

Finite Complete Suites for CSP Refinement Testing

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Abstract. In this paper, new contributions to testing Communicating Sequential Processes (CSP) are presented. The focus of these contributions is on the generation of complete, finite test suites. Test suites are complete if they can guarantee to uncover every conformance violation of the system under test (SUT) with respect to a reference model. Both reference models and implementations are represented as CSP processes. As conformance relation, we consider trace equivalence and trace refinement, as well as failures equivalence and failures refinement. Complete black-box test suites rely on the fact that the SUT's true behaviour is represented by a member of a fault-domain, that is, a collection of CSP processes that may or may not conform to the reference model. We define fault domains by bounding the number of excessive states occurring in a fault domain member's representation as normalised transition graph, when comparing it to the number of states present in the graph of the reference model. This notion of fault domains is quite close to the way they are defined for finite state machines. These fault domains guarantee the existence of finite complete test suites.

Keywords: Model-based testing, Complete testing theories, CSP, Refinement

1 Introduction

Motivation Model-based testing (MBT) is an active research field which is currently evaluated and integrated into industrial verification processes by many companies. This holds particularly for the embedded and cyber-physical systems domain. While MBT is applied in different flavours, we consider the variant to be the most effective one, where test cases and concrete test data, as well as checkers for the expected results are automatically generated from a reference model: it guarantees the maximal return of investment for the time and effort invested into creating the test model. The test suites generated in this way, however, usually have different test strength, depending on then generation algorithms applied.

For the safety-critical systems domain, test suites with guaranteed fault coverage are of particular interest. For black-box testing, these guarantees can only be given under certain hypotheses. These hypotheses are usually identified by specifying a *fault domain*; this is a set of models that may or may not conform to the SUT. The so-called *complete* test strategies guarantee to uncover very conformance violation of the SUT with respect to a reference model, provided that the true SUT behaviour has been captured by a member of the fault domain.

Generation methods for complete test suites have been developed for various modelling formalisms. In this paper, we use *Communicating Sequential Processes (CSP)* [3, 12]; this is a mature process-algebraic approach which has been shown to be well-suited for the description of reactive control systems in many publications over almost 5 decades.

Contributions This paper complements work published by two of the authors in [1]. There, fault domains have been specified as collections of processes refining a “most general” fault domain member. With this concept of fault domains, complete test suites may be finite or infinite. While this gives important insight into the theory of complete test suites, we are particularly interested in finite suites when it comes to their practical application.

Therefore, we present a complementary approach to the definition of CSP fault domains in this paper. To this end, we observe that every CSP process can be semantically represented as a normalised transition graph, whose edges are labelled by the events the process engages in, and whose nodes are labelled by minimal acceptances or, alternatively, maximal refusals [11]. The minimal acceptances express the degree of nondeterminism that is present in a given CSP process state which is in one-one-correspondence to a node of the normalised transition graph. Inspired by the way that fault-domains are specified for finite state machines (FSMs), we define them here as the set of CSP processes whose normalised transition graphs do not exceed the size of the reference model’s graph by more than a give constant.

Our main contributions in this paper are as follows.

1. It is proven that for fault domains of the described type, complete test suite generation methods can be given for verifying (1) Trace equivalence, (2) trace refinement, (3) failures equivalence, and (4) failures refinement.
2. We prove that finite complete test suites can be generated in all 4 cases.
3. We present test suite generation techniques for each of the 4 conformance relations by translating algorithms originally elaborated for the FSM domain into the CSP world. This translation preserves the completeness properties that have previously been established for the FSM domain by other authors.

Overview @todo

2 Preliminaries

2.1 Complete Testing Theories

Fault Models, Test Cases, Test Suites, and Completeness We use the term *signature* to denote a collection of comparable models represented in an arbitrary formalism. In this article, signatures represent sets of finite state machines over fixed input and output alphabets, or CSP processes with finite state, represented by their normalised transition graphs.

Given a signature Sig of models, a *fault model* $\mathcal{F} = (M, \leq, Dom)$ specifies a *reference model* $M \in Sig$, a *conformance relation* $\leq \subseteq Sig \times Sig$ between models, and a *fault domain* $Dom \subseteq Sig$. This terminology follows [9], where fault models were originally introduced in the context of finite state machine testing. Note that fault domains may contain both models conforming to the reference model and models violating the conformance relation. Note further that the reference model M is not necessarily a member of the fault domain. For example, M could be nondeterministic, while only deterministic implementation behaviours might be considered in the fault domain. By $F(Sig, \leq)$ we denote the set of all fault models \mathcal{F} defined for signature Sig and conformance relation \leq .

Let $TC(Sig)$ denote the set of all *test cases* applicable to elements of Sig . The abstract notion of test cases defined here only requires the existence of a relation $\underline{\text{pass}} \subseteq Sig \times TC(Sig)$. For $(M, U) \in \underline{\text{pass}}$, the infix notation $M \underline{\text{pass}} U$ is used, and interpreted as ‘Model M passes the test case U ’. If $(M, U) \notin \underline{\text{pass}}$ holds, this is abbreviated by $M \underline{\text{fail}} U$.

A *test suite* $TS \subseteq TC(Sig)$ denotes a set of test cases. A model M *passes the test suite* TS , also written as $M \underline{\text{pass}} TS$, if and only if $M \underline{\text{pass}} U$ for all $U \in TS$. A test suite TS is called *complete* for fault model $\mathcal{F} = (M, \leq, Dom)$, if and only if the following properties hold.

1. If a member M' of the fault domain conforms to the reference model M , it passes the test suite, that is,

$$\forall M' \in Dom : M' \leq M \Rightarrow M' \underline{\text{pass}} TS$$

This property is usually called *soundness* of the test suite.

2. If a member of the fault domain passes the test suite, it conforms to the reference model, that is,

$$\forall M' \in Dom : M' \underline{\text{pass}} TS \Rightarrow M' \leq M$$

This property is usually called *exhaustiveness*.

A test suite TS is *finite* if it contains finitely many test cases and every test case $U \in TS$ is finite in the sense that it terminates after a finite number of steps. It is trivial to see that, if TS is complete for $\mathcal{F} = (M, \leq, Dom)$ and $Dom' \subseteq Dom$, then TS is also complete for $\mathcal{F}' = (M, \leq, Dom')$.

2.2 Translation of Testing Theories

Let Sig_1 and Sig_2 be two signatures with conformance relations \leq_1 and \leq_2 , and test case relations $\underline{\text{pass}}_1$ and $\underline{\text{pass}}_2$, respectively. A function $T : Sig_1 \rightarrow Sig_2$

defined on a sub-domain $\underline{Sig}_1 \subseteq Sig_1$ is called a *model map*, and a function $T^* : TC(Sig_2) \rightarrow TC(Sig_1)$ is called a *test case map*. Note that models and test cases are mapped in opposite directions (see Fig. 1). The pair (T, T^*) fulfils the *satisfaction condition* if and only if the following conditions **SC1** and **SC2** are fulfilled.

SC1 The model map is compatible with the conformance relations under consideration, in the sense that

$$\forall \mathcal{S}, \mathcal{S}' \in \underline{Sig}_1 : \mathcal{S}' \leq_1 \mathcal{S} \Leftrightarrow T(\mathcal{S}') \leq_2 T(\mathcal{S}),$$

so the left-hand side diagram in Fig. 1 commutes due to the fact that $T; \leq_2 = \leq_1; T$.⁴

SC2 Model map and test case map preserve the pass-relationship in the sense that

$$\forall \mathcal{S} \in \underline{Sig}_1, U \in TC(Sig_2) : T(\mathcal{S}) \underline{pass}_2 U \Leftrightarrow \mathcal{S} \underline{pass}_1 T^*(U),$$

so the right-hand side diagram in Fig. 1 commutes, due to the fact that $\underline{pass}_1 = T; \underline{pass}_2; T^*$.

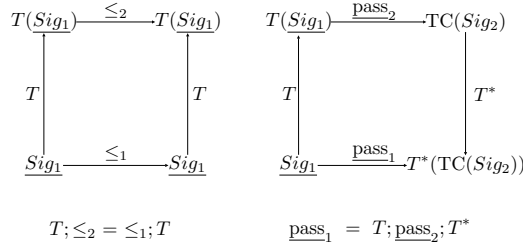


Fig. 1. Commuting diagrams reflecting the satisfaction condition.

The following theorem is a direct consequence of [4, Theorem 2.1].

Theorem 1. *With the notation introduced above, let (T, T^*) fulfil the satisfaction condition. Suppose that $TS_2 \subseteq TC(Sig_2)$ is a complete test suite for fault model $\mathcal{F}_2 = (\mathcal{S}_2, \leq_2, Dom_2)$. Define fault model \mathcal{F}_1 on \underline{Sig}_1 by*

$$\mathcal{F}_1 = (\mathcal{S}_1, \leq_1, Dom_1), \text{ such that } T(\mathcal{S}_1) = \mathcal{S}_2 \text{ and } Dom_1 = \{\mathcal{S} \mid T(\mathcal{S}) \in Dom_2\}.$$

Then

$$TS_1 = T^*(TS_2)$$

is a complete test suite with respect to fault model \mathcal{F}_1 .

□

⁴ Operator “;” denotes the relational composition defined for functions or relations $f \subseteq A \times B$, $g \subseteq B \times C$ by $f; g = \{(a, c) \in A \times C \mid \exists b \in B : (a, b) \in f \wedge (b, c) \in g\}$. Note that $f; g$ is evaluated from left to right (like composition of code fragments), as opposed to right-to-left evaluation which is usually denoted by $g \circ f$.

2.3 CSP and Refinement

Normalised Transition Graphs As shown in [11], any finite-state CSP process P can be represented by a *normalised transition graph*

$$G(P) = (N, \underline{n}, \Sigma, t : N \times \Sigma \rightarrow N, ac : N \rightarrow \mathbb{P}(\Sigma)),$$

with nodes N , initial node $\underline{n} \in N$, and process alphabet Σ . The partial *transition function* t maps a node n and an event $e \in \Sigma$ to its successor node $t(n, e)$, if and only if (n, e) are in the domain of t . Normalisation of $G(P)$ is reflected by the fact that t is a function. The total function a maps each node to its set of *minimal acceptances*: if $n \in N$ corresponds to a deterministic process state of P , $ac(n)$ contains a single acceptance $A \subseteq \Sigma$, and every $e \in A$ is in one-one-correspondence with a transition $t(n, e)$. If n corresponds to a nondeterministic process state, $ac(n)$ contains at least two acceptances A_1, A_2, \dots, A_k . This reflects the fact that in a nondeterministic state, P must accept all events of one acceptance $A_i, i \in \{1, \dots, k\}$, but may refuse all events e from $A_j \setminus A_i, j \neq i$.

Each well-defined transition graph $G(P)$ fulfils the following condition. The union of all minimal acceptances in each node corresponds to the set of events labelling its outgoing transitions.

$$\forall n \in N : (n, e) \in \text{dom } t \Leftrightarrow e \in \bigcup ac(n) \quad (1)$$

In this condition, $\text{dom } t$ denotes the domain of function t .

By construction, normalised transition graphs reflect the failures semantics of finite-state CSP processes: the traces s of a process are exactly the paths through the transition graph, starting at \underline{n} . The maximal refusals in each process state P/s are the complements of the minimal acceptances of the node n corresponding to P/s . As a consequences, all failures of P are represented by some (s, R) , where s is an initialised path through the transition graph and $R \subseteq (\Sigma - A)$ for some minimal acceptance $A \in ac(n)$, such that n is the node corresponding to P/s .

Example 1. Consider CSP process

$$\begin{aligned} P &= a \rightarrow (Q \sqcap R) \\ Q &= a \rightarrow P \sqcap c \rightarrow P \\ R &= b \rightarrow P \sqcap c \rightarrow R \end{aligned}$$

Its transition graph $G(P)$ is shown in Fig. 2. Process state P is represented there as Node_0, with $\{a\}$ as the only acceptance, since event a can never be refused, and no other events are accepted. Having engaged into a , the transition emanating from Node_0 leads to Node_2 representing the process state $P/a = Q \sqcap R$. The internal choice operator induces several acceptance sets derived from Q and R . Since these processes accept their initial events with external choice, process $Q \sqcap R$ induces just two minimal acceptance sets $\{a, c\} = [Q]^0$ and $\{b, c\} = [R]^0$. Note that event c can never be refused, since it is a member of all minimal acceptances.

Having engaged into c , the next process state is represented by Node_1. Due to normalisation, there was only a single transition satisfying $t(\text{Node}_2, c) = \text{Node}_1$. This transition, however, can have been caused by either Q or R engaging into c , so Node_1 corresponds to process state $Q/c \sqcap R/c = P \sqcap R$. This is reflected by the two minimal acceptances labelling Node_1. \square

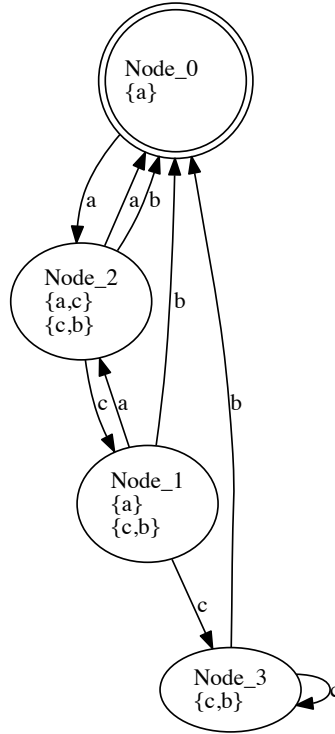


Fig. 2. Normalised transition graph of CSP process P from Example 1.

2.4 Finite State Machines

To make this paper sufficiently self-contained, we introduce definitions, notation, and facts about finite state machines (FSMs) that have been originally described in contributions on FSM testing, such as [8, 10, 2].

A *Finite State Machine (FSM)* is a tuple $M = (Q, \underline{q}, \Sigma_I, \Sigma_O, h)$ with state space Q , input alphabet Σ_I , output alphabet Σ_O , where Q, Σ_I, Σ_O are finite and nonempty sets. $\underline{q} \in Q$ denotes the initial state. $h \subseteq Q \times \Sigma_I \times \Sigma_O \times Q$ is the transition relation, $(q, x, y, q') \in h$ if and only if there is a transition from q to q' with input x and output y . We use both set notation $(q, x, y, q') \in h$ and Boolean notation $h(q, x, y, q')$ for specifying that (q, x, y, q') is a transition in h . We call x a *defined* input in state q , if there is a transition from q with input x . If every input of Σ_I is defined in every state, M is *completely specified*. If in every state q and for every output $y \in \Sigma_O$, and input x and a post-state q' satisfying $h(q, x, y, q')$ exists, the FSM is called *output complete*.

FSM M is called a *deterministic FSM (DFSM)*, if for any state q and defined input x , $h(q, x, y, q') \wedge h(q, x, y', q'')$ implies $(y, q') = (y', q'')$. Intuitively speaking, a specific input applied to a specific state uniquely determines both post-state and associated output. If M is not deterministic, it is called a *non-deterministic FSM (NFSM)*. If there is no emanating transition for $q \in Q$, this state is called a *deadlock state*, and M *terminates in* q . The set of deadlock states is denoted by $\text{deadlock}(Q) \subseteq Q$. The set of states that do not deadlock is denoted by $\text{DF}(Q) = \{q \in Q \mid \exists (q', x, y, q'') \in h : q' = q\}$.

The transition relation h can be extended in a natural way to input traces: let \bar{x} be an input trace and \bar{y} an output trace. Then $(q, \bar{x}, \bar{y}, q') \in h$, if and only if there is a transition sequence from q to q' with input trace \bar{x} and output trace \bar{y} . If q is the initial state \underline{q} , such a transition sequence is called an *execution* of M . Executions are written in the notation

$$q_0 \xrightarrow{x_1/y_1} q_1 \xrightarrow{x_2/y_2} \dots \xrightarrow{x_k/y_k} q_k$$

with $q_0 = \underline{q}$, $h(q_{i-1}, x_i, y_i, q_i)$ for $i = 1, \dots, k$, and $\bar{x} = x_1 \dots x_k$ and $\bar{y} = y_1 \dots y_k$.

The empty trace is denoted by ε , and $(q, \varepsilon, \varepsilon, q) \in h$, for any state q . A *language* of an FSM M is the set consisting of all possible input/output traces in M ; we use notation $L_M(q) = \{\bar{x}/\bar{y} \mid \exists q' \in Q : h(q, \bar{x}, \bar{y}, q')\}$ for $q \in Q$, and $L(M) = L_M(\underline{q})$. By $\text{FSM}(\Sigma_I, \Sigma_O)$ we denote the set of all FSMs with input alphabet Σ_I and output alphabet Σ_O .

An FSM M is called *observable* if in every state q , every existing post-state q' is uniquely determined by the I/O pair x/y satisfying $h(q, x, y, q')$. For observable state machines, the partial function

$$h_1 : Q \times \Sigma_I \times \Sigma_O \rightarrow Q; \quad h_1(q, x, y) = q' \Leftrightarrow h(q, x, y, q')$$

is well-defined. Deterministic FSMs are always observable.

Two FSM M_1, M_2 are *I/O-equivalent* ($M_1 \sim M_2$) if and only if their languages coincide, i.e. $L(M_1) = L(M_2)$. FSM M_1 is a *reduction of* M_2 ($M_1 \preceq M_2$), if and only if $L(M_1) \subseteq L(M_2)$. I/O-equivalence is also called *trace equivalence* by some authors, see, e.g. [5].

FSMs can be composed in parallel by synchronising over common input/output events: Let FSMs $M_i = (Q_i, \underline{q}_i, \Sigma_I, \Sigma_O, h_i)$, $i = 1, 2$ be defined over the same input/output alphabets. Then

$$M_1 \cap M_2 = (Q_1 \times Q_2, (\underline{q}_1, \underline{q}_2), \Sigma_I, \Sigma_O, h)$$

where the transition relation is specified by

$$h((q_1, q_2), x, y, (q'_1, q'_2)) \Leftrightarrow h_1(q_1, x, y, q'_1) \wedge h_2(q_2, x, y, q'_2)$$

By construction, $L(M_1 \cap M_2) = L(M_1) \cap L(M_2)$. Every execution

$$(\underline{q_1}, \underline{q_2}) \xrightarrow{x_1/y_1} (q_1^1, q_2^1) \xrightarrow{x_2/y_2} \dots \xrightarrow{x_k/y_k} (q_1^k, q_2^k)$$

of $M_1 \cap M_2$ is composed of executions

$$\underline{q_1} \xrightarrow{x_1/y_1} q_1^1 \xrightarrow{x_2/y_2} \dots \xrightarrow{x_k/y_k} q_1^k \text{ of } M_1 \text{ and } \underline{q_2} \xrightarrow{x_1/y_1} q_2^1 \xrightarrow{x_2/y_2} \dots \xrightarrow{x_k/y_k} q_2^k \text{ of } M_2$$

3 Finite Complete Testing Theories for CSP

3.1 A Model Map from CSP Processes to Finite State Machines

We will now construct a model map for associating CSP processes represented by normalised transition graphs to finite state machines. The intuition behind this construction is that the finite state machine's input alphabet corresponds to *sets of inputs* that may be offered to a CSP process. Depending on the events contained in this set, the process may (1) accept all of them, (2) accept some of them while refusing others, and (3) refuse all of them. This is reflected in the FSM by output events that represent events that the process really has engaged in and an extra event \perp representing deadlock, if the set of events has been refused.

More formally, we fix a finite CSP process alphabet Σ and consider a finite-state process P over this alphabet with normalised transition graph $G(P) = (N, \underline{n}, \Sigma, t : N \times \Sigma \rightarrow N, ac : N \rightarrow \mathbb{PP}(\Sigma))$, then the model map T maps P to the following observable FSM $T(P) = (Q, \underline{q}, \Sigma_I, \Sigma_O, h)$ satisfying

$$\begin{aligned} Q &= N \cup \{\text{DL}\} \\ \underline{q} &= \underline{n} \\ \Sigma_I &= \mathbb{P}(\Sigma) - \{\emptyset\} \\ \Sigma_O &= \Sigma \cup \{\perp\} \\ h &= \{(n, A, e, n') \mid A \in \Sigma_I \wedge e \in A \wedge (n, e) \in \text{dom } t \wedge t(n, e) = n'\} \cup \\ &\quad \{(n, A, \perp, \text{DL}) \mid A \in \Sigma_I \wedge \exists A' \in ac(n) \wedge A \cap A' = \emptyset\} \end{aligned}$$

We say that FSM trace $(x/s) \in L(T(P))$ and CSP trace $s' \in \text{tr}(P)$ are *corresponding traces*, if $s' = s \upharpoonright \Sigma$. Observe that the FSM output trace s may contain deadlock events \perp that are not contained in the CSP process alphabet Σ .

Example 2. For the CSP process P and its transition graph $G(P)$ discussed in Example 1, the FSM $T(P)$ is depicted in Fig. 3. For displaying its transitions, we used notation

$$\forall A : \text{condition}/e$$

which stands for a set of transitions between the respective nodes: one transition per non-empty set $A \subseteq \Sigma$ fulfilling the specified condition. The arrow $\text{Node_0} \longrightarrow \text{Node_2}$ labelled by $\forall A : a \in A/a$, for example, stands for FSM transitions

$$\begin{aligned} \text{Node_0} &\xrightarrow{\{a\}/a} \text{Node_2} \\ \text{Node_0} &\xrightarrow{\{a,b\}/a} \text{Node_2} \\ \text{Node_0} &\xrightarrow{\{a,c\}/a} \text{Node_2} \\ \text{Node_0} &\xrightarrow{\{a,b,c\}/a} \text{Node_2} \end{aligned}$$

□

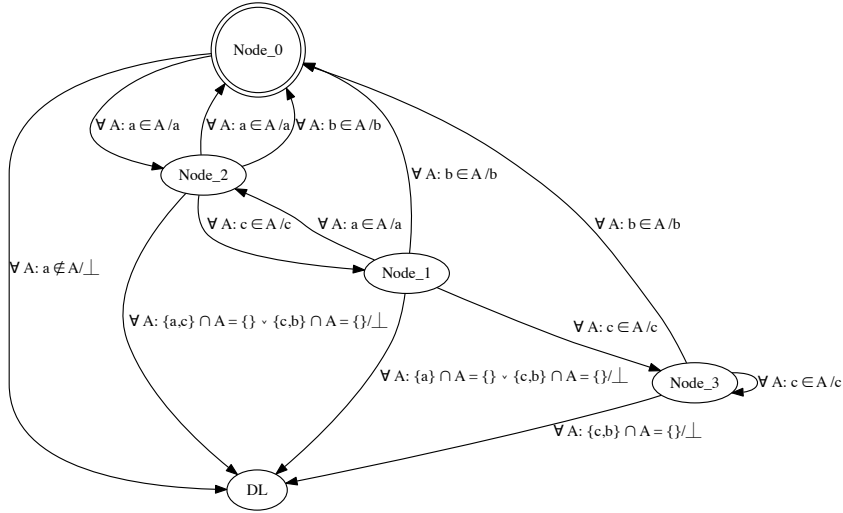


Fig. 3. FSM resulting from applying the model map to CSP process P from Example 1.

We are now in the position to state and prove the theorem about the model map fulfilling the satisfaction condition **SC1** introduced in Section 2.2. To this end, we first introduce three lemmas.

Lemma 1. *Let $s \in \Sigma^*$ be any trace of P . Let \underline{n} be the initial node of $G(P)$ and the initial state of $T(P)$. Let n be the node of $G(P)$ denoting the process state P/s . Then for any input sequences $x \in \Sigma_I^*$ satisfying $\#x = \#s = k$ and $s(i) \in x(i)$, $\forall i \leq k$, we have $x/s \in L(T(P))$ and \underline{n} -after- $x/s = n$. Furthermore, for any $B \in \Sigma_I$,*

$$B \in \text{Ref}(P/s) \Leftrightarrow (x/s).(B/\perp) \in L(T(P))$$

Conversely, any $x/s \in L(T(P))$ fulfils either

1. $s \in \text{tr}(P)$ and $s(i) \in x(i), \forall i \leq \#(x/s)$, or
2. $x/s = (x'.x_k)/(s'.\perp)$ with $s' \in \text{tr}(P)$, $s(i) \in x(i), \forall i < \#(x/s)$ and $x_k \in \text{Ref}(P/s')$.

The following lemmas are a direct consequence of Lemma 1.

Lemma 2. For any $s \in \Sigma^*$,

$$s \in \text{tr}(P) \Leftrightarrow \exists x \in \Sigma_I^* : x/s \in L(T(P))$$

Lemma 3. For any $s \in \Sigma^*$ and $x_k \in \Sigma_I$,

$$s \in \text{tr}(P) \wedge x_k \in \text{Ref}(P/s) \Leftrightarrow \exists x \in \Sigma_I^* : x.x_k/s.\perp \in L(T(P))$$

Theorem 2. Consider the signature Sig_1 of CSP processes over fixed alphabet Σ and the model map T from CSP processes to finite state machines specified above. Then the satisfaction condition **SC1** is valid in the sense that

$$\forall P, Q \in \text{Sig}_1 : P \sqsubseteq_F Q \Leftrightarrow T(Q) \preceq T(P),$$

where \sqsubseteq_F denotes failures refinement and \preceq denotes reduction.

Proof. Applying the lemmas above, we can derive the following sequence of equivalence transformations.

$$\begin{aligned} T(Q) \preceq T(P) &\Leftrightarrow L(T(Q)) \subseteq L(T(P)) \\ &\Leftrightarrow \forall x/s \in L(T(Q)) : x/s \in L(T(P)) \\ &\Leftrightarrow (\forall x/s \in L(T(Q)) : s \in \Sigma^* \Rightarrow x/s \in L(T(P))) \wedge \\ &\quad (\forall (x.x_k)/(s.\perp) \in L(T(Q)) : s \in \Sigma^* \Rightarrow (x.x_k)/(s.\perp) \in L(T(P))) \\ &\Leftrightarrow (\forall s \in \text{tr}(Q), x \in \{z \in \Sigma_I^* \mid z/s \in L(T(Q))\} : \\ &\quad s \in \text{tr}(P) \wedge x/s \in L(T(P))) \wedge \\ &\quad (\forall s \in \text{tr}(Q), x \in \{z \in \Sigma_I^* \mid z/s \in L(T(Q))\}, x_k \in \text{Ref}(Q/s) : \\ &\quad s \in \text{tr}(P) \wedge x/s \in L(T(P)) \wedge x_k \in \text{Ref}(P/s)) \\ &\Leftrightarrow (\forall s \in \text{tr}(Q) : s \in \text{tr}(P)) \wedge \\ &\quad (\forall s \in \text{tr}(Q), x_k \in \text{Ref}(Q/s) : s \in \text{tr}(P) \wedge x_k \in \text{Ref}(P/s)) \\ &\Leftrightarrow \forall s \in \text{tr}(Q) : s \in \text{tr}(P) \wedge \text{Ref}(Q/s) \subseteq \text{Ref}(P/s) \\ &\Leftrightarrow P \sqsubseteq_F Q \end{aligned}$$

□

3.2 A Test Case Map from Finite State Machines to CSP Processes

FSM Test Cases Following [10], an *adaptive FSM test case*

$$tc_{\text{FSM}} = (Q, \underline{q}, \Sigma_I, \Sigma_O, h, in)$$

is a nondeterministic, observable, output-complete, acyclic FSM which only provides a single input in a given state. Running in FSM intersection mode with the SUT, the test case provides a specific input to the SUT; this input is determined by the current state of the test case. It accepts every output and transits either to a fail-state FAIL, if the output is wrong according to the test objectives, or to the next test state uniquely determined by the processed input/output pair. Another state PASS indicates that the test has been completed without failure. Both FAIL and PASS are termination states, that is, they do not have any outgoing transitions.

Since the test case state determines the input for all of its outgoing transitions, this input is typically used as a state label, and the outgoing transitions are just labelled by the possible outputs. A function $in : Q - \{\text{PASS}, \text{FAIL}\} \rightarrow \Sigma_I$ maps the states to these inputs. Termination states of the FSM are not labelled with further inputs.

Example 3. Consider the FSM test case depicted in Fig. 4 which is specified for the same input and output alphabets as defined for the FSM presented in Example 2. The test case is passed by the FSM from Example 2, because intersecting the two state machines results in an FSM which always reaches the PASS state. \square

CSP Test Cases A *CSP test case* is a terminating process with alphabet $\Sigma \cup \{\dagger, \perp, \checkmark\}$, where the extra events stand for (1) test verdict FAIL (\dagger), (2) timeout (\perp), and (3) test verdict PASS (\checkmark). In principle, very general classes of CSP processes can be used for testing, as introduced, for example, in [7, 6]. For the purpose of this paper, however, we can restrict the possible variants of CSP test cases to the ones that are in the range of the test case map which is constructed next.

Test Case Map The test case map $T^* : TC(\text{FSM}) \rightarrow TC(\text{CSP})$ is specified with respect to a fixed CSP process alphabet Σ extended by the events $\{\dagger, \perp, \checkmark\}$ introduced above and the associated FSM input and output alphabets $\Sigma_I = \mathbb{P}(\Sigma) - \{\emptyset\}$ and $\Sigma_O = \Sigma \cup \{\perp\}$. Given an FSM test case $tc_{\text{FSM}} = (Q, \underline{q}, \Sigma_I, \Sigma_O, h, in)$, the image $T^*(tc_{\text{FSM}})$ is the CSP process tc_{CSP} specified as

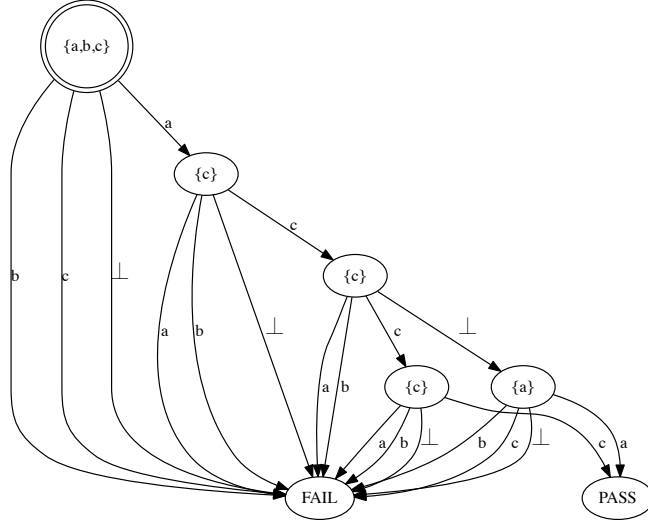


Fig. 4. An FSM test case which is passed by the FSM presented in Example 2.

follows.

$$tc_{CSP} = tc(q)$$

$$tc(q) = (e : \{a \in in(q) \cup \{\perp\} \mid h_1(q, in(q), a) \notin \{PASS, FAIL\}\} \bullet e \rightarrow tc(h_1(q, in(q), e)))$$

□

$$(e : \{a \in in(q) \cup \{\perp\} \mid h_1(q, in(q), a) = PASS\} \bullet e \rightarrow \checkmark \rightarrow Skip)$$

□

$$(e : \{a \in in(q) \cup \{\perp\} \mid h_1(q, in(q), a) = FAIL\} \bullet e \rightarrow \dagger \rightarrow Skip)$$

Example 4. The FSM test case tc_{FSM} shown in Fig. 4 is mapped by T^* to the following CSP test case.

$$T^*(tc_{FSM}) = P_1$$

$$P_1 = (e : \{b, c, \perp\} \bullet e \rightarrow \dagger \rightarrow Skip) \square (a \rightarrow P_2)$$

$$P_2 = (e : \{a, b, \perp\} \bullet e \rightarrow \dagger \rightarrow Skip) \square (c \rightarrow P_3)$$

$$P_3 = (e : \{a, b\} \bullet e \rightarrow \dagger \rightarrow Skip) \square (\perp \rightarrow P_4) \square (c \rightarrow P_5)$$

$$P_4 = (e : \{b, c, \perp\} \bullet e \rightarrow \dagger \rightarrow Skip) \square (a \rightarrow \checkmark \rightarrow Skip)$$

$$P_5 = (e : \{a, b, \perp\} \bullet e \rightarrow \dagger \rightarrow Skip) \square (c \rightarrow \checkmark \rightarrow Skip)$$

□

The following theorem shows the validity of the satisfaction condition **SC2** regarding the test case map, the model map, and the pass conditions for tests on CSP level and FSM level.

Theorem 3. *Fixing a CSP process alphabet Σ , the model map $T : \text{Sig}_1 \rightarrow \text{FSM}$ and the test case map $T^* : \text{TC}(\text{FSM}) \rightarrow \text{TC}(\text{CSP})$ fulfil satisfaction condition **SC2** in the sense that*

$$\forall P \in \text{Sig}_1, tc_{\text{FSM}} \in \text{TC}(\text{FSM}) : T(P) \text{ pass}_2 tc_{\text{FSM}} \Leftrightarrow P \text{ pass}_1 T^*(tc_{\text{FSM}})$$

Proof. Let $T(P) = (Q, \underline{q}, \Sigma_I, \Sigma_O, h)$ and $tc_{\text{FSM}} = (Q', \underline{q}', \Sigma_I, \Sigma_O, h', in)$.

We show by induction over the length of $s \in \Sigma_O^*$ that the following assertions hold for all s .

1. For every pass-trace $x/s \in L(T(P)) \cap L(tc_{\text{FSM}})$, there exists a pass-trace $u \in \text{tr}(P \parallel [\Sigma] \parallel T^*(tc_{\text{FSM}}))$, such that $u \upharpoonright \Sigma$ corresponds to x/s .
2. For every fail-trace $x/s \in L(T(P)) \cap L(tc_{\text{FSM}})$, there exists a fail-trace trace $u \in \text{tr}(P \parallel [\Sigma] \parallel T^*(tc_{\text{FSM}}))$, such that $u \upharpoonright \Sigma$ corresponds to x/s .
3. For all $x/s \in L(T(P))$, the graph nodes of $G(P)$ and the states of $T(P)$ are related by

$$G(P)/(s \upharpoonright \Sigma) = \underline{q}\text{-after-}(x/s).$$

4. FSM test tc_{FSM} and CSP test $T^*(tc_{\text{FSM}})$ perform consistent state changes, in the sense that

$$\begin{aligned} x/s \in L(T(P)) \cap L(tc_{\text{FSM}}) \wedge \underline{q}'\text{-after-}(x/s) \notin \{\text{PASS}, \text{FAIL}\} \Rightarrow \\ T^*(tc_{\text{FSM}})/(s \upharpoonright \Sigma) = tc(\underline{q}'\text{-after-}(x/s)), \end{aligned}$$

where $tc(q)$ has been defined above with the test case map.

Proof of 1 and 2 obviously proves the theorem; assertions 2 and 3 are needed to perform the induction argument.

For the base case, s is the empty trace, so x/s is empty as well. We have $G(P)/\varepsilon = \underline{n} = \underline{q}$, due to the definition of the model map. FSM test case tc_{FSM} resides in its initial state \underline{q}' . By definition of the test case map above, $T^*(tc_{\text{FSM}})$ has initial CSP process state $tc(\underline{q}')$; this proves Assertion 3 and Assertion 4 for the case $\#s = 0$. For assertions 1 and 2, there is nothing to prove: no test can pass or fail on the empty trace.

For the induction hypothesis, assume that the four assertions have been proven for $\#s \leq k$ with $0 \leq k$.

For the induction step, assume that the FSM test has run through trace x/s such that $\#s \leq k$ and $\underline{q}'\text{-after-}(x/s) = \underline{q}'$. The induction hypothesis gives us $G(P)/(s \upharpoonright \Sigma) = \underline{q}\text{-after-}(x/s)$ from Assertion 3 and $T^*(tc_{\text{FSM}})/(s \upharpoonright \Sigma) = tc(\underline{q}')$ from Assertion 4. FSM test tc_{FSM} will offer input $in(\underline{q}')$ to the FSM $T(P)$ which is being tested. We make a case analysis for the outcomes of the resulting test step.

Case 1. $(x.in(\underline{q}'))/(s.\perp) \in L(\underline{q}\text{-after-}(x/s))$.

By construction of $T(P)$, this is exactly the case if $in(\underline{q}') \in r(G(P)/(s \upharpoonright \Sigma))$.

Since tc_{FSM} is output complete, $in(q')/\perp \in L(q')$. Depending on the nature of the test case, q' -after- $(in(q')/\perp)$ is one of the deadlock states PASS, FAIL, or it is a non-blocking FSM state, say, q'' . Since tc_{FSM} is observable, however, this post-state is uniquely determined. Observability of tc_{FSM} implies further that the sets $\{a \in in(q) \cup \{\perp\} \mid q\text{-after-}(in(q)/a) \notin \{\text{PASS}, \text{FAIL}\}\}$, $\{a \in in(q) \cup \{\perp\} \mid q\text{-after-}(in(q)/a) = \text{PASS}\}$, and $\{a \in in(q) \cup \{\perp\} \mid q\text{-after-}(in(q)/a) = \text{FAIL}\}$ used in the definition of $tc(q)$ are disjoint.

Case 2. FSM test tc_{FSM} performs a transition into the FAIL-state. This \square

4 Case Studies

5 Related Work

6 Conclusion

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