

# Alpha inelastic scattering and cluster structures in $^{24}\text{Mg}$

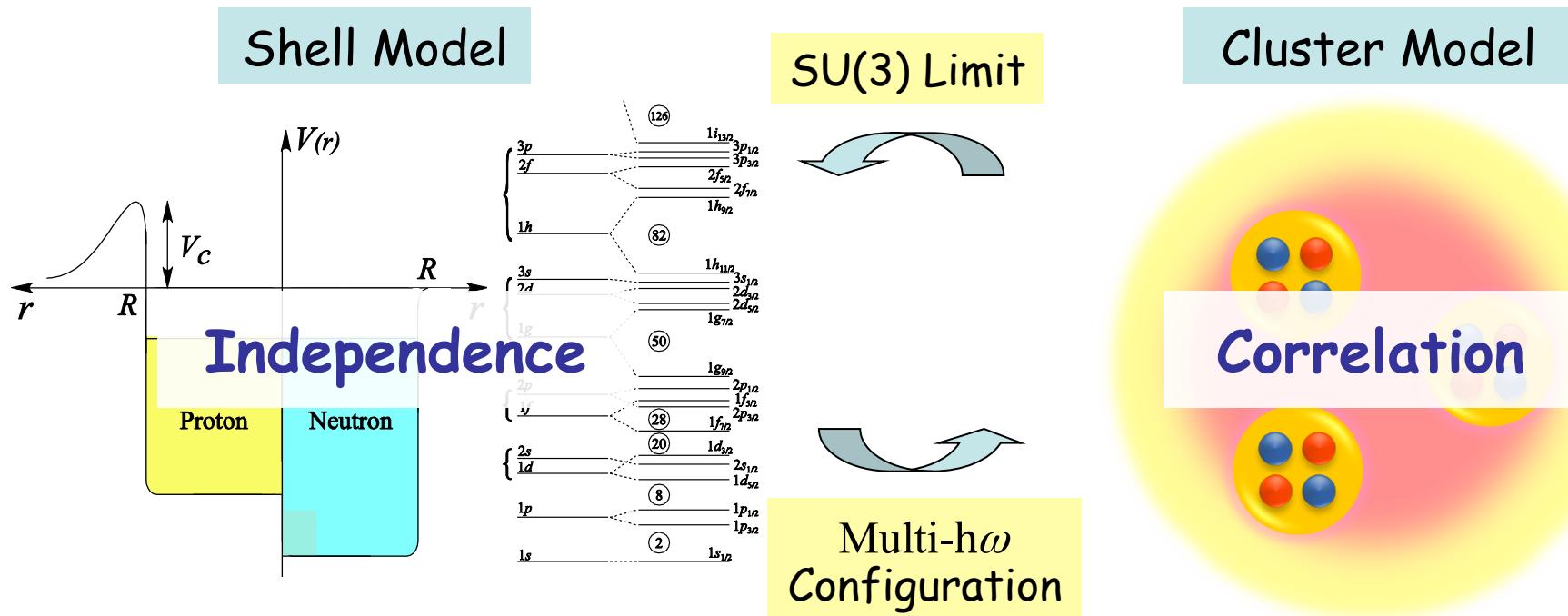
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# Introduction

## Two different pictures of Nuclear Structure



S. P. orbit in the mean-field potential.  
Magic numbers (2, 8, 20, ....).  
Describes well S. P. excited states.

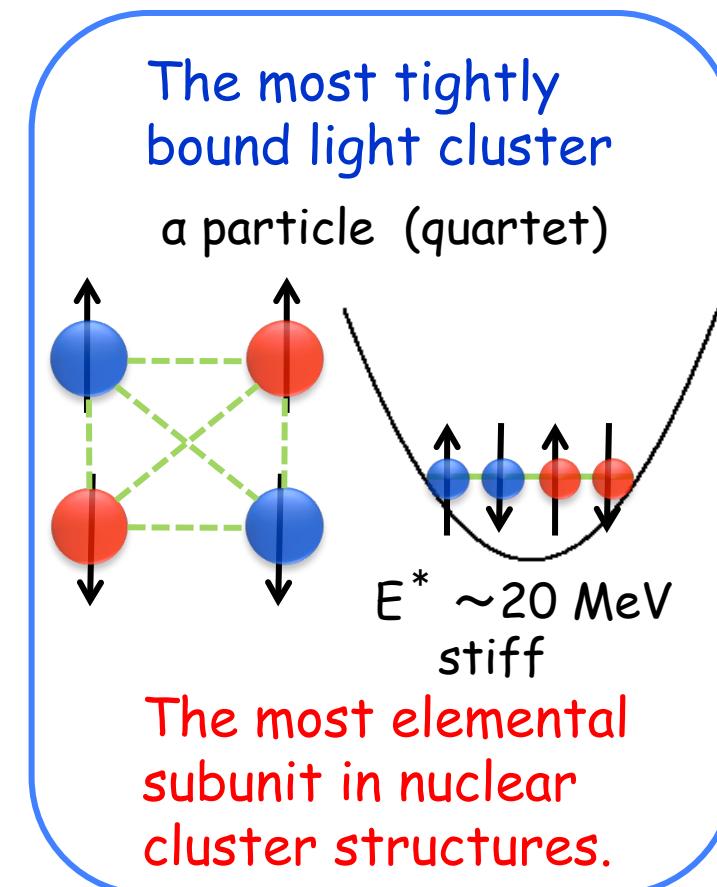
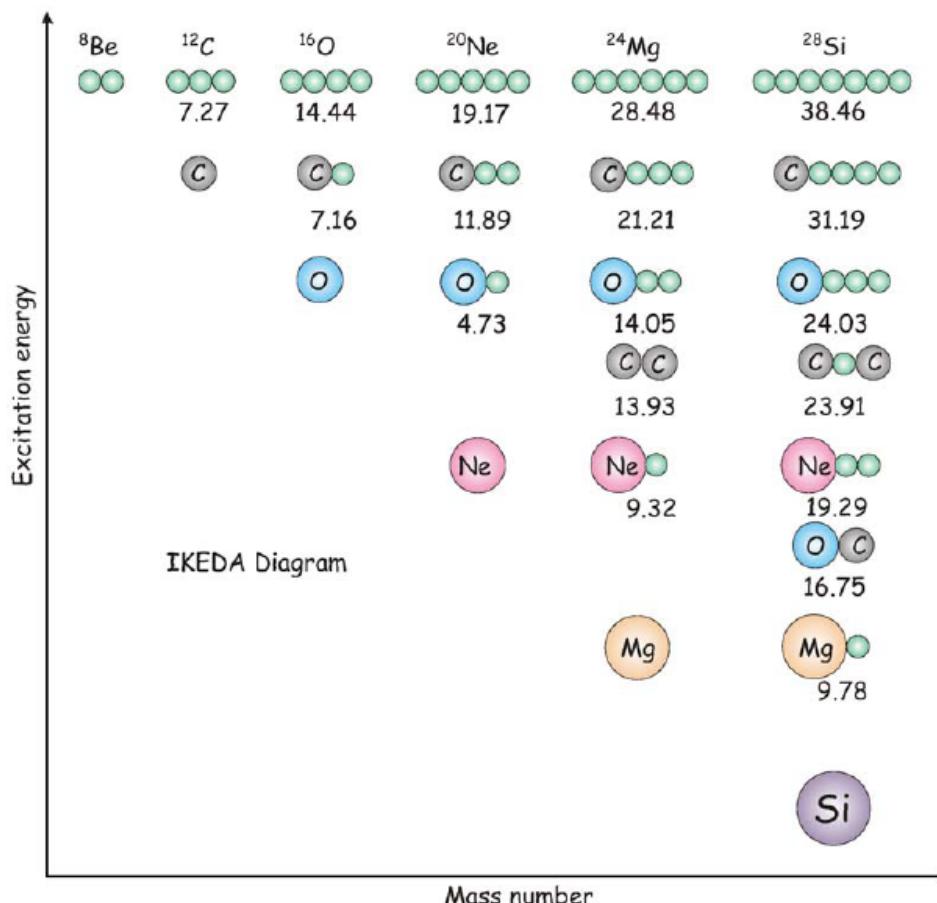
Strong correlation between nucleons.  
Cluster consists of several nucleons.  
Clusters are weakly bound.

It is important to study appearance and disappearance of the cluster correlation for better understanding of "Atomic Nucleus".

# Cluster States in N = 4n Nuclei

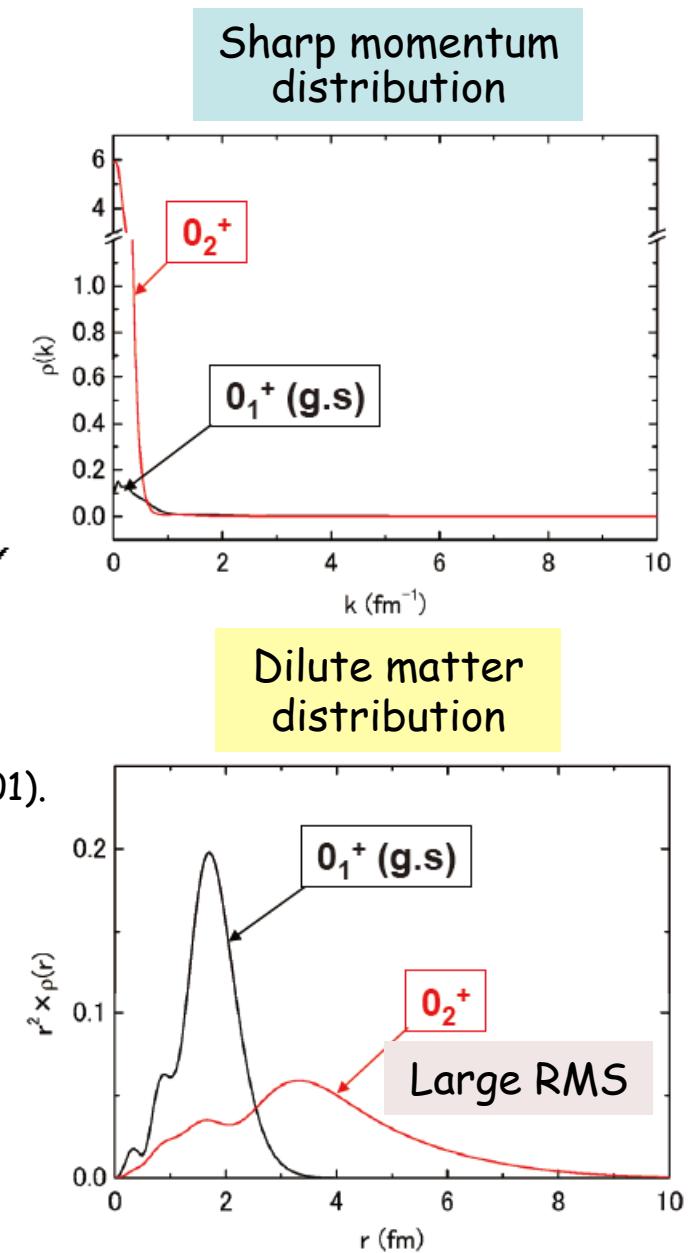
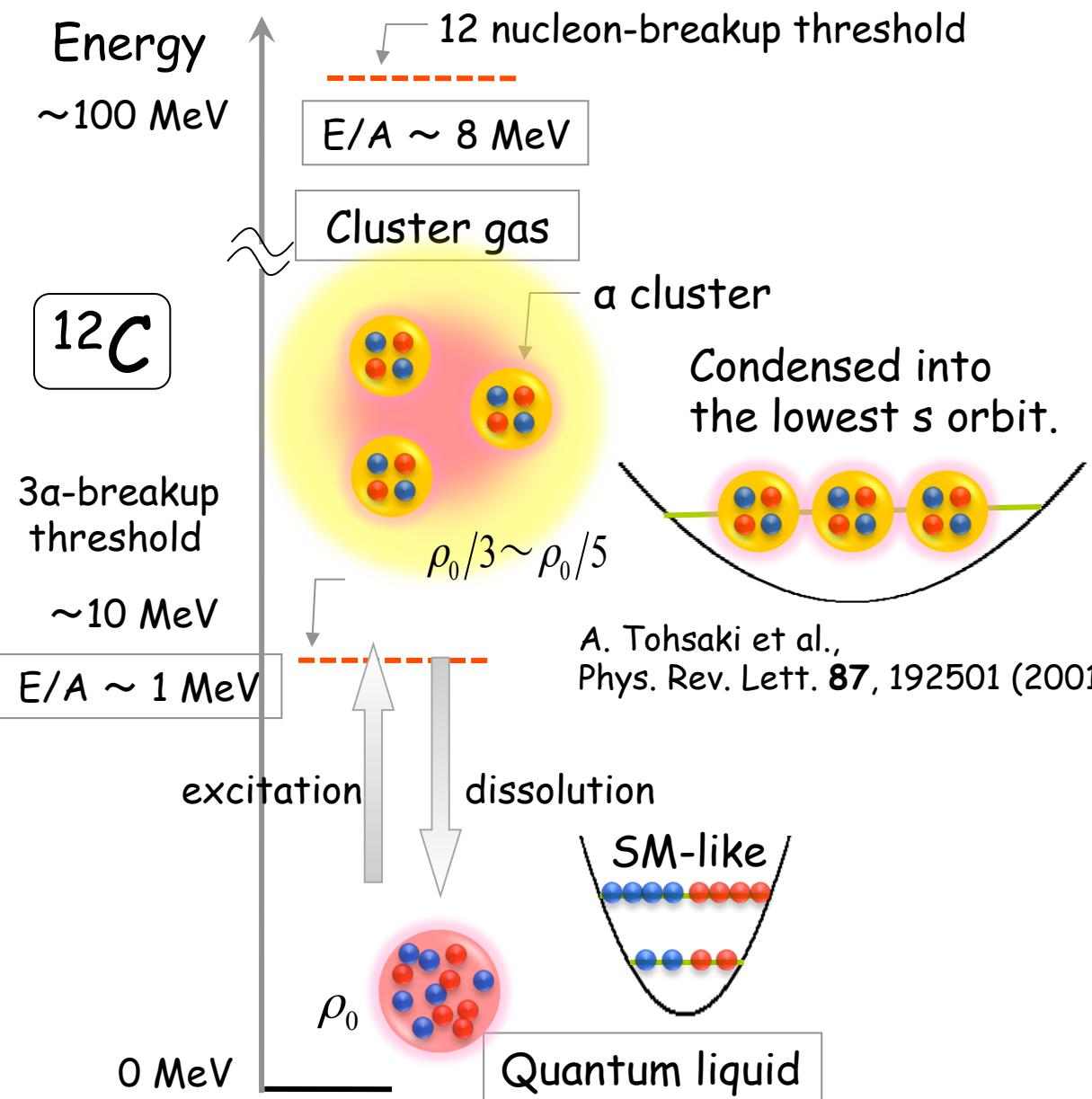
a clustering is an important concept in nuclear physics for light nuclei.

a cluster structure is expected to emerge near the  $\alpha$ -decay thresholds in N = 4n nuclei.



The  $0_{-}^{+}$  state at  $E_x = 7.65 \text{ MeV}$  in  $^{12}\text{C}$  is a famous  $3\alpha$  cluster state.

# Cluster Gas-like States in $^{12}\text{C}$



# a Condensed States in Heavier N = 4n Nuclei

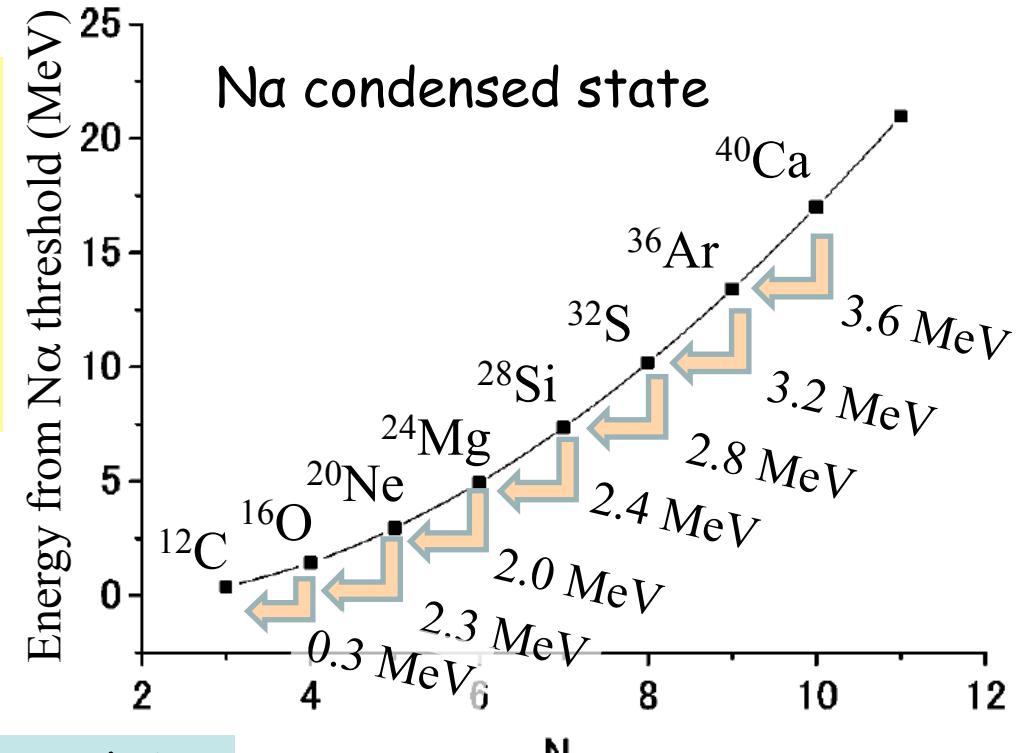
a condensed states in  ${}^8\text{Be}$  and  ${}^{12}\text{C}$  seem to be established.

a condensed states in heavier nuclei ( $A < 40$ ) are theoretically predicted.

Short range  $\alpha$ - $\alpha$  attraction  
Long range Coulomb repulsion



Energy of dilute Na state increase with N.  
Na are confined in Coulomb barrier.



$\frac{N}{N}$   
T. Yamada and P. Schuck,  
Phys. Rev. C 69, 024309 (2004).

If such na condensed states are formed, they should sequentially decay into lighter a condensed states by emitting  $\alpha$  particles.

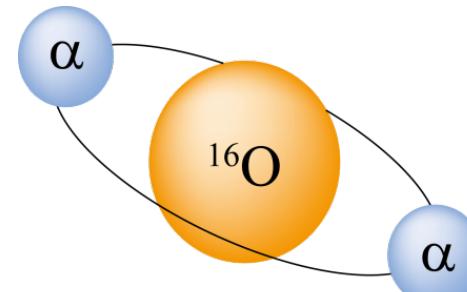
a decay measurement could be a probe to search for the a condensed state.

# a Condensed State with Core Nucleus

Possibility of a condensed states with core nuclei is proposed.

N. Itagaki et al., Phys. Rev. C **75**, 037303 (2007).

Attractive potential for a clusters provided by the core nucleus might stabilize the a condensed state in heavy nuclei.



Schuck-type wave function for  $^{24}\text{Mg}$

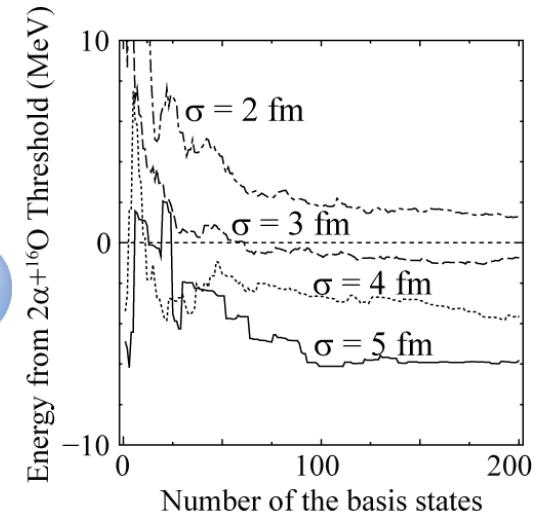
$$\Phi = A \prod_{i=1}^6 d\vec{R}_i G_i(\vec{R}_i) \exp\left[-\vec{R}_i^2 / \sigma^2\right]$$

A : Antisymmetrizer

$G_i(R_i)$  : Wave function for the i-th  $\alpha$  cluster

$R_i$  : i-th  $\alpha$ -cluster center (Randamly generated)

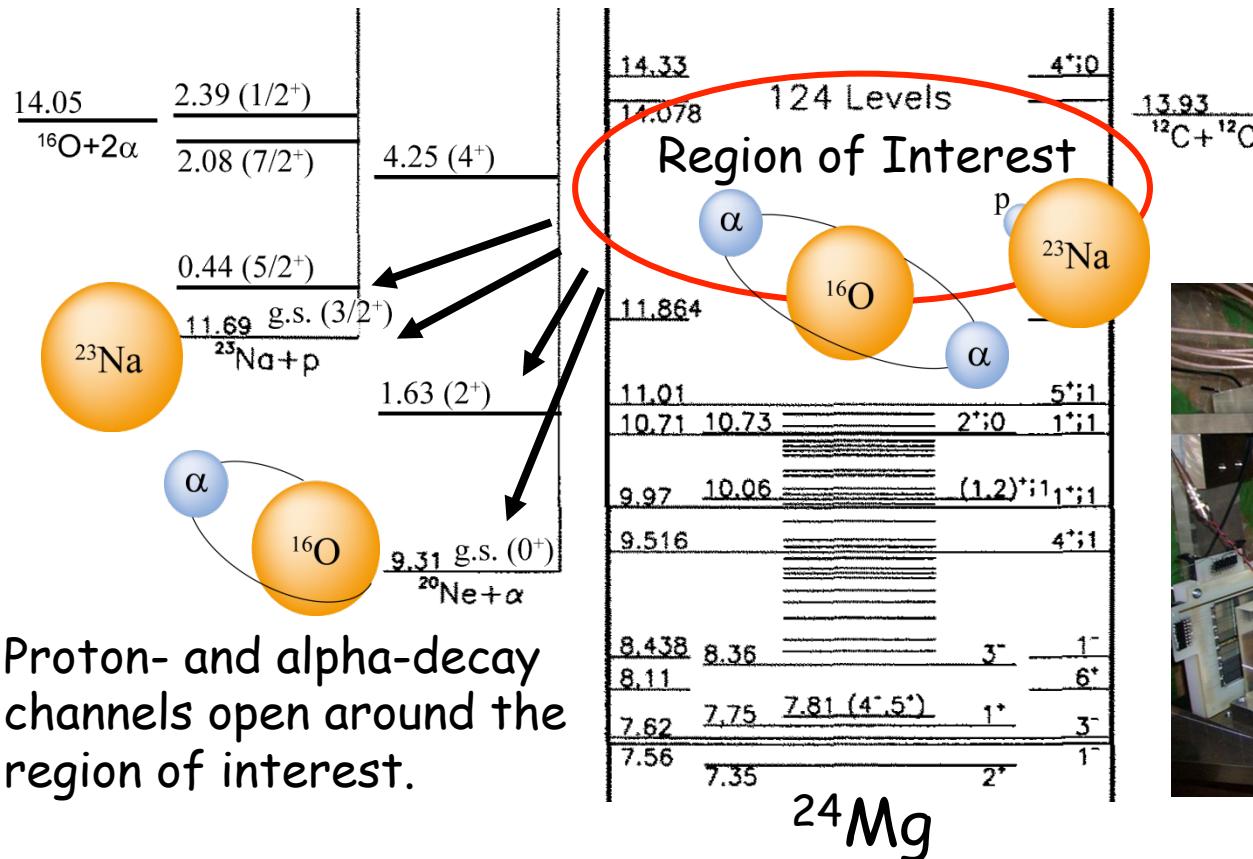
$\sigma$ : Oscillator parameter for the  $\alpha$  condensation



The a condensed state is predicted at  $E_x = 12.2$  MeV with  $B(E0; IS) = 168.4 \text{ fm}^4$ .

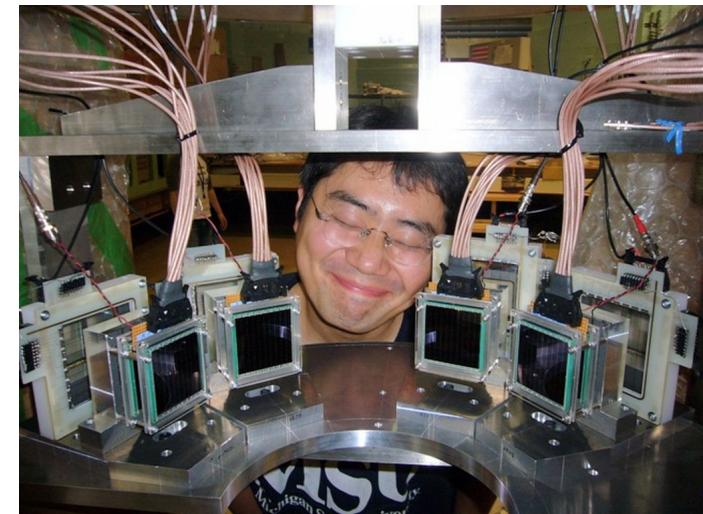
# Decay Particles from a Condensed States

Decay-particle measurement provides structural information.



Proton- and alpha-decay channels open around the region of interest.

4 Si counter telescopes (5 layers) are installed in the SC, and cover 2.5% of  $4\pi$  (309 mSr).



- Complementary information for the E0 strength is expected.
  - a cluster state should prefer to decay into the alpha-decay channel.
  - GS in  $^{20}\text{Ne}$  is a well-known  $\alpha + ^{16}\text{O}$  cluster state.

# E0 Strengths and a Cluster Structure

Large E0 strength could be a signature of spatially developed a cluster states.

T. Kawabata *et al.*, Phys. Lett. B **646**, 6 (2007).

Isoscalar E0 transition:

$$\Delta L=0, \Delta S=0, \Delta T=0$$

$0^+_2$  state in  $^{12}\text{C}$ :  $B(\text{E}0; \text{IS}) = 121 \pm 9 \text{ fm}^4$

Single Particle Unit:  $B(\text{E}0; \text{IS})_{\text{s.p.}} \sim 40 \text{ fm}^4$

$$B(\text{E}0; \text{IS}) = |ME(\text{E}0; \text{IS})|^2$$

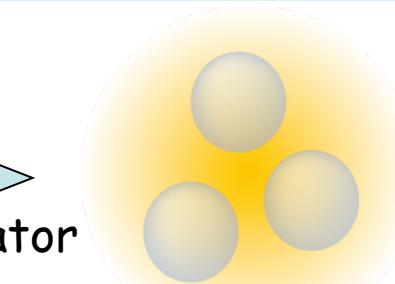
$$ME(\text{E}0; \text{IS}) = \left\langle J_f \left| \sum_{i=1}^A r_i^2 \right| J_i \right\rangle = \int_0^\infty (\rho_t^p + \rho_t^n) r^4 dr$$

- ✓ SM-like compact GS w.f. is equivalent to the CM w.f. at SU(3) limit.
- ✓ GS contains CM-like component due to possible alpha correlation.

✓ SM-like Compact GS.



$r^2$   
EO Operator



✓ Developed Cluster State

Monopole operators excite  
inter-cluster relative motion.

T. Yamada *et al.*,  
Prog. Theor. Phys. **120**, 1139 (2008).

E0 strength is a key observable to examine a cluster structure.

# Inelastic Alpha Scattering

Inelastic alpha scattering is a good probe for nuclear excitation strengths.

- Simple reaction mechanism

- Good linearity between  $d\sigma/d\Omega$  and  $B(\hat{\alpha})$ .

$$\frac{d\sigma}{d\Omega}(\Delta J^\pi) \approx KN |J(q)|^2 B(\hat{\alpha})$$

- Folding model gives a reasonable description of  $d\sigma/d\Omega$ .

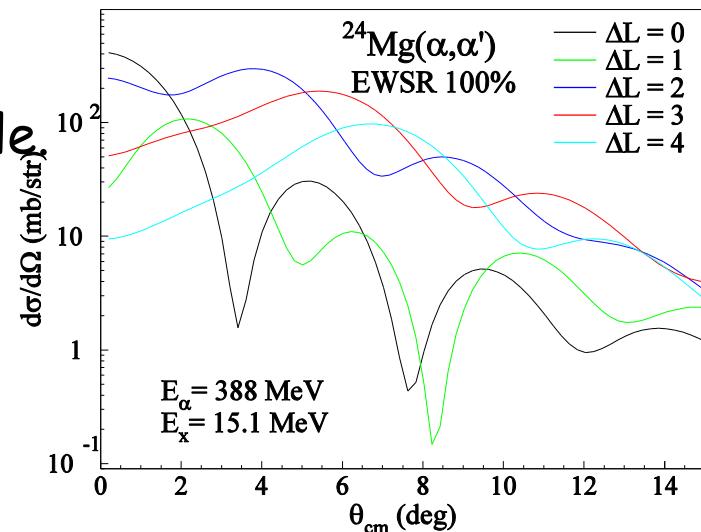
- Relatively large cross section.

- High resolution measurement is possible.

- Selectivity for the  $\Delta T = 0$  and natural-parity transitions.

- Multiple decomposition analysis

$d\sigma_{\text{exp}}^{\Delta J^\pi}$  is useful to separate  $\Delta J^\pi$ .

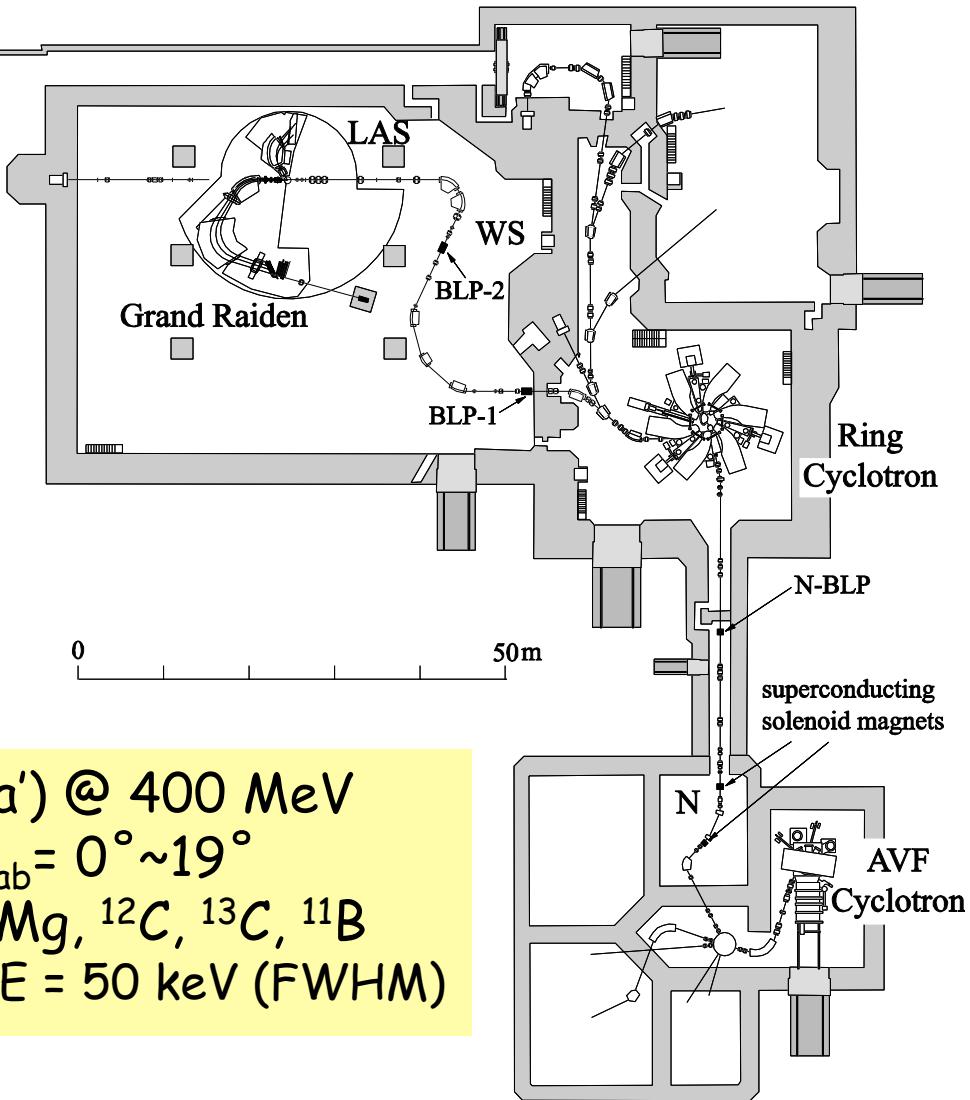
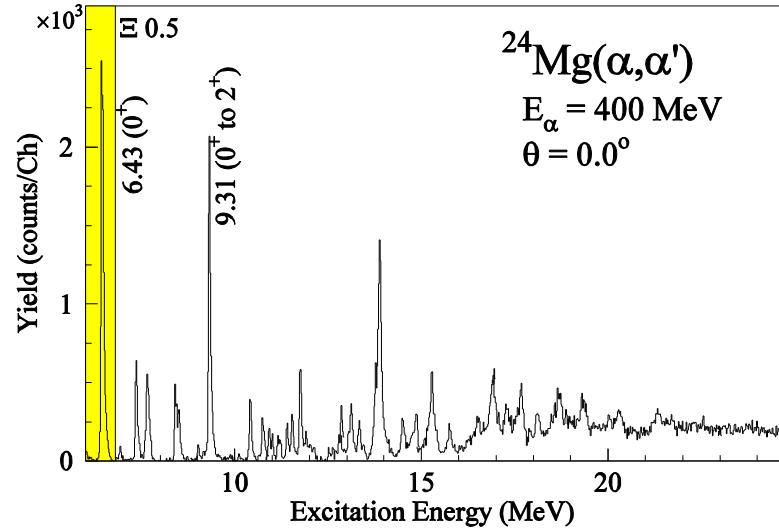
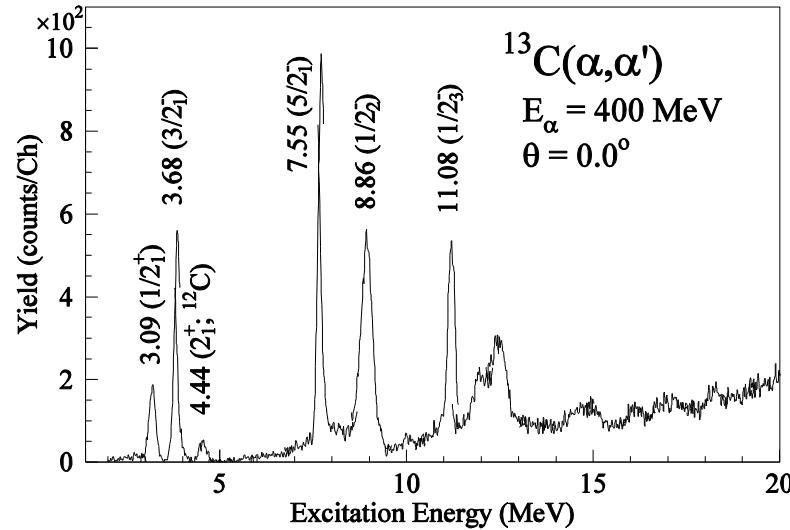
$$\frac{d\sigma}{d\Omega} = \sum_{\Delta J^\pi} A(\Delta J^\pi) \frac{d\sigma}{d\Omega}(\Delta J^\pi)^{\text{calc}}$$


We measured inelastic alpha scattering to extract IS E0 strengths and to examine cluster structures in light nuclei.

# Experiment

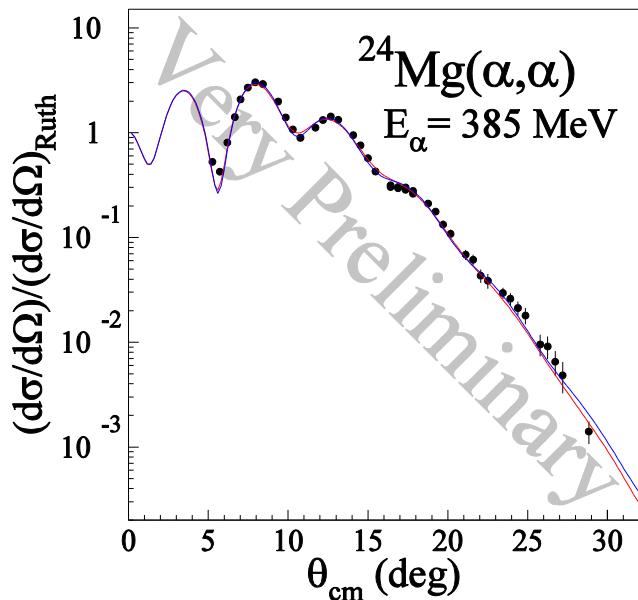
Experiment was performed at RCNP, Osaka

Background-free measurement at extremely forward angles



# Single Folding Model Analysis

Experimental data at RCNP is analyzed by single folding model.



Single folding by phenomenological aN interaction.

$$U_0(r) = \int d\vec{r}' \rho_0(r') V(|\vec{r} - \vec{r}'|)$$
$$V(|\vec{r} - \vec{r}'|) = -V \exp\left(-|\vec{r} - \vec{r}'|^2 / \alpha_V\right) - iW \exp\left(-|\vec{r} - \vec{r}'|^2 / \alpha_W\right)$$

- GS densities are taken from electron scattering assuming  $\rho_{0p} = \rho_{0n}$ .
- aN interaction is determined to reproduce the elastic scattering data.

$$V = 13.1 \text{ MeV}, W = 8.8 \text{ MeV}, \alpha_V = \alpha_W = 5.03 \text{ fm}^2$$

Single folding model gives reasonable description on the elastic scattering.

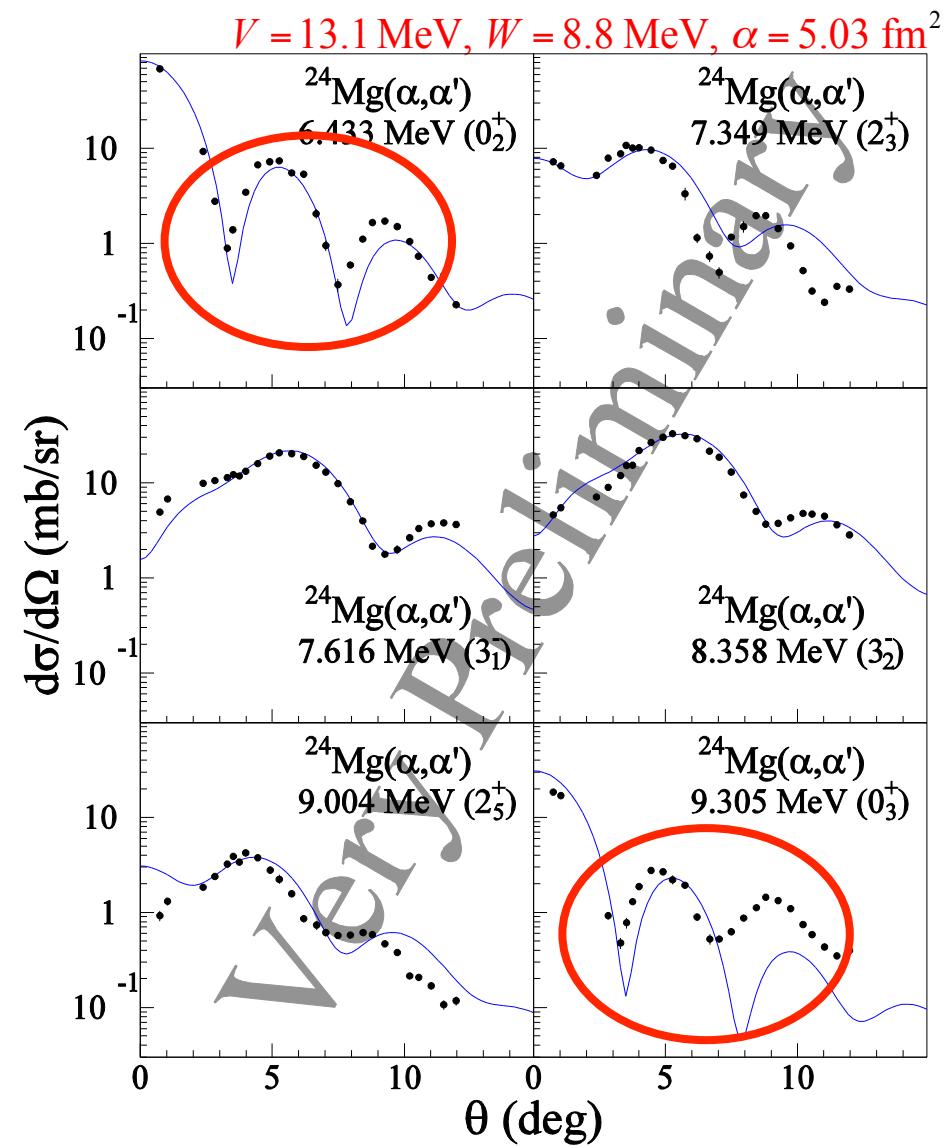
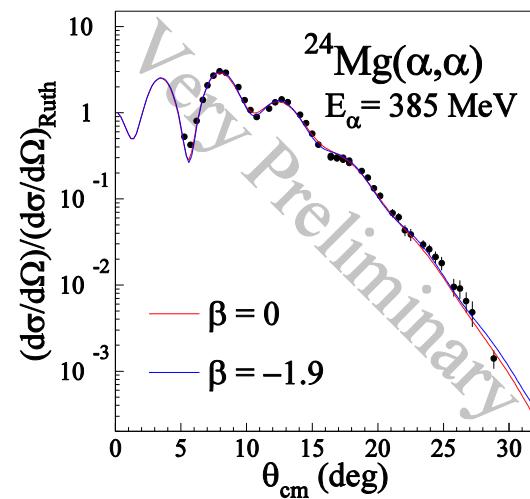
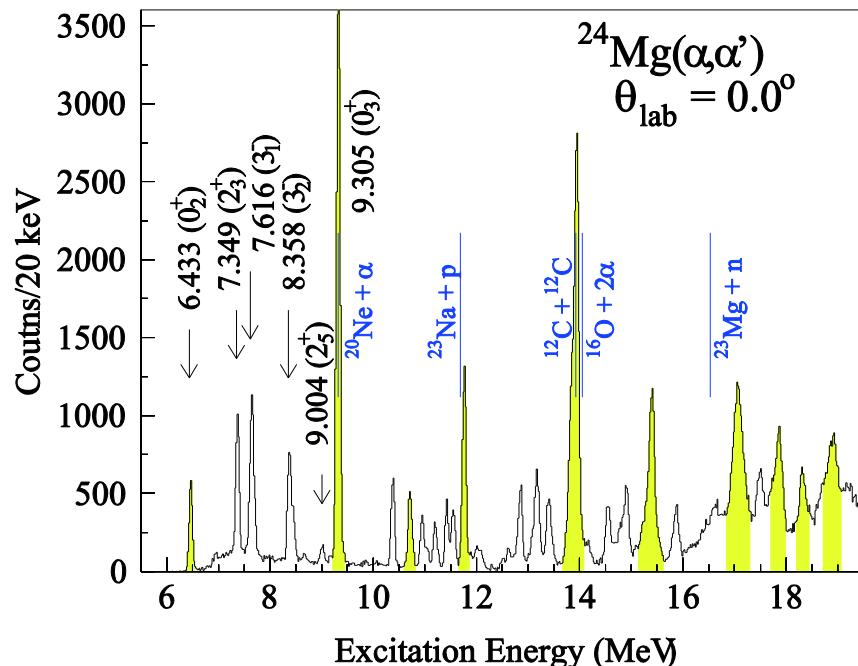
- Transition potential is obtained by a single folding model.

$$\delta U_L(r) = \int d\vec{r}' \delta \rho_L(r) V(|\vec{r} - \vec{r}'|)$$

- Transition densities are taken from the macroscopic model

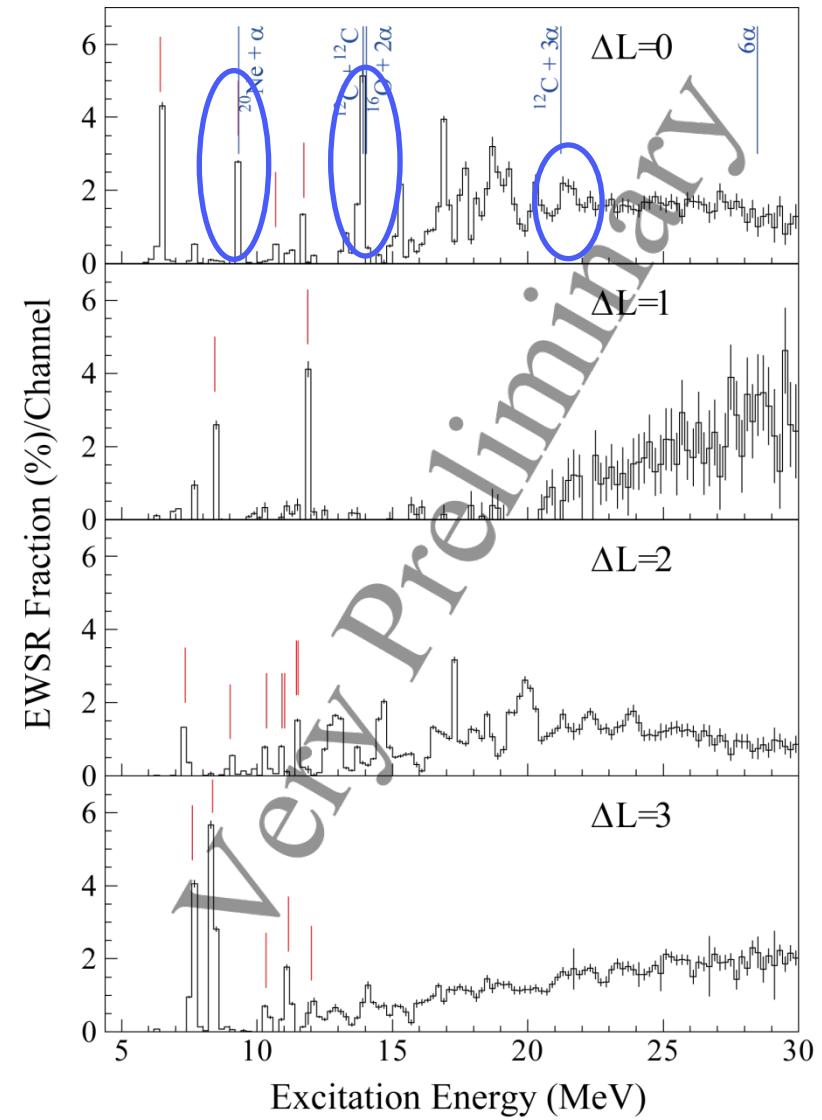
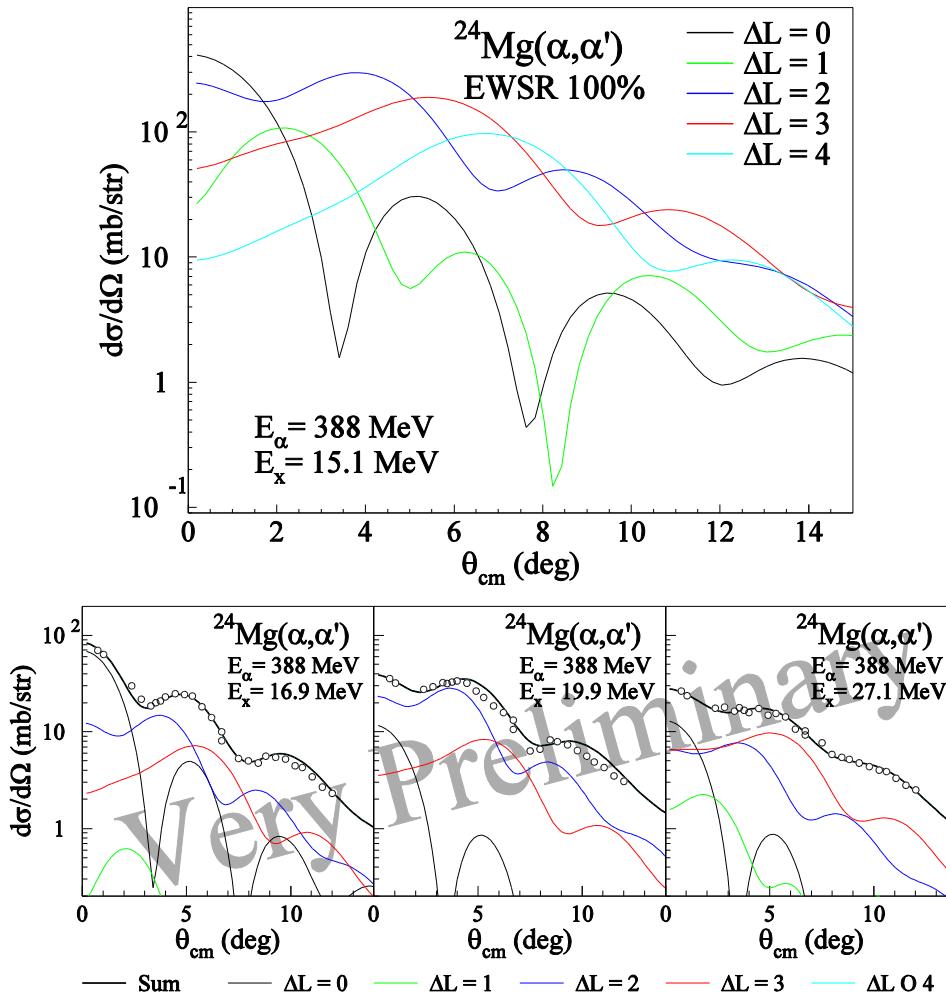
# Discrete States in $^{24}\text{Mg}$

Several discrete states were analyzed by the single folding model.



# Multipole Decomposition Analysis

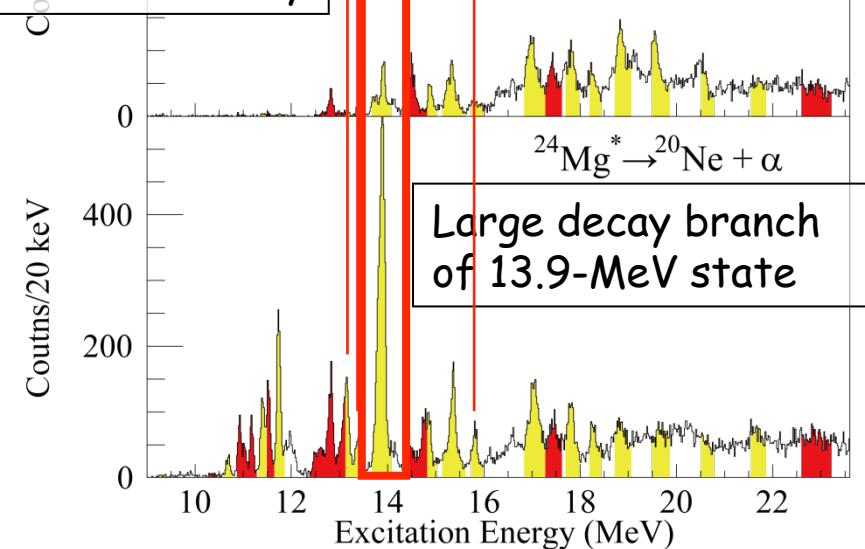
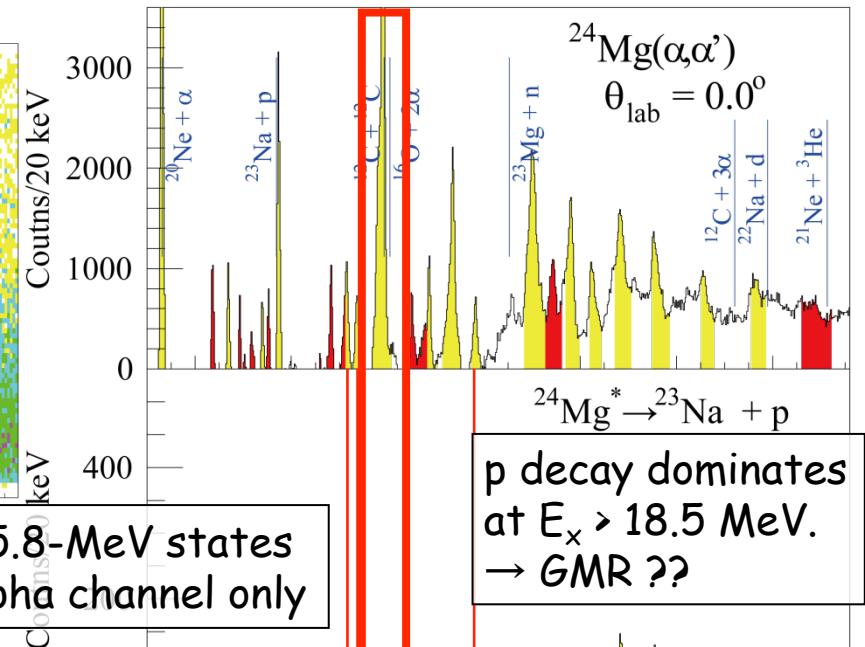
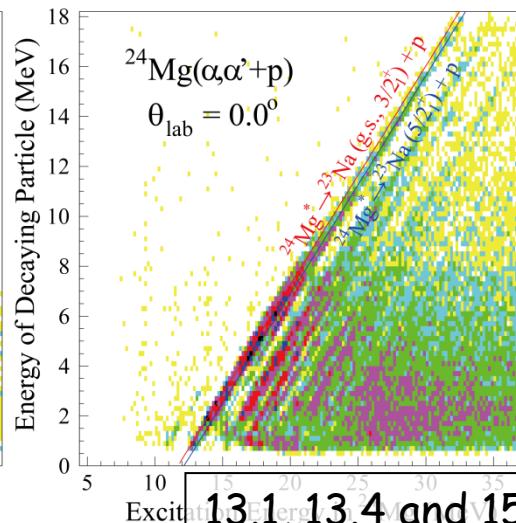
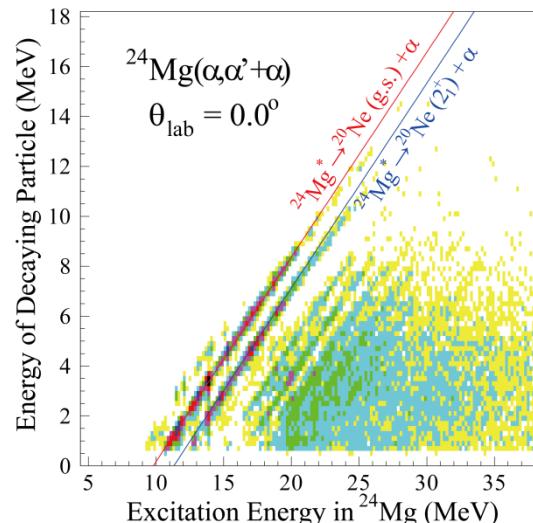
$$\frac{d\sigma}{d\Omega}^{\text{exp}} = \sum_{\Delta J^\pi} A(\Delta J^\pi) \frac{d\sigma}{d\Omega}(\Delta J^\pi)^{\text{calc}}$$



Fine structure in  $\Delta L=0$  strengths was observed.

# Decay Particle Measurement

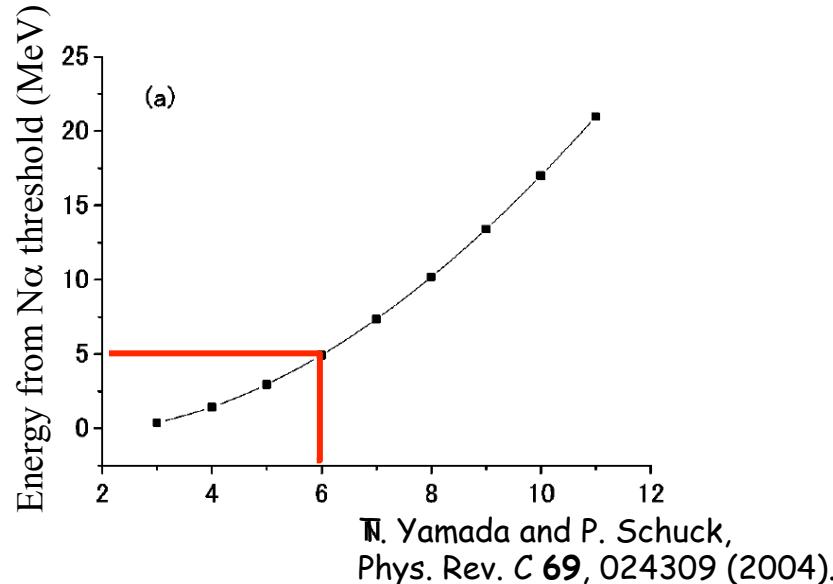
Decay to the proton and alpha emission channels were identified.



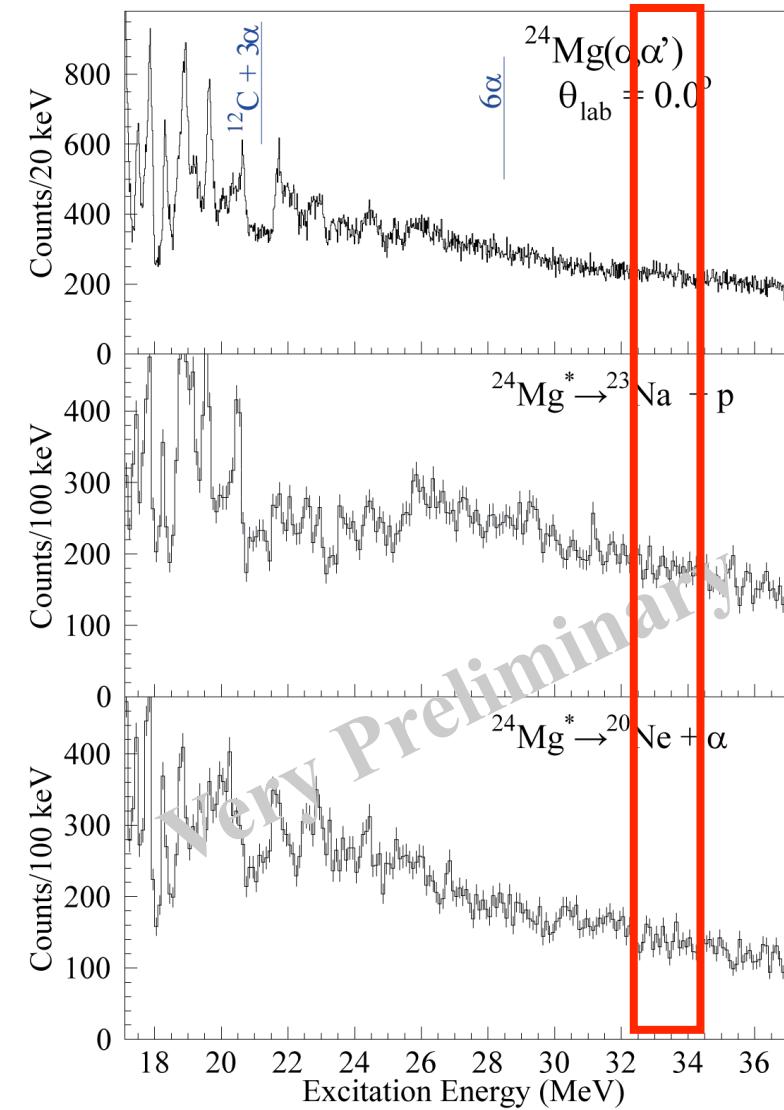
- Proton and alpha decay channels are separated.
- 13.1, 13.4 and 15.8-MeV states decay to  $^{20}\text{Ne}$  only.
- $0^+$  state at 13.9 MeV near the  $^{12}\text{C} + ^{12}\text{C}$  and  $^{16}\text{O} + 2\alpha$  thresholds has a large decay branch to  $^{20}\text{Ne}$ .

# Highly Excited Region

6a condensed state was searched for in the highly excited region.

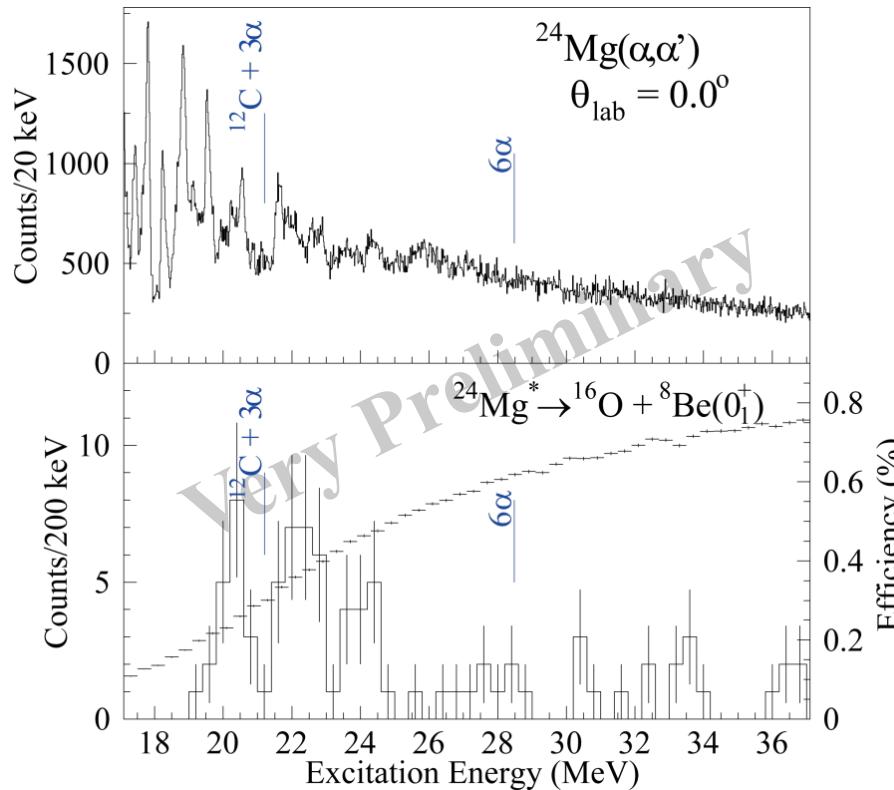
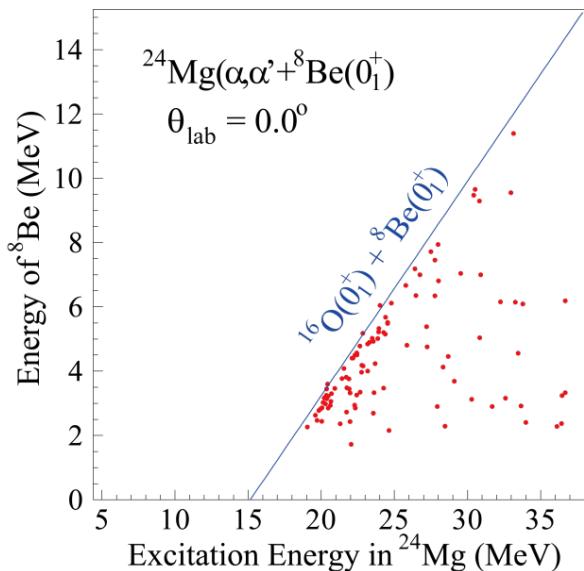
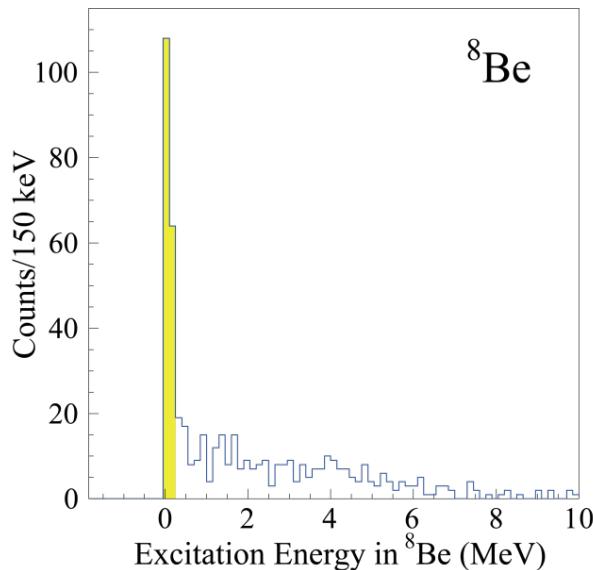


- 6a condensed state is expected at 5 MeV above the 6a threshold.
  - $E_x \sim 28.5 + 5 = 33.5$  MeV
- No significant structure suggesting the 6a condensed state.
  - Several small structures indistinguishable from the statistical fluctuation.  
→ Need more statistics.



# $^8\text{Be}$ Emission Events

$^8\text{Be}(0_1^+)$  emission events were identified from  $2\alpha$  emission events by  $E_x$  in  $^8\text{Be}$ .



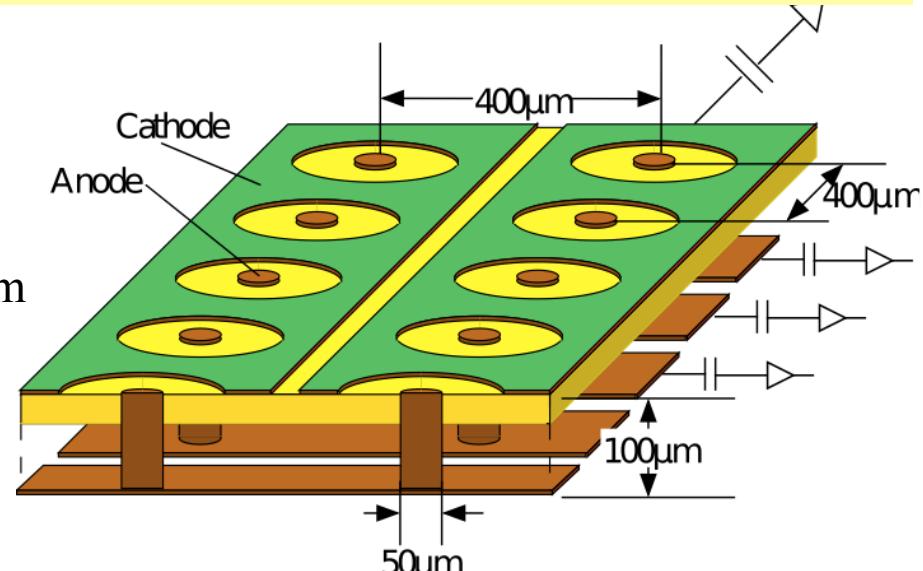
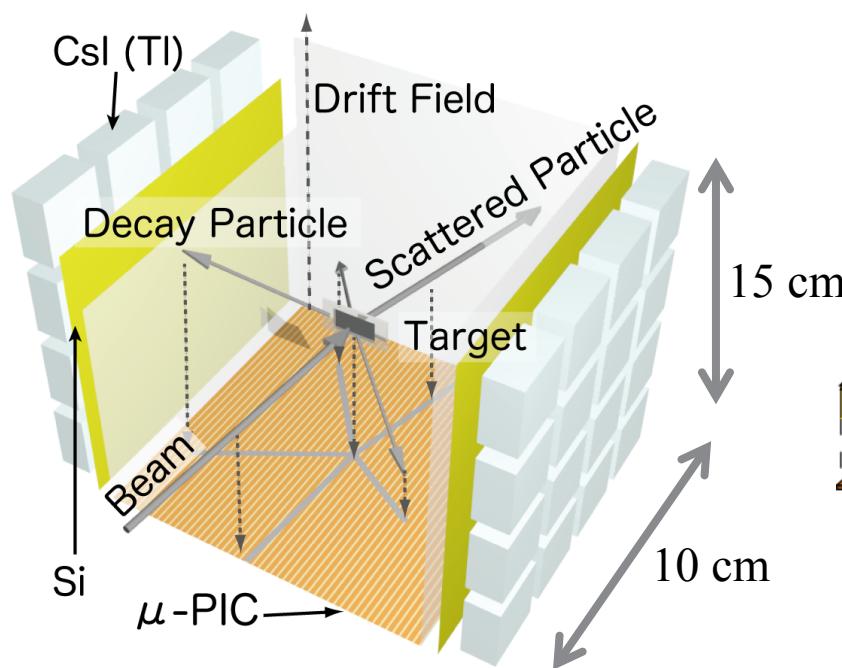
- Several states at 20.5, 22.0, and 24.3 MeV were observed near the  $^{12}\text{C} + 3\alpha$  threshold.
- Possible structures were seen above the  $6\alpha$  threshold although statistically poor .  
→ Need more statistics.

# Future Prospects

New experiment using MAIKo.

# MAIKo Time Projection Chamber

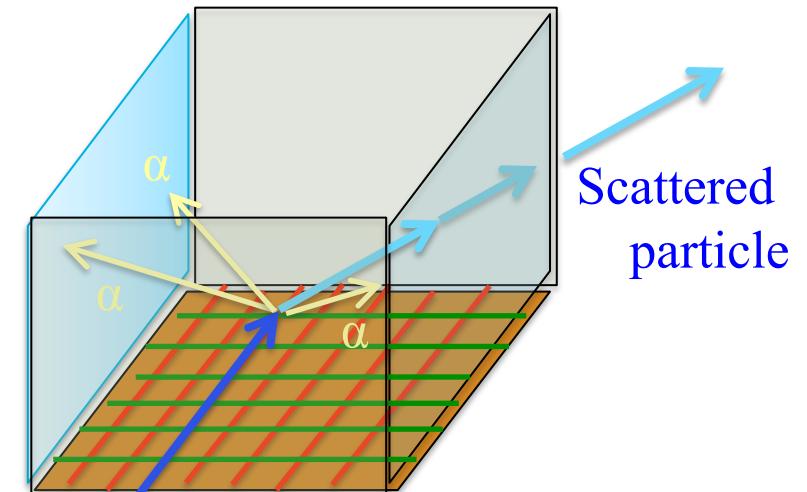
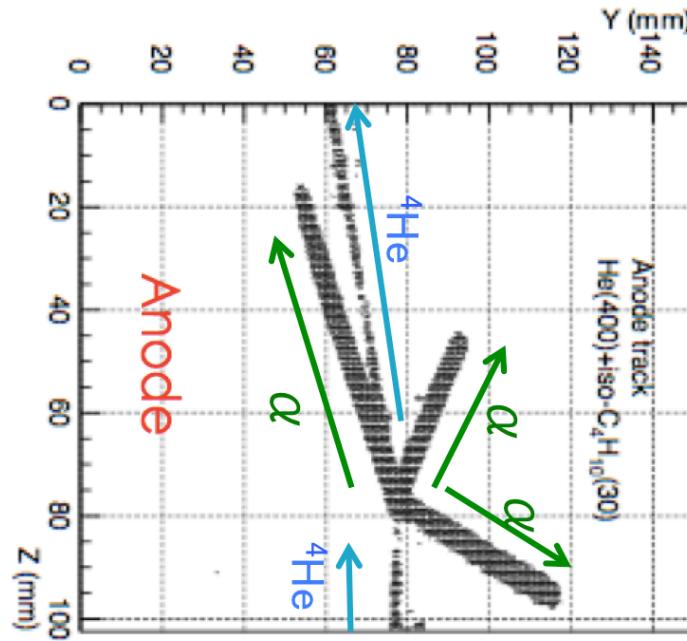
MAIKo TPC is developed by the Kyoto and RCNP groups.  
It will be installed at the target position of Grand Raiden.



Micro-Pixel Chamber ( $\mu$ -PIC)  
A. Ochi, et. al. NIM A **478**, 196 (2002).

- ◆ Detect low-energy decay particles with **large angular coverage**.
- ◆ Introduce  **$\mu$ -PIC + GEM** for multiplication and detection of electrons.
  - **$\mu$ -PIC** : 2-dimensional strip readout (400  $\mu$ m pitch).  
 $256A+256C = 512$  ch.
  - **GEM**: 140  $\mu$ m pitch, d=70  $\mu$ m, t=100  $\mu$ m (thick GEM)

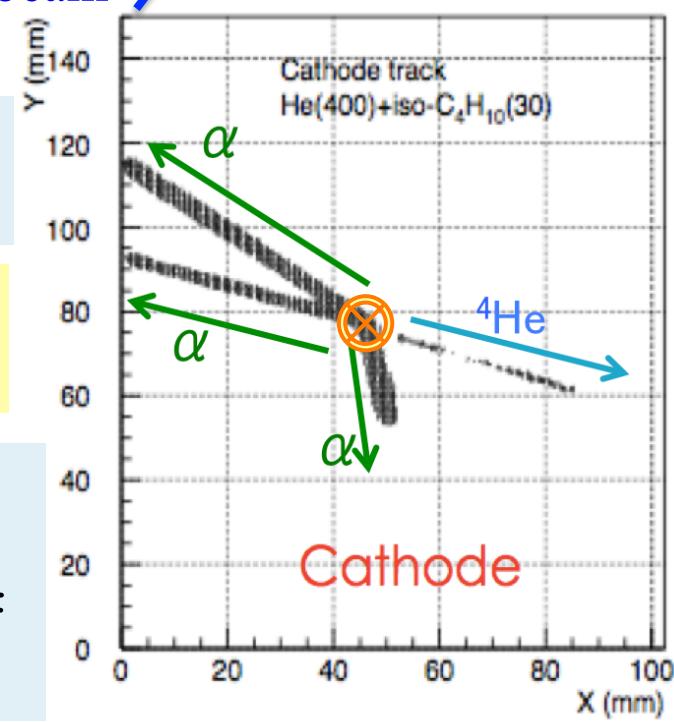
# Test measurement of $3\alpha$ decay



- ◆ Beam:  ${}^4\text{He}$  @ 12.5 MeV/u
- ◆ Gas: He(93%) + iC<sub>4</sub>H<sub>10</sub>(7%) @ 430 hPa

Scattered  $\alpha$  particle and  
3 decay  $\alpha$  particles are clearly observed.

$d\Omega$  for previous detector: 309 mSr  
 $d\Omega$  for MAIKo:  $\sim 4\pi$   
MAIKo will gain solid angle by a factor of  
 $(0.3/4\pi)^6 \sim 5 \times 10^6$  for  $6\alpha$  measurement.



# Summary

Inelastic  $\alpha$  scattering is an useful tool to examine a cluster structure in nuclei.

- E0 strength is a key observable.
- Complementary information is expected from the decaying-particle measurement.

$\alpha$  condensed states in  $^{24}\text{Mg}$  are searched.

- Several candidates of the  $\alpha$  condensed states emitting  $\alpha$  or  $^8\text{Be}$  are found.

New experiments are under going.

- A new time projection chamber MAIKo is under developed.
- Multi  $\alpha$  decay events will be measured in combination of Grand Raiden.

# Collaboration

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