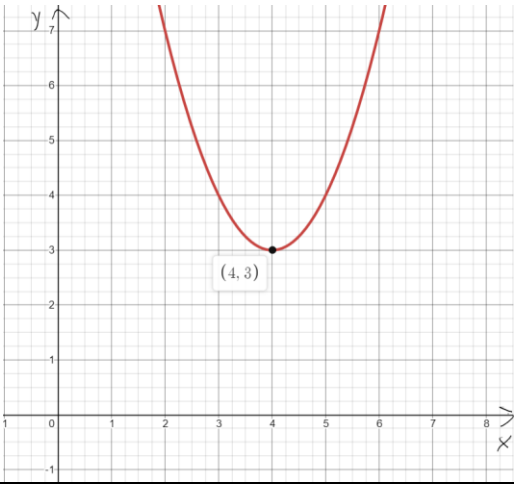


No.	SOLUTION
1(a)	$\left(\frac{x^5 y^4}{64 z^0}\right)\left(\frac{8 y^3}{x^3}\right)$ $= \frac{8 x^{5-3} y^{4+3}}{64(1)}$ $= \frac{x^2 y^7}{8}$
1(b)	$(3 p^2 q^{-2})^2 (27 p^2 q^{-5})^{-1}$ $= (3 p^2 q^{-2})^2 \times \frac{1}{27 p^2 q^{-5}}$ $= 9 p^4 q^{-4} \times \frac{1}{27 p^2 q^{-5}}$ $= \frac{p^2 q}{3}$
1(c)	$\left(\sqrt{\frac{36 x^4}{y^{12}}}\right) \times \frac{y^6}{2 x}$ $= \frac{6 x^2}{y^6} \times \frac{y^6}{2 x}$ $= 3 x$
2(a)	$(2 a + b)^2 - (2 a - b)^2$ $= [2 a + b + 2 a - b][2 a + b - (2 a - b)] \quad \text{or} \quad 4 a^2 + 4 a b + b^2 - (4 a^2 - 4 a b + b^2)$ $= 8 a b$
2(b)	$\begin{array}{r} x^2 + x - 2 \\ x+1 \overline{) x^3 + 2x^2 - x + 5} \\ \underline{-(x^3 + x^2)} \phantom{+ 5} \\ x^2 - x \phantom{+ 5} \\ \underline{-(x^2 + x)} \phantom{+ 5} \\ -2x + 5 \phantom{+ 5} \\ \underline{-(-2x - 2)} \\ 7 \end{array}$ <p><math>\therefore</math> quotient <math>= x^2 + x - 2</math> and remainder <math>= 7</math></p>

2(c)	$(x+5)^3 - 9x - 45$ $= (x+5)^3 - 9(x+5)$ $= (x+5)\left[(x+5)^2 - 9\right]$ $= (x+5)\left[(x+5)+3\right]\left[(x+5)-3\right]$ $= (x+5)(x+8)(x+2)$
2(d)	<p>Let <math>f(x) = 2x^3 + ax^2 - 7x + b</math>,</p> <p>as <math>(x-2)</math> is a factor of <math>2x^3 + ax^2 - 7x + b</math>,</p> $f(2) = 0$ $2(2)^3 + a(2)^2 - 7(2) + b = 0$ $16 + 4a - 14 + b = 0$ $4a + b = -2$ <p>Since <math>2x^3 + ax^2 - 7x + b</math> has a remainder of <math>-10</math> when divided by <math>(x+3)</math>,</p> $f(-3) = -10$ $2(-3)^3 + a(-3)^2 - 7(-3) + b = -10$ $-54 + 9a + 21 + b = -10$ $9a + b = 23$ $4a + b = -2 \quad (1)$ $9a + b = 23 \quad (2)$ $(2) - (1): 5a = 25$ $a = \frac{25}{5} = 5$ <p>Subst <math>a = 5</math> in (1): <math>4(5) + b = -2</math></p> $b = -2 - 20 = -22$
3(a)(i)	$\frac{12a^9b^8}{a^2+3a-4} \times \frac{a-1}{3a^2b^5}$ $= \frac{12a^9b^8}{(a-1)(a+4)} \times \frac{a-1}{3a^2b^5}$ $= \frac{4a^7b^3}{(a+4)}$
3(a)(ii)	$\frac{x+3}{x^2-25} - \frac{1}{x+5}$ $= \frac{x+3}{(x+5)(x-5)} - \frac{1}{x+5}$ $= \frac{x+3}{(x+5)(x-5)} - \frac{(x-5)}{(x+5)(x-5)}$ $= \frac{x+3-x+5}{(x+5)(x-5)}$

	$= \frac{8}{(x+5)(x-5)}$
3(a)(iii)	$\frac{\frac{1}{u} - \frac{1}{3u}}{\frac{1}{u} - \frac{1}{6u}}$ $= \frac{\frac{3u}{6} - \frac{3u}{3u}}{\frac{3u}{6u} - \frac{3u}{6u}}$ $= \frac{\frac{2}{3u}}{\frac{4}{6u}}$ $= \frac{4}{5}$
4	$\frac{2x^2 + 7x - 1}{(x+1)(x^2+5)} = \frac{A}{x+1} + \frac{Bx+C}{x^2+5}$ <p>Multiply every term by <math>(x+1)(x^2+5)</math>,</p> $2x^2 + 7x - 1 = A(x^2 + 5) + (Bx + C)(x + 1)$ <p>Subst <math>x = -1</math>:</p> $-6 = 6A$ $A = -1$ <p>Comparing coefficients of <math>x^2</math>,</p> $2 = A + B$ $2 = -1 + B$ $B = 3$ <p>Comparing constant terms,</p> $-1 = 5A + C$ $-1 = -5 + C$ $C = 4$ $\frac{3x^2 - 4x + 7}{(x-1)(x^2+2)} = -\frac{1}{x-1} + \frac{3x+4}{x^2+2}$

5(a)	$f(-1) = -2$ $f(2) = -5$
5(b)	$x = -0.8, 1, 3.8$
5(c)	$f'(0) = 0$ The gradient of the tangent line at $x = 0$ is 0.
5(d)	$\{0 < x < 1\}$ or $(0, 1)$
5(e)	$f'(1)$ is negative and $f'(4)$ is positive, hence $f'(1)$ is less than $f'(4)$ .
5(f)	The domain is $\{x \mid -\infty < x < \infty\}$ or $(-\infty, \infty)$ The range is $\{f(x) \mid -\infty < f(x) < \infty\}$ or $(-\infty, \infty)$
6(a)(i)	$g(6) = (6-4)^2 + 3$ $= 7$
6(b)(ii)	$g(k+1) = (k+1-4)^2 + 3$ $= (k-3)^2 + 3$ $= k^2 - 6k + 12$
6(b)	<p>The graph <math>g(x) = (x-4)^2 + 3</math> is the graph of <math>f(x) = x^2</math> shifted 4 units to the right, and 3 units upward.</p> 
7 (a)	$R(x) = (12 + 0.5x)(36 - 2x)$ $= 432 - 6x - x^2$ $= -x^2 - 6x + 432$
(b)	$R(0) = 432.$

	This means rental per canoe is kept at \$12, or no increase in rental price																
(c)	$x$ is negative, means you lower the rental price																
(d)	<table><tr><td><math>x</math></td><td>-4</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td></tr><tr><td><math>R(x)</math></td><td>440</td><td>441</td><td>440</td><td>437</td><td>432</td><td>425</td><td>416</td></tr></table>	$x$	-4	-3	-2	-1	0	1	2	$R(x)$	440	441	440	437	432	425	416
$x$	-4	-3	-2	-1	0	1	2										
$R(x)$	440	441	440	437	432	425	416										
(e)	You charge $=12-3(0.5)=\$10.5$ per canoe for maximum revenue																
(f)	It means you rent the canoe for free																