

**REPORT PROJECT TWO CSE306**  
**Free-surface 2D fluid solver using incompressible Euler's equations**

In this report, we will use  $N$  to represent the number of points. I will now outline the progress made on the second project of CSE306. The entire code presented here is my original work. However, I encountered some challenges, and in those instances where I sought assistance from a specific individual or referred to a particular resource, I have provided the citation alongside the relevant code.

## **I. Voronoï Parallel Linear Enumeration**

I have implemented the naive polygon clipping algorithm by Sutherland-Hodgman. This initial lab was mostly completed during class and should follow the professor's solution closely. It resulted in the implementation of a Polygon class, a Voronoi diagram class, and a polygon clipping function.

Here are two diagrams I generated.

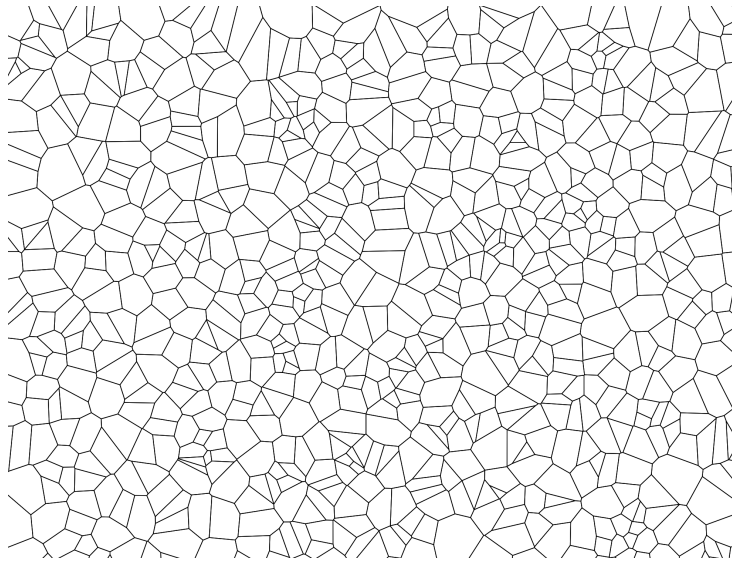


Figure 1: Voronoï Diagram generated with  $N=1000$  points. The generation took 3432.78 milliseconds.

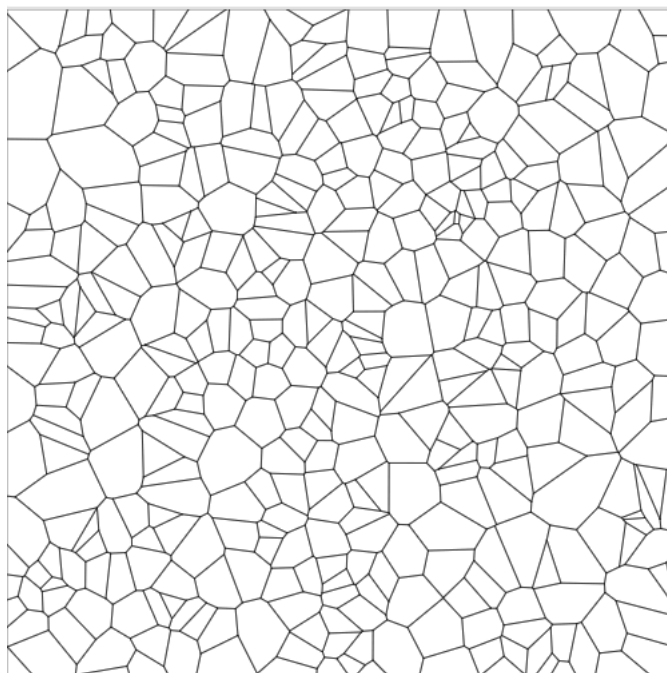


Figure 2: Voronoï Diagram generated with  $N=400$  points. The generation took 667.876 milliseconds.

## II. Semi-Discrete Optimal Transport

I've added Power diagram functionality to my Voronoi Diagram by making some changes to the Sutherland-Hodgman algorithm. Then, I included all the necessary files for the lbfgs to function, which are located in the lbfgs folder. As a result, I implemented an "optimize" function with an evaluate function to perform the gradient descent. To test my code, I decided to set the weights as  $1/N$ .

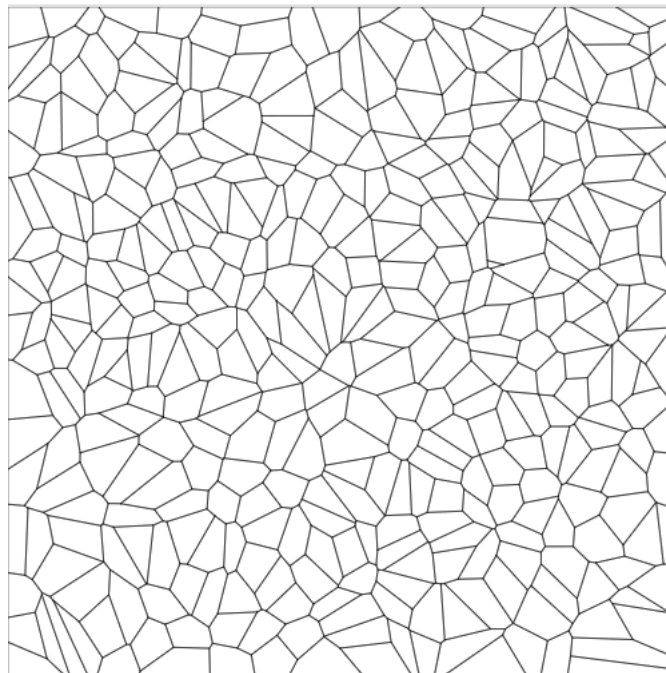
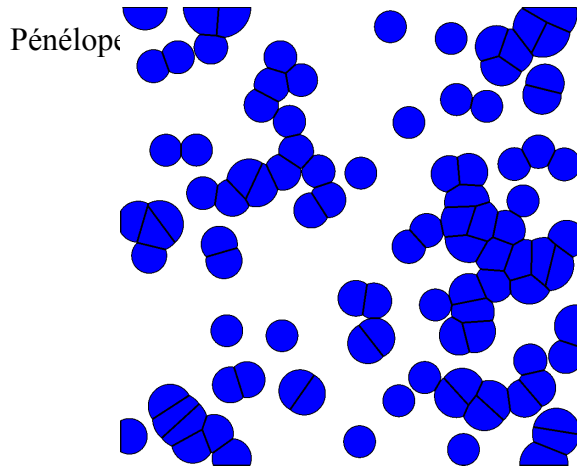


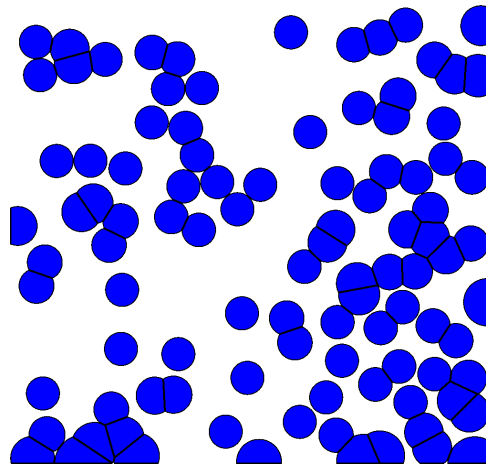
Figure 3: For weights :  $1/N$  ,  $N = 400$ , the generation took 7654.35 milliseconds

### III. Fluid visualiser

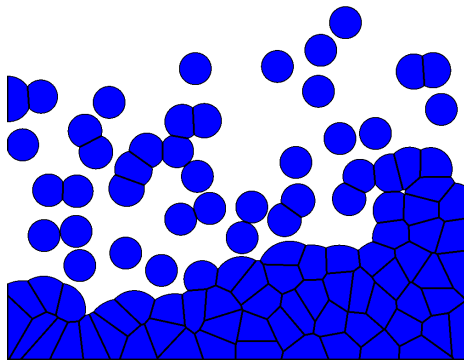
I implemented a semi-discrete optimal transport fluid simulator with free surfaces. I thus changed the evaluate, compute, and optimize functions. The versions before implementing the fluid visualizer are put as comments in the code.



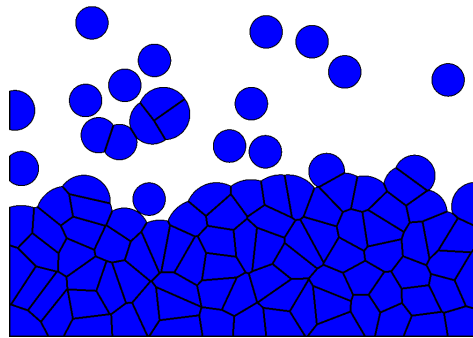
frame n1



frame n10



frame n20



frame n40

$N = 100$ ,  $dt = 0.01$ , number of steps = 50, mass of the particles = 50,  $\epsilon = 10^{-5}$ , volume of the air: 0.4, volume of the fluid: 0.6.

Elapsed time: 1.23657e+06 milliseconds

The corresponding GIF can be found in the repository. It is called “gen1.gif”