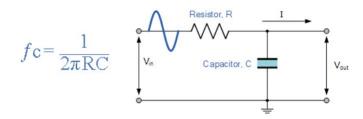
Vout =
$$-\left(\frac{1}{R \cdot C}\right)$$
 Vin di

TWO RULES/LAWS!!

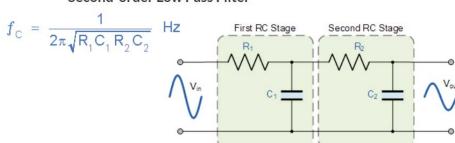
- 1. No current flows into the inputs
- 2. With feedback (loop) the op-amp tries to make the two inputs equal to each other

$$\begin{aligned} \mathbf{V}_{+} &= \mathbf{V}_{-} \\ \Delta \mathbf{V} &= \mathbf{V}_{+} - \mathbf{V}_{-} &= \mathbf{0} \end{aligned}$$

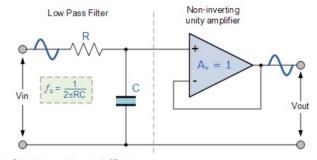
RC Low Pass Filter Circuit



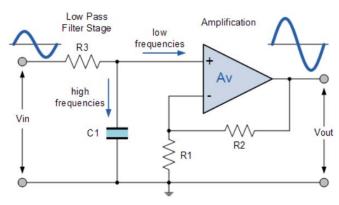
Second-order Low Pass Filter

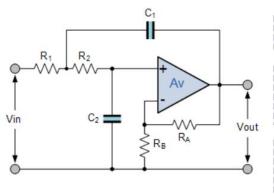


First Order Low Pass Filter



Active Low Pass Filter with Amplification





Gain (Av) = 1 +
$$\frac{R_A}{R_B}$$

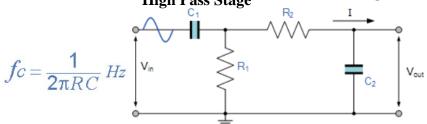
If Resistor and Capacitor values are different:
$$f_{\text{C}} = \frac{1}{2\pi \sqrt{R_1 R_2 C_1 C_2}}$$

If Resistor and Capacitor values are the same:
$$f_C = \frac{1}{1}$$

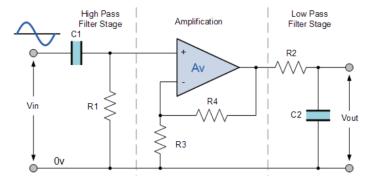
$$DC gain = \left(1 + \frac{R_2}{R_1}\right)$$

Band Pass Filter Circuit

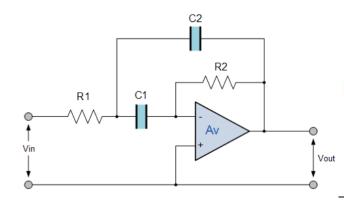
High Pass Stage Low Pass Stage



Active Band Pass Filter Circuit



Infinite Gain Multiple Feedback Active Filter

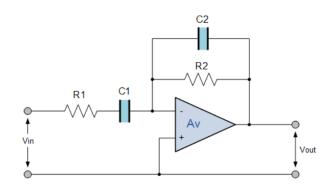


Centre Frequency Equation

$$fr = \sqrt{f_L x f_H}$$

Where, f_r is the resonant or centre frequency f_L is the lower -3dB cut-off frequency point f_H is the upper -3db cut-off frequency point

Inverting Band Pass Filter Circuit



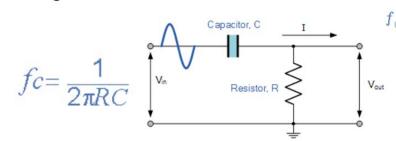
Voltage Gain =
$$-\frac{R_2}{R_1}$$
, $fc_1 = \frac{1}{2\pi R_1 C_1}$, $fc_2 = \frac{1}{2\pi R_2 C_2}$

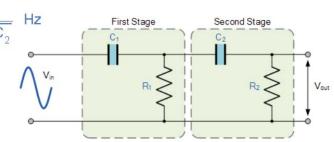
$$f_{\rm r} = \frac{1}{2\pi\sqrt{{
m R}_1{
m R}_2{
m C}_1{
m C}_2}} \qquad {
m Q}_{
m BP} = \frac{f_{
m r}}{{
m BW}_{
m (3dB)}} = \frac{1}{2}\sqrt{\frac{{
m R}_2}{{
m R}_1}}$$

Maximum Gain,
$$(Av) = -\frac{R_2}{2R_1} = -2Q^2$$

The High Pass Filter Circuit

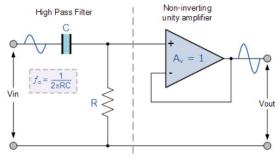
Second-order High Pass Filter

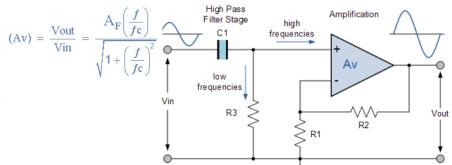




First Order High Pass Filter

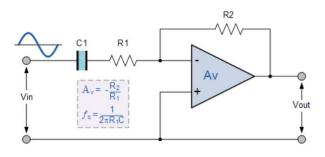
Active High Pass Filter with Amplification

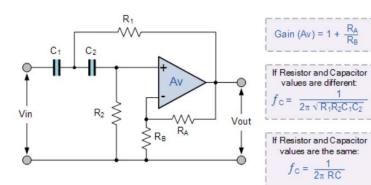




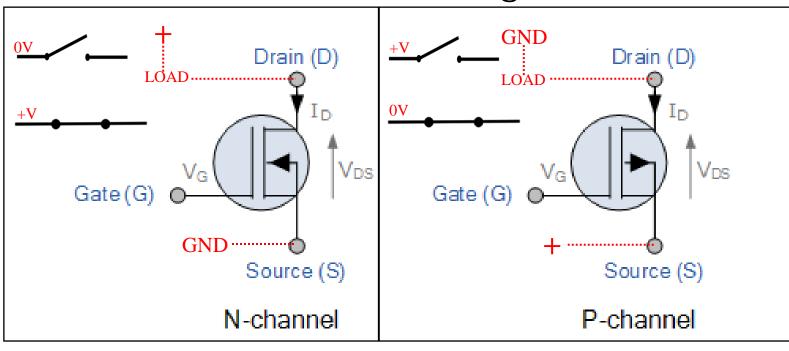
Second Order High Pass Filter

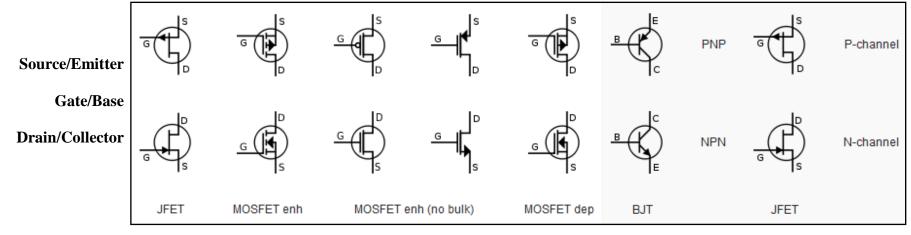
Inverting Operational Amplifier Circuit



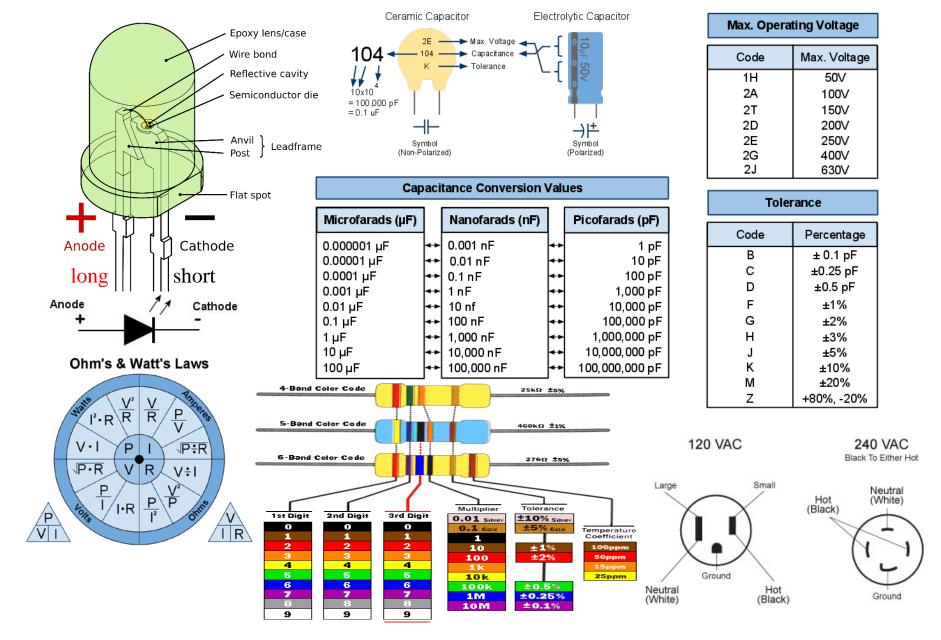


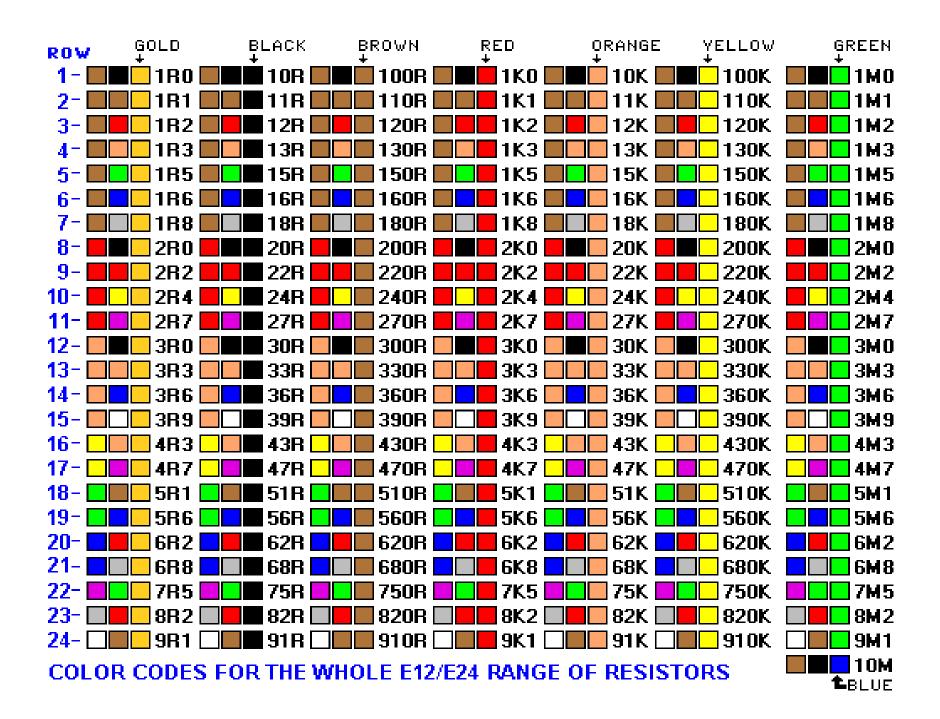
Transistor Logic





Capacitors





Energy E

(Measured in Joules J)

E = P * time

$$J = \frac{kg \cdot m^2}{s^2} = N \cdot m = Pa \cdot m^3 = W$$

Electric Charge

(Measured in Coulombs C)

$$1C = 1A \cdot 1s$$

$$1C = 1F \cdot 1V$$

Power P

(Measured in Watts W)

$$P = I^2 R = \frac{V^2}{R},$$

$$P = IV$$

$$W = \frac{J}{s} = \frac{N \cdot m}{s} = \frac{kg \cdot m^2}{s^3}$$

$$W = V \cdot A \qquad \qquad W = \frac{V^2}{\Omega} = A^2 \cdot \Omega$$

Resistance R

(Measured in Ohms Ω)

$$\Omega = \frac{V}{A} = \frac{m^2 \cdot kg}{s \cdot C^2} = \frac{J}{s \cdot A^2}$$

$$= \frac{kg \cdot m^2}{s^3 \cdot A^2} = \frac{J \cdot s}{C^2}$$

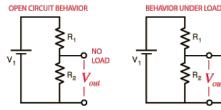
$$V = IR$$
 $R = \frac{v}{I}$ $I = \frac{v}{R}$

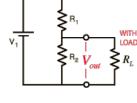
Conductance G

(Measured in Siemens S)

$$G = \frac{1}{R} = \frac{I}{V}$$

$$S = \Omega^{-1} = \frac{A}{V}$$





$$\mathrm{S} = \Omega^{-1} = rac{\mathrm{A}}{\mathrm{V}}$$
 $V_{out} = V_1 rac{IR_2}{I(R_1 + R_2)} = rac{V_1 R_2}{(R_1 + R_2)}$ OUTPUT VOLTAGE UNDER "NO LOAD" CONDITION (open circuit)

Inductance L

(Measured in Henries H)

OUTPUT VOLTAGE
$$V_{out} = V_1 \frac{IR_2}{I(R_1 + R_2)} = \frac{V_1(R_2 \parallel R_L)}{(R_1 + R_2 \parallel R_L)}$$

$$H = \frac{\mathbf{m}^2 \cdot \mathbf{kg}}{\mathbf{s}^2 \cdot \mathbf{A}^2} = \frac{\mathbf{J}}{\mathbf{A}^2} = \frac{\mathbf{Wb}}{\mathbf{A}} = \frac{\mathbf{s}^2}{\mathbf{F}} = \frac{\mathbf{V} \cdot \mathbf{s}}{\mathbf{A}}$$
$$= \frac{\mathbf{J}/\mathbf{C} \cdot \mathbf{s}}{\mathbf{C}/\mathbf{s}} = \frac{\mathbf{J} \cdot \mathbf{s}^2}{\mathbf{C}^2} = \frac{\mathbf{m}^2 \cdot \mathbf{kg}}{\mathbf{C}^2} = \Omega \cdot \mathbf{s}$$

Orders of magnitude for time common/easy conversions

kilo KHz
$$(10^3) \leftarrow \rightarrow ms (10^{-3})$$
 milli mega MHz $(10^6) \leftarrow \rightarrow us (10^{-6})$ micro giga GHz $(10^9) \leftarrow \rightarrow ns (10^{-9})$ nano

$$\frac{1}{5MHz} = \frac{1}{5} * \frac{1}{MHz} = \frac{1}{5} us = 0.2us$$

$$\frac{4}{2KHz} = \frac{4}{2} * \frac{1}{KHz} = \frac{4}{2} ms = 2ms$$

Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin
0	0		00000000	16	10		00010000	32	20		00100000	48	30		00110000
1	1	001	00000001	17	11	021	00010001	33	21	041	00100001	49	31	061	00110001
2	2	002	00000010	18	12		00010010	34	22	042	00100010	50	32	062	00110010
3	3	003	00000011	19	13	023	00010011	35	23	043	00100011	51	33	063	00110011
4	4	004	00000100	20	14	024	00010100	36	24		00100100	52	34	064	00110100
5	5	005	00000101	21	15	025	00010101	37	25	045	00100101	53	35	065	0011010
6	6	006	00000110	22	16	026	00010110	38	26	046	00100110	54	36	066	00110110
7	7	007	00000111	23	17	027	00010111	39	27	047	00100111	55	37	067	0011011
8	8	010	00001000	24	18	030	00011000	40	28	050	00101000	56	38	070	00111000
9	9	011	00001001	25	19		00011001	41	29	051	00101001	57	39	071	0011100
10	Α	012	00001010	26	1A	032	00011010	42	2A	052	00101010	58	3A	072	0011101
11	В	013	00001011	27	1B	033	00011011	43	2B	053	00101011	59	3B	073	0011101
12	С	014	00001100	28	1C	034	00011100	44	2C	054	00101100	60	3C	074	0011110
13	D	015	00001101	29	1D	035	00011101	45	2D	055	00101101	61	3D	075	0011110
14	Ε	016	00001110	30	1E	036	00011110	46	2E	056	00101110	62	3E	076	0011111
15	F	017	00001111	31	1F	037	00011111	47	2F	057	00101111	63	3F	077	0011111
Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin
64	40	100	01000000	80	50	120	01010000	96	60	140	01100000	112	70	160	0111000
65	41		01000001	81	51		01010001	97	61		01100001	113	71		0111000
66	42		01000010	82	52		01010010	98	62		01100010	114	72		0111001
67	43	103	01000011	83	53	123	01010011	99	63	143	01100011	115	73	163	0111001
68	44		01000100	84	54		01010100	100	64		01100100	116	74		0111010
69	45		01000101	85	55		01010101	101	65		01100101	117	75		0111010
70	46		01000110	86	56		01010110	102	66	146	01100110	118	76		0111011
	47	107	01000111	87	57		01010111	103	67	147	01100111	119	77		0111011
71	48		01001000	88	58		01011000	104	68		01101000	120	78		0111100
71 72	70		01001001	89	59		01011001	105	69		01101001	121	79		0111100
72		111					01011010	106	6A		01101010	122	7A		0111101
72 73	49			90	5A	132	01011010								
72 73 74	49 4A	112	01001010	90 91	5A 5B				6B	153	01101011				
72 73 74 75	49 4A 4B	112 113	01001010 01001011	91	5B	133	01011011	107	6B 6C		01101011 01101100	123	7B	173	0111101
72 73 74 75 76	49 4A 4B 4C	112 113 114	01001010 01001011 01001100	91 92	5B 5C	133 134	01011011 01011100	107 108	6C	154	01101100	123 124	7B 7C	173 174	0111101 0111110
72 73 74 75	49 4A 4B	112 113 114 115	01001010 01001011	91	5B	133 134 135	01011011	107		154 155	I	123	7B	173 174 175	0111101

Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin
128	80	200	10000000	144	90	220	10010000	160	A0	240	10100000	176	В0	260	10110000
129	81	201	10000001	145	91	221	10010001	161	A1	241	10100001	177	B1	261	10110001
130	82	202	10000010	146	92	222	10010010	162	A2	242	10100010	178	B2	262	10110010
131	83	203	10000011	147	93	223	10010011	163	A3	243	10100011	179	B3	263	10110011
132	84	204	10000100	148	94	224	10010100	164	A4	244	10100100	180	B4	264	10110100
133	85	205	10000101	149	95	225	10010101	165	A5	245	10100101	181	B5	265	10110101
134	86	206	10000110	150	96	226	10010110	166	A6	246	10100110	182	B6	266	10110110
135	87	207	10000111	151	97	227	10010111	167	A7	247	10100111	183	B7	267	10110111
136	88	210	10001000	152	98	230	10011000	168	A8	250	10101000	184	B8	270	10111000
137	89	211	10001001	153	99	231	10011001	169	A9	251	10101001	185	B9	271	10111001
138	8A	212	10001010	154	9A	232	10011010	170	AA	252	10101010	186	BA	272	10111010
139	8B	213	10001011	155	9B	233	10011011	171	AB	253	10101011	187	BB	273	10111011
140	8C	214	10001100	156	9C	234	10011100	172	AC	254	10101100	188	BC	274	10111100
141	8D	215	10001101	157	9D	235	10011101	173	AD	255	10101101	189	BD	275	10111101
142	8E	216	10001110	158	9E	236	10011110	174	AE	256	10101110	190	BE	276	10111110
143	8F	217	10001111	159	9F	237	10011111	175	AF	257	10101111	191	BF	277	10111111
Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin	Dec	Hex	Oct	Bin
	Hex C0		Bin 11000000	Dec 208	Hex D0		Bin 11010000	Dec 224	Hex E0		11100000	Dec 240	Hex F0		Bin 11110000
192		300				320				340				360	
192 193	CO	300 301	11000000	208	D0	320 321	11010000	224	E0	340 341	11100000	240	FO	360 361	11110000
192 193 194	C0 C1	300 301 302	11000000 11000001	208 209	D0 D1	320 321 322	11010000 11010001	224 225	E0 E1	340 341 342	11100000 11100001	240 241	F0 F1	360 361 362	11110000 11110001
192 193 194 195	C0 C1 C2	300 301 302 303	11000000 11000001 11000010	208 209 210	D0 D1 D2	320 321 322 323	11010000 11010001 11010010	224 225 226	E0 E1 E2	340 341 342 343	11100000 11100001 11100010	240 241 242	F0 F1 F2	360 361 362 363	11110000 11110001 11110010
192 193 194 195 196	C0 C1 C2 C3	300 301 302 303 304	11000000 11000001 11000010 11000011	208 209 210 211	D0 D1 D2 D3	320 321 322 323 324	11010000 11010001 11010010 11010011	224 225 226 227	E0 E1 E2 E3	340 341 342 343 344	11100000 11100001 11100010 11100011	240 241 242 243	F0 F1 F2 F3	360 361 362 363 364	11110000 11110001 11110010 11110011
192 193 194 195 196 197 198	C0 C1 C2 C3 C4	300 301 302 303 304 305 306	11000000 11000001 11000010 11000011 11000100 11000101 11000110	208 209 210 211 212	D0 D1 D2 D3 D4	320 321 322 323 324 325	11010000 11010001 11010010 11010011 11010100	224 225 226 227 228	E0 E1 E2 E3 E4	340 341 342 343 344 345	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244	F0 F1 F2 F3 F4	360 361 362 363 364 365	11110000 11110001 11110010 11110011 11110100
192 193 194 195 196 197 198	C0 C1 C2 C3 C4 C5	300 301 302 303 304 305 306	11000000 11000001 11000010 11000011 11000100 11000101	208 209 210 211 212 213	D0 D1 D2 D3 D4 D5	320 321 322 323 324 325 326	11010000 11010001 11010010 11010011 11010100 11010101	224 225 226 227 228 229	E0 E1 E2 E3 E4 E5	340 341 342 343 344 345 346	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245	F0 F1 F2 F3 F4 F5	360 361 362 363 364 365 366	11110000 11110001 11110010 11110011 11110100 11110101
192 193 194 195 196 197	C0 C1 C2 C3 C4 C5 C6	300 301 302 303 304 305 306 307	11000000 11000001 11000010 11000011 11000100 11000101 11000110	208 209 210 211 212 213 214	D0 D1 D2 D3 D4 D5 D6	320 321 322 323 324 325 326 327	11010000 11010001 11010010 11010011 11010100 11010101	224 225 226 227 228 229 230	E0 E1 E2 E3 E4 E5 E6	340 341 342 343 344 345 346 347	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246	F0 F1 F2 F3 F4 F5 F6	360 361 362 363 364 365 366 367	11110000 11110001 11110010 11110011 11110100 11110101 11110110
192 193 194 195 196 197 198	C0 C1 C2 C3 C4 C5 C6 C7	300 301 302 303 304 305 306 307 310	11000000 11000001 11000010 11000011 11000100 11000101 11000110 11000111	208 209 210 211 212 213 214 215	D0 D1 D2 D3 D4 D5 D6	320 321 322 323 324 325 326 327 330	11010000 11010001 11010010 11010011 11010100 11010101 11010110	224 225 226 227 228 229 230 231	E0 E1 E2 E3 E4 E5 E6	340 341 342 343 344 345 346 347 350	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247	F0 F1 F2 F3 F4 F5 F6	360 361 362 363 364 365 366 367 370 371	11110000 11110001 11110010 11110011 11110100 11110110
192 193 194 195 196 197 198 199 200	C0 C1 C2 C3 C4 C5 C6 C7 C8 C9	300 301 302 303 304 305 306 307 310 311	11000000 11000001 11000010 11000011 11000100 11000101 11000110 11000111 1100100	208 209 210 211 212 213 214 215 216	D0 D1 D2 D3 D4 D5 D6 D7	320 321 322 323 324 325 326 327 330 331	11010000 11010001 11010010 11010011 11010100 11010101 11010111 11010111	224 225 226 227 228 229 230 231 232	E0 E1 E2 E3 E4 E5 E6 E7 E8	340 341 342 343 344 345 346 347 350 351	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247 248	F0 F1 F2 F3 F4 F5 F6 F7	360 361 362 363 364 365 366 367 370 371	11110000 11110001 11110010 11110011 11110100 11110110
192 193 194 195 196 197 198 199 200 201 202	C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA	300 301 302 303 304 305 306 307 310 311 312	11000000 11000001 11000010 11000011 11000100 11000101 11000110 1100100	208 209 210 211 212 213 214 215 216 217	D0 D1 D2 D3 D4 D5 D6 D7 D8	320 321 322 323 324 325 326 327 330 331 332	11010000 11010001 11010010 11010011 11010100 11010101 11010111 11010111 110110	224 225 226 227 228 229 230 231 232 233	E0 E1 E2 E3 E4 E5 E6 E7 E8 E9	340 341 342 343 344 345 346 347 350 351 352	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247 248 249	F0 F1 F2 F3 F4 F5 F6 F7 F8	360 361 362 363 364 365 366 367 370 371 372	11110000 11110001 11110010 11110011 11110100 11110110
192 193 194 195 196 197 198 199 200	C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA CB	300 301 302 303 304 305 306 307 310 311 312 313	11000000 11000001 11000010 11000011 11000100 11000101 11000111 1100100	208 209 210 211 212 213 214 215 216 217 218	D0 D1 D2 D3 D4 D5 D6 D7 D8 D9	320 321 322 323 324 325 326 327 330 331 332 333	11010000 11010001 11010010 11010011 11010100 11010110 11010111 110110	224 225 226 227 228 229 230 231 232 233 234	E0 E1 E2 E3 E4 E5 E6 E7 E8 E9 EA	340 341 342 343 344 345 346 347 350 351 352 353	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247 248 249 250	F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA	360 361 362 363 364 365 366 367 370 371 372 373	11110000 11110010 11110011 11110100 11110101 11110110
192 193 194 195 196 197 198 199 200 201 202 203	C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA CB	300 301 302 303 304 305 306 307 310 311 312 313 314	11000000 11000001 11000010 11000011 11000100 11000101 11000111 1100100	208 209 210 211 212 213 214 215 216 217 218 219	D0 D1 D2 D3 D4 D5 D6 D7 D8 D9 DA	320 321 322 323 324 325 326 327 330 331 332 333 334	11010000 11010001 11010010 11010011 11010100 11010110 11010111 110110	224 225 226 227 228 229 230 231 232 233 234 235	E0 E1 E2 E3 E4 E5 E6 E7 E8 E9 EA	340 341 342 343 344 345 346 347 350 351 352 353 354	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247 248 249 250 251 252	F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA FB FC	360 361 362 363 364 365 366 367 370 371 372 373 374	11110000 11110001 11110010 11110011 11110100 11110110
92 93 94 95 96 97 98 99 200 201 202 203	C0 C1 C2 C3 C4 C5 C6 C7 C8 C9 CA CB CC	300 301 302 303 304 305 306 307 310 311 312 313 314 315	11000000 11000001 11000010 11000011 11000100 11000101 11000111 1100100	208 209 210 211 212 213 214 215 216 217 218 219 220	D0 D1 D2 D3 D4 D5 D6 D7 D8 D9 DA DB	320 321 322 323 324 325 326 327 330 331 332 333 334 335	11010000 11010001 11010010 11010011 11010100 11010110 11010111 110110	224 225 226 227 228 229 230 231 232 233 234 235 236	E0 E1 E2 E3 E4 E5 E6 E7 E8 E9 EA EB EC	340 341 342 343 344 345 346 347 350 351 352 353 354 355	11100000 11100001 11100010 11100011 11100100	240 241 242 243 244 245 246 247 248 249 250 251 252	F0 F1 F2 F3 F4 F5 F6 F7 F8 F9 FA FB FC	360 361 362 363 364 365 366 367 370 371 372 373 374 375	11110000 11110001 11110010 11110011 11110100 11110110

	bit	byte	Kilobyte	Megabyte	Gigabyte
bit	1	8	8,192	8,388,608	8,589,934,592
byte	8	1	1,024	1,048,576	1,073,741,824
Kilobyte	8,192	1,024	1	1,024	1,048,576
Megabyte	8,388,608	1,048,576	1,024	1	1,024
Gigabyte	8,589,934,592	1,073,741,824	1,048,576	1,024	1
Terabyte	8,796,093,022,208	1,099,511,627,776	1,073,741,824	1,048,576	1,024
Petabyte	9,007,199,254,740,990	1,125,899,906,842,620	1,099,511,627,776	1,073,741,824	1,048,576
Exabyte	9,223,372,036,854,780,000	1,152,921,504,606,850,000	1,125,899,906,842,620	1,099,511,627,776	1,073,741,824
Zettabyte	9,444,732,965,739,290,000,000	1,180,591,620,717,410,000,00	0 1,152,921,504,606,850,000	1,125,899,906,842,620	1,099,511,627,77

2 ⁿ	dec	hex	2 ⁿ	dec	hex
2^{0}	0	0	2^{11}	2048	800
2^1	2	2	2^{12}	4096	1000
2^2	4	4	2^{13}	8192	2000
2^3	8	8	2^{14}	16,384	4000
2^{4}	16	10	2^{15}	32,768	8000
2^{5}	32	20	2^{16}	65,536	10,000
2^{6}	64	40	2^{17}	131,072	20,000
2^{7}	128	80	2^{18}	262,144	40,000
2^{8}	256	100	2^{19}	524,288	80,000
2^{9}	512	200	2^{20}	1,048,576	100,000
2^{10}	1024	400	2^{21}	2,097,152	200,000