

$$\tilde{\nabla} \bar{u} = \frac{\partial u_i}{\partial x_j} = \begin{pmatrix} \frac{\partial u_1}{\partial x_1} & \frac{\partial u_1}{\partial x_2} & \frac{\partial u_1}{\partial x_3} \\ \frac{\partial u_2}{\partial x_1} & \frac{\partial u_2}{\partial x_2} & \frac{\partial u_2}{\partial x_3} \\ \frac{\partial u_3}{\partial x_1} & \frac{\partial u_3}{\partial x_2} & \frac{\partial u_3}{\partial x_3} \end{pmatrix}$$

Descomposición aditiva de un tensor de 2º orden

$$\tilde{A} = \underbrace{\frac{1}{2}(\tilde{A} + \tilde{A}^T)}_{\text{simétrico}} + \underbrace{\frac{1}{2}(\tilde{A} - \tilde{A}^T)}_{\text{hemisimétrico}}$$

$$\nabla^s \bar{u}_i = \frac{1}{2} \left(\frac{\partial u_i}{\partial x_j} + \frac{\partial u_j}{\partial x_i} \right)$$

Ejemplo:

$$u(x, y) = x$$

$$v(x, y) = y$$

$$\epsilon_{xx} = \frac{\partial u}{\partial x} = 1$$

$$\epsilon_{yy} = \frac{\partial v}{\partial y} = 1$$

$$\epsilon_{xy} = 0$$

