Recommendation Systems

Question 1: Here is a table of 1-5-star ratings for five movies (M, N, P. Q. R) by three raters (A, B, C).



Normalize the ratings by subtracting the average for each row and then subtracting the average for each column in the resulting table. Then, identify largest element and entry of (C,P) about the normalized table.

SOLUTION

						-		-	200
Give	n ta	lole is		60	1000	Mean	n of E	ach r	ow
	M	N	P	a	R		A ->3		
Α	1	2	3	4	5		$B \Rightarrow 3$		
B	2	3	2	5	3		C> 4	_	
C	5	5	5_	3	2				
Table	e aft	er so	Urbrac	ting	by ron	s med	in		
		N			The second second			-	
A	-2	-1	0	1	2				
B	-1	0	-1	2	0				
C	1	1	1	-1	-2				
Maan	~ I	endh	rs Oct	N. M					
					P >	0	Q > 0	.63	R > 0
Table	af	ter	subt	ncti	ng by	columi	n me	an	
		N							
		-1							
P		0							
_			1	1 /2					
В	1.67			THE RESIDENCE					

Largest element is 2.

Entry of CP is 1.

QUESTION 2

Below is a table giving the profile of three items.

Α	1	0	1	0	1	2
В	1	1	0	0	1	6
С	0	1	0	1	0	2

The first five attributes are Boolean, and the last is an integer "rating." Assume that the scale factor for the rating is α . Compute, as a function of α , the cosine distances between each pair of profiles. For each of α = 0, 0.5, 1, and 2, determine the cosine of the angle between each pair of vectors.

SOLUTION

Assignment 7, Question 2
Given table
Passes Alexander Service Size of the Size
A 130 140 1727 71 13 14 14
B 1 1 0 0 1 C
C 0 1 1 0 1 1 0 1 2 7 1 1 0 0 3 7 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
E de Santa de la Companya de la Comp
For x=0 [multiply x with last integer rating]
A I DO N DO TO DO TO DO TO
8110010
0010100
A CONTRACTOR OF THE PARTY AND A CONT
$\cos(A/B) = \frac{A \cdot B}{A \cdot B} = \frac{2}{5} = 0.67$
11AII .11CII \13.\13
$\cos(A/C) = \frac{0}{\sqrt{3}\sqrt{2}} = 0$
13.12
cos (B,C) = 1 - 0.408

100	For <= 0.5						
ST.	d pilye the Bilxetha						
	A 1 0 1 0200 01 100 0						
	B 1 1 0 10 00 10 . 3 30 100 0						
	c 0 10 0 200000 000000000000000000000000						
1	32000 0 20100 A						
	$cus(A/B) = 5 \times 0000 = 6.7217$						
100	VY. VI2						
	818 2 5008						
	(OS (A/C) = 1 = 0.2886						
	0.10.10.4						
	$cos(B,C) = \frac{4}{\sqrt{12} \cdot \sqrt{3}} - 6.67$						

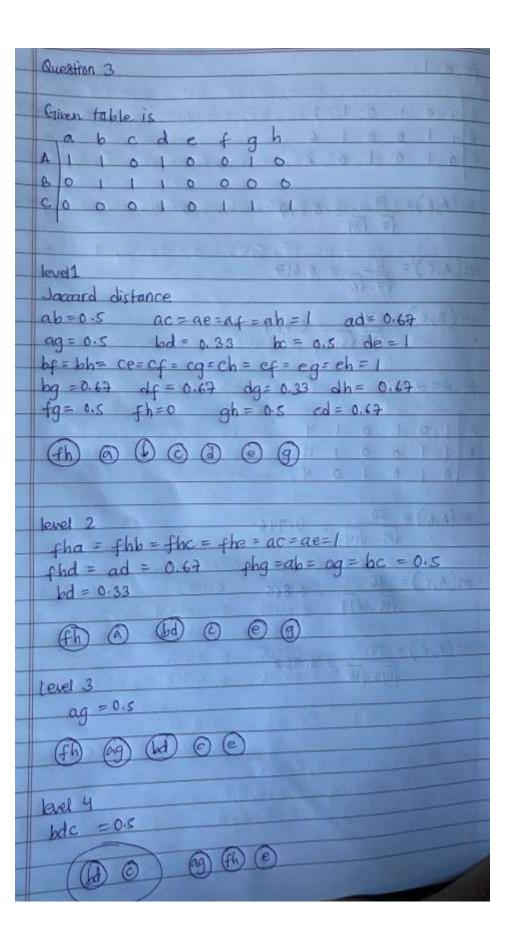
QUESTION 3

Below is a utility matrix representing ratings by users A, B, and C for items a through h.

	a	b	c	d	e	f	g	h
Α	4	5		5	1		3	2
В		3	4	3	1	2	1	
С	2		1	3		4	5	3

Treat ratings of 3, 4, and 5 as 1 and 1, 2, and blank as 0. Compute the Jaccard distance between each pair of items. Then, cluster the items hierarchically into four clusters, using the Jaccard distance. When a cluster consists of more than one item, take the distance between clusters to be the minimum over all pairs of items, one from each cluster, of the Jaccard distance between those items. Break ties lexicographically. That is, sort the items that would be merged alphabetically, and merge those clusters whose resulting set would be first alphabetically.

Note: if you are not familiar with hierarchical clustering, read Sect. 7.2 of the MMDS book.

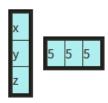


QUESTION 4

We want to do an approximate UV-decomposition of the matrix M =



We shall use only a single column for U and a single row for V, so the goal is to make the product UV as close as possible to M. Initially, we shall set V to [5,5,5] and make the entries of U unknown. Then in the first step, we choose the values of x, y, and z that minimize the root-mean-square error (RMSE) between the product



and the matrix M.

Find the values of x, y, and z that minimize the RMSE.

SOLUTION

Given matrices M, U, V

The product of U and V is

5x	5x	5x
5y	5y	5y
5z	5z	5z

Let the equation be

$$(5x-1)^2 + (5x-2)^2 + (5x-3)^2 + (5y-4)^2 + (5y-5)^2 + (5y-6)^2 + (5z-7)^2 + (5z-8)^2 + (5z-9)^2 = 0$$

Differentiate above equation with x, we get $150x - 60 = 0 \rightarrow x = 2/5$

Differentiate above equation with y, we get $150y - 150 = 0 \rightarrow y = 1$

Differentiate above equation with z, we get $150z - 240 = 0 \rightarrow z = 8/5$