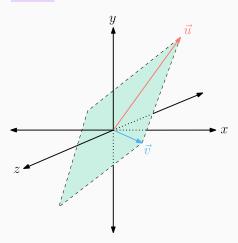
## **Subspaces**

Similarly, any non-zero vector in  $\mathbb{R}^3$  also spans a line going through the origin. In addition, any two linearly independent vectors span a **plane** going through the origin.

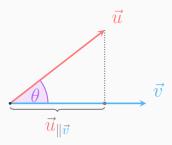


## The Dot Product

If we rotate the two vectors such that one of them lies on the horizontal direction, we can draw a perpendicular line from  $\vec{u}$  to  $\vec{v}$ . Using trigonometry we get

$$\cos(\theta) = \frac{\vec{u}_{\parallel \vec{v}}}{\parallel \vec{u} \parallel},$$

where  $\vec{u}_{\parallel \vec{v}}$  is the length of the projection of  $\vec{u}$  on  $\vec{v}$ .



## The Cross Product

