

Hw10

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1 b-2-2

1.1 VAR(4) model

The model is

$$z_t = \begin{bmatrix} 0.15 \\ 0.08 \\ 0.24 \end{bmatrix} + \begin{bmatrix} 0.52 & 0.07 & 0.06 \\ 0.38 & 0.32 & 0.41 \\ 0.52 & 0.17 & 0.15 \end{bmatrix} z_{t-1} + \begin{bmatrix} -0.05 & 0.16 & -0 \\ -0.17 & -0.25 & 0.06 \\ -0.22 & -0.16 & 0.23 \end{bmatrix} z_{t-2} \\ + \begin{bmatrix} 0.05 & -0.28 & 0.14 \\ 0.10 & 0.12 & 0.01 \\ 0.05 & -0.08 & 0.07 \end{bmatrix} z_{t-3} + \begin{bmatrix} 0.04 & 0.26 & -0.25 \\ 0.07 & -0.09 & -0.10 \\ 0.15 & -0.15 & -0.05 \end{bmatrix} z_{t-4} + a_t$$

```
> temp=tempfile()
> download.file("http://faculty.chicagobooth.edu/ruey.tsay/teaching/mtsbk/data-ch2.zip",temp)
> da=read.table(unz(temp, "Users/rst/Documents/backup/mts/y2012/data/ch2/q-gdp-ukcaus.txt"),header=T)
> gdp=log(da[,3:5])
> dim(gdp)

[1] 126    3

> z=100*(gdp[2:126,]-gdp[1:125,])
> library(MTS)
> m3=VAR(z,4)
```

Constant term:

```
Estimates:  0.1479567 0.07757439 0.2386772
Std.Error:  0.07478564 0.08003665 0.08583514
```

AR coefficient matrix

AR(1)-matrix

```
      [,1] [,2] [,3]
[1,] 0.516 0.0719 0.0639
[2,] 0.378 0.3160 0.4096
[3,] 0.519 0.1730 0.1504
```

standard error

```
      [,1] [,2] [,3]
[1,] 0.0953 0.0945 0.0887
[2,] 0.1020 0.1011 0.0949
[3,] 0.1094 0.1084 0.1018
```

```

AR( 2 )-matrix
      [,1] [,2] [,3]
[1,] -0.0504 0.160 -0.00198
[2,] -0.1740 -0.254 0.06295
[3,] -0.2178 -0.159 0.22561
standard error
      [,1] [,2] [,3]
[1,] 0.101 0.0986 0.0955
[2,] 0.108 0.1055 0.1022
[3,] 0.116 0.1132 0.1096
AR( 3 )-matrix
      [,1] [,2] [,3]
[1,] 0.0524 -0.2788 0.1411
[2,] 0.0962 0.1203 0.0137
[3,] 0.0478 -0.0786 0.0738
standard error
      [,1] [,2] [,3]
[1,] 0.103 0.0983 0.0937
[2,] 0.110 0.1052 0.1003
[3,] 0.118 0.1129 0.1076
AR( 4 )-matrix
      [,1] [,2] [,3]
[1,] 0.0401 0.2617 -0.2465
[2,] 0.0747 -0.0903 -0.0978
[3,] 0.1541 -0.1518 -0.0535
standard error
      [,1] [,2] [,3]
[1,] 0.0910 0.0869 0.0882
[2,] 0.0974 0.0931 0.0944
[3,] 0.1045 0.0998 0.1013

Residuals cov-mtx:
      [,1] [,2] [,3]
[1,] 0.22430413 0.04383870 0.08933612
[2,] 0.04383870 0.25690861 0.09675468
[3,] 0.08933612 0.09675468 0.29548204

det(SSE) = 0.01306715
AIC = -3.761654
BIC = -2.9471
HQ = -3.430743

```

1.2 Simplify VAR(4) model

The simplified VAR(4) model can be written as

$$z_t = \begin{bmatrix} 0.2 \\ 0 \\ 0.32 \end{bmatrix} + \begin{bmatrix} 0.57 & 0 & 0 \\ 0.38 & 0.30 & 0.41 \\ 0.51 & 0.27 & 0 \end{bmatrix} z_{t-1} + \begin{bmatrix} 0 & 0.28 & 0 \\ 0 & -0.15 & 0 \\ 0 & 0 & 0 \end{bmatrix} z_{t-2} + \begin{bmatrix} 0 & -0.25 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} z_{t-3} + \begin{bmatrix} 0 & 0.30 & -0.24 \\ 0 & 0 & 0 \\ 0 & -0.20 & 0 \end{bmatrix} z_{t-4} + a_t$$

```
> options(digits=2)
> m4=refVAR(m3,thres=1.96)
```

Constant term:

Estimates: 0.2 0 0.32

Std.Error: 0.069 0 0.081

AR coefficient matrix

AR(1)-matrix

 [,1] [,2] [,3]

[1,] 0.565 0.000 0.000

[2,] 0.376 0.299 0.408

[3,] 0.508 0.268 0.000

standard error

 [,1] [,2] [,3]

[1,] 0.0798 0.0000 0.0000

[2,] 0.0852 0.0899 0.0887

[3,] 0.0882 0.0751 0.0000

AR(2)-matrix

 [,1] [,2] [,3]

[1,] 0 0.284 0

[2,] 0 -0.153 0

[3,] 0 0.000 0

standard error

 [,1] [,2] [,3]

[1,] 0 0.0728 0

[2,] 0 0.0769 0

[3,] 0 0.0000 0

AR(3)-matrix

 [,1] [,2] [,3]

[1,] 0 -0.249 0

[2,] 0 0.000 0

[3,] 0 0.000 0

standard error

 [,1] [,2] [,3]

[1,] 0 0.09 0

```

[2,]    0 0.00    0
[3,]    0 0.00    0
AR( 4 )-matrix
      [,1] [,2] [,3]
[1,]    0  0.296 -0.243
[2,]    0  0.000  0.000
[3,]    0 -0.199  0.000
standard error
      [,1] [,2] [,3]
[1,]    0 0.0797 0.0849
[2,]    0 0.0000 0.0000
[3,]    0 0.0686 0.0000

```

```

Residuals cov-mtx:
      [,1] [,2] [,3]
[1,] 0.237 0.048 0.10
[2,] 0.048 0.278 0.11
[3,] 0.101 0.110 0.33

```

```

det(SSE) = 0.016
AIC = -3.9
BIC = -3.7
HQ  = -3.8

```

1.3 Model check

We can see all the p-values are more than 0.05. So the model is adequate.

```
> MTSdiag(m4,adj=12)
```

```

[1] "Covariance matrix:"
      uk    ca    us
uk 0.2388 0.0487 0.102
ca 0.0487 0.2790 0.111
us 0.1019 0.1109 0.331
CCM at lag: 0
      [,1] [,2] [,3]
[1,] 1.000 0.189 0.362
[2,] 0.189 1.000 0.365
[3,] 0.362 0.365 1.000
Simplified matrix:
CCM at lag: 1
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. . .
. . +
CCM at lag: 2

```

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CCM at lag:  3
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CCM at lag:  4
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CCM at lag:  5
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CCM at lag:  6
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CCM at lag:  7
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CCM at lag:  8
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CCM at lag: 10
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CCM at lag: 11
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CCM at lag: 12
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. . .
CCM at lag: 13

```

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CCM at lag: 14
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CCM at lag: 15
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CCM at lag: 16
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CCM at lag: 17
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CCM at lag: 18
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CCM at lag: 19
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CCM at lag: 20
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CCM at lag: 22
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CCM at lag: 23
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CCM at lag: 24

```

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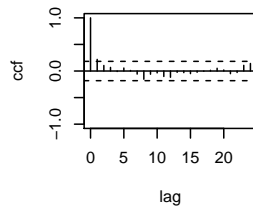
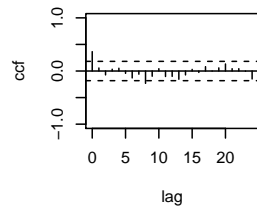
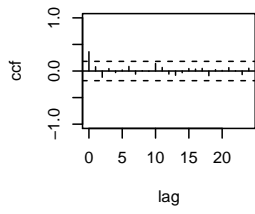
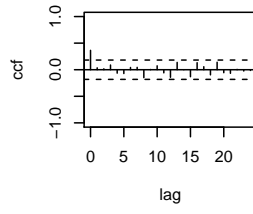
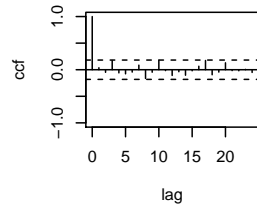
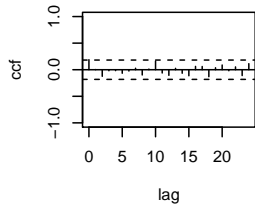
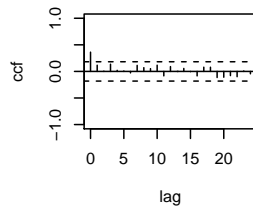
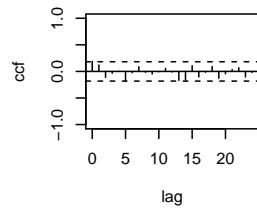
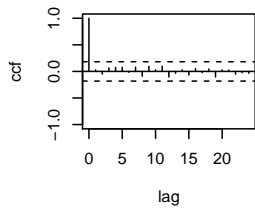
Hit Enter for p-value plot of individual ccm:

Hit Enter to compute MQ-statistics:

Ljung-Box Statistics:

	m	Q(m)	df	p-value
[1,]	1.00	7.93	-3.00	1.00
[2,]	2.00	16.26	6.00	1.00
[3,]	3.00	24.71	15.00	0.05
[4,]	4.00	27.71	24.00	0.27
[5,]	5.00	36.06	33.00	0.33
[6,]	6.00	41.54	42.00	0.49
[7,]	7.00	47.78	51.00	0.60
[8,]	8.00	64.66	60.00	0.32
[9,]	9.00	68.22	69.00	0.50
[10,]	10.00	81.99	78.00	0.36
[11,]	11.00	91.03	87.00	0.36
[12,]	12.00	101.83	96.00	0.32
[13,]	13.00	111.75	105.00	0.31
[14,]	14.00	119.75	114.00	0.34
[15,]	15.00	127.84	123.00	0.36
[16,]	16.00	134.71	132.00	0.42
[17,]	17.00	142.92	141.00	0.44
[18,]	18.00	150.03	150.00	0.48
[19,]	19.00	161.08	159.00	0.44
[20,]	20.00	172.29	168.00	0.39
[21,]	21.00	175.93	177.00	0.51
[22,]	22.00	180.17	186.00	0.61
[23,]	23.00	188.40	195.00	0.62
[24,]	24.00	204.69	204.00	0.47

Hit Enter to obtain residual plots:



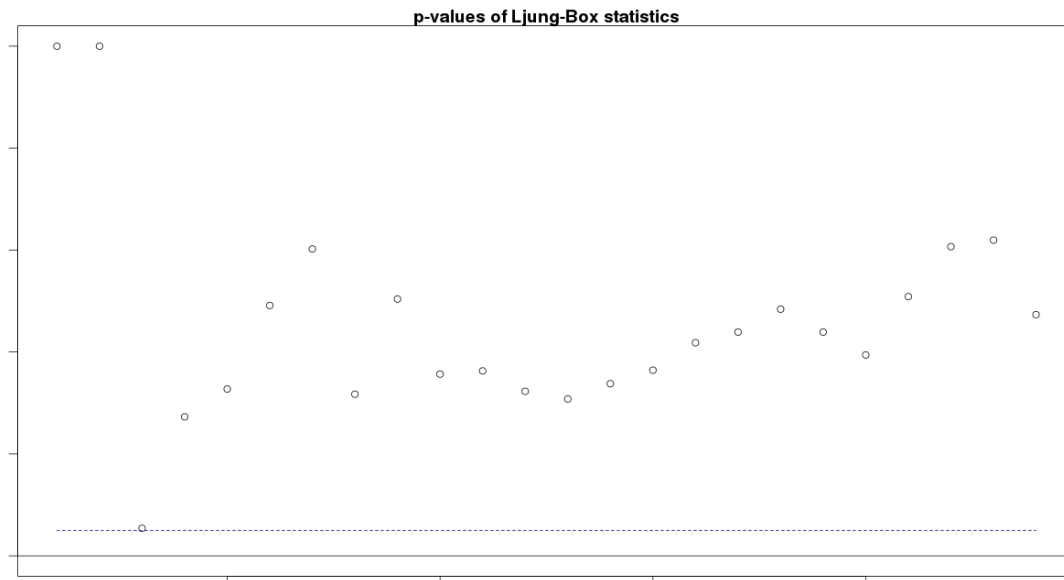


Figure 1: p-values of the $Q_k(m)$ atstatistics applied to the residuals of the simplified VAR(4) model

1.4 Comparing

Let's comparing the model VAR(2). Here we could compare the p-value,the VAR(2) model have a point below the 0.05 line,but VAR(4) are not. We also could compare through AIC,BIC and HQ values.All of values in VAR(4) are smaller than VAR(2). So we can say, simplified VAR(4) is better than simplified VAR(2).

```
> m1=VAR(z,2)
```

Constant term:

Estimates: 0.13 0.12 0.29

Std.Error: 0.073 0.074 0.082

AR coefficient matrix

AR(1)-matrix

	[,1]	[,2]	[,3]
[1,]	0.393	0.103	0.0521
[2,]	0.351	0.338	0.4691
[3,]	0.491	0.240	0.2356

standard error

	[,1]	[,2]	[,3]
[1,]	0.0934	0.0984	0.0911
[2,]	0.0949	0.1000	0.0926
[3,]	0.1050	0.1106	0.1024

AR(2)-matrix

	[,1]	[,2]	[,3]
--	------	------	------

```

[1,] 0.0566 0.106 0.01889
[2,] -0.1914 -0.175 -0.00868
[3,] -0.3120 -0.131 0.08531
standard error
      [,1] [,2] [,3]
[1,] 0.0924 0.0876 0.0938
[2,] 0.0939 0.0890 0.0953
[3,] 0.1038 0.0984 0.1055

```

Residuals cov-mtx:

```

      [,1] [,2] [,3]
[1,] 0.282 0.027 0.074
[2,] 0.027 0.292 0.139
[3,] 0.074 0.139 0.357

```

det(SSE) = 0.023

AIC = -3.5

BIC = -3.1

HQ = -3.3

```
> m2=refVAR(m1,thres=1.96)
```

Constant term:

Estimates: 0.16 0 0.28

Std.Error: 0.068 0 0.08

AR coefficient matrix

AR(1)-matrix

```

      [,1] [,2] [,3]
[1,] 0.467 0.207 0.000
[2,] 0.334 0.270 0.496
[3,] 0.468 0.225 0.232

```

standard error

```

      [,1] [,2] [,3]
[1,] 0.0790 0.0686 0.0000
[2,] 0.0921 0.0875 0.0913
[3,] 0.1027 0.0963 0.1023

```

AR(2)-matrix

```

      [,1] [,2] [,3]
[1,] 0.000 0 0
[2,] -0.197 0 0
[3,] -0.301 0 0

```

standard error

```

      [,1] [,2] [,3]
[1,] 0.0000 0 0
[2,] 0.0921 0 0

```

```
[3,] 0.1008    0    0
```

```
Residuals cov-mtx:
```

```
      [,1] [,2] [,3]  
[1,] 0.290 0.018 0.071  
[2,] 0.018 0.308 0.146  
[3,] 0.071 0.146 0.363
```

```
det(SSE) = 0.025
```

```
AIC = -3.5
```

```
BIC = -3.3
```

```
HQ  = -3.4
```

```
> MTSdiag(m2,adj=12)
```

```
[1] "Covariance matrix:"
```

```
      uk      ca      us  
uk 0.2924 0.0182 0.0711  
ca 0.0182 0.3084 0.1472  
us 0.0711 0.1472 0.3657
```

```
CCM at lag: 0
```

```
      [,1] [,2] [,3]  
[1,] 1.0000 0.0605 0.218  
[2,] 0.0605 1.0000 0.438  
[3,] 0.2175 0.4382 1.000
```

```
Simplified matrix:
```

```
CCM at lag: 1
```

```
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```

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CCM at lag: 2
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CCM at lag: 3
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CCM at lag: 4
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CCM at lag: 5
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CCM at lag:  6
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CCM at lag:  7
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CCM at lag: 15
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CCM at lag: 16
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CCM at lag: 17
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CCM at lag: 20
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CCM at lag: 21
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CCM at lag: 22
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CCM at lag: 23
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CCM at lag: 24
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. . .
Hit Enter for p-value plot of individual ccm:

```

Hit Enter to compute MQ-statistics:

Ljung-Box Statistics:

	m	Q(m)	df	p-value
[1,]	1.00	1.78	-3.00	1.00
[2,]	2.00	12.41	6.00	1.00
[3,]	3.00	22.60	15.00	0.09
[4,]	4.00	37.71	24.00	0.04
[5,]	5.00	41.65	33.00	0.14

[6,]	6.00	44.95	42.00	0.35
[7,]	7.00	51.50	51.00	0.45
[8,]	8.00	64.87	60.00	0.31
[9,]	9.00	72.50	69.00	0.36
[10,]	10.00	81.58	78.00	0.37
[11,]	11.00	86.12	87.00	0.51
[12,]	12.00	98.08	96.00	0.42
[13,]	13.00	112.31	105.00	0.30
[14,]	14.00	121.89	114.00	0.29
[15,]	15.00	134.58	123.00	0.22
[16,]	16.00	139.16	132.00	0.32
[17,]	17.00	145.85	141.00	0.37
[18,]	18.00	152.56	150.00	0.43
[19,]	19.00	165.91	159.00	0.34
[20,]	20.00	175.22	168.00	0.34
[21,]	21.00	180.56	177.00	0.41
[22,]	22.00	187.40	186.00	0.46
[23,]	23.00	193.78	195.00	0.51
[24,]	24.00	204.65	204.00	0.47

Hit Enter to obtain residual plots:

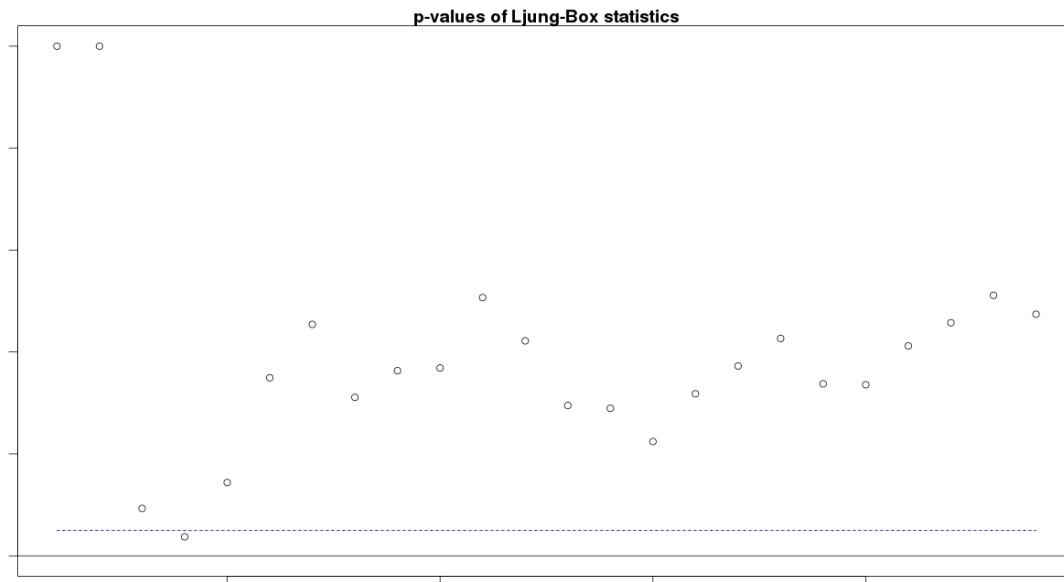


Figure 2: p-values of the $Q_k(m)$ atstatistics appllied to the residuals of the simplied VAR(2) model

2 b-2-3

2.1 z_t graph

```
> temp=tempfile()
> download.file("http://faculty.chicagobooth.edu/ruey.tsay/teaching/mtsbk/data-ch2.zip",temp)
> da=read.table(unz(temp, "Users/rst/Documents/backup/mts/y2012/data/ch2/m-cpitb3m.txt"),header=T)
> dim(da)

[1] 792    4

> z1=da$tb3m[1:791]
> z2=100*(log(da$cpiaucsl[2:792])-log(da$cpiaucsl[1:791]))
> Z=cbind(z1,z2)
> t=1:791/12+1947
```

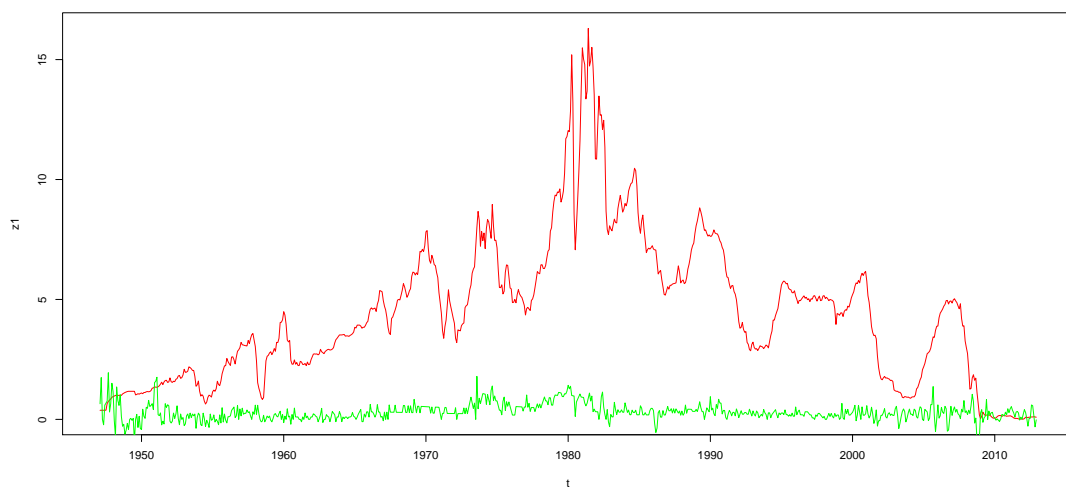


Figure 3: Time series of z_t , change in monthly US treasury bills line is red, the line of inflation rate of CPI is green

2.2 Choose the order by BIC criterion

We can see the best order choosing through BIC criterion is 3. So we are using VAR(3) model.

```
> library(MTS)
> m1=VARorder(Z)

selected order: aic = 13
selected order: bic = 3
selected order: hq = 12
Summary table:
      p   AIC   BIC   HQ   M(p) p-value
[1,]  0 -0.22 -0.22 -0.22    0.0  0.0000
[2,]  1 -4.46 -4.44 -4.45 3291.5  0.0000
[3,]  2 -4.58 -4.53 -4.56   99.5  0.0000
[4,]  3 -4.62 -4.55 -4.60   42.9  0.0000
[5,]  4 -4.63 -4.53 -4.59    8.2  0.0850
[6,]  5 -4.63 -4.51 -4.58    9.1  0.0580
[7,]  6 -4.64 -4.50 -4.58   16.5  0.0024
[8,]  7 -4.70 -4.54 -4.64   56.9  0.0000
[9,]  8 -4.71 -4.52 -4.63   10.7  0.0303
[10,] 9 -4.72 -4.51 -4.64   19.6  0.0006
[11,] 10 -4.73 -4.50 -4.64   14.4  0.0060
[12,] 11 -4.73 -4.47 -4.63    3.4  0.4971
[13,] 12 -4.76 -4.48 -4.65   35.1  0.0000
[14,] 13 -4.77 -4.46 -4.65   14.3  0.0063
```

2.3 VAR(3) model and fitted VAR(3) model

Here is the VAR(3) model.

$$z_t = \begin{bmatrix} 0.03 \\ 0.04 \end{bmatrix} + \begin{bmatrix} 1.39 & 0.13 \\ 0.09 & 0.45 \end{bmatrix} z_{t-1} + \begin{bmatrix} -0.61 & 0.06 \\ -0.08 & 0.02 \end{bmatrix} z_{t-2} + \begin{bmatrix} 0.21 & -0.09 \\ 0.01 & 0.11 \end{bmatrix} z_{t-3} + a_t$$

And the fitted VAR(3) model is

$$z_t = \begin{bmatrix} 0 \\ 0.04 \end{bmatrix} + \begin{bmatrix} 1.39 & 0.14 \\ 0.08 & 0.46 \end{bmatrix} z_{t-1} + \begin{bmatrix} -0.61 & 0 \\ -0.07 & 0 \end{bmatrix} z_{t-2} + \begin{bmatrix} 0.21 & 0 \\ 0 & 0.12 \end{bmatrix} z_{t-3} + a_t$$

```
> options(digits=2)
> m2=VAR(Z,3)
```

Constant term:

Estimates: 0.035 0.042

Std.Error: 0.024 0.018

AR coefficient matrix

AR(1)-matrix

```
      [,1] [,2]
```

```

[1,] 1.3857 0.128
[2,] 0.0886 0.449
standard error
      [,1] [,2]
[1,] 0.0350 0.0491
[2,] 0.0253 0.0355
AR( 2 )-matrix
      [,1] [,2]
[1,] -0.6095 0.0608
[2,] -0.0849 0.0223
standard error
      [,1] [,2]
[1,] 0.0566 0.0528
[2,] 0.0409 0.0381
AR( 3 )-matrix
      [,1] [,2]
[1,] 0.2095 -0.0945
[2,] 0.0149 0.1109
standard error
      [,1] [,2]
[1,] 0.0349 0.0484
[2,] 0.0252 0.0349

Residuals cov-mtx:
      [,1] [,2]
[1,] 0.1405 0.0099
[2,] 0.0099 0.0732

det(SSE) = 0.01
AIC = -4.6
BIC = -4.5
HQ  = -4.5

> m3=refVAR(m2,thres=1.65)

Constant term:
Estimates: 0 0.044
Std.Error: 0 0.017
AR coefficient matrix
AR( 1 )-matrix
      [,1] [,2]
[1,] 1.3887 0.139
[2,] 0.0842 0.456
standard error
      [,1] [,2]

```

```

[1,] 0.0350 0.0428
[2,] 0.0239 0.0324
AR( 2 )-matrix
      [,1] [,2]
[1,] -0.6137 0
[2,] -0.0654 0
standard error
      [,1] [,2]
[1,] 0.0567 0
[2,] 0.0237 0
AR( 3 )-matrix
      [,1] [,2]
[1,] 0.213 0.000
[2,] 0.000 0.119
standard error
      [,1] [,2]
[1,] 0.0348 0.0000
[2,] 0.0000 0.0319

Residuals cov-mtx:
      [,1] [,2]
[1,] 0.1415 0.0099
[2,] 0.0099 0.0732

det(SSE) = 0.01
AIC = -4.6
BIC = -4.5
HQ = -4.5

```

2.4 check the model

We can find this model is not adequate. Since most p-value is below the 0.05 line. That means the residuals have great dependent.

```

> MTSdiag(m3,adj=12)

[1] "Covariance matrix:"
      z1      z2
z1 0.14161 0.00995
z2 0.00995 0.07333
CCM at lag: 0
      [,1] [,2]
[1,] 1.0000 0.0976
[2,] 0.0976 1.0000
Simplified matrix:
CCM at lag: 1

```

```

. .
. .
CCM at lag: 2
. .
. .
CCM at lag: 3
. .
. .
CCM at lag: 4
. .
. .
CCM at lag: 5
+ -
. .
CCM at lag: 6
- .
. .
CCM at lag: 7
- .
. +
CCM at lag: 8
+ .
. .
CCM at lag: 9
+ .
. +
CCM at lag: 10
. .
. +
CCM at lag: 11
. .
. +
CCM at lag: 12
- .
. -
CCM at lag: 13
. .
. .
CCM at lag: 14
+ .
. .
CCM at lag: 15
- .
. +

```

```

CCM at lag: 16
. .
. .
CCM at lag: 17
. .
. .
CCM at lag: 18
. .
. .
CCM at lag: 19
. .
. .
CCM at lag: 20
- .
. .
CCM at lag: 21
- .
. .
CCM at lag: 22
. .
. .
CCM at lag: 23
. .
. .
CCM at lag: 24
. .
- .
Hit Enter for p-value plot of individual ccm:

```

Hit Enter to compute MQ-statistics:

Ljung-Box Statistics:

	m	Q(m)	df	p-value
[1,]	1.000	0.674	-8.000	1
[2,]	2.000	3.230	-4.000	1
[3,]	3.000	11.058	0.000	1
[4,]	4.000	15.185	4.000	0
[5,]	5.000	33.410	8.000	0
[6,]	6.000	60.387	12.000	0
[7,]	7.000	80.578	16.000	0
[8,]	8.000	89.132	20.000	0
[9,]	9.000	114.434	24.000	0
[10,]	10.000	125.633	28.000	0
[11,]	11.000	139.892	32.000	0

[12,]	12.000	161.040	36.000	0
[13,]	13.000	164.302	40.000	0
[14,]	14.000	186.355	44.000	0
[15,]	15.000	209.769	48.000	0
[16,]	16.000	218.822	52.000	0
[17,]	17.000	223.414	56.000	0
[18,]	18.000	227.421	60.000	0
[19,]	19.000	229.788	64.000	0
[20,]	20.000	262.002	68.000	0
[21,]	21.000	272.053	72.000	0
[22,]	22.000	276.621	76.000	0
[23,]	23.000	281.061	80.000	0
[24,]	24.000	288.536	84.000	0

Hit Enter to obtain residual plots:

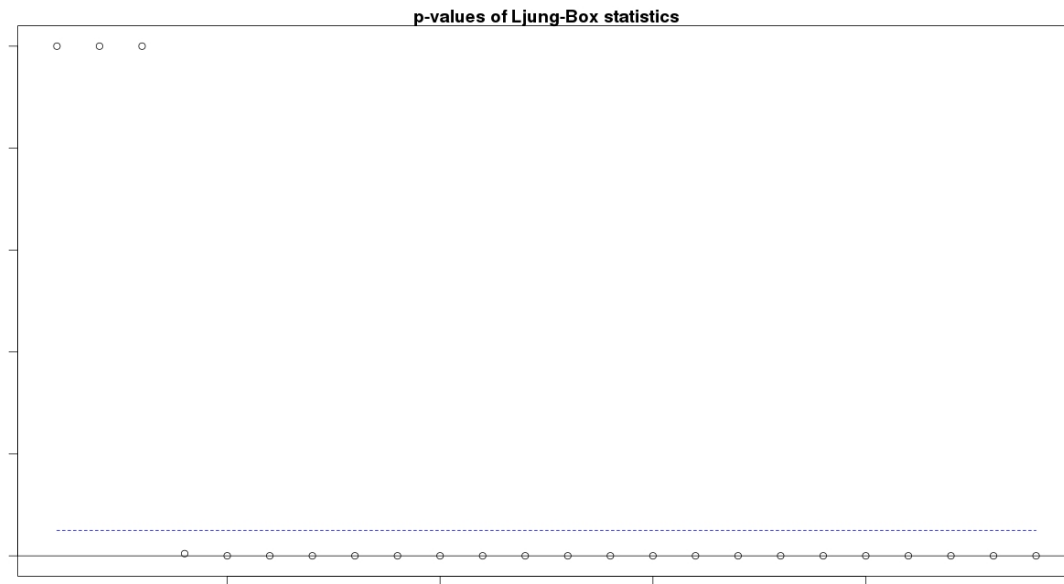


Figure 4: p-values of the $Q_k(m)$ atstatistics appllied to the residuals of the simplied VAR(3) model

2.5 Impulse response functions

The upper-left plot shows that there is a delayed effect on the US treasury bill if one changed the US treasury bill by 1. The upper two plots does not decay to 0 quickly.

```
> Phi=m3$Phi  
> Sig=m3$Sigma  
  
> VARirf(Phi,Sig)
```

Press return to continue

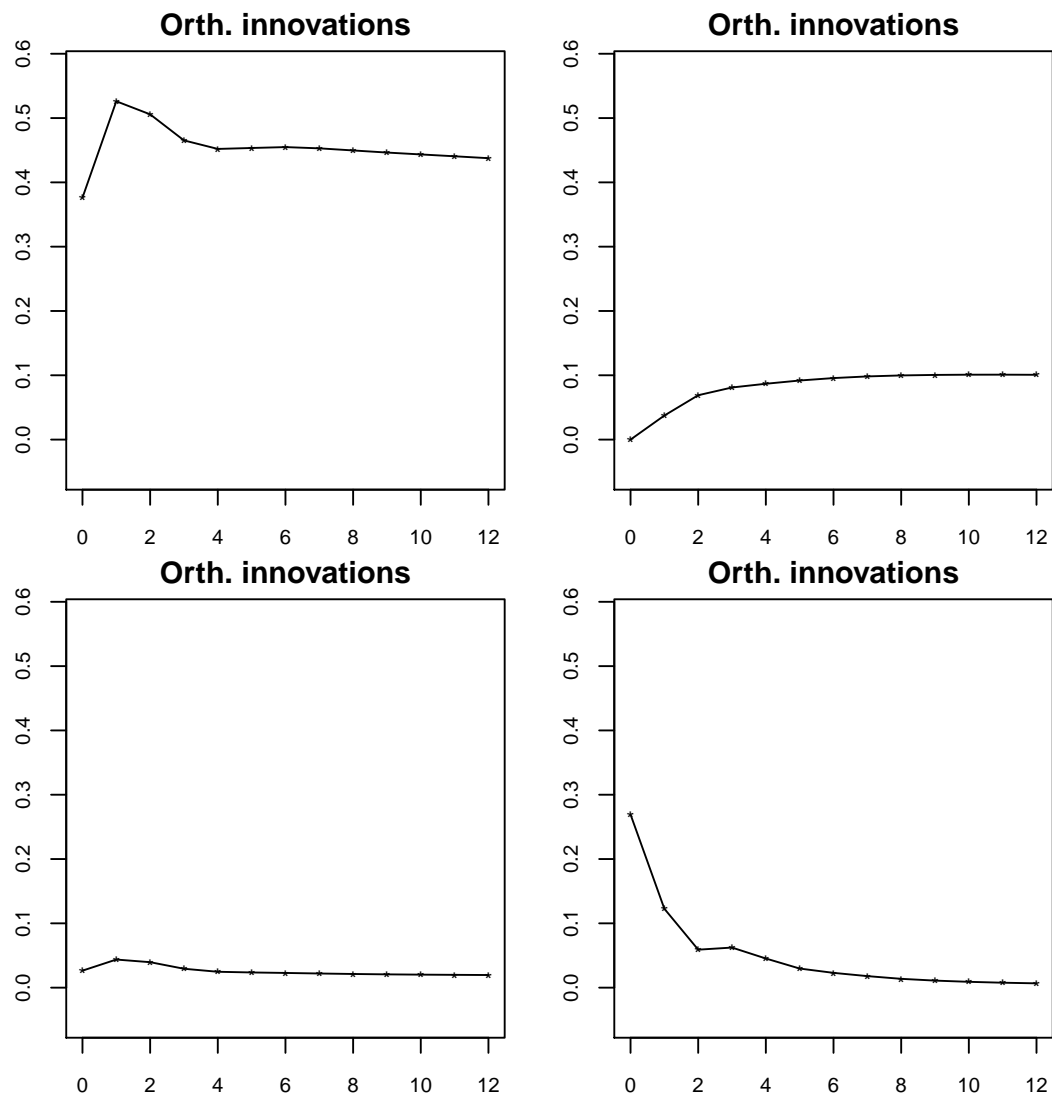


Figure 5: Impulse response function of the simplified VAR(3)

2.6 Cholesky decomposition and transformed innovations

Since a_t is the residual matrix, we find the covariance matrix and the Cholesky decomposition matrix are

$$Cov(a_t) = \begin{bmatrix} 0.14 & 0.01 \\ 0.01 & 0.07 \end{bmatrix}$$

$$U = \begin{bmatrix} 0.4 & 0.03 \\ 0.0 & 0.27 \end{bmatrix}$$

So we could see

$$Cov(a_t) = U'U \quad (2.1)$$

And the transformed innovations are $\eta_t = (U')^{-1}a_t$

```
> Resi=t(m3$residuals)
> Cov=cov(t(Resi))
> Cov
```

```
      [,1] [,2]
[1,] 0.1416 0.0099
[2,] 0.0099 0.0733
```

```
> dd=t(chol(Cov))
> dd
```

```
      [,1] [,2]
[1,] 0.376 0.00
[2,] 0.026 0.27
```

```
> ent=solve(dd)%*%Resi
> t1=4:791/12+1947
```

```
> plot(t1,ent[1,],type='l',col="red")  
> lines(t1,ent[2,],lty=2,col="green")
```

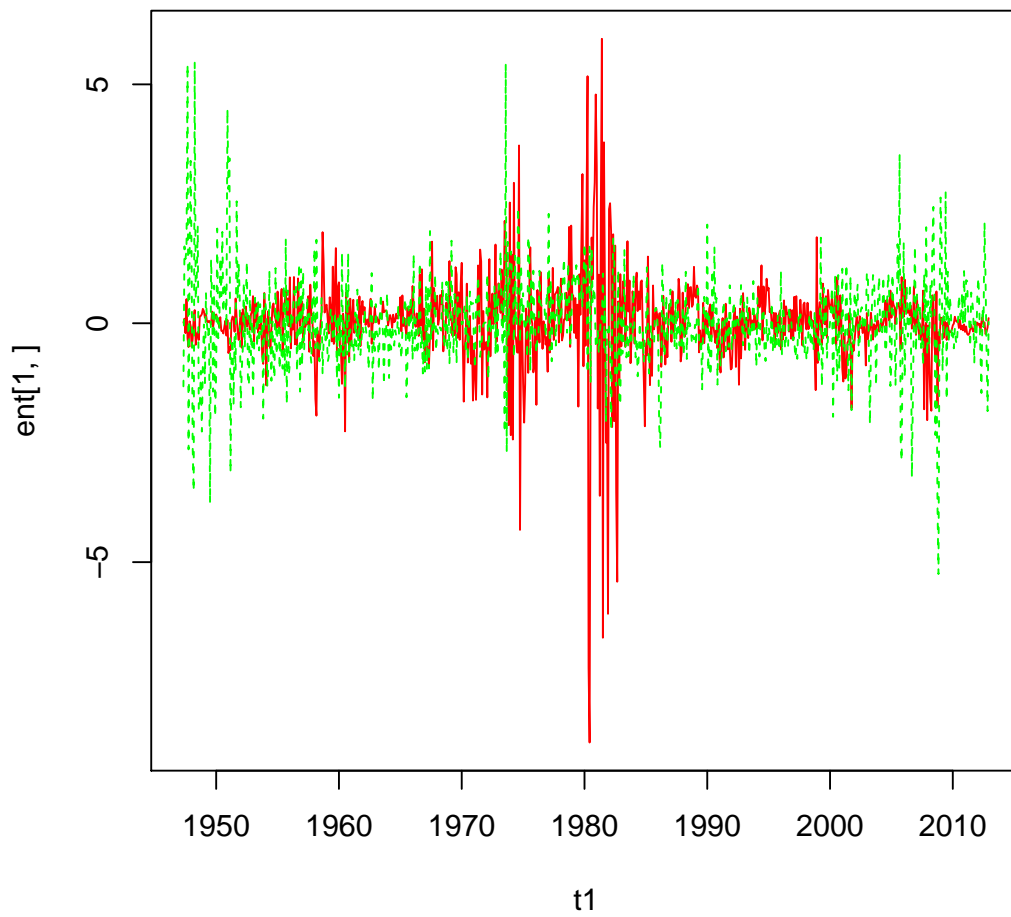


Figure 6: The transformed innovations plot