

Formal Analysis of Real-World Security Protocols

Lecture 0: Organization and Motivation



What is a protocol?

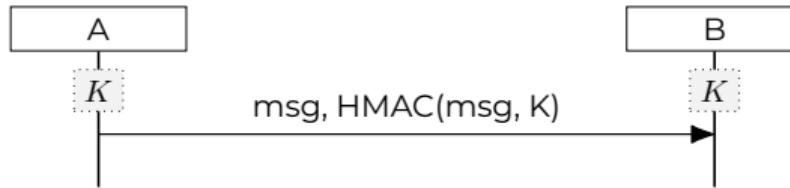
- A **protocol** is a set of rules that determine how two or more parties can achieve a common goal by exchanging messages





What is a protocol?

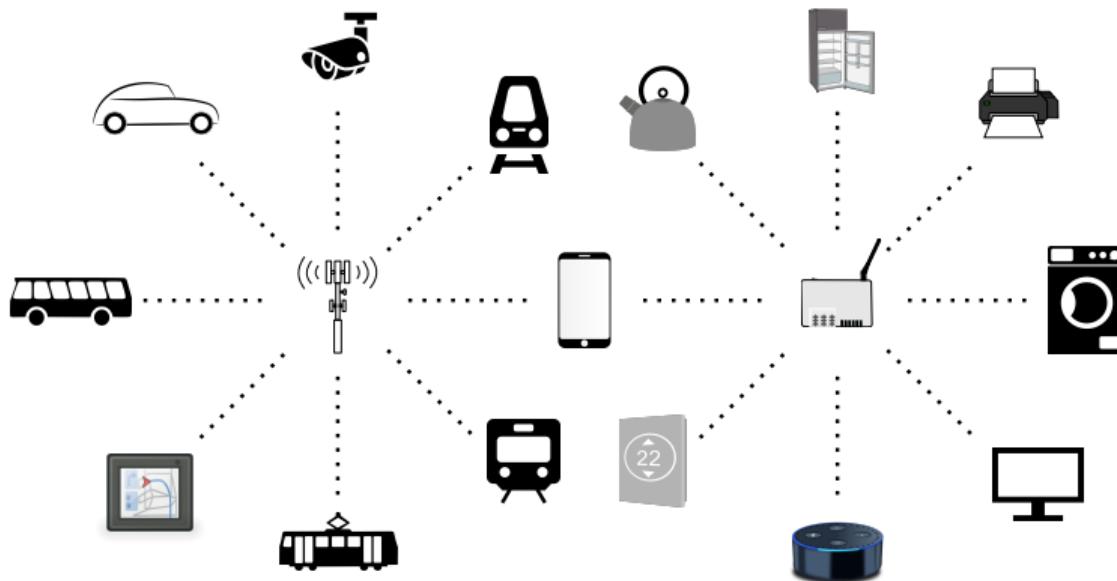
- A **protocol** is a set of rules that determine how two or more parties can achieve a common goal by exchanging messages
- Protocols that use cryptography to achieve security-related goals are called **security** or **cryptographic** protocols





Why should we care about protocol security?

- New things are constantly connected to the Internet
 - security **protocols** are everywhere





Why should we care about protocol security?

- New things are constantly connected to the Internet
 - security **threats** are everywhere

Nokia Threat Intelligence Report finds malicious IoT botnet activity has sharply increased¹

Number of IoT devices (bots) engaged in botnet-driven DDoS attacks rose from around 200,000 a year ago to approximately 1 million devices.

Researchers find 36 new security flaws in LTE protocol²

South Korean researchers apply fuzzing techniques to LTE protocol and find 51 vulnerabilities, of which 36 were new.

The tech flaw that lets hackers control surveillance cameras³

Hackers Can Clone Millions of Toyota, Hyundai, and Kia Keys⁴

Encryption flaws in a common anti-theft feature expose vehicles from major manufacturers.

Massive HTTP DDoS Attack Hits Record High of 71 Million Requests/Second⁵

¹<https://www.nokia.com/about-us/news-releases/2023/05/07/nokia-threat-intelligence-report-finds-malicious-iot-botnet-activity-has-sharply-increased/>

²<https://www.zdnet.com/article/researchers-find-36-new-security-flaws-in-lte-protocol/>

³<https://www.bbc.com/news/technology-65975446>

⁴<https://www.wirec.com/story/hackers-can-clone-millions-of-toyota-hyundai-kia-keys/>

⁵<https://thehackernews.com/2023/02/massive-http-ddos-attack-hits-record.html>

**How do we know
a protocol is
secure?**



Before 1970

- **No proofs**
- Trial and error – we're not quite sure what a clever attacker could do
- Security: break - patch - repeat





1970-1980

- **Let's prove security** (Goldwasser, Micali, Yao)
- Attacker is any polynomial-time Turing machine
- Reduce security problem to generically solving a hard problem (e.g., discrete logarithm, factoring)





- **Computational proofs**

- Proofs scale from primitives (“a signature scheme”) to small protocols (“a simple key exchange protocol”)
- Typically pen-and-paper proofs, very error prone
- *Not the focus of this lecture*

- **Symbolic proofs**

- 1983: symbolic attacker model (Dolev-Yao)
- Reason about abstract terms instead of bitstrings
- “Perfect cryptography” assumption: Attacker can only decrypt an encrypted message if they know the key
- Example property: Show that attacker can (not) learn a secret term

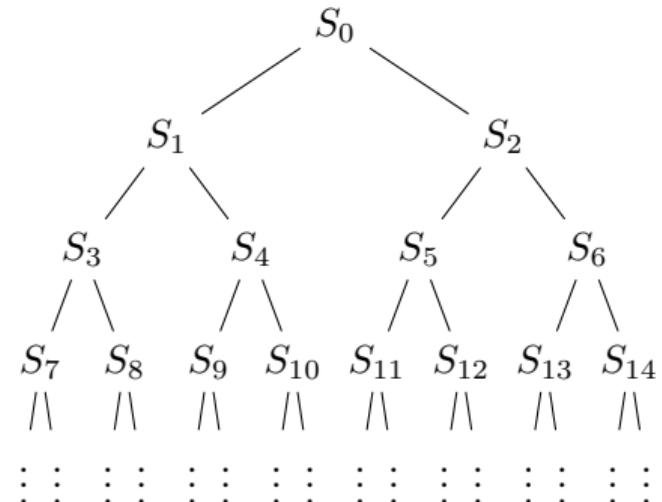


1990-2000

- **Model checkers become more widespread**
 - Analyze small finite cases
 - Found many flaws on basic designs
 - 1995: MitM attack on the NSPK protocol discovered with automated verification
- **Proliferation of tools & methods**
 - CSP/FDR, Prolog, NRL Protocol Analyzer, ...
 - BAN Logic and variants
 - Isabelle (Paulson)



- **Bounded analysis matures**
 - AVISPA/Avantssar (OFMC, SAT-MC, CL-Atse)
 - Hit scaling barrier: State space explosion
- **Unbounded analysis?**
 - Undecidable.. Yet workable in practice?
 - ProVerif, Maude-NPA, Scyther, CPSA, Athena



- Tool situation stabilizes
 - ProVerif
 - **Tamarin prover**
- Increased expressiveness
 - Equational theories
 - Loops / stateful protocols
- **Real-world analysis**
 - Scaling to real-world protocols
 - Stronger threat models
 - Visibility to security engineers and standards bodies



Course Overview



This lecture



- What is formal analysis of security protocols?
- Learn about one state-of-the-art tool: the **Tamarin prover**
 - Learn how Tamarin works
 - Learn how to use Tamarin
 - Analyze protocols!
- Understand the **guarantees** and **limitations** of such analyses
- How have they been applied to **real-world protocols**?
- What **research** still needs to be done to make protocols secure?



Lecture plan

Lecture	Content
0	Organization and Motivation
1	Terms and Equational Theories
2	Protocols in the Symbolic Model
3	Attacker Model and Trace Properties
4	Verification Theory (Part 1)
5	Verification Theory (Part 2)
6	Using Tamarin in Practice
7	Advanced Security Properties and Threat Models
8	Advanced Features (Part 1)
9	Advanced Features (Part 2)
10	Security Protocol Standards
11	Relation to Cryptography, Scaling, and the Future



Course book

- David Basin, Cas Cremers, Jannik Dreier, and Ralf Sasse. **Modeling and Analyzing Security Protocols with Tamarin: A Comprehensive Guide.**
 - Available online: <https://tamarin-prover.com/book/index.html>
 - Each lecture will have a list of references to the relevant sections (based on v0.9.5)
- Other references will be included as additional reading when necessary

Analysis of Real-World Protocols



The Tamarin prover



- Symbolic analysis of security protocols
- First released in 2012, still under active development
- Simple protocols: Fully automatic
- Complex protocols: Interactive mode
- Considers an **unbounded number of sessions**, supports advanced features like stateful protocols and loops
- Open source on GitHub:
<https://tamarin-prover.com/>

Running Tamarin 1.6.0

Proof scripts

Message theory

Multiset rewriting rules (0)

Tactic(s)

New sources (0 cases, deconstructions complete)

Refined sources (0 cases, deconstructions complete)

all-traces

lemmas

```
Client_Session_key_secrecy
  -> S k #R.
    ((SesskeyCC(S, k) #R) & (R(k > #R)))
    C-C R. (LkReveal(S, k) #R))
simplify
solveF Client_1
case Client_1
  solved (S k #R)
  case Client_3
    solved (S k #R)
    case Client_3
      solved (S k #R)
      case Client_3
        solved (S k #R)
        by contradiction
        by from formulae
      qed
    qed
  qed
qed

lemmas Client_auth:
all-traces
  -> S k #R.
    ((SesskeyCC(S, k) #R) &
     ((C R. AnswerRequest(S, k) #R) & (R(k > #R)) &
     (C R. (LkReveal(S, k) #R) & (R(k > #R))))
by sorry

lemmas Client_auth_injective:
all-traces
  -> S k #R.
    ((SesskeyCC(S, k) #R) &
     (C R. (AnswerRequest(S, k) #R) & (R(k > #R)) &
     (C R. (LkReveal(S, k) #R) & (R(k > #R))))
by sorry

lemmas Client_session_key_honest_setup:
exists-trace
  -> S k #R.
    ((SesskeyCC(S, k) #R) & (C-C R. LkReveal(S, k) #R))
simplify
solveF Client_1
case Client_1
  solved (S k #R)
  case Client_3
    solved (S k #R)
    case Client_3
      solved (S k #R)
      case Client_3
        solved (S k #R)
        by contradiction
        by from formulae
      qed
    qed
  qed
qed
```

Constraint System is Solved

Constraint system



The Tamarin prover



Constraint solver



The Tamarin prover



← Theorem prover

← Constraint solver



Application domain examples

Key Exchange

- Naxos
- Signed DH
- Station-to-Station
- IKEv2
- Wireguard
- PQ-Wireguard
- Noise protocol family

Large Case Studies

- TLS 1.3
- IEEE 802.11 WPA2
- 5G-AKA
- 5G handover
- SPDM 1.2
- Apple iMessage PQ3

Payment

- EMV

Authentication

- WS-Security
- ACME

E-voting

- Alethea
- Belenios
- Selene

PKI

- ARPKI



Application domain examples

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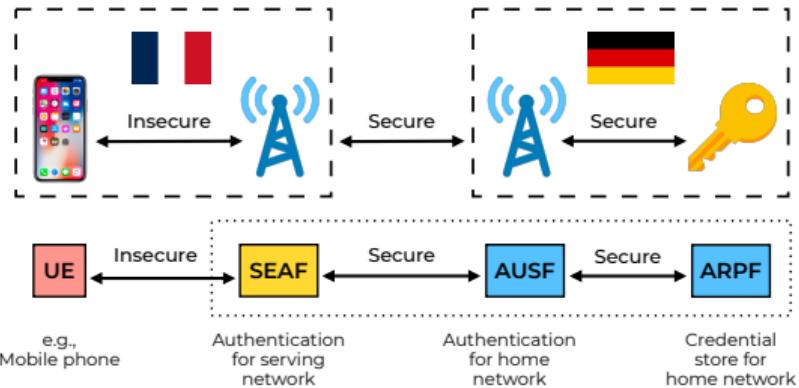
Example 1 - TLS 1.3

- **What is it?**
 - Transport Layer Security, version **1.3**
 - Likely the world's most used security protocol
- **Tamarin analysis**
 - Explicit support for the IETF during the development of TLS 1.3
 - Several person months of work: much of it in just understanding the standard
- **Results**
 - Tamarin finds complete break for the main proposal for Rev 10+'s “delayed authentication”
 - Minimal attack involves 3 modes & 18 messages
 - Motivated change to other mechanism
 - Proven core properties for final version



Example 2 - 5G-AKA

- What is it?
 - 5G Authentication and Key Agreement
 - The core key exchange of 5G
- Tamarin analysis
 - Analysis of the near-final standard (>1 000 pages)
 - Standard notably harder to parse than TLS 1.3's RFC, yet semi-stable
- Results
 - Tamarin finds that privacy is not guaranteed (linkable) – needs redesign
 - Tamarin proves other properties under some assumptions
 - (Prediction: many current wontfix'es will cause trouble later)





Example 3 - EMV

- **What is it?**

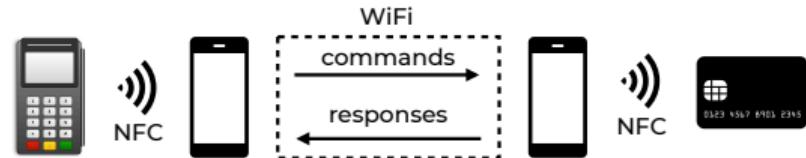
- Europay, Mastercard, and Visa
- Protocol between your bank, terminal, credit card
- Modern versions have many different modes: Contactless, PIN, etc.

- **Tamarin analysis**

- Standard documentation complex
- Partial reverse engineering

- **Results**

- Main attacks by researchers from ETH Zürich
 - PIN bypass: use man-in-the-middle to perform arbitrarily large transaction
 - Card mixup attack allow bypassing PIN codes
- Later refined attacks by researchers from Birmingham and Surrey
 - Relay attacks and attacks on locked iPhones



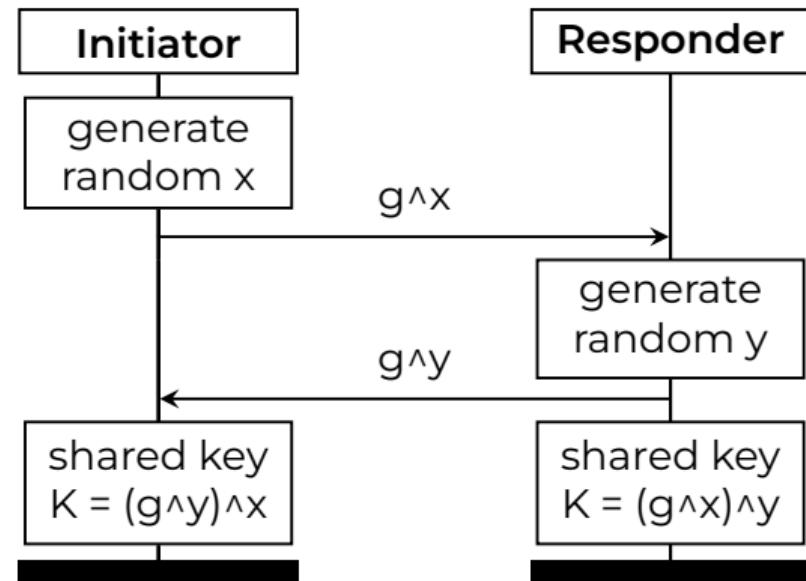
Back to Basics: Diffie-Hellman



Diffie-Hellman key exchange

One of the first proposals for secure protocols, for which we will see several variants.

- “ g^x ” is shorthand for “ $gx \bmod P$ ”, where g is the generator of a prime order group of order P . It is **efficient to compute g^x**
- If the group is sufficiently large, it is **infeasible to compute x from g^x**

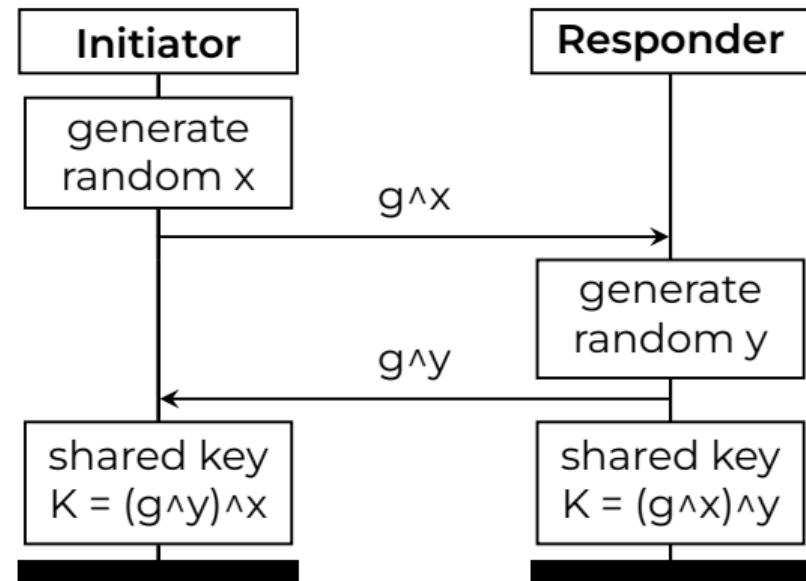




Diffie-Hellman key exchange

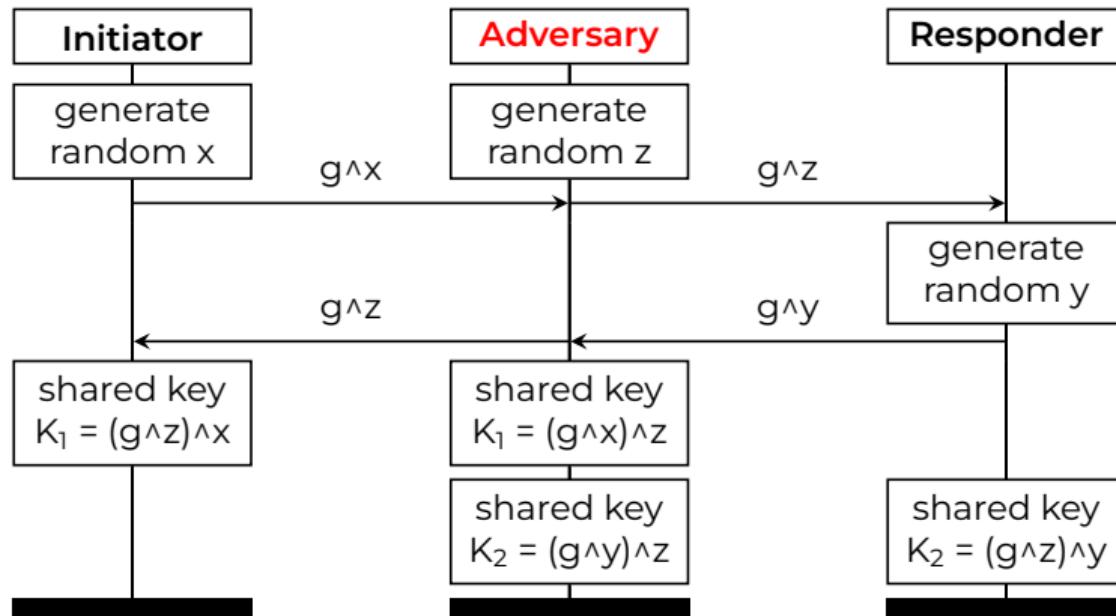
What should this protocol achieve?

- If an adversary observes the network messages g^x and g^y , they cannot compute the shared key!
- What if the adversary can insert messages too?



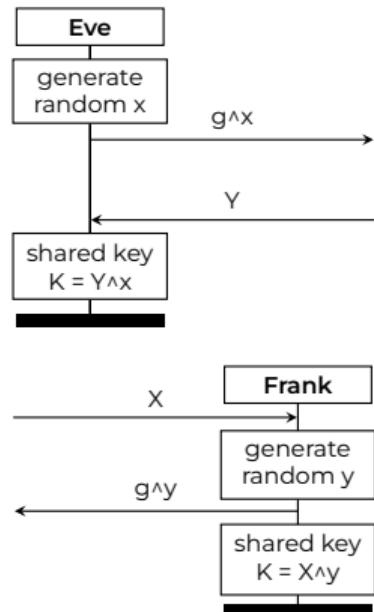
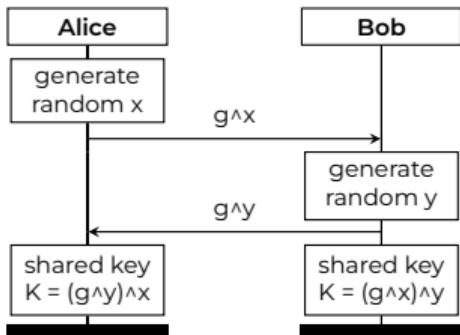


Man-in-the-middle attack



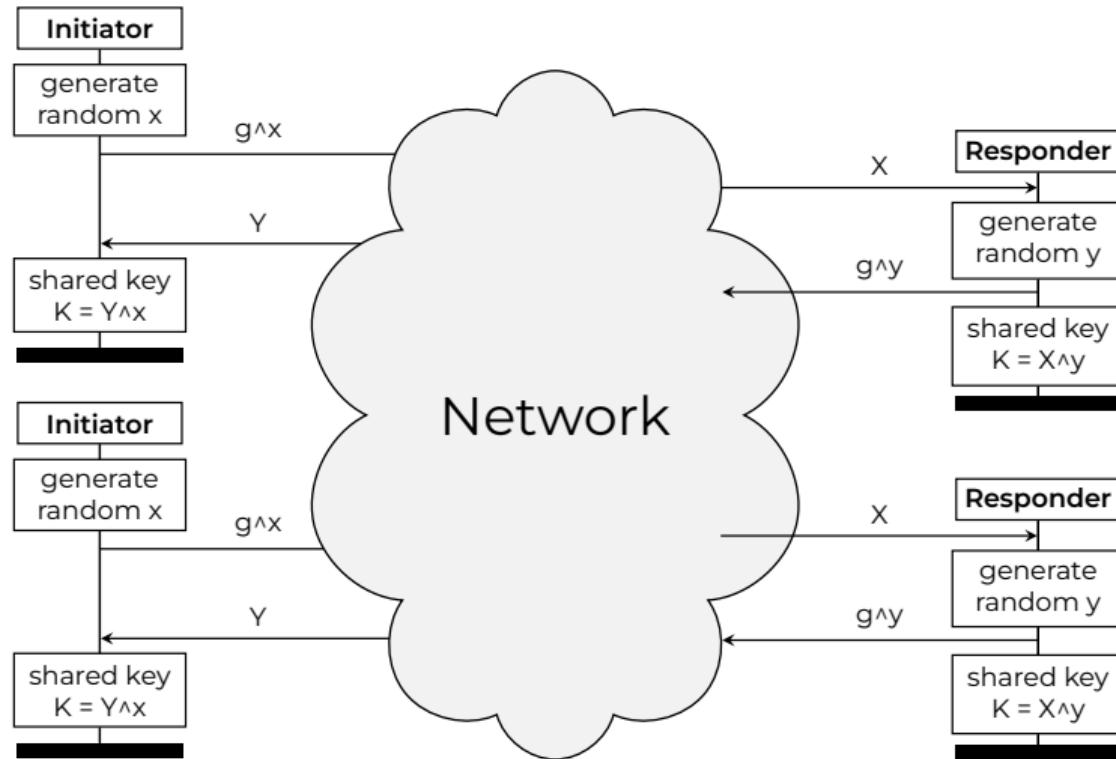


Execution model





Adversary view



Summary



Summary



- Today, we learned that..
 - ..protocol security can be analyzed computationally or **symbolically**
 - ..we can automate the process using modern tools like **TAMARIN**
- In the next lecture, we will learn more about modeling..
 - messages as **terms**, and
 - cryptographic primitives as **equations**

Running Tamari 1.8.0

Index Download Actions Options

Proof scripts

Message theory

Multiset rewriting rules (0)

Tactics(0)

Raw sources (0) cases, deconstructions complete

Defined sources (0) cases, deconstructions complete

all-traces

Issue Client.CipherKeyKeyAgreement

simplicity

solved Client.CipherKeyKeyAgreement

case Client

simplicity

case Revolver

by contradiction

and

and

Issue ClientAuth

all-traces

* S K R

(ClientKey(C S, K) # P) =
((ClientKey(C S, K) # R) & (R < R))
&
(ClientKey(C S, K) # R) =
(ClientKey(C S, K) # R) & (R < R))

by sorry

Issue ClientAuth.Injective

all-traces

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(ClientKey(C S, K) # R) & (R < R) =
ClientKey(C S, K) # R

simplicity

case Client

simplicity

case Revolver

simplicity

case Revolver

simplicity

and

and

Client.CipherKeyKeyAgreement

Revolver.CipherKeyKeyAgreement

test: none

formulas: r = (LsRevolver(S) # R) = L

subterms:

equations:

subc:

lemmas:

allowed cases: refind

The screenshot shows the TAMARIN interface with a proof script window on the left containing terms and equations, and a constraint system window on the right showing a state transition graph with nodes for clients and servers.



Reading material

Recommended reading: [Bas+25, Ch. 1–2]

[Bas+25] D. Basin, C. Cremers, J. Dreier, and R. Sasse. **Modeling and Analyzing Security Protocols with Tamarin: A Comprehensive Guide.** Draft v0.9.5. May 2025.



Case studies i

Case studies:

TLS 1.3 [Cre+16; Cre+17],

5G-AKA [Bas+18; CD19],

EMV [BST21b; BST21a; Rad+22]

- [Bas+18] D. Basin, J. Dreier, L. Hirschi, S. Radomirovic, R. Sasse, and V. Stettler. **A Formal Analysis of 5G Authentication.** In: Proceedings of the 2018 ACM SIGSAC Conference on Computer and Communications Security. 2018.

Case studies ii

- [BST21a] D. Basin, R. Sasse, and J. Toro-Pozo. **Card Brand Mixup Attack: Bypassing the PIN in non-Visa Cards by Using Them for Visa Transactions.** In: 30th USENIX Security Symposium (USENIX Security 21). 2021.
- [BST21b] D. Basin, R. Sasse, and J. Toro-Pozo. **The EMV Standard: Break, Fix, Verify.** In: 2021 IEEE Symposium on Security and Privacy (SP). 2021.
- [CD19] C. Cremers and M. Dehnel-Wild. **Component-Based Formal Analysis of 5G-AKA: Channel Assumptions and Session Confusion.** In: 26th Annual Network and Distributed System Security Symposium, NDSS. 2019.

Case studies iii

- [Cre+16] C. Cremers, M. Horvat, S. Scott, and T. van der Merwe. **Automated Analysis and Verification of TLS 1.3: 0-RTT, Resumption and Delayed Authentication.** In: 2016 IEEE Symposium on Security and Privacy (SP). 2016.
- [Cre+17] C. Cremers, M. Horvat, J. Hoyland, S. Scott, and T. van der Merwe. **A Comprehensive Symbolic Analysis of TLS 1.3.** In: Proceedings of the 2017 ACM SIGSAC Conference on Computer and Communications Security. 2017.
- [Rad+22] A.-I. Radu, T. Chothia, C. J. Newton, I. Boureanu, and L. Chen. **Practical EMV Relay Protection.** In: 2022 IEEE Symposium on Security and Privacy (SP). 2022.