Finite Complete Suites for CSP Refinement Testing

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1 Introduction

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2.1 Complete Testing Theories

Fault Models, Test Cases, Test Suites, and Completeness We use the term *signature* to denote a collection of comparable models represented in an arbitrary formalism. In this article, signatures represent sets of finite state machines over fixed input and output alphabets, or CSP processes with finite state, represented by their normalised transition graphs.

Given a signature Sig of models, a fault model $\mathcal{F} = (M, \leq, Dom)$ specifies a reference model $M \in Sig$, a conformance relation $\leq \subseteq Sig \times Sig$ between models, and a fault domain $Dom \subseteq Sig$. This terminology follows [2], where fault models were originally introduced in the context of finite state machine testing. Note that fault domains may contain both models conforming to the reference model and models violating the conformance relation. Note further that the reference model M is not necessarily a member of the fault domain. For example, M could be nondeterministic, while only deterministic implementation behaviours might be considered in the fault domain. By $F(Sig, \leq)$ we denote the set of all fault models \mathcal{F} defined for signature Sig and conformance relation \leq .

Let $\mathrm{TC}(Sig)$ denote the set of all $test\ cases$ applicable to elements of Sig. The abstract notion of test cases defined here only requires the existence of a relation $\underline{\mathrm{pass}} \subseteq Sig \times \mathrm{TC}(Sig)$. For $(M,U) \in \underline{\mathrm{pass}}$, the infix notation $M\ \underline{\mathrm{pass}}\ U$ is used, and interpreted as 'Model $M\ passes\ the\ test\ case\ U$ '. If $(M,U) \not\in \underline{\mathrm{pass}}$ holds, this is abbreviated by $M\ \underline{\mathrm{fail}}\ U$.

A test suite $TS \subseteq TC(Sig)$ denotes a set of test cases. A model M passes the test suite TS, also written as M pass TS, if and only if M pass U for all $U \in TS$. A test suite TS is called *complete* for fault model $\mathcal{F} = (M, \leq, Dom)$, if and only if the following properties hold.

1. If a member M' of the fault domain conforms to the reference model M, it passes the test suite, that is,

$$\forall M' \in Dom : M' \leq M \Rightarrow M' \text{ pass TS}$$

This property is usually called *soundness* of the test suite.

2. If a member of the fault domain passes the test suite, it conforms to the reference model, that is,

$$\forall M' \in Dom : M' \text{ pass TS} \Rightarrow M' \leqslant M$$

This property is usually called *exhaustiveness*.

A test suite TS is *finite* if it contains finitely many test cases and every test case $U \in TS$ is finite in the sense that it terminates after a finite number of steps. It is trivial to see that, if TS is complete for $\mathcal{F} = (M, \leq, Dom)$ and $Dom' \subseteq Dom$, then TS is also complete for $\mathcal{F}' = (M, \leq, Dom')$.

2.2 Translation of Testing Theories

Let Sig_1 and Sig_2 be two signatures with conformance relations \leq_1 and \leq_2 , and test case relations pass_1 and pass_2 , respectively. A function $T: Sig_1 \to Sig_2$ defined on a sub-domain $Sig_1 \subseteq Sig_1$ is called a *model map*, and a function $T^*: \operatorname{TC}(Sig_2) \to \operatorname{TC}(Sig_1)$ is called a *test case map*. Note that models and test cases are mapped in opposite directions (see Fig. 1). The pair (T, T^*) fulfils the *satisfaction condition* if and only if the following conditions **SC1** and **SC2** are fulfilled.

SC1 The model map is compatible with the conformance relations under consideration, in the sense that

$$\forall \mathcal{S}, \mathcal{S}' \in Sig_1 : \mathcal{S}' \leqslant_1 \mathcal{S} \Leftrightarrow T(\mathcal{S}') \leqslant_2 T(\mathcal{S}),$$

so the left-hand side diagram in Fig. 1 commutes due to the fact that $T;\leqslant_2=\leqslant_1;\ T.^4$

⁴ Operator ";" denotes the relational composition defined for functions or relations $f \subseteq A \times B$, $g \subseteq B \times C$ by f; $g = \{(a, c) \in A \times C \mid \exists b \in B : (a, b) \in f \land (b, c) \in g\}$. Note that f; g is evaluated from left to right (like composition of code fragments), as opposed to right-to-left evaluation which is usually denoted by $g \circ f$.

SC2 Model map and test case map preserve the <u>pass</u>-relationship in the sense that

$$\forall \mathcal{S} \in \underline{Sig_1}, U \in \mathrm{TC}(Sig_2) : T(\mathcal{S}) \ \underline{\mathrm{pass}}_2 \ U \Leftrightarrow \mathcal{S} \ \underline{\mathrm{pass}}_1 \ T^*(U),$$

so the right-hand side diagram in Fig. 1 commutes, due to the fact that $pass_1 = T$; $pass_2$; T^* .

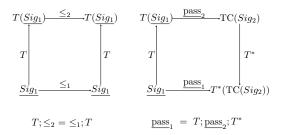


Fig. 1. Commuting diagrams reflecting the satisfaction condition.

The following theorem is a direct consequence of [1, Theorem 2.1].

Theorem 1. With the notation introduced above, let (T, T^*) fulfil the satisfaction condition. Suppose that $TS_2 \subseteq TC(Sig_2)$ is a complete test suite for fault model $\mathcal{F}_2 = (\mathcal{S}_2, \leqslant_2, Dom_2)$. Define fault model \mathcal{F}_1 on Sig_1 by

$$\mathcal{F}_1 = (\mathcal{S}_1, \leqslant_1, Dom_1), \text{ such that } T(\mathcal{S}_1) = \mathcal{S}_2 \text{ and } Dom_1 = \{\mathcal{S} \mid T(\mathcal{S}) \in Dom_2\}.$$

Then

$$TS_1 = T^*(TS_2)$$

is a complete test suite with respect to fault model \mathcal{F}_1 .

2.3 CSP and Refinement

Normalised Transition Graphs As shown in [4], any finite-state CSP process P can be represented by a *normalised transition graph*

$$G(P) = (N, \underline{n}, \Sigma, t : N \times \Sigma \to N, a : N \to \mathbb{PP}(\Sigma)),$$

with nodes N, initial node $\underline{n} \in N$, and process alphabet Σ . The partial transition function t maps a node n and an event $e \in \Sigma$ to its successor node t(n, e), if and only if (n, e) are in the domain of t. Normalisation of G(P) is reflected by the fact that t is a function. The total function a maps each node to its set of minimal acceptances: if $n \in N$ corresponds to a deterministic process state

of P, a(n) contains a single acceptance $A \subseteq \Sigma$, and every $e \in A$ is in one-one-correspondence with a transition t(n, e). If n corresponds to a nondeterministic process state, a(n) contains at least two acceptances A_1, A_2, \ldots, A_k . This reflects the fact that in a nondeterministic state, P must accept all events of one acceptance $A_i, i \in \{1, \ldots, k\}$, but may refuse all events e from $A_i \setminus A_i, j \neq i$.

Each well-defined transition graph G(P) fulfils the following condition. The union of all minimal acceptances in each node corresponds to the set of events labelling its outgoing transitions.

$$\forall n \in N : (n, e) \in \text{dom } t \Leftrightarrow e \in \bigcup a(n)$$
 (1)

In this condition, dom t denotes the domain of function t.

By construction, normalised transition graphs reflect the failures semantics of finite-state CSP processes: the traces s of a process are exactly the paths through the transition graph, starting at \underline{n} . The maximal refusals in each process state P/s are the complements of the minimal acceptances of the node n corresponding to P/s. As a consequences, all failures of P are represented by some (s,R), where s is an initialised path through the transition graph and $R \subseteq (\Sigma - A)$ for some minimal acceptance $A \in a(n)$, such that n is the node corresponding to P/s.

Example 1. Consider CSP process

$$P = a \to (Q \sqcap R)$$

$$Q = a \to P \sqcap c \to P$$

$$R = b \to P \sqcap c \to R$$

Its transition graph G(P) is shown in Fig. 2. Process state P is represented there as Node_0, with $\{a\}$ as the only acceptance, since event a can never be refused, and no other events are accepted. Having engaged into a, the transition emanating from Node_0 leads to Node_2 representing the process state $P/a = Q \sqcap R$. The internal choice operator induces several acceptance sets derived from Q and R. Since these processes accept their initial events with external choice, process $Q \sqcap R$ induces just two minimal acceptance sets $\{a, c\} = [Q]^0$ and $\{b, c\} = [R]^0$. Note that event c can never be refused, since it is a member of all minimal acceptances.

Having engaged into c, the next process state is represented by Node_1. Due to normalisation, there was only a single transition satisfying $t(\text{Node}_2, c) = \text{Node}_1$. This transition, however, can have been caused by either Q or R engaging into c, so Node_1 corresponds to process state $Q/c \sqcap R/c = P \sqcap R$. This is reflected by the two minimal acceptances labelling Node_1.

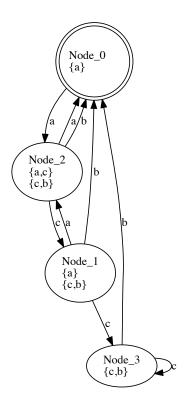


Fig. 2. Normalised transition graph of CSP process P from Example 1.

2.4 Finite State Machines

3 Finite Complete Testing Theories for CSP

3.1 A Model Map from CSP Processes to Finite State Machines

We will now construct a model map for associating CSP processes represented by normalised transition graphs to finite state machines. The intuition behind this construction is that the finite state machine's input alphabet corresponds to sets of inputs that may be offered to a CSP process. Depending on the events contained in this set, the process may (1) accept all of them, (2) accept some of them while refusing others, and (3) refuse all of them. This is reflected in the FSM by output events that represent events that the process really has engaged in and an extra event \bot representing deadlock, if the set of events has been refused.

More formally, we fix a finit CSP process alphabet Σ and consider a finite-state process P over this alphabet with normalised transition graph $G(P) = (N, \underline{n}, \Sigma, t : N \times \Sigma \to N, a : N \to \mathbb{PP}(\Sigma))$, then the model map T maps P to the following observable FSM $T(P) = (Q, q, h, \Sigma_I, \Sigma_O)$ satisfying

$$\begin{split} Q &= N \cup \{ \mathrm{DL} \} \\ \underline{q} &= \underline{n} \\ \Sigma_I &= \mathbb{P}(\Sigma) - \{ \varnothing \} \\ \Sigma_O &= \Sigma \cup \{ \bot \} \\ h &= \{ (n, A, e, n') \mid A \in \Sigma_I \land e \in A \land (n, e) \in \mathrm{dom} \ t \land t(n, e) = n' \} \cup \\ \{ (n, A, \bot, \mathrm{DL}) \mid A \in \Sigma_I \land \exists A' \in a(n) \land A \cap A' = \varnothing \} \end{split}$$

Example 2. For the CSP process P and its transition graph G(P) discussed in Example 1, the FSM T(P) is depicted in Fig. 3. For displaying its transitions, we used notation

$$\forall A : \text{condition}/e$$

which stands for a set of transitions between the respective nodes: one transition per non-empty set $A \subseteq \Sigma$ fulfilling the specified condition. The arrow Node_0 \longrightarrow Node_2 labelled by $\forall A: a \in A/a$, for example, stands for FSM transitions

Node_0
$$\xrightarrow{\{a,b\}/a}$$
 Node_2
Node_0 $\xrightarrow{\{a,b\}/a}$ Node_2
Node_0 $\xrightarrow{\{a,c\}/a}$ Node_2
Node_0 $\xrightarrow{\{a,b,c\}/a}$ Node_2

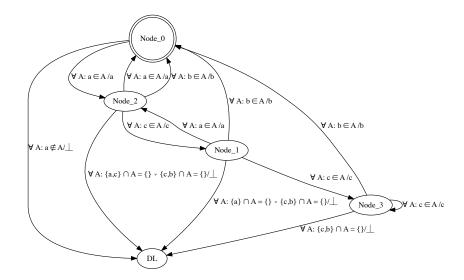


Fig. 3. FSM resulting from applying the model map to CSP process P from Example 1.

3.2 A Test Case Map from Finite State Machines to CSP Processes

FSM Test Cases Following [3], an adaptive FSM test case is a nondeterministic, observable, output-complete, acyclic FSM which only provides a single input in a given state. Running in FSM intersection mode with the SUT, the test case provides a specific input to the SUT; the input is determined by the current state of the test case. It accepts every output and transits either to a fail-state, if the output is wrong according to the reference model, or to the next test state uniquely determined by the processed input/output pair. Since the test case state determines the input for all of its outgoing transitions, this input is typically used as a state label, and the outgoing transitions are just labelled by the possible outputs.

Example 3. Consider the FSM test case depicted in Fig. 4 which is specified for the same input and output alphabets as defined for the FSM presented in Example 2. The test case is passed by the FSM from Example 2, because intersecting the two state machines results in an FSM which always reaches the PASS state. \Box

CSP Test Cases A *CSP test case* is a terminating process with alphabet $\Sigma \cup \{\dagger, \perp, \checkmark\}$, where the extra events stand for (1) test verdict FAIL (\dagger) , (2)

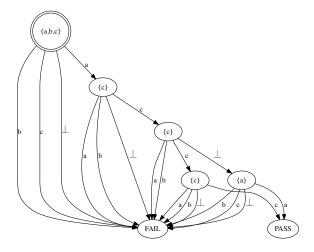


Fig. 4. An FSM test case which is passed by the FSM presented in Example 2.

timeout (\bot) , and (3) test verdict PASS (\checkmark) . In principle, very general classes of CSP processes can be used for testing, as introduced, for example, in [?,?]. For the purpose of this paper, however, we can restrict the possible variants of CSP test cases to the ones that are in the range of the test case map which is constructed next.

Test Case Map The test case map $T^*: TC(FSM) \to TC(CSP)$ is specified with respect to a fixed CSP process alphabet Σ and the associated FSM input and output alphabets $\Sigma_I = \mathbb{P}(\Sigma) - \{\emptyset\}$ and $\Sigma_O = \Sigma \cup \{\bot\}$.

- 4 Case Studies
- 5 Related Work
- 6 Conclusion

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