## spellingcorrector

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A simple spelling corrector Inspired by the one found on Peter Norvig's page (https://norvig.com/spell-correct.html). It finds the correction c maximizing the conditional probability  $P(c \mid w)$  that c is the "right" word given that the user entered w.

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By Bayes law: P(c \mid w) = P(w \mid c) P(c) / P(w)
```

About these probabilities:

 $P(w \mid c)$  is modeled as a function of edits needed to transform w into c. The number of edits is supposed to follow a binomial distribution.

**P(c)** is the "language model", telling us how much c is likely to occur. This is estimated from data. **P(w)** is the same for all c and can be ignored.

The file big.txt is used to estimate P(c). It can be downloaded from Norvig's page: https://norvig.com/big.txt

Any other large file of text could be used instead.

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[3]: # Necessary imports.
     import sys
     import math
     # Read the source file content.
     # Return a dictionary mapping (lowercase) words to probabilities
     def read_words(filename):
         counters = {}
         total = 0
         f = open(filename)
         for line in f:
             for word in line.lower().split():
                 # exclude strings including non-alphabetic characters
                 if word.isalpha():
                     if word in counters:
                         counters[word] += 1
                     else:
                         counters[word] = 1
                     total += 1
         probs = {}
         for word in counters:
             probs[word] = counters[word] / total
         return probs
```

```
[4]: # Edits for the given word.
     def edit1(word):
         # Set of single editings starting from the given word.
         n = len(word)
         letters = "abcdefghijklmnopqrstuvwxyz"
         variations = set()
         # Deletions
         for i in range(n):
             newword = word[:i] + word[(i + 1):]
             variations.add(newword)
         # Substitutions
         for i in range(n):
             for 1 in letters:
                 if l != word[i]:
                     newword = word[:i] + 1 + word[(i + 1):]
                     variations.add(newword)
         # Insertions
         for i in range(n + 1):
             for 1 in letters:
                 newword = word[:i] + 1 + word[i:]
                 variations.add(newword)
         # Inversions
         for i in range(n - 1):
             newword = word[:i] + word[i + 1] + word[i] + word[(i + 2):]
             variations.add(newword)
         return variations
[5]: # Set of editings obtained with k operations from the given word.
     def edit_k(word, k):
         variations = {word}
         for _ in range(k):
             newvars = set()
             for v in variations:
                 newvars |= edit1(v)
             variations = newvars
         return variations
     \# Binomial coefficient 'n choose k'.
     def binomial_coefficient(n, k):
         denominator = math.factorial(k) * math.factorial(n - k)
         return math.factorial(n) // denominator
     # Formula to count P(w|c) given n, e, q - probability of e errors on a word of
      \rightarrow length n.
     def probability_error(n, e, q):
         binc = binomial_coefficient(n, e)
         return binc * (q ** e) * ((1-q) ** (n - e))
```

```
[6]: # Spelling corrector.
     def correct_word(word, dictionary):
         q = 0.01
         candidates = []
         for e in range(3):
             variations = edit_k(word, e)
             for c in variations:
                 if c in dictionary:
                     p_c = dictionary.get(c)
                     p_wc = probability_error(len(c), e, q)
                     score = p_wc * p_c
                     candidates.append((score, c))
         candidates = candidates[:5]
         candidates.sort(reverse=True)
         return candidates
     dictionary = read_words("big.txt")
     word = input("Enter a word: ").lower()
     candidates = correct_word(word, dictionary)
     for score, c in candidates:
         print(c)
     print(candidates)
    Enter a word: frnak
    frank
    freak
    creak
    prank
    crank
    [(1.2059752748332442e-06, 'frank'), (1.0486741520289079e-07, 'freak'),
    (7.414867741618542e-09, 'creak'), (3.1778004606936607e-09, 'prank'),
    (1.0592668202312202e-09, 'crank')]
```

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